DEPARTMENT OF STATISTICS FACULTY OF MATHEMATICAL SCIENCES UNIVERSITY OF DELHI



PROJECT REPORT

ADVANCE STATISTICAL COMPUTING USING R RANDOM NUMBER GENERATION FROM VARIOUS DISTRIBUTIONS

(AS PART OF THE COURSE PAPER 404: ADVANCED STATISTICAL COMPUTING AND DATA MINING)

UNDER THE GUIDANCE AND SUPERVISION OF

MR. ABHISHEK K. UMRAWAL (ASSISTANT PROFESSOR)

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PLACE: NEW DELHI

SUBMITTED BY:

VISHAL KUMAR M. Sc. Statistics, Semester – IV

ABSTRACT

To understand the computational aspect of Data Mining, a practical approach using statistical software R was introduced in Statistics Department of University of Delhi. The main purpose of this approach is to understand how random numbers are generated, to validate that the numbers generated mimic the actual population under consideration. Then using that generated sample to estimate population parameters using method of Maximum Likelihood estimation and using some iterative techniques for those distribution involving two parameters.

This study has been divided into 4 parts:

- 1. In this part random numbers were generated using Linear Congruential Generator (LCG) for the choice of a priori integers due to Lehmer (1951). Then validity tests like histogram, Q-Q plot, Chi-square test for goodness of fit and Kolmogorov-Smirnov test were performed on the random numbers.
- 2. In this part random numbers were generated from Normal and Gamma distribution using Acceptance/Rejection method. Then MLE's were computed and validity tests like histogram, Q-Q plot, Chi-square test for goodness of fit and Kolmogorov-Smirnov test were performed on the random numbers.
- **3.** In this part random numbers were generated from Bivariate Normal distribution and 3-D histogram was made. Then random numbers were generated from Marshall-Olkin Bivariate Exponential (MOBE) distribution and from Block & Basu Bivariate Exponential Distribution (BBBE).
- **4.** In this part random numbers were generated from Weibull distribution, then MLE's were computed using Newton-Raphson method. Expectation-Maximization Algorithm was used to find MLE's from a mixture of two normal distribution.

ACKNOWLEDGEMENTS

I have given my best efforts to make this a good report. However, it would not have been possible without the kind support, guidance and constant supervision of our professor **MR. ABHISHEK K. UMRAWAL** and I would like to express my gratitude towards him for providing necessary help regarding the concepts and techniques used in this case study.

Lecture notes released by MR. ABHISHEK K. UMRAWAL, provided the necessary knowledge to tackle the given problem at hand and to understand the basic "why" concept behind any technique and algorithm used in this report.

Question 1. Construct a Uniform Random Number Generator between 0 and 1 using the Linear Congruential Generator (LCG) for the choice of a priori integers due to Lehmer (1951), viz. Multiplier = 23, Shift = 0 and Modulus = $10^8 + 1$.

Generate random samples each of size 1000 from a U(0,1) distribution using your own generator. Check **validity** of the generated random samples.

Solution:

Linear Congruential Generator (LCG):

$$X_i = (aX_{i-1} + c) \bmod M$$

Where a = multiplier

c = shift

M = modulus, and the first element is denoted as X_0 and is called seed value (priori).

Some restrictions are imposed on the parameters of the generator:

$$M > 0, 0 \le a < M, 0 \le c < M, 0 \le X_0 < M$$

R Code:

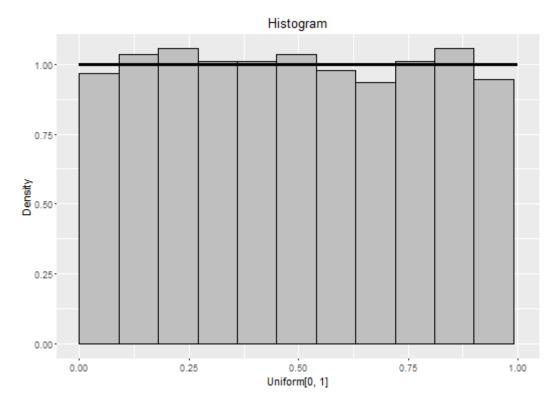
```
rm(list=ls())
LGC <- function(a, c, M, n, y){
    x <- c()
    x[1] <- y
    for(i in 1:n)
        x[i+1] <- (a*x[i]+c) %% (M)
    return(x[-1]/M)
}
uni_01 <- LGC(a= 23, c= 0, M= 10^8, n= 1000, y= 123)</pre>
```

Conclusion: "**LCG**" function can be called to generate random numbers from U[0, 1] distribution using linear Congruential Generator (LCG). For given set of parameters 1000 random numbers are generated and are given in the appendix.

We will check validity of our random sample:

1. Histogram overlaid with a theoretical frequency curve:

R code:

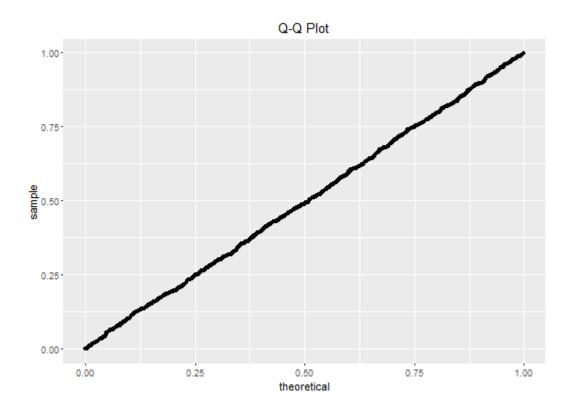


Conclusion: We see that observed sample density is close to expected density. No skewness is observed.

2. Q-Q Plot:

R Code:

```
q <- ggplot(mapping = aes(sample = uni_01)) + ggtitle("Q-Q Plot")
q + stat_qq(distribution = stats::qunif)</pre>
```



Conclusion: We observe that sample and theoretical quantiles lies along a straight line. No skewness is observed.

3. Chi - Square Test:

H₀: The data are consistent with the uniform distribution. H₁: The data are not consistent with the uniform distribution.

R Code:

```
breaks <- seq(0, 1, length = 6)
intervals <- cut(uni_01, breaks, right=FALSE)
observed <- table(intervals)
prob <- c()
for(i in 1:5)
   prob[i] <- punif(breaks[i+1], 0, 1) - punif(breaks[i], 0, 1)
expected <- prob*1000
chisq.test(cbind(observed, expected))</pre>
```

Output:

```
Pearson's Chi-squared test

data: cbind(observed, expected)

X-squared = 0.40835, df = 4, p-value = 0.9818
```

Conclusion: We observe that p-value is insignificant, hence we conclude that data fits well to Uniform[0, 1].

4. Kolmogorov-Smirnov Test:

H₀: Samples are from same distribution.H₁: Samples are not from same distribution.

R Code:

```
ks.test(uni_01, "punif", 0, 1)
```

Output:

```
One-sample Kolmogorov-Smirnov test
: uni_01
```

D = 0.015665, p-value = 0.9668 alternative hypothesis: two-sided

Conclusion: We observe that p-value is insignificant, hence we conclude that data is coming from Uniform[0, 1].

All the validity test holds true, hence we conclude that Lehmer Linear Congruential Generator is a valid generator in generating random sample from Uniform[0, 1].

Question 2:

(i) Generate a random sample of size 1000 from a N(7,3) distribution using a suitable algorithm. Check **validity** of the generated random sample. Now assuming that the generated random sample is a random sample from some $N(\mu, \sigma^2)$ distribution, find MLEs of the parameters and comment on your results.

Solution:

We will generate the required sample by generating 1000 random numbers from N(0, 1) and then transforming into N(7, 3). We will generate random sample from N(0, 1) by Acceptance/Rejection method. Algorithm is described as follows:

1. Generate X₁ from h(.) and U₁ from U(0, 1), independently. h(.) will be pdf of double exponential distribution. To generate data from double exponential, we generate "n" numbers from Exponential(1) distribution and take negative for half of them. To generate data from exponential distribution we use simple inversion method:

$$x = F^{-1}(u) = -\ln(1 - u)$$

2. We will check if the following condition is satisfied:

$$cU_1h(X_1) \le f_{\nu}(X_1)$$

Where $c=\sqrt{\frac{2}{\pi}}e^{\frac{1}{2}}$ and $f_{\mathcal{Y}}(X_1)$ is the pdf from which we want to generate our random sample.

If satisfied then that X_1 will be our first data point from $f_{\nu}(.)$. If not, then go back to step 1.

- 3. Repeat step 1 and step 2as many times as the data points are required.
- 4. After generating sample from N(0, 1), we will transform them into N(7, 3) by following transformation:

$$Y = 7 + \sqrt{3} * Z$$

Where $Z \sim N(0, 1)$ and $Y \sim N(7, 3)$.

R Code:

```
set.seed(122)
rand snormal <- function(n){</pre>
  uni_01 <- runif(2*n)
  y1 <- uni 01[1:n]
  y2 <- uni 01[n+1:1000]
  y < -c(y1, y2)
  x \leftarrow c()
  for(i in 1:n){
                                     # Random number from double
exponential(1)
    x[i] < -\log(1-y1[i])
    x[n + i] \leftarrow log(1-y2[i])
  }
  p \leftarrow c()
  i<-1
  while(length(p) < 1000){  # Acceptance/Rejection condition</pre>
    U = sample(uni_01, 1)
    z = sample(x, 1)
    if(exp(-abs(z))*1.315*U/2 <= dnorm(z, 0, 1)){</pre>
      p[i] \leftarrow z
      i <- i+1
    }
```

```
else i <- i-1
}
return(p)
}

norm_01 <- rand_snormal(1000)  # Generating from N(0, 1)
norm <- norm_01*sqrt(3) + 7  # Transforming into N(7, 3)

mean(norm)
[1] 7.011245
> var(norm)
[1] 2.893641
```

Conclusion: "norm_01" function can be called to generate random numbers from N[0, 1] distribution using Acceptance/Rejection Method. 1000 random numbers are generated and are given in the appendix.

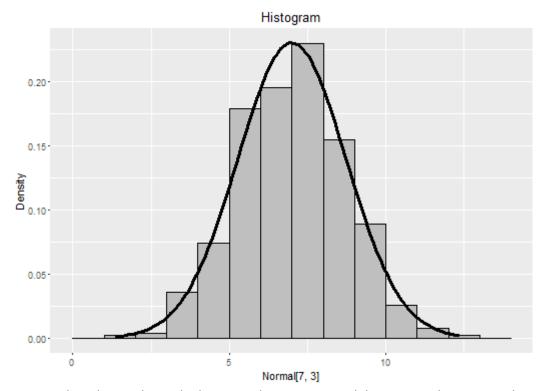
MLE of population mean is given by the sample mean = 7.011

MLE of population variance is given by the sample variance = 2.893

We will check validity of our random sample:

1. Histogram overlaid with a theoretical frequency curve:

R Code:

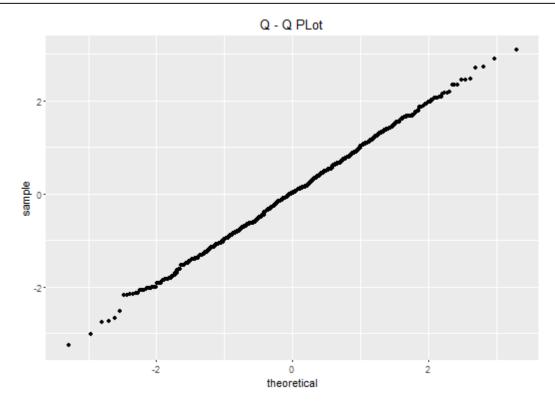


Conclusion: We see that observed sample density is close to expected density. No skewness is observed.

2. Q-Q Plot:

R Code:

```
q <- ggplot(mapping = aes(sample = norm_01))
q + stat_qq(distribution = stats::qnorm) + ggtitle("Q - Q PLot")</pre>
```



Conclusion: We observe that sample and theoretical quantiles lies along a straight line, i.e. they coincides.

3. Chi - Square Test:

 H_0 : The data are consistent with the normal distribution. H_1 : The data are not consistent with the normal distribution.

R Code:

```
breaks <- seq(min(norm), max(norm), length = 6)
intervals <- cut(norm, breaks, right=FALSE)
observed <- table(intervals)
prob <- c()
for(i in 1:5)
   prob[i] <- pnorm(breaks[i+1], 7, sqrt(3)) - pnorm(breaks[i], 7, sqrt(3))
expected <- prob*1000
chisq.test(cbind(observed, expected))</pre>
```

Output:

```
Pearson's Chi-squared test

data: cbind(observed, expected)

X-squared = 0.20693, df = 4, p-value = 0.995
```

Conclusion: We observe that p-value is insignificant, hence we conclude that data fits well to N[7, 3].

4. Kolmogorov-Smirnov Test:

 H_0 : The samples are from the same population.

H₁: The samples are not from the same population.

R Code:

ks.test(norm, "pnorm", mean=7, sd=sqrt(3))

Output:

One-sample Kolmogorov-Smirnov test

data: norm D = 0.021345, p-value = 0.7524 alternative hypothesis: two-sided

Conclusion: We observe that p-value is insignificant, hence we conclude that data is coming from N[7, 3].

All the validity test holds true, hence we conclude that our random number generator is a valid generator in generating random sample from N[0, 1], which can be transformed into N[7,3].

Question 2

(ii) Generate a random sample of size 1000 from a Gamma(5.8) distribution using a suitable algorithm. Check validity of the generated random sample. Now assuming that the generated random sample is a random sample from some Gamma(α) distribution, find MLE of the parameter and comment on your results.

Solution:

Here we will use the fact that, sum of "n" independent exponential distribution follows Gamma distribution and sum of Gamma distribution is also a Gamma distribution. So we will generate Gamma(5) from exponential distribution and Gamma(0.8) from Acceptance/Rejection method and then we will add them up.

Let X_1, X_2, X_3, X_4, X_5 be 5 independent observation from Exponential(1) distribution, then:

$$\sum_{i=1}^{5} X_i \sim Gamma(5)$$

Acceptance/Rejection Method:

1. Generate X_1 from h(.) and U_1 from U(0, 1) independently such that h(.) is generated from:

$$F_X^{-1}(u) = \begin{cases} \left(uc\Gamma(\alpha+1)\right)^{\frac{1}{\alpha}}, & 0 < u < \frac{1}{\Gamma(\alpha+1)} \\ -\ln\left\{\left(\frac{1}{c\Gamma(\alpha+1)} - u\right)c\Gamma(\alpha) + \frac{1}{e}\right\}, & u > \frac{1}{\Gamma(\alpha+1)} \end{cases}$$

2. Check, if $cU1h(X_1) \le f_{\mathcal{V}}(X_1)$ is true then $Y = X_1$ and if false then go back to step 1, where:

$$f_{y}(x) = \frac{1}{\Gamma(\alpha)} e^{-x} x^{\alpha - 1}, \quad x > 0, 0 < \alpha < 1$$

$$h(x) = \begin{cases} \frac{1}{c\Gamma(\alpha)} x^{\alpha - 1} & 0 < x < 1\\ \frac{1}{c\Gamma(\alpha)} e^{-x} & x \ge 1 \end{cases}$$
 and $c = \frac{1}{\Gamma(\alpha)} \left(\frac{1}{\alpha} + \frac{1}{e}\right)$

3. Repeat step 1 and step 2as many times as the data points are required.

```
set.seed(1234)
                                      # Random number from U[0, 1]
uni 01 <- runif(2000, 0, 1)
y < -\log(uni \ 01)
                                         # Random number from exp(1)
z \leftarrow c()
for(i in 1:2000)
  z[i] <- sum(sample(y, 5)) # Random number from gamma(5)</pre>
rand_gamma <- function(n, alpha){ # Random number from gamma(alpha)</pre>
  c \leftarrow (1/alpha + 1/exp(1))/gamma(alpha)
  x \leftarrow c()
  for(i in 1:(2*n)){
    if(uni_01[i] < 1/(c*gamma(1 + alpha)))</pre>
      x[i] \leftarrow (uni \ 01[i]*c*gamma(1 + alpha))^(1/alpha)
    else if(uni_01[i] > 1/(c*gamma(1 + alpha)))
      x[i] \leftarrow -\log((1/(c*gamma(1 + alpha))-uni_01[i])*c*gamma(alpha) +
                   1/\exp(1)
  }
  x <- na.omit(x)</pre>
  i <- 1
  p<-c()
  while(length(p) < n){</pre>
    u <- sample(uni 01, 1)
    if(x[i] < 1){
      if(u*(x[i]^-0.2)/gamma(alpha) < dgamma(x[i], shape=alpha)){
         p[i] \leftarrow x[i]
         i < -i + 1
       }
      else i <- i - 1
    else if(x[i] > 1){
      if(u*(exp(-x[i]))/gamma(alpha) < dgamma(x[i], shape=alpha)){}
         p[i] \leftarrow x[i]
         i < -i + 1
      else i <- i - 1
    }
  return(p)
gam <- rand gamma(1000, 0.8)
gam < - gam + z
> mean(gam)
[1] 5.889198
> var(gam)
[1] 5.967602
```

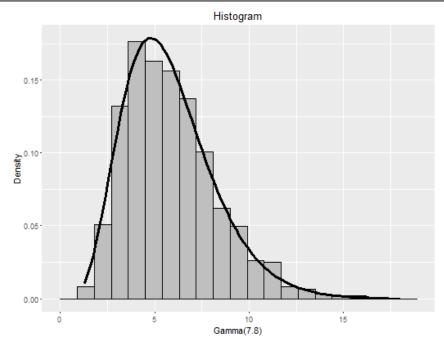
Conclusion: "rand_gamma" function can be called to generate 1000 random numbers from gamma(0.8) distribution, the numbers generate here are given in the appendix, then these numbers can be added to gamma(5) random number so as to obtain a random sample from gamma(5.8) distribution.

We will check validity of our random sample:

1. Histogram overlaid with a theoretical frequency curve:

R code:

```
library(ggplot2)
p <- ggplot(mapping = aes(x = gam))
p <- p + geom_histogram(aes(y=..density..), binwidth = 0.9, colour="black",
fill="gray75")
p <- p + stat_function(fun=dgamma, args = list(shape=5.8), col = 'black',
lwd=1.2)
p + xlab("Gamma(7.8)") + ylab("Density") + ggtitle("Histogram")</pre>
```

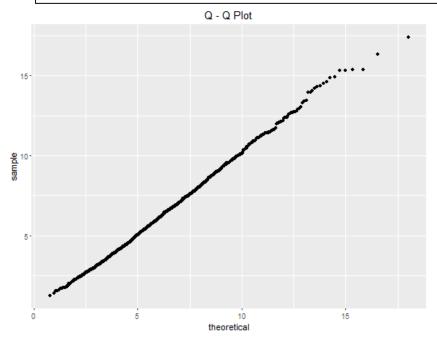


Conclusion: We see that observed sample density is close to expected density. Data is skewed to the right.

2. Q-Q Plot:

R code:

```
q <- ggplot(mapping = aes(sample = gam))+ ggtitle("Q-Q Plot")
q + stat_qq(distribution = stats::qgamma, dparams = list(shape=5.8))</pre>
```



Conclusion: We observe that sample and theoretical quantiles lies along a straight line, i.e. they coincides.

3. Chi-Square Test:

H₀: The data are consistent with the gamma distribution. H₁: The data are not consistent with the gamma distribution.

R code:

```
breaks <- seq(0, max(gam), length = 6)
intervals <- cut(gam, breaks, right=FALSE)
observed <- table(intervals)
prob <- c()
for(i in 1:5)
   prob[i] <- pgamma(breaks[i+1], 5.8) - pgamma(breaks[i], 5.8)
expected <- prob*1000
chisq.test(cbind(observed, expected))</pre>
```

```
Output:

data: cbind(observed, expected)
X-squared = 1.0292, df = 4, p-value = 0.9053
```

Conclusion: We observe that p-value is insignificant, hence we conclude that data fits well to Gamma (5.8).

4. Kolmogorov-Smirnov Test:

 H_0 : The samples are coming from the same population. H_1 : The samples are not coming from the same population.

R Code:

```
ks.test(gam, "pgamma", shape=5.8)
```

Output:

```
One-sample Kolmogorov-Smirnov test

data: gam
D = 0.021098, p-value = 0.3355
alternative hypothesis: two-sided
```

Conclusion: We observe that p-value is insignificant, hence we conclude that data is coming from Gamma(5.8).

All the validity test holds true, hence we conclude that our random number generator is a valid generator in generating random sample from Gamma(0.8), which can be transformed into Gamma(5.8).

Question 3

(i) Generate a random sample of size 1000 from a $N_2\begin{bmatrix} 9\\2 \end{pmatrix}$, $\begin{pmatrix} 8&2.3\\2.3&5 \end{pmatrix}$ distribution using a suitable algorithm. Check validity of the generated random sample using 3-D Histogram overlaid with the Theoretical Bivariate Normal Frequency Curve. Now assuming that the generated random sample is a random sample from some $N_2\begin{bmatrix} \mu_1\\\mu_2 \end{pmatrix}$, $\begin{pmatrix} \sigma_1^2&\sigma_{12}\\\sigma_{21}&\sigma_2^2 \end{pmatrix}$ distribution, find MLEs of the parameters and comment on your results.

Solution: A p-dimension random vector is said to follow a multivariate normal distribution, if pdf is given as:

$$f_{y}(x;\mu,\Sigma) = \frac{1}{(2\pi)^{\frac{p}{2}}|\Sigma|^{\frac{1}{2}}} \exp\left(-\frac{1}{2}(x-\mu)^{T}\Sigma^{-1}(x-\mu)\right); x \in \mathbb{R}^{p}, \mu \in \mathbb{R}^{p}$$

Here we will generate samples from N[0, 1] and then transform them into bivariate normal sample.

We will follow the following steps:

- 1. Using Spectral decomposition of Σ we can write: $\Sigma = U \wedge U^T$, where U is the matrix of p orthonormalized eigenvectors of Σ and $\Lambda = \text{diag}(\lambda_1, \lambda_2, ..., \lambda_p)$ is the matrix of corresponding eigenvalues of Σ .
- 2. Define A = U $\Lambda^{1/2}U^T$, which is completely specified in terms of eigenvalues and eigenvectors of Σ .
- 3. If $Z \sim N(0, I_P)$ then $AZ + \mu \sim N_P(\mu, AIA^T)$. Then we can define:

$$Y = AZ + \mu$$

Hence we have started with p univariate N(0, 1) random variables as Z_1 , Z_2 ,..., Z_P and then stacking them in a column vector and then multiplying with any non-singular matrix A and adding p-dimensional vector μ .

R code:

```
set.seed(1)
mu \leftarrow matrix(c(9, 2), nrow=2, ncol=1)
sigma \leftarrow matrix(c(8, 2.3, 2.3, 5), nrow=2, ncol=2)
u <- svd(sigma)$u
eig <- diag(eigen(sigma)$values, 2)</pre>
z \leftarrow matrix(c(rnorm(1000, 0, 1), rnorm(1000, 0, 1)), nrow=2)
a <- u %*% t(eig^0.5) %*% u
b <- a %*% z
b[1,] \leftarrow b[1,] + 9
b[2,] \leftarrow b[2,] + 2
> mean(b[1, ])
[1] 8.880603
> mean(b[2, ])
[1] 2.017876
> var(b[1, ])
[1] 9.072315
> var(b[2, ])
[1] 5.089713
> cov(b[1, ], b[2, ])
[1] 2.485204
```

MLE's are:

$$\hat{\mu} = \begin{pmatrix} 8.88060 \\ 2.01787 \end{pmatrix}$$
 and $\hat{\Sigma} = \begin{pmatrix} 9.07231 & 2.48520 \\ 2.48520 & 5.08971 \end{pmatrix}$

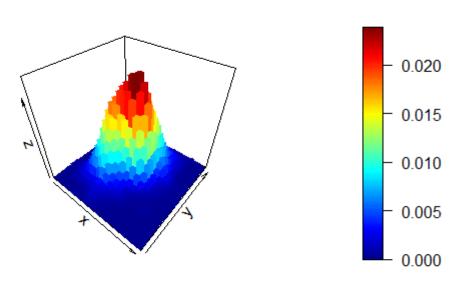
We will check validity of our random sample:

1. 3-D Histogram:

R code:

```
library(plot3D)
library(MASS)
a <- kde2d(b[1,],b[2,])
hist3D(z=a$z, main="3-D histogram")</pre>
```

3-D histogram



Question 3

(ii) Generate a random sample of size 1000 from a MOBE (5,5,2) distribution using a suitable algorithm. Suppose $\{Y_{1i}, Y_{2i}: i=1,...,1000\}$ is the generated sample then observe that the proportions of sample values in each of the three classes viz. $I_1 = \{Y_1 < Y_2\}$, $I_2 = \{Y_2 < Y_1\}$ and $I_3 = \{Y_1 = Y_2\}$ are in accordance with the model parameters.

Solution: Pdf of Marshall-Olkin Bivariate Exponential Distribution is given by:

$$f_{Y_1Y_2}(y_1, y_2) = \begin{cases} \lambda_1 e^{-\lambda_1 y_1} (\lambda_2 + \lambda_3) e^{-(\lambda_2 + \lambda_3) y_2}, & y_1 < y_2 \\ \lambda_2 e^{-\lambda_2 y_2} (\lambda_1 + \lambda_3) e^{-(\lambda_1 + \lambda_3) y_1}, & y_1 > y_2 \\ \frac{\lambda_3}{\lambda_1 + \lambda_2 + \lambda_3} e^{-(\lambda_1 + \lambda_2 + \lambda_3) y} & y_1 = y_2 = y_3 \end{cases}$$

To generate random sample from this distribution:

- 1. First generate independent samples from $X_1 \sim exp(\lambda_1)$, $X_2 \sim exp(\lambda_2)$ and $X_3 \sim exp(\lambda_3)$.
- 2. $F(x) = 1 e^{-\lambda x}$, we have used the formula:

$$x = -\frac{\log(1-u)}{\lambda}$$

3. Define: $Y_1 = \min(X_1, X_2)$ and $Y_2 = \min(X_1, X_3)$

R Code:

```
set.seed(123)
MOBE <- function(n, 11, 12, 13){
  uni 01 <- runif(n)
  uni_02 <- runif(n)
  uni_03 <- runif(n)
  x1 < -\log(uni_01)/11
  x2 < -\log(uni_02)/12
  x3 < -\log(uni \ 03)/13
  y1 < -c()
  y2 < - c()
  for(i in 1:1000){
    y1[i] <- min(x1[i], x3[i])
    y2[i] <- min(x2[i], x3[i])</pre>
  y \leftarrow rbind(y1, y2)
  return(y)
y \leftarrow MOBE(1000, 5, 5, 2)
> sum(y[1, ] < y[2,])
[1] 415
> sum(y[1, ] > y[2,])
[1] 424
> sum(y[1, ] == y[2, ])
[1] 161
```

Conclusion: The sample is generated and stored in "y". The number of sample points falling in each class is:

$$I_1 = \{Y_1 < Y_2\} = 415; I_2 = \{Y_2 < Y_1\} = 424; I_3 = \{Y_1 = Y_2\} = 161$$

Further expected number of observation in 3 classes are: 416, 416 and 166 respectively.

Question 3

(iii) Generate a random sample of size 1000 from a BBBE (5,5,2) distribution using a suitable algorithm.

Solution: The pdf of Block and Basu Bivariate Exponential Distribution is given by:

$$f_{Y_1Y_2}(y_1, y_2) = \begin{cases} \left(\frac{\lambda_2 + \lambda_3}{\lambda_1 + \lambda_2 + \lambda_3}\right)^{-1} \lambda_1 e^{-\lambda_1 y_1} (\lambda_2 + \lambda_3) e^{-(\lambda_2 + \lambda_3) y_2}, & y_1 < y_2 \\ \left(\frac{\lambda_2 + \lambda_3}{\lambda_1 + \lambda_2 + \lambda_3}\right)^{-1} \lambda_2 e^{-\lambda_2 y_2} (\lambda_1 + \lambda_3) e^{-(\lambda_1 + \lambda_3) y_1}, & y_1 > y_2 \end{cases}$$

To generate random sample from this distribution:

- 1. First generate independent samples from $X_1 \sim exp(\lambda_1)$, $X_2 \sim exp(\lambda_2)$ and $X_3 \sim exp(\lambda_3)$.
- 2. $F(x) = 1 e^{-\lambda x}$, we have used the formula:

$$x = -\frac{\log(1-u)}{\lambda}$$

3. Define: $Y_1 = \min(X_1, X_2)$ and $Y_2 = \min(X_1, X_3)$. Accept if $Y_1 \neq Y_2$ otherwise go back to step 1.

R Code:

```
set.seed(123)
BBBE <- function(n, 11, 12, 13){
  uni_01 <- runif(n)
  uni 02 <- runif(n)
  uni_03 <- runif(n)
  x1 < -\log(uni \ 01)/11
  x2 < -\log(uni_02)/12
  x3 < -\log(uni_03)/13
  y1 < - c()
  y2 < - c()
  i <- 1
  while(length(y1) < n){</pre>
    y1[i] <- min(sample(x1, 1), sample(x3, 1))</pre>
    y2[i] <- min(sample(x2, 1), sample(x3, 1))</pre>
    if(y1[i] == y2[i])
      i <- i - 1
    else i <- i + 1
  y \leftarrow rbind(y1, y2)
  return(y)
y \leftarrow BBBE(1000, 5, 5, 2)
> sum(y[1, ] < y[2,])
[1] 496
 sum(y[1, ] > y[2,])
[1] 504
 sum(y[1, ] == y[2, ])
Γ17 0
```

Conclusion: The sample is generated and stored in "y". The number of sample points falling in each class is:

$$I_1 = \{Y_1 < Y_2\} = 496; I_2 = \{Y_2 < Y_1\} = 504; I_3 = \{Y_1 = Y_2\} = 0$$

Further expected number of observation in 3 classes are: 500, 500 and 0 respectively.

Question 4.

(i) Generate a random sample of size 1000 from a Weibull (7,3) distribution using a suitable algorithm. Check **validity** of the generated random sample. Now assuming that the generated random sample is a random sample from some Weibull (α, λ) distribution, find MLEs of the parameters using the method of Profile Log Likelihood function before using the Newton-Raphson Algorithm and comment on your results.

Solution: Pdf of Weibull distribution is given by:

$$f_Y(x) = \alpha \lambda x^{\alpha - 1} e^{-\lambda x^{\alpha}}; \quad x > 0, \alpha > 0, \lambda > 0$$

$$F_Y^{-1}(u) = 1 - e^{-\lambda x^{\alpha}}$$

From the CDF we can generate random sample from Weibull(7, 3), in order to find MLE, we will use Profile Log Likelihood method, which involves Newton-Raphson method.

1. Log likelihood function is given by $I(\alpha, \lambda)$ as a function of λ in terms of α :

$$l(\alpha, \lambda) = n \ln \lambda - \lambda \sum_{i=1}^{n} x_{i}^{\alpha} + c(constant)$$

2. We will differentiate log-likelihood and equate it to zero, then we get:

$$\hat{\lambda} = \frac{n}{\sum_{i}^{n} x_{i}^{\alpha}}$$

3. Substituting the value of λ in I(α , λ) equation and call it h(α). We differentiate h(α) and get:

$$h'(\alpha) = \frac{n}{\alpha} - \frac{n}{\sum_{i}^{n} x_{i}^{\alpha}} \sum_{i}^{n} x_{i}^{\alpha} \ln x_{i} + \sum_{i}^{n} \ln x_{i}$$

$$h''(\alpha) = -\frac{n}{\alpha^{2}} - \frac{n}{\sum_{i}^{n} x_{i}^{\alpha}} \sum_{i}^{n} x_{i}^{\alpha} (\ln x_{i})^{2} + \frac{n}{(\sum_{i}^{n} x_{i}^{\alpha})^{2}} \left(\sum_{i}^{n} x_{i}^{\alpha} \ln x_{i}\right)^{2}$$

4. We use the Newton Raphson Method to maximize $h(\alpha)$ (single parameter) where we iterate:

$$\alpha^{(1)} = \alpha^{(0)} - \frac{h'(\alpha)}{h''(\alpha)}; \text{ where } \alpha = \alpha^{(0)}$$

R code:

```
set.seed(123)

rand_web <- function(n, alpha, lambda){
  webu <- (-log(runif(n))/lambda)^(1/alpha)
}

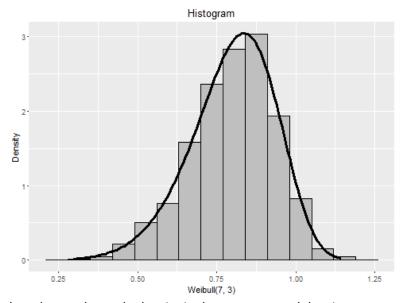
webu <- rand_web(1000, 7, 3)</pre>
```

Conclusion: "rand_web" function can be called to generate 1000 random numbers from Weibull(7, 3) distribution, the numbers generate here are given in the appendix.

We will check validity of our random sample:

1. Histogram overlaid with a theoretical frequency curve:

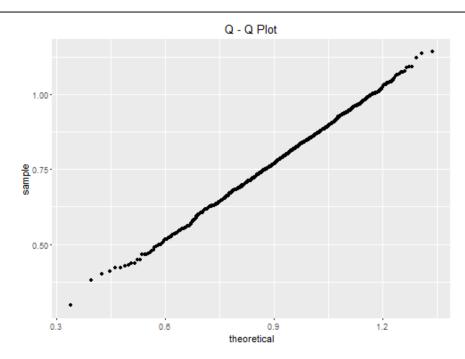
R code:



Conclusion: We see that observed sample density is close to expected density.

2. Q-Q Plot:

```
R code:
q <- ggplot(mapping = aes(sample = webu)) + ggtitle("Q - Q Plot")
q + stat_qq(distribution = stats::qweibull, dparams = list(shape=7))</pre>
```



Conclusion: We observe that sample and theoretical quantiles lies along a straight line, i.e. they coincides.

3. Chi-Square Test:

H₀: The data are consistent with the Weibull distribution. H₁: The data are not consistent with the Weibull distribution.

R code:

```
breaks <- seq(min(webu), max(webu), length = 6)
intervals <- cut(webu, breaks, right=FALSE)
observed <- table(intervals)
prob <- c()
for(i in 1:5)
    prob[i] <- pweibull(breaks[i+1], 7, 1/3^(1/7)) - pweibull(breaks[i], 7, 1/3^(1/7))
expected <- prob*1000
chisq.test(cbind(observed, expected))</pre>
```

```
Pearson's Chi-squared test

data: cbind(observed, expected)
X-squared = 0.17233, df = 4, p-value = 0.9965
```

Conclusion: We observe that p-value is insignificant, hence we conclude that data fits well to Weibull(7, 3).

4. Kolmogorov-Smirnov Test:

 H_0 : The samples are coming from the same population. H_1 : The samples are not coming from the same population.

R Code:

Output:

```
ks.test(webu, "pweibull", 7, 1/3^(1/7))
```

Output:

```
One-sample Kolmogorov-Smirnov test
```

data: webu D = 0.014051, p-value = 0.9891 alternative hypothesis: two-sided

Conclusion: We observe that p-value is insignificant, hence we conclude that data is coming from Weibull (7, 3).

To find MLE using Profile Log Likelihood:

R Code:

```
# Initial guess for the parameter
al <- 8
d <- 1
n <- 1000
while(d > 0.00001){
  ao <- al
  h1 \leftarrow n/al-(n/sum(webu^al))*sum(webu^al*log(webu)) + sum(log(webu))
  h2 <- -(n/a1^2) - n*(sum((webu^a1)*log(webu)^2)/sum(webu^a1))+
            n*sum((webu^al)*log(webu))^2/(sum(webu^al))^2
  al \leftarrow ao - h1/h2
  d \leftarrow abs(al - ao)
}
> alpha_hat <- al</pre>
> alpha_hat
[1] 7.054301
 lambda_hat <- n/sum(webu^alpha_hat)</pre>
> lambda_hat
[1] 2.996589
```

Conclusion: The MLE of the parameters is given by: $\hat{a} = 7.0543$ and $\hat{\lambda} = 2.99658$.

All the validity test holds true, hence we conclude that our random number generator is a valid generator in generating random sample from Weibull(7, 3).

Question 4

(ii) Generate a random sample of size 1000 from the following mixture of two distributions:

$$f_X(x; \boldsymbol{\theta}) = \pi f_0(x; \boldsymbol{\theta_0}) + (1 - \pi) f_1(x; \boldsymbol{\theta_1})$$

where $\pi=\frac{2}{5}$ and, f_0 and f_1 are defined the density functions of N(3,2) and N(10,3) distributions respectively. Clearly $\boldsymbol{\theta_0}=(3,2)^T$, $\boldsymbol{\theta_1}=(10,3)^T$ and $\boldsymbol{\theta}=\left[\frac{2}{5},(3,2)^T(10,3)^T\right]^T$. Now assuming that the generated random sample is a random sample from some mixture of two normal distributions with unknown parameters, find the MLEs of the parameters viz., $\pi,\boldsymbol{\theta_0}=(\mu_0,\sigma_0^2)$ and $\boldsymbol{\theta_1}=(\mu_1,\sigma_1^2)$ using the Expectation-Maximization (EM) Algorithm.

Solution:

To generate the sample from the mixture of 2 distributions, we first generate the required number of samples from the two univariate normal distributions independently. Then we generate the mixture by taking proportion of data coming from $f_0(x;\theta_0)$ to be equal to π and that from $f_1(x;\theta_1)$ to be equal to π .

```
set.seed(123)
rand_snormal <- function(n){</pre>
  uni 01 <- runif(2*n)
  y1 <- uni 01[1:n]
  y2 <- uni_01[n+1:1000]
  y < -c(y1, y2)
  x \leftarrow c()
  for(i in 1:n){  # Random number from double exponential(1)
    x[i] \leftarrow -\log(1-y1[i])
    x[n + i] < -log(1-y2[i])
  p \leftarrow c()
  i<-1
  while(length(p) < 1000){  # Acceptance/Rejection condition</pre>
    U = sample(uni 01, 1)
    z = sample(x, 1)
    if(exp(-abs(z))*1.315*U/2 <= dnorm(z, 0, 1)){
      p[i] \leftarrow z
      i <- i+1
    }
    else i <- i-1
  return(p)
> rn1 <- rand_snormal(1000)*sqrt(2) + 3
> c(mean(rn1), var(rn1))
[1] 3.009182 1.929094
> rn2 <- rand_snormal(1000)*sqrt(3) + 10</pre>
> c(mean(rn2), var(rn2))
[1] 10.083094 2.975097
```

Conclusion: We have generated 2 samples from N(3,2) and N(10,3) distribution in "rn1" and "rn2" respectively.

Then from the mixture we try to find MLE of parameters by using Expectation-Maximization (EM) Algorithm:

1. A initial guess is made about the parameters:

$$\theta^t = (\pi^t, \mu_0^t, \mu_1^t, \Sigma_0^t, \Sigma_1^t)^T$$

- $\text{2. Next we calculate } \delta_i^{\ t} = \frac{f_1\!\left(x_i\,; \theta_1^{\ t}\right) x \left(1-\pi^t\right)}{f_1\!\left(x_i\,; \theta_1^{\ t}\right) x \left(1-\pi^t\right) + f_0\!\left(x_i\,; \theta_0^{\ t}\right) x \left(\pi^t\right)}$
- 3. The next iterate of the parameter vector is obtained as:

$$\hat{\pi}^{(t+1)} = \frac{1}{n} \sum_{i=1}^{n} (1 - \delta_i^t)$$

$$\hat{\mu_0}^{(t+1)} = \frac{1}{\sum_{i=1}^{n} (1 - \delta_i^t)} \sum_{i=1}^{n} (1 - \delta_i^t) x_i$$

$$\widehat{\mu_1}^{(t+1)} = \frac{1}{\sum_{i=1}^n \delta_i^t} \sum_{i=1}^n \delta_i^t x_i$$

$$\widehat{\Sigma_0}^{(t+1)} = \frac{1}{\sum_{i=1}^n (1 - \delta_i^t)} \sum_{i=1}^n (1 - \delta_i^t) (x_i - \widehat{\mu_0}^{(t+1)}) (x_i - \widehat{\mu_0}^{(t+1)})^T$$

$$\widehat{\Sigma_1}^{(t+1)} = \frac{1}{\sum_{i=1}^n \delta_i^t} \sum_{i=1}^n \delta_i^t (x_i - \widehat{\mu_1}^{(t+1)}) (x_i - \widehat{\mu_1}^{(t+1)})^T$$

After this we will get new parameters:

$$\widehat{\theta}^{(t+1)} = (\,\widehat{\pi}^{(t+1)}\,,\,\widehat{\mu_0}^{(t+1)}\,,\,\widehat{\mu_1}^{(t+1)}\,,\,\widehat{\varSigma_0}^{(t+1)},\widehat{\varSigma_1}^{(t+1)})$$

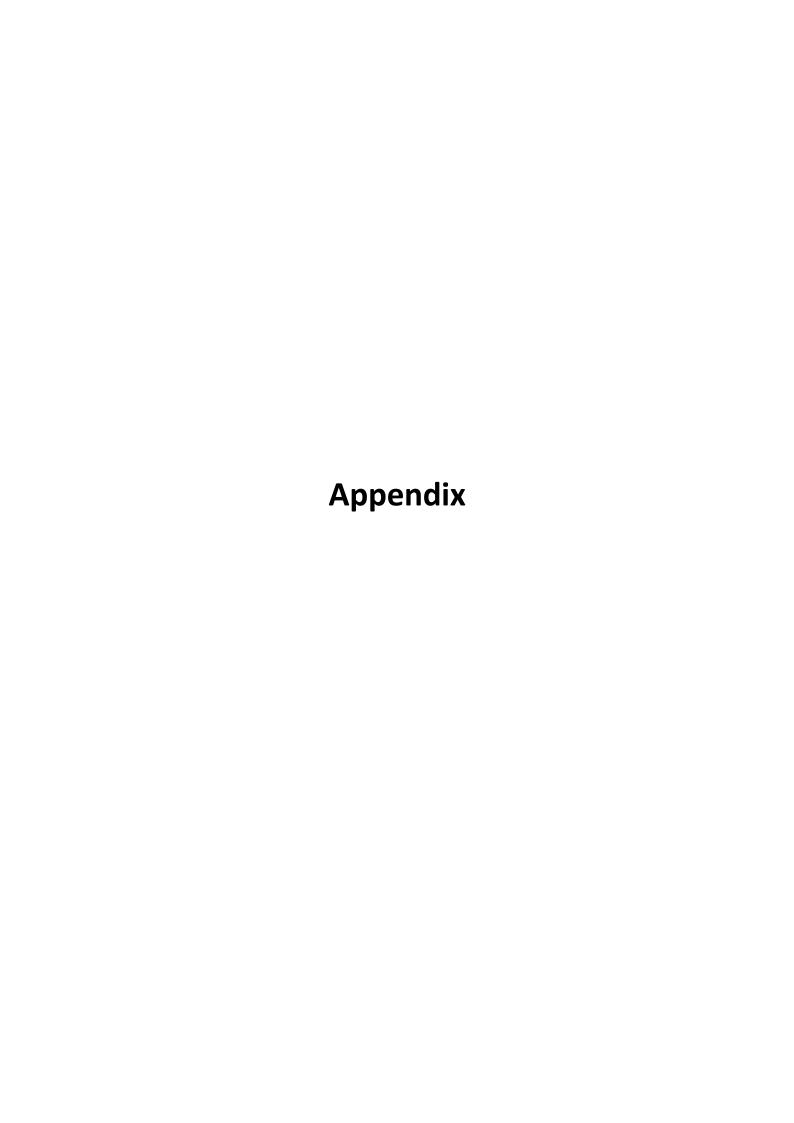
4. We will repeat this procedure till convergence criteria is satisfied i.e.

 $|\hat{\theta}^{(t+1)} - \hat{\theta}^{\hat{t}}| < \epsilon|$, for some pre-specified threshold ϵ .

R Code:

```
x <- c(sample(rn1, 400), sample(rn2, 600))</pre>
p < -0.4
m1 < -6
m2 < -18
v1 <- 4
v2 <- 8
d \leftarrow rep(1, 5)
a <- 0.00001
i <- 0
while(sum(d > a) > 0){
  d1 \leftarrow c(p, m1, m2, v1, v2)
  delta <- (dnorm(x, m2, sqrt(v2))*(1-p))/(dnorm(x, m1, sqrt(v2))*p +
                                              dnorm(x, m2, sqrt(v2))*(1-p))
  p <- sum(1 - delta)/1000</pre>
  m1 \leftarrow sum((1-delta)*x)/sum(1-delta)
  m2 <- sum((delta)*x)/sum(delta)</pre>
  v1 \leftarrow sum((1-delta)*(x-m1)^2)/sum(1-delta)
  v2 \leftarrow sum((delta)*(x-m2)^2)/sum(delta)
  d2 \leftarrow c(p, m1, m2, v1, v2)
  d \leftarrow abs(d2 - d1)
  d1 <- d2
  i <- i+1
 # Number of iterations performed:
[1] 13
> # Parameter estimates are:
> d1
    0.4109478 3.0905900 10.1426955 2.3751448 2.8903687
```

Conclusion: MLE'S of the parameters obtained by EM algorithm are very close to the actual parameters, hence EM algorithm is a valid technique to obtain MLE of parameters from a mixture of 2 distributions.



Random Numbers from U[0, 1]

```
[1] 0.000028 0.000651 0.014965 0.344204 0.916702 0.084143 0.935300 0.511896 0.773599
[10] 0.792788 0.234130 0.384995 0.854881 0.662265 0.232097 0.338222 0.779107 0.919454
[19] 0.147439 0.391097 0.995236 0.890435 0.479997 0.039940 0.918630 0.128487 0.955212
[28] 0.969872 0.307047 0.062092 0.428122 0.846811 0.476649 0.962929 0.147369 0.389478
[37] 0.957995 0.033878 0.779191 0.921393 0.192044 0.417019 0.591429 0.602876 0.866158
[46] 0.921631 0.197524 0.543048 0.490095 0.272196 0.260514 0.991827 0.812017 0.676393
[55] 0.557041 0.811934 0.674483 0.513102 0.801343 0.430889 0.910452 0.940403 0.629261
[64] 0.473012 0.879286 0.223575 0.142236 0.271424 0.242743 0.583100 0.411306 0.460043
[73] 0.580985 0.362657 0.341113 0.845590 0.448571 0.317126 0.293895 0.759585 0.470460
[82] 0.820587 0.873493 0.090348 0.078014 0.794319 0.269348 0.195000 0.484991 0.154804
[91] 0.560498 0.891459 0.503553 0.581721 0.379585 0.730446 0.800259 0.405950 0.336847
[100] 0.747481 0.192068 0.417571 0.604125 0.894884 0.582342 0.393863 0.058860 0.353776
[109] 0.136839 0.147308 0.388090 0.926075 0.299721 0.893585 0.552457 0.706502 0.249547
[118] 0.739574 0.010199 0.234577 0.395276 0.091355 0.101157 0.326620 0.512270 0.782207
[127] 0.990772 0.787752 0.118287 0.720612 0.574082 0.203891 0.689489 0.858249 0.739729
[136] 0.013758 0.316435 0.277998 0.393951 0.060873 0.400084 0.201939 0.644589 0.825556
[145] 0.987798 0.719351 0.545084 0.536928 0.349335 0.034716 0.798474 0.364907 0.392857
[154] 0.035713 0.821401 0.892214 0.520923 0.981222 0.568103 0.066369 0.526492 0.109323
[163] 0.514421 0.831692 0.128926 0.965295 0.201796 0.641304 0.749983 0.249620 0.741266
[172] 0.049123 0.129825 0.985977 0.677473 0.581870 0.383011 0.809246 0.612655 0.091065
[181] 0.094500 0.173507 0.990653 0.785028 0.055654 0.280039 0.440908 0.140880 0.240231
[190] 0.525324 0.082458 0.896539 0.620393 0.269041 0.187945 0.322726 0.422699 0.722070
[199] 0.607607 0.974961 0.424108 0.754491 0.353285 0.125564 0.887982 0.423583 0.742420
[208] 0.075656 0.740079 0.021828 0.502050 0.547155 0.584561 0.444905 0.232817 0.354782
[217] 0.159987 0.679694 0.632959 0.558057 0.835316 0.212275 0.882317 0.293300 0.745910
[226] 0.155927 0.586332 0.485632 0.169527 0.899132 0.680042 0.640971 0.742329 0.073569
[235] 0.692089 0.918038 0.114875 0.642118 0.768711 0.680353 0.648124 0.906859 0.857749
[244] 0.728236 0.749438 0.237071 0.452644 0.410808 0.448575 0.317236 0.296434 0.817987
[253] 0.813697 0.715033 0.445761 0.252494 0.807363 0.569342 0.094863 0.181849 0.182532
[262] 0.198243 0.559581 0.870372 0.018566 0.427015 0.821356 0.891184 0.497223 0.436140
[271] 0.031226 0.718203 0.518665 0.929297 0.373833 0.598150 0.757451 0.421366 0.691415
[280] 0.902545 0.758540 0.446427 0.267813 0.159708 0.673294 0.485759 0.172468 0.966760
[289] 0.235471 0.415844 0.564418 0.981619 0.577233 0.276361 0.356305 0.195006 0.485139
[298] 0.158190 0.638367 0.682441 0.696148 0.011411 0.262445 0.036244 0.833622 0.173303
[307] 0.985980 0.677536 0.583319 0.416348 0.576010 0.248235 0.709401 0.316225 0.273177
[316] 0.283062 0.510427 0.739814 0.015719 0.361537 0.315356 0.253195 0.823477 0.939980
[325] 0.619550 0.249647 0.741892 0.063512 0.460767 0.597652 0.746002 0.158051 0.635169
[334] 0.608889 0.004449 0.102318 0.353315 0.126238 0.903471 0.779833 0.936164 0.531779
[343] 0.230909 0.310916 0.151078 0.474791 0.920204 0.164688 0.787815 0.119756 0.754394
[352] 0.351067 0.074537 0.714353 0.430121 0.892774 0.533803 0.277462 0.381623 0.777329
[361] 0.878572 0.207163 0.764741 0.589052 0.548206 0.608735 0.000916 0.021064 0.484463
[370] 0.142660 0.281186 0.467283 0.747505 0.192617 0.430193 0.894430 0.571891 0.153486
[379] 0.530175 0.194025 0.462580 0.639347 0.704973 0.214388 0.930934 0.411479 0.464028
[388] 0.672640 0.470711 0.826364 0.006378 0.146699 0.374073 0.603681 0.884665 0.347286
[397] 0.987579 0.714310 0.429127 0.869921 0.008188 0.188331 0.331605 0.626924 0.419262
[406] 0.643023 0.789540 0.159416 0.666559 0.330868 0.609970 0.029315 0.674241 0.507545
[415] 0.673537 0.491342 0.300867 0.919934 0.158479 0.645017 0.835396 0.214115 0.924637
[424] 0.266660 0.133190 0.063367 0.457452 0.521392 0.992007 0.816172 0.771962 0.755131
[433] 0.368009 0.464209 0.676809 0.566598 0.031755 0.730358 0.798231 0.359313 0.264204
[442] 0.076699 0.764069 0.573596 0.192718 0.432511 0.947764 0.798568 0.367055 0.442276
[451] 0.172354 0.964147 0.175377 0.033673 0.774481 0.813054 0.700243 0.105582 0.428383
[460] 0.852809 0.614612 0.136083 0.129901 0.987732 0.717846 0.510455 0.740476 0.030944
[469] 0.711703 0.369180 0.491146 0.296363 0.816345 0.775937 0.846553 0.470710 0.826331
[478] 0.005606 0.128935 0.965505 0.206620 0.752267 0.302133 0.949068 0.828574 0.057199
[487] 0.315588 0.258520 0.945951 0.756884 0.408338 0.391779 0.010913 0.251001 0.773025
[496] 0.779566 0.930019 0.390430 0.979887 0.537401 0.360228 0.285251 0.560765 0.897604
[505] 0.644902 0.832743 0.153100 0.521296 0.989799 0.765388 0.603930 0.890395 0.479081
[514] 0.018865 0.433897 0.979622 0.531307 0.220054 0.061239 0.408497 0.395436 0.095035
[523] 0.185797 0.273340 0.286830 0.597087 0.733012 0.859272 0.763247 0.554692 0.757922
[532] 0.432211 0.940849 0.639529 0.709169 0.310878 0.150195 0.454478 0.452991 0.418793
[541] 0.632244 0.541619 0.457229 0.516276 0.874358 0.110231 0.535324 0.312448 0.186295
[550] 0.284796 0.550314 0.657227 0.116217 0.672993 0.478841 0.013334 0.306683 0.053702
[559] 0.235143 0.408289 0.390652 0.985003 0.655061 0.066412 0.527486 0.132175 0.040036
[568] 0.920824 0.178943 0.115700 0.661106 0.205443 0.725185 0.679257 0.622913 0.326990
[577] 0.520771 0.977726 0.487695 0.216985 0.990660 0.785187 0.059293 0.363748 0.366214
[586] 0.422919 0.727148 0.724400 0.661191 0.207404 0.770298 0.716859 0.487753 0.218321
[595] 0.021385 0.491846 0.312459 0.186550 0.290647 0.684881 0.752268 0.302171 0.949925
[604] 0.848284 0.510542 0.742463 0.076660 0.763176 0.553039 0.719908 0.557890 0.831475
```

```
[613] 0.123921 0.850185 0.554257 0.747902 0.201747 0.640174 0.723999 0.651977 0.995476
 [622] 0.895955 0.606957 0.960020 0.080470 0.850807 0.568572 0.077152 0.774487 0.813212
 [631] 0.703882 0.189291 0.353689 0.134849 0.101529 0.335158 0.708635 0.298598 0.867751
 [640] 0.958273 0.040284 0.926539 0.310389 0.138956 0.195998 0.507951 0.682884 0.706328
 [649] 0.245535 0.647316 0.888274 0.430307 0.897057 0.632313 0.543201 0.493614 0.353123
 \begin{bmatrix} 658 \end{bmatrix} 0.121822 0.801903 0.443769 0.206692 0.753923 0.340221 0.825092 0.977126 0.473895
 [667] 0.899596 0.690704 0.886183 0.382220 0.791066 0.194523 0.474025 0.902577 0.759273
 [676] 0.463270 0.655211 0.069846 0.606455 0.948465 0.814700 0.738107 0.976453 0.458428
 [685] 0.543854 0.508639 0.698708 0.070280 0.616431 0.177924 0.092258 0.121939 0.804593
 [694] 0.505641 0.629745 0.484126 0.134899 0.102670 0.361407 0.312361 0.184308 0.239091
 [703] 0.499085 0.478964 0.016182 0.372183 0.560220 0.885056 0.356279 0.194428 0.471850
 [712] 0.852555 0.608761 0.001505 0.034617 0.796182 0.312187 0.180294 0.146759 0.375457
 [721] 0.635516 0.616875 0.188117 0.326700 0.514110 0.824527 0.964132 0.175032 0.025727
 [730] 0.591732 0.609842 0.026371 0.606529 0.950169 0.853889 0.639438 0.707075 0.262718
 [739] 0.042511 0.977753 0.488324 0.231459 0.323549 0.441636 0.157638 0.625671 0.390444
 [748] 0.980208 0.544775 0.529836 0.186234 0.283387 0.517897 0.911633 0.967561 0.253894
 [757] 0.839563 0.309942 0.128663 0.959249 0.062732 0.442843 0.185381 0.263772 0.066766
 [766] 0.535615 0.319156 0.340584 0.833423 0.168740 0.881026 0.263603 0.062865 0.445897
 [775] 0.255633 0.879550 0.229651 0.281966 0.485215 0.159945 0.678740 0.611027 0.053613
 [784] 0.233108 0.361494 0.314359 0.230268 0.296160 0.811671 0.668444 0.374218 0.607019
 [793] 0.961433 0.112961 0.598105 0.756406 0.397339 0.138790 0.192167 0.419841 0.656348
 [802] 0.096011 0.208245 0.789644 0.161822 0.721903 0.603780 0.886936 0.399519 0.188948
 [811] 0.345810 0.953635 0.933601 0.472825 0.874977 0.124462 0.862627 0.840414 0.329519
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Random Numbers from Multivariate Normal

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1.78142

Random Numbers from MOBE(5, 5, 2)

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y2 0.25920 0.10422 0.36629 0.03170 0.03304 0.14768 0.05132 0.24388 0.54475 0.16395 0.08069
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y1 0.15823 0.07785 0.11150 0.00394 0.02111 0.14159 0.63373 0.22300 0.00931 0.00129 0.07340
y2 0.21521 0.25658 0.13585 0.00394 0.05132 0.11608 0.08880 0.15167 0.25515 0.00129 0.04645
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y1 0.00116 0.00115 0.08441 0.06891 0.12174 0.10413 0.24816 0.15792 0.00754 0.02056 0.07401
y2 0.00116 0.18590 0.04184 0.22879 0.10845 0.15728 0.26275 0.11769 0.27740 0.12204 0.16078
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y2 0.40760 0.09505 0.12030 0.24518 0.02501 0.02048 0.1473 0.03647 0.06582 0.15666 0.1303
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y1 0.04222 0.04897 0.10197 0.15273 0.26487 0.03067 0.26348 0.16320 0.02518 0.42091 0.04087
y2 0.04222 0.04897 0.10197 0.80534 0.02843 0.00148 0.06882 0.03806 0.02288 0.12346 0.04087
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y1 0.31546 0.20569 0.05666 0.02218 0.19645 0.08156 0.08049 0.19144 0.08932 0.04100 0.16036
y2 0.25715 0.08335 0.12165 0.13419 0.06688 0.06362 0.08049 0.23663 0.08932 0.51092 0.06761
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y1 0.04213 0.04156 0.04605 0.03432 0.05635 0.04532 0.06845 0.45779 0.14875 0.13224 0.19361
y2 0.11923 0.39922 0.00524 0.03432 0.04755 0.03276 0.02601 0.04451 0.08921 0.09275 0.26083
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y1 0.09795 0.01741 0.43940 0.28243 0.08068 0.15887 0.04760 0.38332 0.16653 0.00303 0.00481
y2 0.46506 0.01741 0.20688 0.18713 0.18060 0.15887 0.17659 0.05506 0.22149 0.43155 0.00481
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y2 0.04292 0.14674 0.04307
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y2 0.32198 0.04440 0.06356 0.30553 0.01845 0.02862 0.12720 0.10262 0.01288 0.01011 0.08294
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y2 0.16382 0.03815 0.14698 0.18769 0.24138 0.28186 0.13518 0.01285 0.17020 0.08665 0.03584
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y2 0.20618 0.06609 0.23198 0.07089 0.56936 0.01428 0.11301 0.41567 0.03559 0.12314 0.03977
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y1 0.07920 0.06101 0.13035
y2 0.07049 0.11322 0.06534 0.05689 0.19277 0.10468 0.01917 0.26969 0.03683 0.18059 0.51787
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y2 0.00947 0.30540 0.18047 0.09379 0.09291 0.22280 0.17332 0.01784 0.01772 0.05764 0.01690
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y2 0.12744 0.19778
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y2 0.00174 0.07393 0.00499 0.14698 0.00559 0.17807 0.18235 0.08660 0.01748 0.09875 0.12030
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y2 0.06569 0.08574 0.47289
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y1 0.11433 0.01816 0.02066 0.19906 0.22696 0.00289 0.0361 0.01295 0.12354 0.17987 0.08334
y2 0.04753 0.07337 0.10408 0.19906 0.11773 0.15996 0.0361 0.08069 0.12354 0.02529 0.26266
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           0.11142 0.09913
                            0.00767 0.10171 0.13271 0.18198 0.02551 0.20207 0.17314 0.28664
y1 0.37632
y2 0.00639 0.19080 0.03049 0.02390 0.11892 0.06623 0.14402 0.00227 0.54744 0.17314 0.04833
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y1 0.35185 0.14594 0.19821 0.30626 0.07879 0.3142 0.07109 0.20889 0.17884 0.03946 0.01692
y2 0.12243 0.17515 0.00022 0.27277 0.13550 0.3142 0.04124 0.19237 0.04408 0.28631 0.01102
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y1 0.25280 0.00793 0.06338 0.07527 0.00385 0.18566 0.14769 0.11587 0.07183 0.01762 0.09614
y2 0.21245 0.13000 0.09271 0.02421 0.00385 0.64188 0.14120 0.29739 0.03044 0.12662 0.11448
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y1 0.07608 0.12247 0.21678 0.26876 0.18469 0.02966 0.03680 0.37561 0.01674 0.12072 0.08240
  0.07608 0.22466 0.10597 0.27751 0.38164 0.02966 0.07027 0.01258 0.01674 0.50895 0.21224
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y1 0.35240 0.01562 0.04249 0.06444 0.18379 0.00622 0.00663 0.06385 0.00036 0.00652 0.10450
```

```
y2 0.09403 0.01562 0.04249 0.07069 0.11217 0.12357 0.33139 0.06374 0.00036 0.00652 0.11322
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    [,254]
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y1 0.13572 0.12657 0.04834 0.24075 0.18107 0.15033 0.00911 0.01544 0.02512 0.07885 0.01022
y2 0.13572 0.38790 0.02878 0.24075 0.28165 0.00373 0.00911 0.18695 0.07414 0.38642 0.38425
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    [,265]
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y1 0.13216 0.11015 0.21793 0.05501 0.78216 0.13751 0.02761 0.58259 0.52606 0.36132 0.05100
y2 0.07046 0.54496 0.09503 0.01294 0.48632 0.00551 0.70524 0.06425 0.15806 0.11377 0.02723
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y1 0.02072 0.00571 0.15251 0.41315 0.08652 0.05526 0.05455 0.18497 0.29834 0.31971 0.18532
y2 0.02072 0.02942 0.09460 0.23357 0.18720 0.31981 0.03185 0.09990 0.05592 0.11507 0.25754
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y1 0.30939 0.29754 0.24379 0.08001 0.24231 0.05184 0.52648 0.02547 0.05641 0.04052 0.00360
y2 0.06143 0.11983 0.21219 0.13273 0.04073 0.05184 0.31887 0.03295 0.06144 0.23859 0.05212
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y1 0.06597 0.23977 0.04492 0.04852 0.0559 0.04993 0.06311 0.09237 0.14641 0.28219 0.1991
y2 0.06200 0.03513 0.07698 0.36982 0.0559 0.12225 0.03567 0.06331 0.11772 0.28219 0.1991
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y1 0.04212 0.14174 0.18853 0.15329 0.06758 0.22501 0.20725 0.04393 0.03590 0.20522 0.20770
y2 0.04212 0.46127 0.30188 0.20104 0.03340 0.22501 0.06995 0.10027 0.04993 0.20522 0.12028
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y1 0.03089 0.03162 0.24355 0.38340 0.07020 0.37359 0.67789 0.00012 0.67120 0.21671 0.01775
y2 0.26648 0.04311 0.21709 0.01749 0.17943 0.00499 0.19123 0.14321 0.14235 0.67802 0.08880
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y1 0.09650 0.25015 0.06082 0.03629 0.12625 0.14163 0.07209 0.02755 0.03581 0.00448 0.17602
                           0.09647 0.12625 0.35396 0.06707 0.02755 0.03394 0.04090 0.21544
y2 0.13366 0.22767 0.10845
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y1 0.42505 0.04708 0.04057 0.14414 0.19873 0.00336 0.18919 0.29459 0.09455 0.12493 0.00661
y2 0.15683 0.04708 0.04057 0.08474 0.00914 0.24683 0.08610 0.12459 0.10302 0.12493 0.09699
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y1 0.13269 0.15737 0.09499 0.00283 0.08046 0.17402 0.22581 0.03600 0.29914 0.16862 0.02180
y2 0.40593 0.15737 0.35062 0.14865 0.32526 0.04099 0.28207 0.14316 0.08650 0.16862 0.03559
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y1 0.05508 0.20250 0.04868 0.32862 0.20451 0.15869 0.14548 0.06466 0.21412 0.02866 0.15744
y2 0.05508 0.29092 0.24156 0.36724 0.10703 0.15869 0.27980 0.06466 0.33867 0.18051 0.09770
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y1 0.12556 0.00737 0.03896 0.31320 0.23502 0.00582 0.10726 0.05467 0.00983 0.05248 0.00712
y2 0.07547 0.03883 0.03896 0.00966 0.79444 0.02923 0.15376 0.20728 0.00983 0.48704 0.00712
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y1 0.01799 0.28793 0.11511 0.47085 0.17075 0.00463 0.24328 0.06405 0.04824 0.03797 0.00236
y2 0.33403 0.28793 0.02796 0.55991 0.17075 0.00140 0.07766 0.16626 0.19494 0.03797 0.00236
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v1 0.26146 0.30331 0.21895 0.00176 0.00281 0.24739 0.01990 0.04378 0.10985 0.15979 0.06949
y2 0.08221 0.15271 0.21895 0.05207 0.15577 0.24739 0.55701 0.04378 0.10985 0.05537 0.12055
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y1 0.20958 0.15345 0.0769 0.07332 0.03689 0.30726 0.13945 0.0719 0.33003 0.01013 0.22681
y2 0.01067 0.15345 0.0107 0.06504 0.01624 0.09760 0.36531 0.0719 0.06289 0.10569 0.23264
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y1 0.14744 0.54055 0.12049 0.08794 0.10341 0.22668 0.02306 0.09360 0.23887 0.08366 0.36592
y2 0.05155 0.21795 0.03117 0.09336 0.17555 0.01396 0.15414 0.35086 0.15295 0.00321 0.01553
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y1 0.02957 0.00961 0.11467 0.22201 0.00068 0.28979 0.09799 0.44479 0.14388 0.46163 0.11282
y2 0.14359 0.02792 0.24056 0.04514 0.04450 0.18990 0.19268 0.08754 0.02978 0.08413 0.11282
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y1 0.20579 0.10761 0.06247 0.35973 0.02867 0.0689 0.05478 0.38335 0.20541 0.07910 0.10894
y2 0.20579 0.09795 0.63418 0.13929 0.06035 0.0565 0.55263 0.16307 0.13836 0.26169 0.10256
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y1 0.21008 0.28498 0.12834 0.06549 0.00605 0.04169 0.05820 0.22201 0.39857 0.00512 0.16596
y2 0.06135 0.06749 0.12834 0.06549 0.00605 0.21170 0.06436 0.03534 0.39857 0.00838 0.05813
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y1 0.01285 0.36000 0.10725 0.26129 0.29385 0.07386 0.25257 0.04205 0.47307 0.03920 0.16999
y2 0.01285 0.33223 0.41648 0.02929 0.01685 0.39664 0.14778 0.15402 0.07128 0.54491 0.06211
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y1 0.05597 0.08238 0.16215 0.09332 0.88874 0.08502 0.06995 0.30727 0.04118 0.11792 0.07487
y2 0.18530 0.15466 0.06423 0.14229 0.00010 0.03346 0.03770 0.05446 0.43766 0.03511 0.04120
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y1 0.01394 0.43121 0.41161 0.07766 0.16928 0.03621 0.00580 0.53046 0.15540 0.04406 0.17236
y2 0.00172 0.60600 0.05839 0.17383 0.10821 0.03709 0.14893 0.66903 0.00071 0.04406 0.17236
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y1 0.00142 0.04172 0.60100 0.07528 0.04792 0.07919 0.20078 0.15508 0.50521 0.20132 0.34518
y2 0.04165 0.00176 0.32113 0.08738 0.16531 0.01280 0.00241 0.15508 0.29340 0.07263 0.11717
```

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y1 0.12470 0.12054 0.01131 0.21499 0.15327 0.49892 0.03014 0.18544 0.06133 0.23330 0.15760
y2 0.10733 0.12054 0.05173 0.10322 0.15878 0.00887 0.03382 0.30032 0.16213 0.17351 0.39663
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y1 0.05222 0.31791 0.04089 0.13020 0.20175 0.12786 0.65738 0.13125
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y2 0.19328 0.17238 0.33065 0.06982 0.22707 0.06261 0.16753 0.06260
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y1 0.00220 0.02579 0.01256 0.07491 0.16102 0.04055 0.03948 0.06048 0.21070 0.03745 0.06972
y2 0.08806 0.02579 0.03644 0.07284 0.02127 0.17626 0.03948 0.27725 0.19682 0.12281 0.01417
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y1 0.05182 0.04439 0.47797 0.03676 0.13755 0.05671 0.00730 0.47108 0.02199 0.04407 0.19081
y2 0.05182 0.10451 0.05136 0.15752 0.11852 0.07821 0.04824 0.47108 0.02199 0.09882 0.00485
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y1 0.22319 0.31701 0.11264 0.02374 0.09484 0.10656 0.08137 0.12702 0.13473 0.72943 0.57905
y2 0.00613 0.48499 0.13928 0.18543 0.09484 0.22883 0.07638 0.25132 0.18827 0.00198 0.04664
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y1 0.01465 0.05246 0.32081 0.08608 0.08500 0.18565 0.04158 0.12065 0.02440 0.11837 0.01973
y2 0.07144 0.04039 0.30200 0.13820 0.09112 0.42462 0.02160 0.47350 0.02899 0.25704 0.31524
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y2 0.04781 0.20508 0.73695 0.05858 0.70382 0.16700 0.27203 0.13629 0.08513 0.49621 0.01942
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y1 0.19999 0.02695 0.28554 0.03505 0.08108 0.00458 0.10800 0.12827 0.11362 0.00629 0.42366
y2 0.45179 0.04155 0.09320 0.03505 0.09921 0.16775 0.21075 0.04625 0.02400 0.08581 0.10456
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y1 0.48526 0.02539 0.13531 0.12599 0.02234 0.60712 0.28775 0.07523 0.29760 0.06053 0.34976
y2 0.22306 0.08592 0.10506 0.12599 0.05986 0.24492 0.08951 0.23873 0.27309 0.03955 0.04369
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y1 0.04427 0.22435 0.03903 0.20435 0.19661 0.09249 0.46737 0.76340 0.00140 0.10759 0.04923
y2 0.61654 0.02658 0.41113 0.09924 0.15119 0.11693 0.06283 0.15106 0.00229 0.00309 0.15038
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y1 0.02288 0.05624 0.00420 0.03288 0.02032 0.02889 0.05087 0.17956 0.13511 0.20189 0.25911
y2 0.09924 0.21256 0.16551 0.03288 0.04699 0.74697 0.56686 0.05369 0.13511 0.03231 0.10835
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y1 0.03239 0.20300 0.23783 0.05512 0.03372 0.15621 0.06304 0.45252 0.30284 0.00943 0.05699
y2 0.33545 0.09917 0.02256 0.04605 0.13700 0.17206 0.08481 0.02382 0.02285 0.05430 0.24295
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y1 0.03995 0.17456 0.10423 0.02831 0.02366 0.19080 0.01449 0.09376 0.00017 0.49213 0.24045
y2 0.22259 0.04534 0.44230 0.02831 0.05200 0.01159 0.01449 0.01241 0.00017 0.02680 0.18605
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y1 0.09737 0.05676 0.01732 0.05848 0.11344 0.06114 0.03076 0.01905 0.17180 0.13747 0.20965
y2 0.46112 0.11015 0.06360 0.05848 0.19209 0.68860 0.13023 0.42226 0.02439 0.51900 0.04861
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y1 0.03355 0.04303 0.15519 0.06774 0.28941 0.18964 0.01330 0.30610 0.08706 0.35030 0.78167
y2 0.03153 0.64918 0.15519 0.08861 0.04839 0.18323 0.01338 0.18806 0.17162 0.25006 0.09829
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                                                                                       Γ.6821
y1 0.13028 0.11227 0.25246 0.17329 0.10645 0.04296 0.0789 0.15556 0.16053 0.06192 0.06716
y2 0.11639 0.11227 0.05880 0.31550 0.08417 0.12986 0.0789 0.09639 0.25113 0.29939 0.12360
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y2 0.00073 0.03626 0.22581 0.15783 0.12864 0.03081 0.05966 0.0057 0.14282 0.49709 0.26947
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                                                                               [,703]
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y1 0.26874 0.20901 0.00192 0.36033 0.10137 0.16944 0.00725 0.03370 0.16135 0.75320 0.02961
y2 0.02674 0.03202 0.00192 0.01091 0.08533 0.14342 0.00725 0.06765 0.16135 0.15478 0.01325
    [,705]
                                                               [,712]
            [,706]
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                                             [,710]
                                                      [,711]
                                                                       [,713]
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y1 0.21897 0.04217 0.10416 0.07767 0.10121 0.16929 0.01135 0.13046 0.08322 0.06312 0.14397
y2 0.03361 0.04217 0.10416 0.07767 0.00204 0.09709 0.01135 0.34721 0.34800 0.02705 0.20277
    [,716]
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y1 0.04861 0.75453 0.60590 0.00102 0.28403 0.01456 0.06629 0.05954 0.02739 0.06795 0.05016
y2 0.01118 0.11656 0.13363 0.01073 0.28403 0.01456 0.19492 0.11717 0.04421 0.06795 0.04971
    [,727]
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y1 0.03315 0.09795 0.04633 0.75572 0.17497 0.02673 0.05041 0.01570 0.10566 0.23052 0.04357
y2 0.12501 0.08445 0.16641 0.32476 0.00107 0.12591 0.05041 0.01301 0.02763 0.10175 0.19386
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y1 0.00222 0.19037 0.08269 0.00157 0.38163 0.60171 0.10305 0.05134 0.11404 0.04578 0.53493
y2 0.04231 0.00981 0.03202 0.41223 0.00632 0.11700 1.04559 0.05134 0.11404 0.04045 0.04914
    [,749]
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y1 0.07276 0.01055 0.15373 0.27773 0.36722 0.29687 0.11688 0.14274 0.14093 0.02367 0.15558
y2 0.01428 0.19956 0.00518 0.03878 0.04779 0.09470 0.00664 0.13866 0.02248 0.04081 0.15558
    [,760]
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```

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y1 0.31818 0.13319 0.28850 0.11053 0.14586 0.11265 0.38738 0.17032 0.17721 0.07625 0.08510
y2 0.01328 0.07615 0.62154 0.20515 0.14030 0.17041 0.00160 0.02354 0.21240 0.06967 0.01914
                                    [,775]
                                            [,776] [,777] [,778] [,779]
                    [,773]
                            [,774]
    [,771]
            [,772]
                                                                            [,780]
                                                                                    [,781]
y1 0.01755 0.04138 0.07834 0.04276 0.30369 0.07356 0.1335 0.17966 0.09071 0.04249 0.27034
y2 0.07823 0.08954 0.37995 0.10179 0.25984 0.07356 0.1335 0.27336 0.08503 0.15016 0.36532
                                                    [,788] [,789] [,790] [,791]
                   [,784]
                           [,785]
                                    [,786]
                                            [,787]
    Γ.782]
            [,783]
                                                                                     [,792]
y1 0.03982 0.83367 0.01134 0.04172 0.15471 0.05292 0.79512 0.12132 0.01771 0.01372 0.12230
y2 0.15576 0.06767 0.01134 0.07844 0.26899 0.00686 0.19979 0.07788 0.03346 0.28405 0.38198
    [,793]
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                                                                                     [,803]
y1 0.19700 0.14290 0.04434 0.17948 0.28398 0.21255 0.20352 0.05718 0.15071 0.20111 0.42194
y2 0.10376 0.03578 0.06675 0.22041 0.08778 0.00845 0.10343 0.05718 0.37253 0.03348 0.30800
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y1 0.61155 0.13548 0.00637 0.14329 0.04734 0.05786 0.02753 0.05139 0.07274 0.16531 0.02463
y2 0.08013 0.09633 0.25013 0.01039 0.04734 0.02994 0.02753 0.05139 0.10304 0.04574 0.07442
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                                                                                     [,825]
y1 0.04506 0.39436 0.24415 0.00592 0.10556 0.11537 0.07458 0.23342 0.10031 0.00180 0.05936
y2 0.04506 0.15274 0.09612 0.00592 0.10126 0.17050 0.00100 0.18005 0.16525 0.02796 0.12317
    [,826] [,827]
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y1 0.50113 0.1179 0.58548 0.21602 0.06186 0.25206 0.05178 0.15402 0.06547 0.08114 0.11170
y2 0.02520 0.1179 0.02524 0.06505 0.05232 0.02933 0.13833 0.01541 0.10281 0.39518 0.23053
                   [,839] [,840] [,841] [,842] [,843] [,844] [,845] [,846]
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y1 0.07025 0.08395 0.14948 0.08165 0.00766 0.06121 0.08072 0.15940 0.11947 0.17834 0.02144
y2 0.08307 0.23123 0.01143 0.04996 0.21610 0.14611 0.08072 0.05063 0.14455 0.17834 0.08849
                                            [,853]
                                                    [,854]
            [,849]
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                                                            [,855]
                                                                    [,856]
                                                                             [,857]
                                                                                     [,858]
y1 0.67000 0.28859 0.40798 0.02935 0.06393 0.00166 0.06706 0.11049 0.16600 0.01051 0.03567
y2 0.28978 0.05833 0.24374 0.01970 0.03172 0.15445 0.52804 0.10970 0.10909 0.00129 0.03567
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y1 0.47096 0.02353 0.12192 0.63231 0.08695 0.15159 0.09628 0.13213 0.21305 0.03424 0.13558
y2 0.08105 0.01268 0.11073 0.07372 0.48213 0.02867 0.13817 0.13213 0.17714 0.02414 0.14040
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y1 0.12028 0.22026 0.35466 0.05437 0.12796 0.02993 0.07904 0.56205 0.07329 0.02292 0.02237
y2 0.07928 0.22026 0.04041 0.28040 0.19904 0.14698 0.01328 0.17586 0.39690 0.01791 0.02237
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y1 0.34931 0.01644 0.04434 0.24803 0.05878 0.01182 0.17011 0.24232 0.22824 0.07965 0.11395
y2 0.03182 0.18232 0.04434 0.24803 0.61623 0.04227 0.17011 0.18738 0.22567 0.07965 0.12277
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                                                                             [,901]
    [,892]
                                                                                     [,902]
y1 0.02458 0.08021 0.12084 0.04178 0.05511 0.17175 0.19304 0.36063 0.04515 0.01587 0.12228
y2 0.00184 0.27425 0.06150 0.00453 0.11666 0.17175 0.03855 0.36063 0.12481 0.01632 0.25896
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                            [,906]
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                                                    [,909]
                                                            [,910]
                                                                    [,911]
                                                                             [,912]
    [,903]
                                                                                     [,913]
y1 0.03195 0.10772 0.08060 0.13415 0.04773 0.02033 0.03957 0.15620 0.18192 0.41586 0.02864
y2 0.16641 0.02743 0.11017 0.11932 0.04773 0.06354 0.08959 0.09741 0.18192 0.11413 0.10643
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    [,914]
            [,915]
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                                                                                     [.924]
y1 0.11024 0.04466 0.00828 0.10512 0.12644 0.19146 0.17613 0.04254 0.25702 0.13252 0.03096
y2 0.09286 0.04466 0.23115 0.12605 0.07506 0.03719 0.17613 0.04879 0.14412 0.00216 0.13899
[,925] [,926] [,927] [,928] [,929] [,930] [,931] [,932] [,933] [,934] [,935] y1 0.07192 0.07582 0.15256 0.02845 0.20467 0.04843 0.02401 0.31783 0.05211 0.10338 0.00865
            [,926]
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y2 0.11516 0.19444 0.13131 0.02845 0.12380 0.00794 0.12780 0.16549 0.37819 0.65544 0.14113
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            [,937]
                   [,938]
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y1 0.36816 0.12850 0.02713 0.02792 0.31250 0.00488 0.07408 0.18875 0.17467 0.47519 0.03325
y2 0.36532 0.15139 0.04315 0.25417 0.05626 0.13008 0.07408 0.81052 0.08059 0.54068 0.03325
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                                                            [,954]
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                    [,949]
                            [,950]
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                                                                    [,955]
                                                                             [,956]
y1 0.18057 0.19697 0.17577 0.23811 0.11586 0.23899 0.00888 0.62486 0.19769 0.00762 0.08757
y2 0.39999 0.08436 0.03536 0.27123 0.39903 0.05397 0.07258 0.26338 0.12629 0.07240 0.19700
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                                    [,962]
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y1 0.12272 0.17835 0.17071 0.04894 0.15988 0.09456 0.39325 0.01931 0.11262 0.06293 0.42941
y2 0.05089 0.11661 0.37256 0.00213 0.28175 0.14645 0.30959 0.19351 0.20454 0.06293 0.62290
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    [,969]
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                                    [,973]
                                            [,974]
                                                    [,975]
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y1 0.05435 0.14747 0.04919 0.47601 0.03973 0.26231 0.25257 0.08825 0.00674 0.97549 0.09086
y2 0.01349 0.11287 0.13250 0.02603 0.15216 0.12237 0.04857 0.08681 0.00674 0.22687 0.01004
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y1 0.17396 0.12503 0.06802 0.01671 0.09333 0.02059 0.03405 0.00562 0.37513 0.33077 0.16732
y2 0.33405 0.05743 0.15567 0.39128 0.31676 0.07852 0.03405 0.00562 0.15915 0.09466 0.20701
           [,992]
    [,991]
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                                                                    [,999] [,1000]
y1 0.26815 0.29942 0.10292 0.18317 0.08371 0.03736 0.07428 0.18755 0.06862 0.19273
y2 0.15351 0.35975 0.03068 0.37087 0.08371 0.02254 0.07428 0.05698 0.18246 0.16034
```

Random Numbers from BBBE(5, 5, 2)

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                                                                 [,8]
                                                                                 [,10]
                                                                                         [,11]
y1 0.02551 0.20991 0.13558 0.02366 0.25069 0.15979 0.22080 0.05248 0.24328 0.56880 0.05671
y2 0.09808 0.02763 0.31676 0.26382 0.01772 0.06688 0.25281 0.03361 0.04779 0.24156 0.35246
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                                                                                 [,21]
                                                                                         [,22]
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                                               [,17]
                                                       [,18]
                                                                [,19]
y1 0.15251 0.04734 0.02713 0.12049 0.13539 0.38198 0.03355 0.18924 0.11174 0.36993 0.04205
y2 0.19671 0.34244 0.45081 0.24145 0.04839 0.09808 0.01143 0.35799 0.21240 0.15119 0.03719
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                                                                [,30]
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y1 0.08500 0.16215 0.47111 0.53046 0.01900 0.11537 0.07890 0.07408 0.18379 0.22824 0.04852
y2 0.37924 0.00107 0.01956 0.00936 0.06505 0.09414 0.07049 0.06765 0.04996 0.03361 0.39554
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                                                                                         [,44]
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                                                                [,41]
                                                                        [,42]
             [,35]
y1 0.11537 0.15979 0.02033 0.14769 0.20323 0.17671 0.23568 0.02551 0.19361 0.14624 0.01762
y2 0.22306 0.17426 0.09403 0.01294 0.03578 0.10468 0.06331 0.07839 0.09829 0.02048 0.14159
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                                                                [,52]
                                                                                 [,54]
     [,45]
             [,46]
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                                      [,49]
                                                                        [,53]
                                               [,50]
                                                       [,51]
                                                                                         [,55]
y1 0.00481 0.02111 0.38718 0.19999 0.04773 0.07785 0.15752 0.45304 0.19948 0.18317 0.62486
y2 0.01428 0.00613 0.11301 0.03081 0.08681 0.13456 0.16636 0.06086 0.13560 0.01143 1.07595
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                              [,59]
                                      [,60]
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             [,57]
                      [,58]
                                               [,61]
                                                       [,62]
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y1 0.12796 0.03697 0.31524 0.29943 0.28859 0.45908 0.08510 0.80610 0.04378 0.31320 0.00036
y2 0.03505 0.31981 0.11764 0.15274 0.29230 0.16034 0.00216 0.00172 0.19545 0.08013 0.11772
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     L,67]
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                                                                [,74]
                                      [,71]
                                                                        [,75]
                                                                                         L,77]
                                                                                 [,76]
y1 0.15238 0.21544 0.23177 0.10406 0.38334 0.21470 0.18695 0.32482 0.06186 0.02111 0.04254
y2 0.02414 0.12459 0.02414 0.18323 0.27322 0.13131 0.00174 0.08069 0.04466 0.01553 0.26680
                                                                                         [,887
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y1 0.02551 0.03567 0.20253 0.02144 0.19118 0.10450 0.06393 0.08706 0.06311 0.15143 0.10031
y2 0.30369 0.00652 0.10845 0.15691 0.00148 0.14321 0.05833 0.03573 0.14455 0.11322 0.51113
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                                      [,93]
                                               [,94]
                                                                                         [,99]
     [,89]
             [,90]
                      [,91]
                              [,92]
                                                       [,95]
                                                                [,96]
                                                                                 [,98]
y1 0.60150 0.03089 0.05699 0.23413 0.35185 0.04894 0.33411 0.07274 0.02323 0.06082 0.04492
y2 0.11772 0.09740 0.08778 0.18694 0.02763 0.05132 0.06053 0.01917 0.08069 0.02674 0.02502
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                                              [,105]
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y1 0.64629 0.22320 0.04757 0.39325 0.00068 0.00766 0.13629 0.08574 0.08137 0.13269 0.21470
y2 0.07263 0.21224 0.11287 0.05689 0.34673 0.12481 0.02254 0.11015 0.27802 0.19572 0.04897
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                                                      [,117]
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                                                                                        [,121]
y1 0.29760 0.36271 0.28775
                           0.00036 0.23314 0.33680 0.04773 0.00174 0.04434 0.30726 0.04699
y2 0.45179 0.42780 0.15167 0.03683 0.17558 0.01956 0.15274 0.00236 0.20056 0.07240 0.13273
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                                     [,126]
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    [,122]
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y1 0.02867 0.05786 0.01789 0.03957 0.07332 0.05478 0.31990 0.08706 0.04834 0.91190 0.23568
y2 0.04434 0.08932 0.14316 0.18664 0.02923 0.03977 0.13419 0.01917 0.01118 0.00148 0.05839
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                             [,136]
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y1 0.41015 0.03626 0.06706 0.07183 0.26231 0.02341 0.09184 0.15540 0.07523 0.19661 0.14264
y2 0.03815 0.03346 0.03584 0.10451 0.58593 0.00216 0.05839 0.38106 0.11227 0.12030 0.29989
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            [,145]
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                     [,146]
                                     [,148]
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y1 0.25196 0.04809 0.02673 0.14258 0.08500 0.04407 0.25246 0.15238 0.25206 0.05184 0.24045
y2 0.24374 0.20045 0.45081 0.01784 0.04664 0.10569 0.10246 0.49884 0.11666 0.03231 0.13979
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                                                      [,161]
                                                               [,162]
                                                                                        [,165]
                                              [,160]
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y1 0.04089 0.10759 0.03372 0.12657 0.03626 0.03154 0.09927 0.32081 0.02889 0.04760 0.14388
y2 0.18713 0.05212 0.26266 0.36531 0.02867 0.03081 0.09336 0.32678 0.01772 0.12629 0.14040
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                                                                       [,174]
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y1 0.00220 0.03581 0.04081 0.38331 0.22817 0.06716 0.10197 0.14770 0.00385 0.07844 0.01228
y2 0.34401 0.02755 0.08778 0.49955 0.01428 0.01784 0.02796 0.16653 0.42625 0.06688 0.00794
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y1 0.33077 0.21489 0.04843 0.02587 0.17139 0.28243 0.07910 0.08665 0.31783 0.07329 0.02587
y2 0.00499 0.32113 0.05455
                           0.12030 0.03559 0.03117 0.10909 0.21219 0.10643 0.01440 0.19248
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                                                      [,194]
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                                                                               [,197]
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                             [,191]
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    [,188]
                                              [,193]
                                                                       [,196]
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y1 0.09216 0.11167 0.03903 0.30535 0.01755 0.39307 0.01587 0.04897 0.15238 0.02993 0.22080
y2 0.10909 0.04184 0.10197 0.06688 0.04408 0.16003 0.06688 0.00936 0.11932 0.28201 0.25069
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                                                                       [,207]
                                                                                        [,209]
                                                      [,205]
                                                               [,206]
y1 0.36506 0.25013 0.02713
                           0.41161 0.21412 0.00394 0.30466 0.05016 0.28859 0.08137 0.02695
y2 0.04192 0.06967 0.00499
                           0.27123 0.03304 0.04753 0.00216 0.11362 0.04192 0.10146 0.09086
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y1 0.03089 0.15678 0.02218 0.02306 0.01035 0.02367 0.10341 0.36722 0.04434 0.05219 0.04217
y2 0.09470 0.02867 0.10985 0.28631 0.60871 0.14402 0.03182 0.06356 0.05506 0.18738 0.11613
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y1 0.10772 0.01562 0.51817 0.18107 0.00448 0.22319 0.28793 0.10512 0.01131 0.06082 0.12281
y2 0.36946 0.04450 0.66962 0.15376 0.05698 0.10894 0.28201 0.10703 0.04837 0.04857 0.08865
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  0.02180 0.08910 0.08080 0.00793 0.12796 0.03689 0.05100 0.25246 0.00036 0.02234 0.08069
  0.10643 0.02933 0.06356 0.70382 0.07190 0.24830 0.06505 0.03581 0.09776 0.00216 0.00499
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y1 0.00166 0.03148 0.39746 0.03925 0.21724 0.10217 0.28775 0.21897 0.09237 0.05641 0.02440
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y2 0.06425 0.00570 0.05626 0.37576 0.41679 0.03644 0.15119 0.01749 0.04734 0.22567 0.00551
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y1 0.14771 0.10566 0.00767 0.78167 0.00463 0.08681 0.12072 0.12599 0.03432 0.00360 0.26146
y2 0.10978 0.11983 0.21489 0.10179 0.07928 0.05446 0.03878 0.08459 0.14657 0.00227 0.06211
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y1 0.01066 0.04809 0.00192 0.01285 0.03559 0.34817 0.24518 0.03067 0.03744 0.09332 0.19984
y2 0.11426 0.15683 0.05100 0.00613 0.28089 0.00966 0.08072 0.00192 0.72778 0.31454 0.31213
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y1 0.12049 0.25419 0.00142 0.03920 0.25330 0.28589 0.2111 0.01973 0.28979 0.00931 0.06629
y2 0.29092 0.15139 0.29914 0.32877 0.10456 0.31465 0.1970 0.11983 0.01241 0.11377 0.02482
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y2 0.68993 0.03806 0.05132 0.04124 0.03683 0.06749 0.13213 0.16307 0.14698 0.02899 0.15792
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y2 0.33139 0.03770 0.21075 0.20323 0.06035 0.11790 0.05813 0.04534 0.12357 0.15119 0.04124
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y1 0.39823 0.08001 0.02753 0.09875 0.47479 0.20536 0.22883 0.46991 0.78216 0.12769 0.35235
y2 0.02256 0.09882 0.32397 0.03348 0.03855 0.21709 0.05207 0.06707 0.12780 0.04450 0.12165
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y1 0.05676 0.10566 0.11150 0.08608 0.19906 0.03422 0.19273 0.00970 0.17329 0.07785 0.12556
y2 0.04184 0.02843 0.04699 0.28165 0.04605 0.02929 0.03536 0.17314 0.08738 0.52542 0.60214
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y1 0.04090 0.33873 0.37765 0.05671 0.09376 0.04118 0.27157 0.05184 0.10292 0.02755 0.11947
y2 0.31524 0.07766 0.14316 0.13439 0.08574 0.22879 0.00524 0.31814 0.06283 0.11639 0.07768
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y2 0.07372 0.07414 0.05063 0.04605 0.43092 0.04378 0.00184 0.18464 0.01328 0.21709 0.10304
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y1 0.04421 0.04578 0.30183 0.03676 0.05526 0.53493 0.09723 0.06890 0.03559 0.09875 0.02066
y2 0.02878 0.25754 0.01301 0.06508 0.30959 0.47691 0.14698 0.07844 0.10126 0.15440 0.05455
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y1 0.07582 0.15345 0.03505 0.22026 0.02739 0.14163 0.19999 0.10171 0.04144 0.30466 0.25654
y2 0.04861 0.24968 0.04222 0.33469 0.02414 0.30079 0.02072 0.33065 0.09770 0.15167 0.45525
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y1 0.30560 0.02323 0.20894 0.08481 0.13962 0.39052 0.16928 0.01692 0.08706 0.0587 0.09723
y2 0.35084 0.04510 0.18590 0.09612 0.16626 0.15141 0.15996 0.17011 0.07767 0.1908 0.15478
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y2 0.00172 0.02199 0.12519 0.05155 0.22773 0.12165 0.11772 0.04514 0.12864 0.35246 0.00241
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v1 0.01449 0.03567 0.13046 0.02501 0.03154 0.03014 0.03946 0.39631 0.45304 0.20175 0.03982
y2 0.20402 0.25132 0.08069 0.08806 0.15295 0.04861 0.05184 0.12780 0.09505 0.26476 0.08294
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y1 0.07920 0.35179 0.30335 0.20569 0.39307 0.03372 0.14258 0.09456 0.05041 0.08238 0.58144
y2 0.18543 0.02994 0.06795 0.05848 0.08778 0.08049 0.14865 0.09709 0.02256 0.10281 0.43766
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y1 0.46737 0.02957 0.04852 0.06845 0.04057 0.01762 0.00408 0.10413 0.22319 0.07329 0.04138
y2 0.05839 0.04781 0.05212 0.02458 0.01685 0.18964 0.09291 0.08307 0.07049 0.01301 0.06504
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y2 0.00838 0.07788 0.11772 0.04773 0.16498 0.10566 0.01258 0.26348 0.12864 0.05743 0.26083
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y2 0.19386 0.25896 0.19209 0.04087 0.05134 0.01102 0.10390 0.52542 0.00394 0.02994 0.03584
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y2 0.23931 0.19210 0.12204 0.00198 0.36946 0.12380 0.02862 0.02899 0.04217 0.01956 0.05430
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y2 0.06374 0.17020 0.04231 0.24038 0.0626 0.00725 0.12834 0.39479 0.18738 0.00936 0.05184
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y1 0.09144 0.06588 0.57512 0.16215 0.12989 0.35179 0.13028 0.09723 0.11983 0.09376 0.14274
y2 0.30560 0.08738 0.18192 0.28972 0.05446 0.01624 0.24877 0.09913 0.08049 0.15508 0.07919
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y1 0.20045 0.21370 0.02292 0.29687 0.09249 0.02942 0.00592 0.20132 0.43877 0.05139 0.23303
y2 0.18051 0.28972 0.06135 0.05966 0.08474 0.09500 0.00499 0.02601 0.04708 0.01070 0.19821
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y1 0.04897 0.00571 0.08315 0.03744 0.07608 0.00663 0.12072 0.27034 0.00580 0.01074 0.17396
y2 0.25651 0.01268 0.02354 0.10569 0.03202 0.06360 0.05212 0.19697 0.83599 0.02831 0.00107
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y2 0.41015 0.02831 0.11217 0.13866 0.18192 0.11282 0.20594 0.19378 0.02873 0.04120 0.22879
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v2 0.00073 0.03340 0.01268 0.07928 0.14229 0.07046 0.01325 0.15167 0.10175 0.52492 0.35213
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y2 0.11282 0.15141 0.03581 0.03578 0.05455 0.02414 0.49286 0.37253 0.25704 0.10126 0.11661
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y1 0.15471 0.16862 0.06312 0.06774 0.02323 0.45304 0.15979 0.00674 0.19851 0.02761 0.14875
y2 0.01900 0.01685 0.49286 0.11791 0.18766 0.01562 0.19545 0.16080 0.18738 0.23931 0.04434
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y2 0.17332 0.10304 0.15216 0.13030 0.05136 0.04120 0.04734 0.30800 0.03304 0.17807 0.02285
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y1 0.07582 0.04016 0.00166 0.06972 0.03629 0.40052 0.36993 0.20522 0.38201 0.14559 0.18198
y2 0.11526 0.09924 0.05718 0.50870 0.15878 0.15737 0.11792 0.35396 0.14832 0.41617 0.17314
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y1 0.38738 0.06247 0.12786 0.02237 0.05511 0.09376 0.01256 0.05870 0.10305 0.15345 0.00236
y2 0.23348 0.52492 0.05966 0.18059 0.68674 0.04039 0.41617 0.04212 0.38106 0.00172 0.00838
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y1 0.03744 0.13125 0.20078 0.20688 0.30626 0.10171 0.17186 0.10450 0.04993 0.23342 0.39468
y2 0.12277 0.10845 0.24075 0.05764 0.28040 0.13366 0.07442 0.14402 0.24301 0.02501 0.08921
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y1 0.06891 0.02792 0.54689 0.04052 0.54738 0.12848 0.08910 0.03067 0.14626 0.31990 0.02923
y2 0.00887 0.03536 0.05718 0.80167 0.34482 0.03044 0.05155 0.05340 0.02458 0.30331 0.03325
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y1 0.10450 0.17884 0.30726 0.12228 0.04843 0.37664 0.11983 0.08366 0.04773 0.00663 0.00762
y2 0.06466 0.01396 0.02256 0.04605 0.00373 0.08165 0.42226 0.06505 0.12055 0.07768 0.04996
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y1 0.25619 0.08510 0.36427 0.14744 0.00017 0.00605 0.15678 0.38335 0.21470 0.07920 0.05786
y2 0.04897 0.43877 0.30800 0.33972 0.28207 0.05848 0.22680 0.32198 0.01067 0.18961 0.01917
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y1 0.12932 0.33875 0.20217 0.01285 0.06101 0.18232 0.03372 0.00605 0.09455 0.15327 0.14414
y2 0.21170 0.10473 0.07919 0.01067 0.04699 0.44230 0.66962 0.54068 0.05132 0.11700 0.24295
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y1 0.15159 0.73361 0.02957 0.06547 0.03081 0.46266 0.05936 0.17948 0.06144 0.03355 0.31554
y2 0.03361 0.04073 0.19595 0.03584 0.18232 0.02873 0.05134 0.06982 0.19682 0.19261 0.15295
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y1 0.12065 0.26280 0.19361 0.06114 0.07089 0.01013 0.28576 0.03315 0.10772 0.05478 0.17858
y2 0.03883 0.05689 0.19700 0.00914 0.09776 0.70382 0.07578 0.07638 0.12314 0.23264 0.20045
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y1 0.05820 0.00571 0.00394 0.27157 0.09249 0.15678 0.06554 0.24328 0.12019 0.11362 0.14324
y2 0.22811 0.06534 0.04836 0.15292 0.24038 0.03567 0.01070 0.22466 0.41617 0.00481 0.64188
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y1 0.03903 0.03567 0.06774 0.02829 0.06304 0.25257 0.37513 0.14664 0.08240 0.09332 0.15249
y2 0.03185 0.06967 0.17314 0.24848 0.18005 0.00983 0.10894 0.10390 0.00664 0.04406 0.04853
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y2 0.08592 0.03644 0.11322 0.01102 0.25515 0.21240 0.04861 0.16078 0.01070 0.10343 0.13220
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y2 0.16753 0.10597 0.07284 0.47289 0.04699 0.04311 0.01456 0.22879 0.09112 0.02482 0.04853
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y2 0.07608 0.20217 0.16234 0.11322 0.02923 0.48632 0.01748 0.21240 0.03513 0.02382 0.08371
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y1 0.12786 0.06554 0.05467 0.25196 0.14388 0.14093 0.05478 0.09376 0.03697 0.14113 0.02539
y2 0.28339 0.04227 0.16071 0.01690 0.17555 0.18530 0.03505 0.01301 0.11656 0.00010 0.08681
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y1 0.11790 0.14825 0.07332 0.00116 0.16929 0.02539 0.30272 0.10217 0.01990 0.09456 0.20904
y2 0.25896 0.19700 0.36946 0.01541 0.26680 0.05743 0.31465 0.13833 0.13836 0.03185 0.19832
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y1 0.05416 0.29459 0.11790 0.29131 0.03736 0.08238 0.15357 0.17180 0.02401 0.01632 0.20889
y2 0.10835 0.24056 0.03896 0.16034 0.11276 0.39365 0.07823 0.20194 0.13585 0.19545 0.10909
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y1 0.07919 0.07850 0.25247 0.75453 0.03736 0.11537 0.02755 0.07839 0.19948 0.06949 0.19081
y2 0.09647 0.00845 0.31807 0.09403 0.03626 0.15295 0.03346 0.28438 0.15274 0.12380 0.13131
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y2 0.16575 0.20594 0.18827 0.01942 0.28631 0.00632 0.19386 0.06362 0.13363 0.09503 0.04450
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y1 0.39764 0.35179 0.21517 0.06972 0.04169 0.58808 0.05246 0.37765 0.01055 0.04100 0.02867
y2 0.65841 0.08459 0.02199 0.12357 0.02036 0.14455 0.04755 0.08754 0.39128 0.14359 0.11608
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y1 0.07766 0.37513 0.31783 0.06053 0.37561 0.11433 0.01905 0.06153 0.00420 0.00828 0.01134
y2 0.06086 0.10422 0.05063 0.01900 0.19955 0.00481 0.01268 0.31981 1.02081 0.12864 0.37253
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                                                                            [,802]
                                                                                     [,803]
y1 0.02547 0.28012 0.19948 0.02218 0.29253 0.03946 0.05526 0.30022 0.08695 0.04515 0.03920
y2 0.04421 0.17206 0.34482 0.31989 0.09724 0.05207 0.13000 0.07356 0.22761 0.08294 0.06967
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y1 0.33003 0.19081 0.20965 0.00961 0.05954 0.08240 0.56782 0.07885 0.19080 0.63350 0.26146
y2 0.38106 0.18323 0.15666 0.15106 0.03883 0.26047 0.06135 0.23175 0.08502 0.06676 0.03709
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y2 0.02482 0.04839 0.09460 0.11773 0.22707 0.11015 0.04090 0.32198 0.15915 0.15577 0.05966
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                                                                                     [,836]
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y2 0.31887 0.24156 0.14120 0.29230 0.11717 0.05650 0.07742 0.05292 0.04406 0.28793 0.00116
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y1 0.04708 0.08049 0.30726 0.05577 0.25237 0.20904 0.33003 0.09795 0.01931 0.07020 0.12702
y2 0.21132 0.17264 0.01325 0.24038 0.07356 0.20728 0.19652 0.40760 0.09990 0.19572 0.11717
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y1 0.00385 0.06186 0.24301 0.00911 0.10406 0.12769 0.06758 0.19210 0.05676 0.00129 0.00180
y2 0.05590 0.02036 0.06423 0.05016 0.03719 0.12054 0.38635 0.49192 0.34482 0.22687 0.04057
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y2 0.03996 0.06150 0.00160 0.00485 0.09724 0.21219 0.06354 0.01791 0.23125 0.02501 0.49884
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y1 0.06675 0.07386 0.37765 0.04757 0.27664 0.07785 0.16944 0.17948 0.13020 0.03797 0.05108
y2 0.33403 0.02518 0.12346 0.00725 0.04231 0.00129 0.15402 0.14040 0.03626 0.10146 0.16307
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y2 0.09336 0.19682 0.10451 0.06569 0.18713 0.02796 0.35206 0.08269 0.08650 0.38201 0.1303
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y1 0.11587 0.00318 0.13539 0.03982 0.00116 0.14174 0.05430 0.04406 0.03239 0.05292 0.1477
y2 0.36215 0.10137 0.48533 0.03081 0.05689 0.12481 0.07442 0.06362 0.06289 0.05173 0.0107
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y1 0.24816 0.46612 0.03903 0.07965 0.00176 0.04824 0.11792 0.15256 0.07356 0.17882 0.26559
y2 0.02796 0.01241 0.10292 0.29092 0.06967 0.30079 0.06356 0.30079 0.01674 0.01241 0.42226
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                                                                                   Γ.924]
y1 0.03096 0.02367 0.19080 0.04303 0.39325 0.02961 0.2067 0.01990 0.07834 0.15556 0.01135
y2 0.46127 0.08072 0.10451 0.11523 0.01285 0.11772 0.1663 0.04779 0.15119 0.02680 0.19682
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v1 0.07458 0.07240 0.33654 0.04809 0.00289 0.01900 0.06466 0.03995 0.29827 0.27740 0.14258
y2 0.80167 0.07608 0.13220 0.03340 0.02502 0.04861 0.09477 0.04155 0.02923 0.66864 0.01917
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y1 0.05676 0.49697 0.03493 0.75320 0.01372 0.04249 0.01465
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y2 0.21219 0.10376 0.13273 0.17558 0.00453 0.03683 0.08474
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y1 0.21470 0.17698 0.13511 0.37009 0.08046 0.00582 0.05699 0.01741 0.16445 0.03957 0.12230
y2 0.09484 0.04532 0.24295 0.11507 0.08307 0.01772 0.00321 0.12519 0.29939 0.10506 0.07144
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y1 0.02867 0.19361 0.00970 0.11792 0.02673 0.01013 0.01900 0.24925 0.14229 0.02488 0.02923
y2 0.03325 0.27725 0.04779 0.04755 0.14030 0.32877 0.04155 0.28403 0.25417 0.01325 0.20467
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y1 0.08865 0.04492 0.02306 0.05512 0.20175 0.24355 0.22761 0.06393 0.27474 0.27218 0.05437
y2 0.46112 0.01241 0.05764 0.49937 0.20277 0.06293 0.03185 0.02414 0.04222 0.09112 0.19700
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y2 0.03996 0.28089 0.14653 0.15567 0.03883 0.1272 0.06260 0.01004 0.03534 0.02390 0.04857
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y1 0.00754 0.05455 0.09561 0.02829 0.15256 0.12174 0.11053 0.03584 0.07386 0.04760
y2 0.14359 0.10175 0.29939 0.13220 0.15519 0.05212 0.01349 0.01070 0.11511 0.03744
```

Random Numbers from Weibull(7, 3)

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[1] 0.882060 0.696218 0.841191 0.634649 0.573719 1.004176 0.801681 0.626634 0.793692
[10] 0.825535 0.547299 0.826615 0.746964 0.786303 0.961177 0.619922 0.897030 1.007845
[19] 0.868145 0.551520 0.629145 0.740714 0.761508 0.409032 0.755648 0.734066 0.796230
[28] 0.778655 0.881505 0.937994 0.535084 0.617592 0.741586 0.692373 1.030590 0.818538
[37] 0.711335 0.908340 0.871461 0.902465 0.940061 0.839361 0.839631 0.854431 0.935485
[46] 0.942006 0.901930 0.822452 0.889753 0.653898 1.003897 0.830278 0.690483 0.950617
55 0.790393 0.912249 0.947675 0.713814 0.624296 0.852569 0.751949 0.966042 0.849426
[64] 0.886734 0.681588 0.828201 0.684232 0.682894 0.692984 0.831057 0.713256 0.765777
[73] 0.733355 1.137188 0.819359 0.906891 0.850798 0.771884 0.860108 0.956473 0.897948
[82] 0.750782 0.838343 0.696276 0.961212 0.832679 0.469817 0.626075 0.631767 0.925335
[91] 0.946056 0.756661 0.862882 0.755237 0.870713 0.919954 0.699376 0.966815 0.822182
[100] 0.807291 0.776545 0.866485 0.814946 0.551573 0.816844 0.628443 0.605428 0.773364
[109] 0.840628 0.938003 0.580808 0.877295 0.990267 0.562853 0.728816 0.940305 0.794434
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[127] 0.934668 0.968418 0.940493 0.741875 0.769492 0.627533 0.748806 0.721408 0.804043
[136] 0.754030 0.677350 0.697288 0.490130 0.831188 0.873680 0.841028 1.061625 0.921570
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[154] 0.896896 0.956495 0.847438 0.786549 0.908150 0.829434 0.907721 0.810380 0.859404
[163] 0.757869 0.852486 0.858889 0.799782 0.719909 0.906509 0.839953 0.889856 0.765494
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[190] 0.617995 0.886812 0.870334 0.466681 0.769219 0.578102 0.822264 0.841896 0.754269
[199] 0.935530 0.786221 0.899780 0.536475 0.776046 0.806105 0.843296 0.636915 0.856010
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[217] 0.860077 0.841202 0.677862 0.600655 0.883841 0.539042 0.725346 0.743373 0.997138
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[235] 0.891605 0.845080 0.915799 0.671146 0.935279 0.687992 0.795281 0.753055 0.926796
[244] 0.764334 0.873623 0.727063 0.844492 0.520674 0.525377 0.726104 0.892931 0.906243
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[262] 0.635504 0.748329 0.558920 0.805628 0.784934 0.865301 0.861605 1.038602 0.810208
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[595] 0.970134 0.636495 0.808344 0.864908 0.624933 1.019867 0.900343 0.743326 0.904687
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