# **Calculus**

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# **Calculus**

This wikibook aims to be a high quality <u>calculus</u> textbook through which users can master the discipline. Standard topics such as *limits, differentiation* and *integration* are covered, as well as several others. Please <u>contribute</u> wherever you feel the need. You can simply help by rating individual sections of the book that you feel were inappropriately rated!

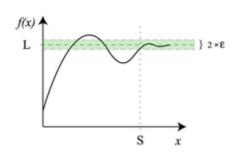
- Introduction
- Contributing

### **Precalculus**

- 1.1 Algebra
- 1.2 Trigonometric functions
- 1.3 Functions
- 1.4 Graphing linear functions
- 1.5 Exercises

### Limits

- 2.1 An Introduction to Limits
- 2.2 Finite Limits
- 2.3 Infinite Limits
- 2.4 Continuity
- 2.5 Formal Definition of the Limit
- 2.6 Proofs of Some Basic Limit Rules
- 2.7 Exercises



### **Differentiation**

#### **Basics of Differentiation**

3.1 Differentiation Defined

- 3.2 Product and Quotient Rules
- 3.3 Derivatives of Trigonometric Functions
- 3.4 Chain Rule
- 3.5 Higher Order Derivatives: an introduction to second order derivatives
- 3.6 Implicit Differentiation
- 3.7 Derivatives of Exponential and Logarithm Functions
- 3.8 Some Important Theorems
- 3.9 Exercises

### **Applications of Derivatives**

- 3.10 L'Hôpital's Rule
- 3.11 Extrema and Points of Inflection
- 3.12 Newton's Method
- 3.13 Related Rates
- 3.14 Optimization
- 3.15 Euler's Method
- 3.16 Exercises

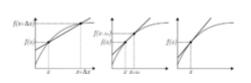
# **Integration**

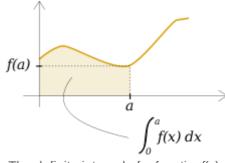
### **Basics of Integration**

- 4.1 Definite integral
- 4.2 Fundamental Theorem of Calculus
- 4.3 Indefinite integral
- 4.4 Improper Integrals

### **Integration Techniques**

- 4.5 Infinite Sums
- 4.6 Derivative Rules and the Substitution Rule
- 4.7 Integration by Parts
- 4.8 Trigonometric Substitutions
- 4.9 Trigonometric Integrals





The definite integral of a function f(x) from x=0 to x=a is equal to the area under the curve from 0 to a.

4.10 Rational Functions by Partial Fraction Decomposition

4.11 Tangent Half Angle Substitution

4.12 Reduction Formula

4.13 Irrational Functions

4.14 Numerical Approximations

4.15 Exercises

**Applications of Integration** 

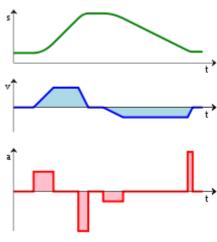
4.16 Area

4.17 Volume

4.18 Volume of solids of revolution

4.19 Arc length

- Surface area
- Work
- Centre of mass
- Pressure and force
- Probability



From bottom to top

- an acceleration functiona(t);
- the integral of the acceleration is the velocity function v(t);
- and the integral of the velocity is the distance functions(t).

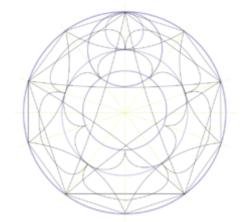
# **Parametric and Polar Equations**

#### **Parametric Equations**

- Introduction to Parametric Equations
- Differentiation and Parametric Equations
- Integration and Parametric Equations
- Exercises

#### **Polar Equations**

- Introduction to Polar Equations
- Differentiation and Polar Equations
- Integration and Polar Equations



### **Sequences and Series**

#### **Sequences**

- Definition of a Sequence
- Sequences

#### **Series**

Definition of a Series

- Series
- Limit Test for Convergence
- Comparison Test for Convergence
- Integral Test for Convergence

#### Series and calculus

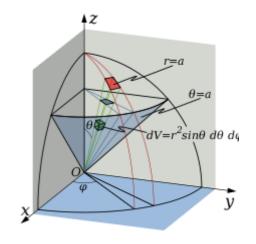
- Taylor series
- Power series

#### **Exercises**

Exercises

### **Multivariable and Differential Calculus**

- Vectors
- Lines and Planes in Space
- Multivariable Calculus
- Derivatives of multivariate functions
- The chain rule and Clairaut's theorem
- Inverse function theorem, implicit function theorem
- Vector calculus
- Vector calculus identities
- Inverting vector calculus operators
- Helmholtz Decomposition Theorem
- Discrete analog to Vector calculus
- Exercises



# **Differential Equations**

- Ordinary Differential Equations
- Partial Differential Equations

### **Extensions**

### Advanced Integration Techniques

Complexifying

#### **Further Analysis**

Systems of Ordinary Differential Equations

#### **Formal Theory of Calculus**

- Real numbers
- Complex numbers

### References

- Table of Trigonometry
- Summation notation
- Tables of Derivatives
- Tables of Integrals

# **Acknowledgements and Further Reading**

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