

Bubble Sort → Puts largest element at the end (sorted position)

$arr = \{ 5, 3, 2, 4, 1 \}$ $0 \quad 1 \quad 2 \quad 3 \quad 4$ index

{ if $arr[0] > arr[1]$
 $swap(arr[0], arr[1])$ 1 2 index

$3 \quad 5 > 2 \quad [3, 2, 5, 4, 1] \quad 2, 3$

$3, 2, 4, 5, 1$ if $(arr[i] > arr[i+1])$
 $swap(arr[i], arr[i+1])$ 3, 4
 $3, 2, 4, 1, 5$ 4 $[0, n-1]$

1st time → largest element
 comparison is done upto n^{th} element
 that $i \rightarrow [0, 3]$ open not including
 $[0, n-1]$ $[0, n-2]$ close including

→ 3, 2, 4, 1, 5

2nd time → 2nd largest

$3, 2, 4, 1, 5$
 $2, 3, 4, 1, 5$
 $2, 3, 1, 4$

largest at in index $a[:] \quad a[i+1]$
 $3 > 2$
 $3 < 4$
 $4 > 1$

2, 5, 1, 4, 3 $i > 1$
 $[0, 2], [0, \underline{n-2}]$
 $[0, n-3]$

3rd time

2, 1, 3, 4, 5

$[0, 2] [0, \underline{n-4}]$

4th time

1, 2, 3, 4, 5

$i \rightarrow [0], i+1 \rightarrow$

array is sorted.

$\{ \text{for (int } i=0; i < \underline{n-1}; i++)$

$\text{5} = n$
 $\text{4} < \text{5}$

$\{ \{ \text{for (int } j=0; j < n-i-1; j++)$
 $\{ \text{if } (arr[i] > arr[i+1]) \rightarrow \text{true}$
 $\text{swaps } arr[i], arr[i+1];$

Bubble sort.

$i=0, i=1, i=2, i=3, i=4$
 $j=0, j < n-i-1, i=3, i=2, i=1, i=0$

4 times
 $\{$
 1
 2
 3

$0 \rightarrow 0 \quad n-1$

$0 \rightarrow 1 \quad n-2$

$0 \rightarrow 2 \quad n-3$

$0 \rightarrow 3 \quad n-4$

outer loop

$i = 1$ \rightarrow outer loop in brackets

my code will run

$$n-1 + n-2 + n-3 + n-4 \dots \dots$$

$\dots \dots \dots$

$$1+2+3+\dots+n-1$$

\sum_{n-1} natural nos.

$n-1$ n

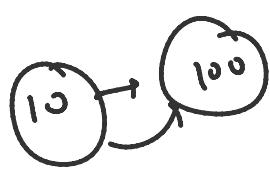
$\frac{n(n-1)}{2}$

$$\Rightarrow \frac{n(n-1)}{2}$$

$$\frac{10 \times 9}{2} = 45$$

$$\frac{n(n-1)}{2} \approx \frac{n^2 - n}{2}$$

$$= \underline{\underline{\alpha(n^2)}}$$



$$\frac{10 \times 9}{2} = 45$$

$$\text{arr} = [1, 2, 3, 4, 5, 6, 7, 8, 9, 10] \rightarrow$$

$$\frac{10 \times 9}{2} = 45$$

Optimising Bubble Sort $i \in [0, n]$

if $(\text{arr}[i]) > \text{arr}[i+1]$
swap \leftarrow \times

5 000 x 999

Before & optimising
for best case
 $\frac{n(n-1)}{2} = O(n^2)$

1000

$\rightarrow \frac{1000 \times 999}{2}$

After optimising
for best case
 $O(n)$

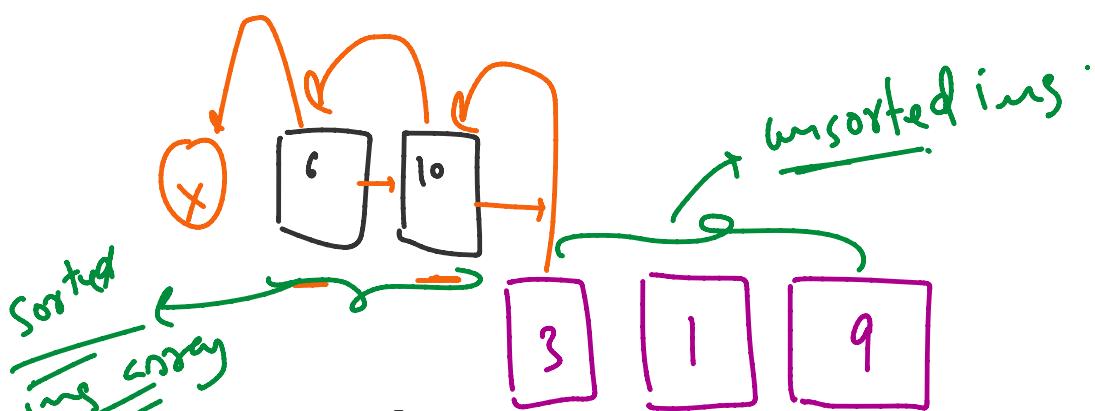
$\rightarrow 1000$

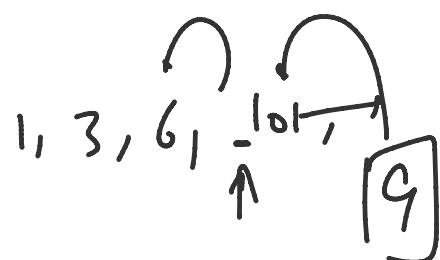
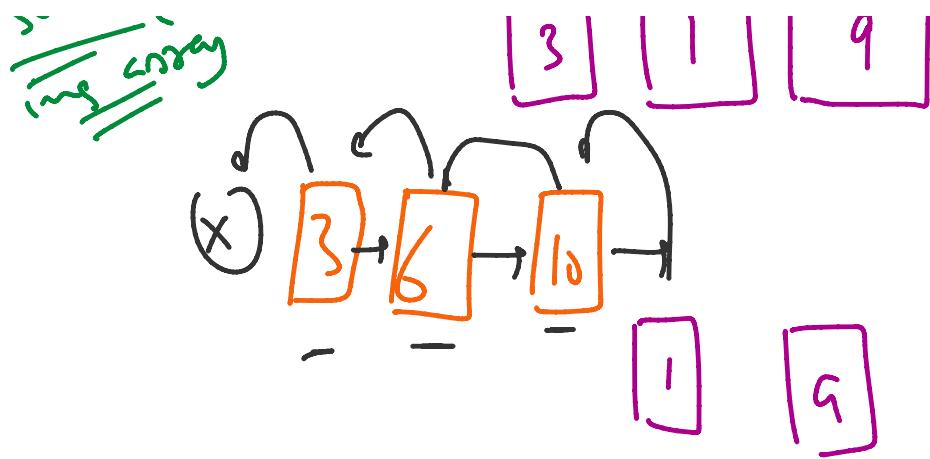
best case means \rightarrow already sorted array.

4th method \rightarrow I will swap function
in know k.c

swap ($\underline{-}, \underline{-}$) ;

Insertion Sort : It is similar to the way
we sort playing cards in our hands
one by one





$1, 3, 6, 9, 10$

$arr = \{5, 3, 2, 4, 1\};$ $i = 1$

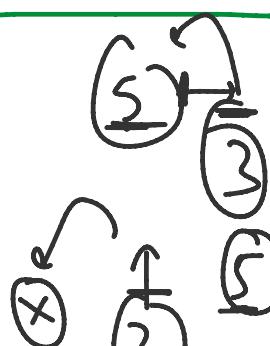
sorted

unsorted.

5

3, 2, 4, 1

for 3



1st element

unsorted with 0 element

$i \rightarrow i-1$

single element
is always sorted.

if $arr[i-1] > arr[i]$

shifted rightwards
swap $arr[i-1], arr[i]$

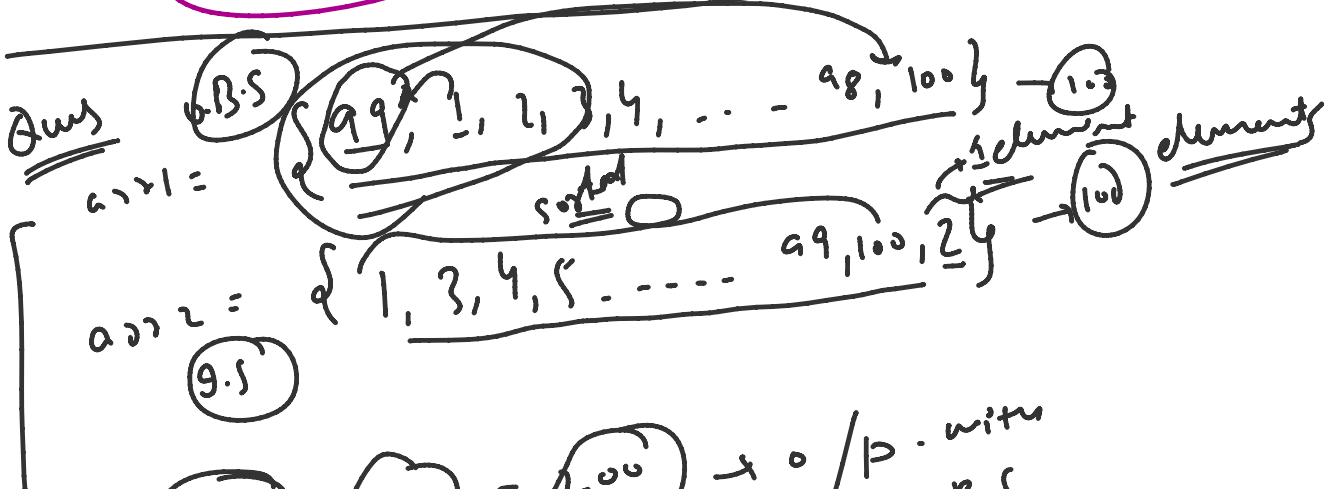
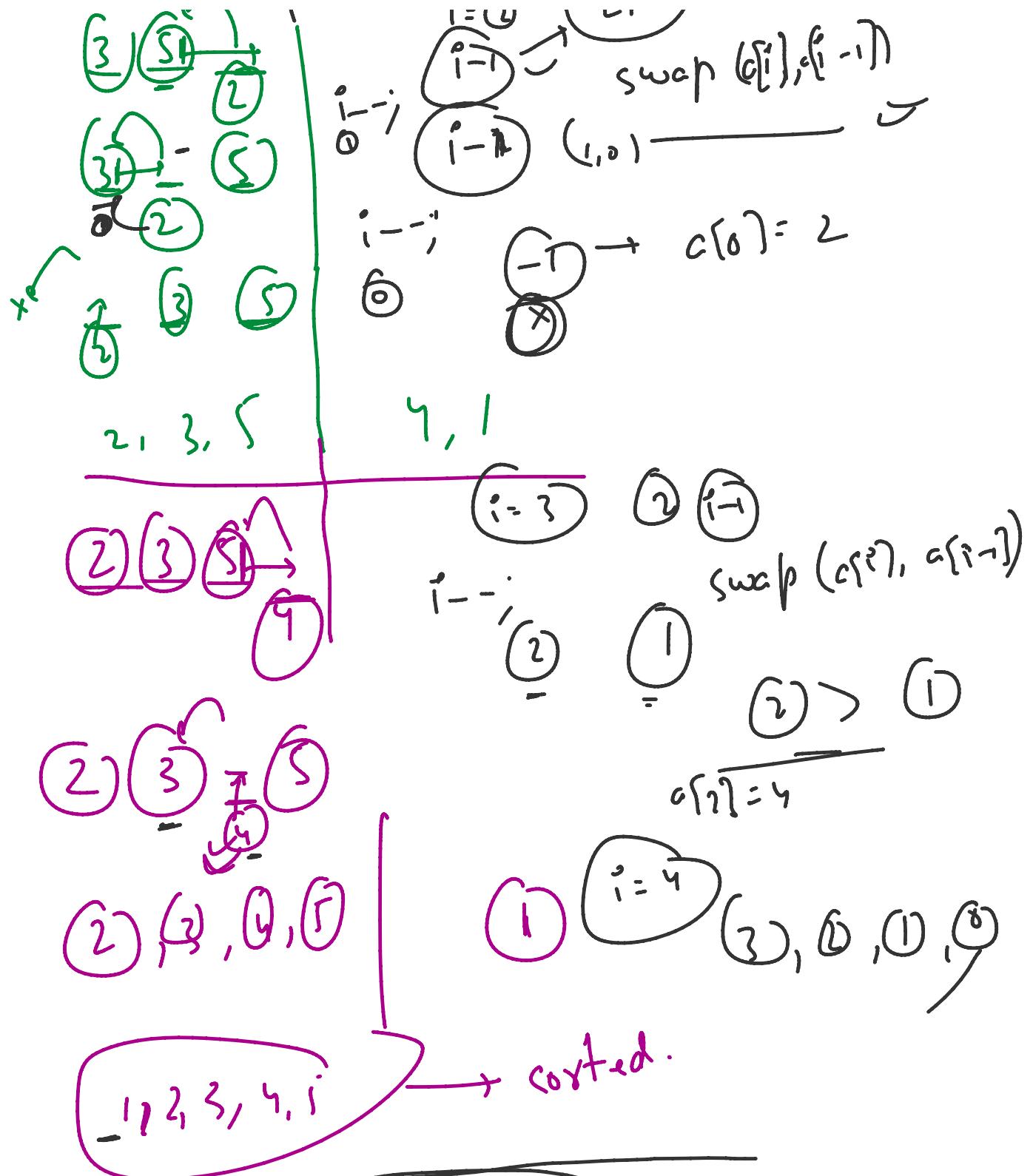


2, 4, 1

3, 5

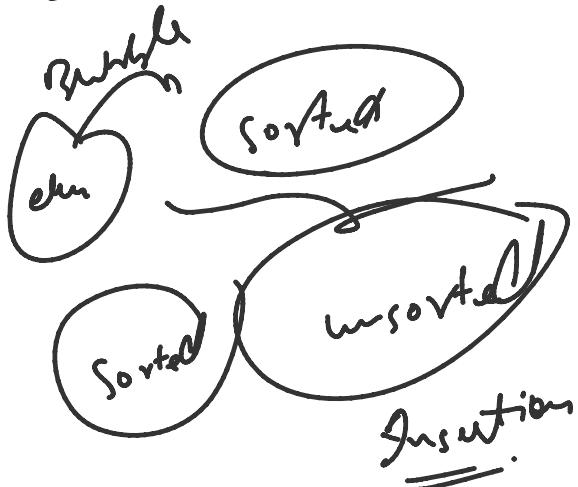
$i = 2$
 $i-1 \rightarrow i$

swap $arr[i], arr[i-1]$



$$100 + 100 = 200 \rightarrow O/P \text{ with O.R.S}$$

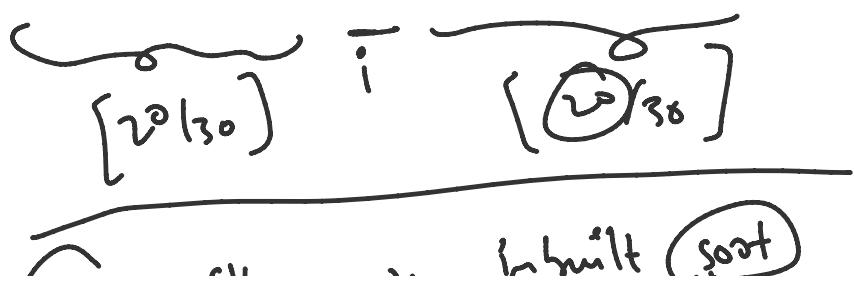
$$1 + 2 + 3 + 4 + \dots + \frac{100}{49} = \underline{\text{very high}}$$

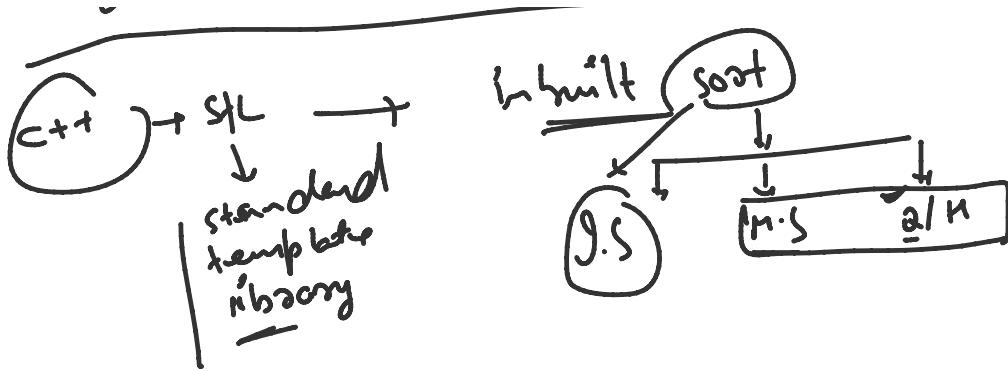


Insertion sort will take least time in case of almost sorted / sorted array

If you are given an array and each element is k positions away from its sorted pos. then insertion sort is fastest ($O_{\underline{\underline{C=1 \leq i \leq 2, 1, 1}}}$)

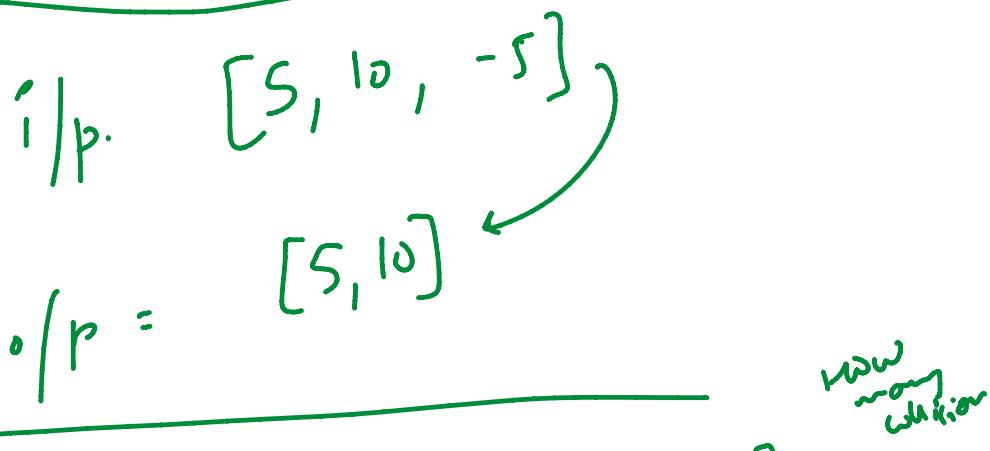
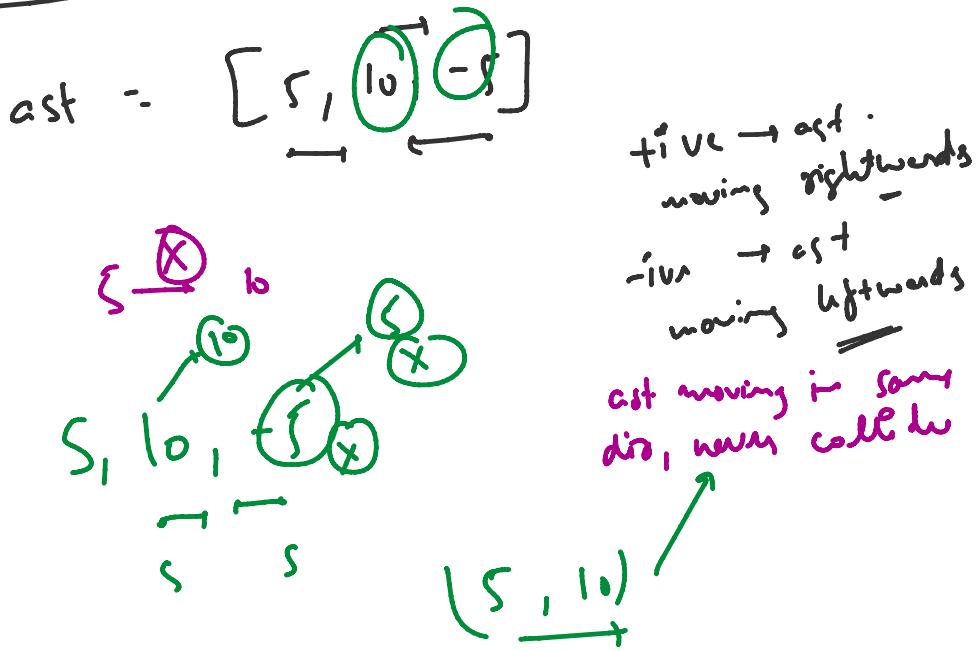
array size = 10^6





Insertion sort (most of the time)
is fastest among these 3 sorting algo.

Selection sort is always the slowest
among these 3 algo.



1.

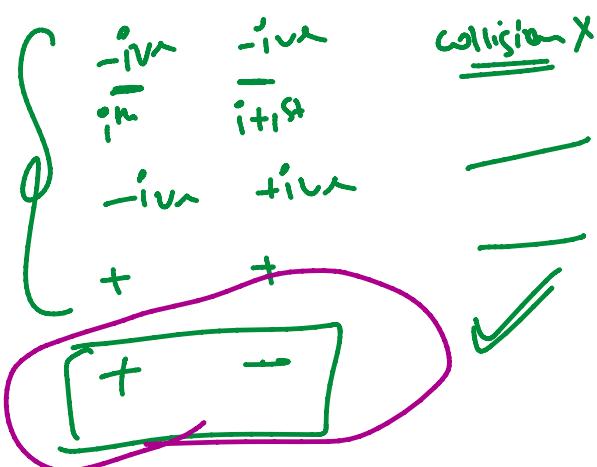
$$ast1 = [1, 2, 3, 4, 5, \dots, 10] \rightarrow 0$$

$$ast2 = [10, 9, 8, \dots, 1] \rightarrow 0$$

$$ast3 = [-1, -2, -3, \dots, -10] \rightarrow 0$$

$$ast4 = [-1, -2, -3, \dots, -9, 10] \textcircled{6}$$

$$ast5 = [1, 2, 3, \dots, 9, \cancel{10}] \textcircled{9}$$



$$ast1 = [1, 2, 3, 4, 5, \cancel{6}, \cancel{7}, \cancel{8}, \cancel{9}, \cancel{10}]$$

$\cancel{+} \times \times \times \times \times \rightarrow [-]$

$$ast2 = [1, 2, \cancel{8}, \cancel{9}, \cancel{7}, \cancel{6}, \cancel{5}, \cancel{4}, \cancel{3}, \cancel{2}, \cancel{1}, \cancel{-9}]$$

$$\begin{bmatrix} 1, 2, 8 \\ 1, 2, 8, 9 \end{bmatrix}$$

\Rightarrow

new value

$\{1, 2, 8, 9\}$ \Rightarrow