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MA 473: Computational Finance Lab – VII 04/10/2021

1. The PDE modelling the Asian option for the European arithmetic average strike call (for $S > 0, A > 0, 0 \le t \le T$) is given by

$$\frac{\partial V}{\partial t} + \frac{1}{2}\sigma^2 S^2 \frac{\partial^2 V}{\partial S^2} + rS \frac{\partial V}{\partial S} + S \frac{\partial V}{\partial A} - rV = 0.$$

By using the transformation $V(S, A, t) = \widetilde{V}(S, R, t) = S \cdot H(R, t)$, with R = A/S, transform the above PDE into the following form:

$$\begin{cases} \frac{\partial H}{\partial t} + \frac{1}{2}\sigma^2 R^2 \frac{\partial^2 H}{\partial R^2} + (1 - rR) \frac{\partial H}{\partial R} = 0, \\ H = 0, & \text{for } R \to \infty, \\ \frac{\partial H}{\partial t} + \frac{\partial H}{\partial R} = 0, & \text{for } R = 0, \\ H(R_T, T) = \left(1 - \frac{R_T}{T}\right)^+ \end{cases}$$

- (a) Solve the above transformed PDE by the following schemes:
 - (i) Forward-Euler for time & central difference for space (FTCS) scheme.
 - (ii) Backward-Euler for time & central difference for space (BTCS) scheme.
 - (iii) Crank-Nicolson finite difference scheme with a suitable second-order approximation for the left boundary condition.
- (b) Plot the solution surfaces for K = 100, T = 0.2, r = 0.05, $\sigma = 0.25$ at different time levels.