# Package 'arqas'

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Type Package
Title Application in R for Queueing Analysis and Simulation
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<b>Depends</b> R (>= 1.8.0), distr, ggplot2
<b>Imports</b> methods, reshape, iterators, doParallel, foreach, fitdistrplus, grid, gridExtra
<b>Description</b> Provides functions to compute the main characteristics of the following queueing models: M/M/1, M/M/s, M/M/1/k, M/M/s/k, M/M/1/Inf/H, M/M/s/Inf/H, M/M/s/Inf/H, W/M/s/Inf/H with Y replacements, M/M/Inf, Open Jackson Networks and Closed Jackson Networks. Moreover, it is also possible to simulate similar queueing models with any type of arrival or service distribution: G/G/1, G/G/s, G/G/1/k, G/G/s/k, G/G/1/Inf/H, G/G/s/Inf/H, G/G/s/Inf/H with Y replacements, Open Networks and Closed Networks. Finally, contains functions for fit data to a statistic distribution.
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cdfcompggplot2

Cumulative Density plot using the package ggplot2

# Description

Cumulative Density plot using the package ggplot2

# Usage

cdfcompggplot2(lfitdata)

# Arguments

lfitdata a list of fitted data

# See Also

 $\label{thm:compggplot2} Other Distribution Analysis: \verb|denscompggplot2|; fitData|; goodnessFit|; qqcompggplot2|; summaryFit|$ 

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ClosedJacksonNetwork

Obtains the main characteristics of a Closed Jackson Network model

# Description

Obtains the main characteristics of a Closed Jackson Network model

## Usage

```
ClosedJacksonNetwork (mu = c(5, 5, 10, 15), s = c(2, 2, 1, 1), p = matrix(c(0.25, 0.15, 0.2, 0.4, 0.15, 0.35, 0.2, 0.3, 0.5, 0.25, 0.15, 0.1, 0.4, 0.3, 0.25, 0.05), 4, byrow = TRUE), <math>n = 3)
```

# Arguments

mu	Vector of mean service rates
S	Vector of servers at each node
р	Routing matrix, where $p_{ij}$ is the routing probability from node i to node j
n	Number of customers in the network

#### Value

Returns the next information of a Closed Jackson Network model:

```
rho Traffic intensity: \rho

1 Number of customers in the system: L

1q Number of customers in the queue: L_q

w Waiting time in the system: W

wq Waiting time in the queue: W_q

eff System efficiency: Eff = W/(W-W_q)
```

### See Also

```
Other AnaliticalModels: M_M_1_INF_H; M_M_1_K; M_M_1; M_M_INF; M_M_S_INF_H_Y; M_M_S_INF_H; M_M_S_K; M_M_S; OpenJacksonNetwork
```

```
# A system is composed of 4 workstations #interconnected. The monitoring of the #system is carried out by three programs #in continuous execution in some of the #workstations. Once each program ends, #it creates a copy of itself and sends this #copy to be executed in any of the #workstations, taking into account the #following probabilities:

# Origin-destiny 1 2 3 4
```

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```
0.25
                          0.15 0.20 0.40
#
                   0.15
                          0.35 0.20 0.30
                          0.25 0.15 0.10
#
       3
                   0.50
                          0.30 0.25 0.05
                   0.40
#The servers 1 and 2 have two processors and
#each of one have a process time with exponential
#distribution and capacitiy of 5 tasks per
#minute.
#The servers 3 and 4 have a single processor
#and they can serve 10 and 15 task per minute
#respectively.
ClosedJacksonNetwork (mu=c(5,5,10,15),
                     s=c(2,2,1,1),
                     p=matrix(c(0.25, 0.15, 0.20, 0.40,
                                0.15, 0.35, 0.20, 0.30,
                                0.50, 0.25, 0.15, 0.10,
                                0.40, 0.30, 0.25, 0.05), 4, byrow = TRUE),
                     n = 3)
```

# ClosedNetwork

Obtains the main characteristics of a Closed Network model by simulation

#### **Description**

Obtains the main characteristics of a Closed Network model by simulation

#### Usage

```
ClosedNetwork (serviceDistribution = c(Exp(5), Exp(5), Exp(10), Exp(15)), s = c(2, 2, 1, 1), p = array(c(0.25, 0.15, 0.5, 0.4, 0.15, 0.35, 0.25, 0.3, 0.2, 0.2, 0.15, 0.25, 0.4, 0.3, 0.1, 0.05), dim = c(4, 4), staClients = 100, nClients = 3, transitions = 1000, historic = FALSE, nsim = 10, nproc = 1)
```

# **Arguments**

serviceDistribution Service distributions for the nodes of the network (Each element must be an object of S4-class distr defined in distr package) Vector of servers at each node S Routing matrix, where  $p_{ij}$  is the routing probability from node i to node j р Number of customers used in the stabilization stage staClients nClients Number of customers in the system Number of transitions between nodes used in the simulation stage transitions Parameter to activate/deactivate the historic information historic nsim Number of simulations Processors used in the simulation. nproc

combineSimulations 5

#### Value

Returns the next information of a Closed Network model:

pn	Vector of empirical steady-state probabilities of having n customers in the system: $P_n$ (Only the probabilities bigger than 0 are included)
1	Vector of empirical number of customers in the nodes: $L$
lq	Vector of empirical number of customers in the queues of the nodes: $\mathcal{L}_q$
lqt	Empirical number of customers in the all the queues: $L_{qTotal}$
W	Vector of empirical waiting times in the nodes: $W$
wq	Vector of empirical waiting times in the queues of the nodes: $\mathcal{W}_q$
eff	Empirical system efficiency: $Eff = W/(W-W_q)$
rho	Empirical traffic intensity: $\rho$
historic	Optional parameter that stores the evolution of $L$ , $L_q$ , $W$ and $W_q$ , Customers in the system, Rho and Elapsed time during the simulation.

#### See Also

```
Other SimulatedModels: G_G_1_INF_H; G_G_1_K; G_G_1; G_G_INF; G_G_S_INF_H_Y; G_G_S_INF_H; G_G_S_K; G_G_S; OpenNetwork
```

# **Examples**

combineSimulations Combines a list of independent simulations of a queueing model, computing the mean and variance of each characteristic of interest

# Description

Combines a list of independent simulations of a queueing model, computing the mean and variance of each characteristic of interest

### Usage

```
combineSimulations(listsims)
```

# **Arguments**

listsims A list of independent simulations

6 fitData

#### Value

an object with the mean and estimated precision of estimated parameters L, Lq, W, Wq, Rho and Eff.

# **Examples**

```
combineSimulations(G_G_1 (nsim=5))
```

denscompggplot2

Density histogram Plot using the package ggplot2

# Description

Density histogram Plot using the package ggplot2

## Usage

```
denscompggplot2(lfitdata)
```

## **Arguments**

lfitdata a list of data fitted

## See Also

 $\label{thm:continuity:continuit$ 

fitData

Computes the estimated parameters of the distributions for the input data

# Description

Computes the estimated parameters of the distributions for the input data

## Usage

```
fitData(data, ldistr = c("exp", "norm", "weibull", "unif", "lnorm", "gamma",
    "beta"))
```

# Arguments

data data to estimate parameters

ldistr A list of distributions

#### Value

A list of estimate parameters for each distribution

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#### See Also

 $\label{thm:compggplot2} Other \ Distribution Analysis: \ \texttt{cdfcompggplot2}; \ \texttt{denscompggplot2}; \ \texttt{goodnessFit}; \ \texttt{qqcompggplot2}; \ \texttt{summaryFit}$ 

## **Examples**

```
mydata <- rnorm(100, 10, 0.5)
fitData(mydata)</pre>
```

FW

Distribution function of the waiting time in the system

### **Description**

Returns the value of the cumulative distribution function of the waiting time in the system for a queueing model

$$W(x) = P(W \le x)$$

# Usage

FW(qm, x)

## **Arguments**

qm Queueing model

x Time

Value

W(x)

## Methods (by class)

- MarkovianModel: Implements the default method (generates a message)
- M\_M\_1: Implements the method for a M/M/1 queueing model
- M\_M\_S: Implements the method for a M/M/S queueing model
- M\_M\_1\_K: Implements the method for a M/M/1/K queueing model
- M\_M\_S\_K: Implements the method for a M/M/S/K queueing model
- M\_M\_1\_INF\_H: Implements the method for a M/M/1/ $\infty$ /H queueing model
- M\_M\_S\_INF\_H: Implements the method for a M/M/s/∞/H queueing model
- M\_M\_S\_INF\_H\_Y: Implements the method for a M/M/s/∞/H with Y replacements queueing model
- M\_M\_INF: Implements the method for a M/M/∞ queueing model

FWq

### **Examples**

```
#Cumulative probability of waiting 1 units
#of time in the system
FW(M_M_1(), 1)
FW(M_M_S_K(), 1)

#You can also get multiple probabilities
#at once
FW(M_M_1_INF_H(), c(0, 0.25, 0.8))
FW(M_M_INF(), c(0, 0.25, 0.8))
```

FWq

Distribution function of the waiting time in the queue

# Description

Returns the value of the cumulative distribution function of the waiting time in the queue

$$W_q = P(W_q \le x)$$

#### Usage

```
FWq(qm, x)
```

# **Arguments**

qm Queueing model x Time

Value

 $W_q(x)$ 

# Methods (by class)

- MarkovianModel: Implements the default method (generates a message)
- M\_M\_1: Implements the method for a M/M/1 queueing model
- M\_M\_S: Implements the method for a M/M/S queueing model
- M\_M\_1\_K: Implements the method for a M/M/1/K queueing model
- M\_M\_S\_K: Implements the method for a M/M/S/K queueing model
- M\_M\_1\_INF\_H: Implements the method for a M/M/1/∞/H queueing model
- M\_M\_S\_INF\_H: Implements the method for a M/M/s/ $\infty$ /H queueing model
- M\_M\_S\_INF\_H\_Y: Implements the method for a M/M/s/∞/H with Y replacements queueing model
- M\_M\_INF: Implements the method for a M/M/∞ queueing model

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### **Examples**

```
#Cumulative probability of waiting 1 units
#of time in the system
FWq(M_M_1(), 1)
FWq(M_M_S_K(), 1)

#You can also get multiple probabilities
#at once
FWq(M_M_1_INF_H(), c(0, 0.25, 0.8))
FWq(M_M_INF(), c(0, 0.25, 0.8))
```

goodnessFit

Computes the p-value of the chi-square test and Kolmogorov-Smirnov test

# Description

Computes the p-value of the chi-square test and Kolmogorov-Smirnov test

# Usage

```
goodnessFit(lfitdata)
```

# Arguments

lfitdata a list of fitted data

# Value

the p-values and the values of the statistics in the chi-square test and Kolmogorov-Smirnov test

# See Also

```
mydata <- rnorm(100, 10, 0.5)
goodnessFit(fitData(mydata))</pre>
```

 $G_{-}G_{-}10$ 

G\_G\_1

Obtains the main characteristics of a G/G/1 model by simulation

# Description

Obtains the main characteristics of a G/G/1 model by simulation

# Usage

```
G_G_1(arrivalDistribution = Exp(3), serviceDistribution = Exp(6),
    staClients = 100, nClients = 1000, historic = FALSE, nsim = 10,
    nproc = 1)
```

# **Arguments**

arrivalDistribution

Arrival distribution (object of S4-class distr defined in distr package)

serviceDistribution

Service distribution (object of S4-class distr defined in **distr** package)

staClients Number of customers used in the stabilization stage nClients Number of customers used in the simulation stage

historic Parameter used to activate/deactivate the historic information

nsim Number of simulations

nproc Processors used in the simulation.

#### Value

Returns the next information of a G/G/1 model:

pn	Stores all the empirical steady-state probabilities of having n customers, with n from 0 to staClients+nClients: $P_n$ (Only the probabilities bigger than 0 are included)
1	Empirical number of customers in the system: $L$
lq	Empirical number of customers in the queue: $L_q$
W	Empirical waiting time in the system: $W$
wq	Empirical waiting time in the queue: $W_q$
eff	Empirical system efficiency: $Eff = W/(W - W_q)$
rho	Empirical traffic intensity: $\rho$
historic	Optional parameter that stores the evolution of $L$ , $L_q$ , $W$ and $W_q$ , $Customers$ in the system, $Rho$ and $Elapsed$ time during the simulation

#### See Also

```
\label{lem:other-simulated-models: ClosedNetwork; G_G_1_INF_H; G_G_1_K; G_G_INF; G_G_S_INF_H_Y; G_G_S_INF_H; G_G_S_K; G_G_S; OpenNetwork
```

```
G_G_1(Norm(10, 0.5), Unif(5,6), staClients=10, nClients=100, nsim=10)
```

 $G_G_1_INF_H$ 

G_G_1_INF_H	Obtains the main characteristics of a G/G/1/ $\infty$ /H model by simulation
-------------	--

#### **Description**

Obtains the main characteristics of a G/G/1/∞/H model by simulation

# Usage

```
G_G_1_INF_H(arrivalDistribution = Exp(3), serviceDistribution = Exp(6), H = 5, staClients = 100, IR_1R_2R_3 nSim = 10, IR_2R_3 nProc = 1)
```

## **Arguments**

arrivalDistribution

Arrival distribution (object of S4-class distr defined in distr package)

 ${\tt serviceDistribution}$ 

Service distribution (object of S4-class distr defined in **distr** package)

H Population size

staClients Number of customers used in the stabilization stage

nClients Number of customers used in the simulation stage

historic Parameter to activate/deactivate the historic information

nsim Number of simulations

nproc Processors used in the simulation.

### Value

Returns the next information of a G/G/1/ $\infty$ /H model:

pn	Vector of empirical steady-state probabilities of having n customers in the system: $P_n$ (Only the probabilities bigger than 0 are included)
1	Empirical number of customers in the system: $L$
lq	Empirical number of customers in the queue: $L_q$
W	Empirical waiting time in the system: $W$
мd	Empirical waiting time in the queue: $W_q$
eff	Empirical system efficiency: $Eff = W/(W-W_q)$
rho	Empirical traffic intensity: $\rho$
historic	Optional parameter that stores the evolution of $L, L_q, W$ and $W_q$ , Customers in the system, Rho and Elapsed time during the simulation

#### See Also

```
Other SimulatedModels: ClosedNetwork; G_G_1_K; G_G_1; G_G_INF; G_G_S_INF_H_Y; G_G_S_INF_H; G_G_S_K; G_G_S; OpenNetwork
```

```
 \texttt{G\_G\_1\_INF\_H} \, (\texttt{Norm} \, (10,\ 0.5) \, , \ \texttt{Unif} \, (5,6) \, , \ 10, \ \texttt{staClients=10}, \ \texttt{nClients=100}, \ \texttt{nsim=10} )
```

 $G_{-}G_{-}I_{-}K$ 

G	G	1	K

Obtains the main characteristics of a G/G/1/K model by simulation

#### **Description**

Obtains the main characteristics of a G/G/1/K model by simulation

# Usage

```
G_G_1_K(arrivalDistribution = Exp(3), serviceDistribution = Exp(6), K = 2,
    staClients = 100, nClients = 1000, historic = FALSE, nsim = 10,
    nproc = 1)
```

## **Arguments**

arrivalDistribution

Arrival distribution (object of S4-class distr defined in distr package)

 ${\tt serviceDistribution}$ 

Service distribution (object of S4-class distr defined in **distr** package)

K Maximun size of the queue

staClients Number of customers used in the stabilization stage

nClients Number of customers used in the simulation stage

historic Parameter to activate/deactivate the historic information

nsim Number of simulations

nproc Processors used in the simulation.

### Value

Returns the next information of a G/G/1/K model:

pn	Vector of empirical steady-state probabilities of having n customers in the system: $P_n$ (Only the probabilities bigger than 0 are included)
1	Empirical number of customers in the system: $L$
lq	Empirical number of customers in the queue: $L_q$
W	Empirical waiting time in the system: $W$
wd	Empirical waiting time in the queue: $W_q$
eff	Empirical system efficiency: $Eff = W/(W - W_q)$
rho	Empirical traffic intensity: $\rho$
historic	Optional parameter that stores the evolution of $L$ , $L_q$ , $W$ and $W_q$ , Customers in the system, Rho and Elapsed time during the simulation.

#### See Also

```
Other Simulated Models: Closed Network; G_G_1_INF_H; G_G_1; G_G_INF; G_G_S_INF_H_Y; G_G_S_INF_H; G_G_S_K; G_G_S; OpenNetwork
```

```
 \texttt{G\_G\_1\_K(Norm(10, 0.5), Unif(5,6), 5, staClients=10, nClients=100, nsim=10)} \\
```

 $G_G_INF$ 13

G_G_INF	Obtains the main characteristics of a G/G/ $\infty$ model by simulation

# **Description**

Obtains the main characteristics of a  $G/G/\infty$  model by simulation

#### Usage

```
G_G_{INF} (arrivalDistribution = Exp(3), serviceDistribution = Exp(6),
  staClients = 100, nClients = 1000, historic = FALSE, nsim = 10,
  nproc = 1)
```

# **Arguments**

arrivalDistribution

Arrival distribution (object of S4-class distr defined in **distr** package)

serviceDistribution

Service distribution (object of S4-class distr defined in **distr** package)

Number of customers used in stabilization stage staClients nClients Number of customers used in the simulation stage historic Parameter to activate/deactivate the historic information Number of simulations nsim

Processors used in the simulation. nproc

# Value

Returns the next information of a  $G/G/\infty$  model:

pn	Vector of empirical steady-state probabilities of having n customers in the system: $P_n$ (Only the probabilities bigger than 0 are included)
1	Empirical number of customers in the system: $L$
lq	Empirical number of customers in the queue: $L_q$
W	Empirical waiting time in the system: $W$
wq	Empirical waiting time in the queue: $W_q$
eff	Empirical system efficiency: $Eff = W/(W - W_q)$
rho	Empirical traffic intensity: $\rho$
historic	Optional parameter that stores the evolution of $L, L_q, W$ and $W_q$ , Customers in the system, Rho and Elapsed time during the simulation

# See Also

```
Other Simulated Models: Closed Network; G_G_1_INF_H; G_G_1_K; G_G_1; G_G_S_INF_H_Y;
\label{eq:G_G_S_INF_H; G_G_S_K; G_G_S; OpenNetwork} G\_G\_S\_INF\_H; G\_G\_S\_K; G\_G\_S; OpenNetwork
```

```
G_G_{INF}(Norm(10, 0.5), Unif(2,4), staClients=50, nClients=100, nsim=10)
```

 $G_{-}G_{-}S_{-}$ 

G\_G\_S

Obtains the main characteristics of a G/G/s model by simulation

#### **Description**

Obtains the main characteristics of a G/G/s model by simulation

# Usage

```
G_G_S(arrivalDistribution = Exp(3), serviceDistribution = Exp(6), s = 2, staClients = 100, nClients = 1000, historic = FALSE, nsim = 10, nproc = 1)
```

## **Arguments**

arrivalDistribution

Arrival distribution (object of S4-class distr defined in distr package)

 ${\tt serviceDistribution}$ 

Service distribution (object of S4-class distr defined in **distr** package)

s Number of servers

staClients Number of customers used in the stabilization stage nClients Number of customers used in the simulation stage

historic Parameter used to activate/deactivate the historic information

nsim Number of simulations

nproc Processors used in the simulation.

### Value

Returns the next information of a G/G/S model:

pn	vector of empirical steady-state probabilities of having n customers in the system: $P_n$ (Only the probabilities bigger than 0 are included)
1	Empirical number of customers in the system: $L$
lq	Empirical number of customers in the queue: $L_q$
W	Empirical waiting time in the system: $W$
мd	Empirical waiting time in the queue: $W_q$
eff	Empirical system efficiency: $Eff = W/(W - W_q)$
rho	Empirical Traffic intensity: $\rho$
historic	Optional parameter that stores the evolution of $L$ , $L_q$ , $W$ and $W_q$ , Customers in the system, Rho and Elapsed time during the simulation

#### See Also

```
Other SimulatedModels: ClosedNetwork; G_G_1_INF_H; G_G_1_K; G_G_1; G_G_INF; G_G_S_INF_H_Y; G_G_S_INF_H; G_G_S_K; OpenNetwork
```

```
 \texttt{G\_G\_S} \; (\texttt{Norm} \; (\texttt{10, 0.5}) \;, \; \; \texttt{Unif} \; (\texttt{5, 6}) \;, \; \; \texttt{2, staClients=10, nClients=100, nsim=10)}
```

 $G\_G\_S\_INF\_H$  15

G_G_S_INF_H	Obtains the main characteristics of a G/G/S/ $\infty$ /H model by simulation
-------------	--

# **Description**

Obtains the main characteristics of a G/G/S/ $\infty$ /H model by simulation

#### Usage

```
G_G_S_INF_H(arrivalDistribution = Exp(3), serviceDistribution = Exp(6), s = 3, H = 5, staClients = 100, nClients = 1000, historic = FALSE, nsim = 10, nproc = 1)
```

# **Arguments**

```
arrivalDistribution
                 Arrival distribution (object of S4-class distr defined in distr package)
serviceDistribution
                 Service distribution (object of S4-class distr defined in distr package)
                 Number of servers
S
                 Population size
Η
staClients
                 Number of customers used in the stabilization stage
nClients
                 Number of customers used in the simulation stage
                 Parameter to activate/deactivate the historic information
historic
nsim
                 Number of simulations
nproc
                 Processors used in the simulation.
```

#### Value

Returns the next information of a G/G/S/∞/H model

pn	Vector of empirical steady-state probabilities of having n customers in the system: $P_n$ (Only the probabilities bigger than 0 are included)
1	Empirical number of customers in the system: $L$
lq	Empirical number of customers in the queue: $L_q$
W	Empirical waiting time in the system: $W$
wq	Empirical waiting time in the queue: $W_q$
eff	Empirical system efficiency: $Eff = W/(W - W_q)$
rho	Empirical traffic intensity: $\rho$
historic	Optional parameter that stores the evolution of $L$ , $L_q$ , $W$ and $W_q$ , Customers in the system, Rho and Elapsed time during the simulation

# See Also

```
Other SimulatedModels: ClosedNetwork; G_G_1_INF_H; G_G_1_K; G_G_1; G_G_INF; G_G_S_INF_H_Y; G_G_S_K; G_G_S; OpenNetwork
```

```
G_G_S_INF_H(Norm(10, 0.5), Unif(5,6), 3, 10, staClients=10, nClients=100, nsim=10)
```

 $G_{-}G_{-}S_{-}INF_{-}H_{-}Y$ 

G_G_S_INF_H_Y	Obtains the main characteristics of a G/G/S/ $\infty$ /H with Y replacements model by simulation
	model of simulation

#### **Description**

Obtains the main characteristics of a G/G/S/\infty/H with Y replacements model by simulation

## Usage

```
G_G_S_INF_H_Y (arrivalDistribution = Exp(3), serviceDistribution = Exp(6), s = 3, H = 5, Y = 3, staClients = 100, nClients = 1000, historic = FALSE, nsim = 10, nproc = 1)
```

## **Arguments**

arrivalDistribution

Arrival distribution (object of S4-class distr defined in **distr** package)

serviceDistribution

Service distribution (object of S4-class distr defined in **distr** package)

Number of serversPopulation size

Y Number of replacements

staClients Number of customers used in the stabilization stage

nClients Number of customers used in the simulation stage

historic Parameter to activate/deactivate the historic information

nsim Number of simulations

nproc Processors used in the simulation.

## Value

Returns the next information of a G/G/1/S/∞/H/Y model:

pn	Vector of empirical steady-state probabilities of having n customers in the system: $P_n$ (Only the probabilities bigger than 0 are included)
1	Empirical number of customers in the system: $L$
lq	Empirical number of customers in the queue: $L_q$
W	Empirical waiting time in the system: $W$
wq	Empirical waiting time in the queue: $W_q$
eff	Empirical system efficiency: $Eff = W/(W - W_q)$
rho	Empirical traffic intensity: $\rho$
historic	Optional parameter that stores the evolution of $L$ , $L_q$ , $W$ and $W_q$ , Customers in the system, Rho and Elapsed time during the simulation

# See Also

```
Other SimulatedModels: ClosedNetwork; G_G_1_INF_H; G_G_1_K; G_G_1; G_G_INF; G_G_S_INF_H; G_G_S_K; G_G_S; OpenNetwork
```

 $G\_G\_S\_K$ 

#### **Examples**

```
 \texttt{G\_G\_S\_INF\_H\_Y} \ (\texttt{Norm} \ (10,\ 0.5) \ , \ \texttt{Unif} \ (5,6) \ , \ 3,\ 10,\ 2,\ \texttt{staClients=10},\ \texttt{nClients=100},\ \texttt{nsim=10} )
```

G\_G\_S\_K

Obtains the main characteristics of a G/G/s/K model by simulation

### **Description**

Obtains the main characteristics of a G/G/s/K model by simulation

## Usage

```
G_G_S_K(arrivalDistribution = Exp(3), serviceDistribution = Exp(6), s = 2,
  K = 3, staClients = 100, nClients = 1000, historic = FALSE,
  nsim = 10, nproc = 1)
```

### **Arguments**

arrivalDistribution

Arrival distribution (object of S4-class distr defined in distr package)

serviceDistribution

Service distribution (object of S4-class distr defined in **distr** package)

s Number of servers

K Maximun size of the queue

staClients Number of customers used in the stabilization stage

nClients Number of customers used in the simulation stage

historic Parameter to activate/deactivate the historic information

nsim Number of simulations

nproc Processors used in the simulation.

### Value

Returns the next information of a G/G/S/K model:

pn	Vector of empirical steady-state probabilities of having n customers in the system: $P_n$ (Only the probabilities bigger than 0 are included)
1	Empirical number of customers in the system: $L$
lq	Empirical number of customers in the queue: $L_q$
W	Empirical waiting time in the system: $\boldsymbol{W}$
wq	Empirical waiting time in the queue: $W_q$
eff	Empirical system efficiency: $Eff = W/(W-W_q)$
rho	Empirical traffic intensity: $\rho$
historic	Optional parameter that stores the evolution of $L, L_q, W$ and $W_q$ , Customers in the system, Rho and Elapsed time during the simulation

18 maxCustomers

#### See Also

```
Other SimulatedModels: ClosedNetwork; G_G_1_INF_H; G_G_1_K; G_G_1; G_G_INF; G_G_S_INF_H_Y; G_G_S_INF_H; G_G_S; OpenNetwork
```

# **Examples**

```
G_G_S_K(Norm(10, 0.5), Unif(5,6), 2, 5, staClients=10, nClients=100, nsim=10)
```

MarkovianModel

Defines a queueing model

## **Description**

Constructor for Markovian Model class.

# Usage

```
MarkovianModel(arrivalDistribution = Exp(1), serviceDistribution = Exp(1))
```

## **Arguments**

arrivalDistribution

Arrival distribution (object of S4-class distr defined in **distr** package)

serviceDistribution

Service distribution (object of S4-class distr defined in **distr** package)

#### Value

An object of class MarkovianModel, a list with the following components:

arrivalDistribution

Arrival distribution (object of S4-class distr defined in **distr** package)

serviceDistribution

Service distribution (object of S4-class distr defined in **distr** package)

 ${\tt maxCustomers}$ 

Returns the maximun value of n that satisfies the condition

 $P\_n$ 

> 0

### **Description**

Returns the maximun value of n that satisfies the condition

 $P_n$ 

*M\_M\_1* 

# Usage

```
maxCustomers(qm)
## S3 method for class 'M_M_S_INF_H'
maxCustomers(qm)
```

## **Arguments**

qm

object MarkovianModel

## **Details**

maxCustomers.M\_M\_S\_INF\_H implements the method for a M/M/s/ $\infty$ /H queueing model

### Methods (by class)

- MarkovianModel: implements the default method. Returns infinite.
- M\_M\_1\_K: Implements the method for a M/M/1/K queueing model
- M\_M\_S\_K: Implements the method for a M/M/S/K queueing model
- M\_M\_1\_INF\_H: Implements the method for a M/M/1/\infty/H queueing model
- M\_M\_S\_INF\_H\_Y: Implements the method for a M/M/s/\infty/H/Y queueing model

## **Examples**

```
maxCustomers(M_M_1_K())
maxCustomers(M_M_S_INF_H_Y())
maxCustomers(M_M_S_INF_H(lambda=1/2, mu=60/5, s=2, h=5))
```

 $M_{M_1}$ 

Obtains the main characteristics of a M/M/1 queueing model

# Description

Obtains the main characteristics of a M/M/1 queueing model

# Usage

```
M_M_1 (lambda = 3, mu = 6)
```

#### **Arguments**

lambda Mean arrival ratemu Mean service rate

20 M\_M\_1\_INF\_H

#### Value

Returns the next information of a M/M/1 model:

rho	Traffic intensity: $\rho$
cn	Coefficients used in the computation of $P_n$ : $C_n$
р0	Probability of empty system: $P_0$
1	Number of customers in the system: $L$
lq	Number of customers in the queue: $L_q$
W	Waiting time in the system: ${\cal W}$
wq	Waiting time in the queue: $W_q$
eff	System efficiency: $Eff = W/(W - W_q)$

# See Also

```
Other Analitical Models: Closed Jackson Network; M_M_1_INF_H; M_M_1_K; M_M_INF; M_M_S_INF_H_Y; M_M_S_INF_H; M_M_S_K; M_M_S; Open Jackson Network
```

### **Examples**

```
#A workstation with a single processor

#runs programs with CPU time following

#an exponential distribution with mean 3 minutes.

#The programs arrives to the workstation following

#a Poisson process with an intensity of 15

#programs per hour.

M_M_1(lambda=15, mu=60/3)
```

M\_M\_1\_INF\_H

Obtains the main characteristics of a M/M/1/\infty/H queueing model

# Description

Obtains the main characteristics of a  $M/M/1/\infty/H$  queueing model

# Usage

```
M_M_1_INF_H(lambda = 1/2, mu = 60/5, h = 5)
```

# Arguments

lambda	Mean arrival rate
mu	Mean service rate
h	Population size

*M\_M\_1\_K* 21

#### Value

Returns the next information of a M/M/1/ $\infty$ /H model :

Constant:  $\lambda/\mu$ rho Traffic intensity:  $\bar{\rho}$ barrho Mean effective arrival rate:  $\bar{\rho}$ barlambda Coefficients used in the computation of  $P_n$ :  $C_n$ cn 0g Probability of empty system:  $P_0$ 1 Number of customers in the system: L Number of customers in the queue:  $L_q$ lq Waiting time in the system: WWaiting time in the queue:  $W_q$ wq System Efficiency:  $Eff = W/(W - W_q)$ eff

#### See Also

```
Other Analitical Models: Closed Jackson Network; M_M_1_K; M_M_1; M_M_INF; M_M_S_INF_H_Y; M_M_S_INF_H; M_M_S_K; M_M_S; Open Jackson Network
```

### **Examples**

```
# A computer system with five workstations must
# make a back- up from time to time, preventing
# users from using the system.
# The time between ending a back -up until the
# next begins is random and follows an
# exponential distribution with mean 2 hours.
# The duration of the backup is also random and
# follows an exponential distribution with mean
# 5 minutes.
# There exists a single tape drive to perform the
# back-up process, the station will wait if it is
# busy.

M M 1 INF H (lambda =1/2, mu=60/5, h=5)
```

M\_M\_1\_K

Obtains the main characteristics of a M/M/1/K queueing model

# **Description**

Obtains the main characteristics of a M/M/1/K queueing model

## Usage

```
M_M_1_K(lambda = 3, mu = 6, k = 2)
```

 $M_M_{INF}$ 

### **Arguments**

lambda Mean arrival ratemu Mean service rate

k Maximun size of the queue

#### Value

rho

Returns the next information of a M/M/1/K model:

 $\begin{array}{ll} {\rm barrho} & {\rm Traffic\ intensity:}\ \bar{\rho} \\ {\rm barlambda} & {\rm Effective\ arrival\ rate:}\ \bar{\lambda} \\ {\rm l} & {\rm Mean\ number\ of\ customers\ in\ the\ system:}\ L} \\ {\rm lq} & {\rm Mean\ number\ of\ customers\ in\ the\ queue:}\ L_q} \end{array}$ 

Constant coefficient:  $\lambda/\rho$ 

w Waiting time in the system: W wq Waiting time in the queue:  $W_q$  eff Efficiency:  $Eff = W/(W-W_q)$ 

#### See Also

```
Other Analitical Models: Closed Jackson Network; M_M_1_INF_H; M_M_1; M_M_INF; M_M_S_INF_H_Y; M_M_S_INF_H; M_M_S_K; M_M_S; Open Jackson Network
```

# **Examples**

```
#A workstation with a single processor #runs programs with CPU time following #an exponential distribution with mean 3 minutes. #The programs arrive to the workstation following #a Poisson process with an intensity of 15 #programs per hour. #The workstation has a limited memory and only #one program is allowed to wait if the processor #is busy.

M_M_1_K(lambda=15, mu=60/3, k=1)
```

M\_M\_INF

Obtains the main characteristics of a  $M/M/\infty$  queueing model

# Description

Obtains the main characteristics of a M/M/\infty queueing model

# Usage

```
M_M_{INF}(lambda = 3, mu = 6)
```

M\_M\_S 23

### **Arguments**

lambda Mean arrival ratemu Mean service rate

#### Value

Returns the next information of a M/M/ $\infty$  model:

Constant coefficient:  $\lambda/\mu$ rho Traffic intensity:  $\bar{\rho}$ barrho Probability of empty system:  $P_0$ р0 Number of customers in the system: L1 Number of customers in the queue:  $L_q$  ( $L_q = 0$  in this model) lq Waiting time in the system:  ${\cal W}$ W Waiting time in the queue:  $W_q$  ( $W_q = 0$  in this model) рw System efficiency:  $Eff = W/(W - W_q)$ eff

#### See Also

```
Other Analitical Models: Closed Jackson Network; M_M_1_INF_H; M_M_1_K; M_M_1; M_M_S_INF_H_Y; M_M_S_INF_H; M_M_S_K; M_M_S; Open Jackson Network
```

# **Examples**

```
#The number of people turning on their television sets #on Saturday evening during prime time can be described #rather well by a Poisson distribution with a mean of #100000/hr.
#There are five major TV stations, and a given person #choose among these essentially at random.
#Surveys have also shown that the average person tunes #in for 90 min and that viewing times are approximately #exponentially distributed.
M_M_INF(lambda=100000/5, mu=60/90)
```

Obtains the main characteristics of a M/M/s queueing model

# Description

 $M_M_S$ 

Obtains the main characteristics of a M/M/s queueing model

# Usage

```
M_M_S (lambda = 3, mu = 6, s = 2)
```

# **Arguments**

lambda	Mean arrival rate
mu	Mean service rate
S	Number of servers

 $M_M_S_INF_H$ 

#### Value

Returns the next information of a M/M/s model:

rho	Traffic intensity: $\rho$
cn	Coefficients used in the computation of $P_n$ : $C_n$
p0	Probability of empty system: $P_0$
1	Number of customers in the system: $L$
lq	Number of customers in the queue: $L_q$
W	Waiting time in the system: $W$
wq	Waiting time in the queue: $W_q$
eff	System efficiency: $Eff = W/(W - W_q)$

## See Also

```
\label{lem:other-analitical-Models:ClosedJacksonNetwork; M_M_1_INF_H; M_M_1_K; M_M_1; M_M_INF; M_M_S_INF_H_Y; M_M_S_INF_H; M_M_S_K; OpenJacksonNetwork
```

## **Examples**

```
#A workstation with three processors
#runs programs with CPU time following
#an exponential distribution with mean 3 minutes.
#The programs arrives to the workstation following
#a Poisson process with an intensity of 15
#programs per hour.

M_M_S(lambda=15, mu=60/3, s=3)
```

 $M_M_S_INF_H$  Obtains the main characteristics of a M/M/s/ $\infty$ /H queueing model

# Description

Obtains the main characteristics of a M/M/s/ $\infty$ /H queueing model

# Usage

```
M_M_S_INF_H(lambda = 1/2, mu = 60/5, s = 2, h = 5)
```

# Arguments

lambda	Mean arrival rate
mu	Mean service rate
S	Number of servers
h	Population size

 $M_{M_S_INF_H_Y}$  25

#### Value

Returns the next information of a M/M/s/ $\infty$ /H model:

Constant coefficient:  $\lambda/\mu$ rho barrho Traffic intensity:  $\bar{\rho}$ barlambda Mean effective arrival rate:  $\bar{\rho}$ Coefficients used in the computation of  $P_n$ :  $C_n$ cn рO Probability of empty system:  $P_0$ 1 Number of customers in the system: Llq Number of customers in the queue:  $L_q$ Waiting time in the system: WW Waiting time in the queue:  $W_q$ wq System efficiency:  $Eff = W/(W - W_a)$ eff

#### See Also

 $\label{loss} Other Analitical Models: {\tt ClosedJacksonNetwork}; {\tt M\_M\_1\_INF\_H}; {\tt M\_M\_1\_K}; {\tt M\_M\_1}; {\tt M\_M\_INF}; {\tt M\_M\_S\_INF\_H\_Y}; {\tt M\_M\_S\_K}; {\tt M\_M\_S}; {\tt OpenJacksonNetwork}$ 

### **Examples**

```
# A computer system with five workstations must
# make a back- up from time to time, preventing
# users from using the system.
# The time between ending a back -up until the
# next begins is random and follows an
# exponential distribution with mean 2 hours.
# The duration of the backup is also random and
# follows an exponential distribution with mean
# 5 minutes.
# There are 2 tape drives to perform the
# back-up process, the station remained on hold
# if both were occupied.

M_M_S_INF_H(lambda=1/2, mu=60/5, s=2, h=5)
```

 $M_M_S_INF_H_Y$  Obtains the main characteristics of a M/M/s/ $\infty$ /H with Y replacements queueing model

# **Description**

Obtains the main characteristics of a M/M/s/ $\infty$ /H with Y replacements queueing model

## Usage

```
M_M_S_INF_H_Y (lambda = 3, mu = 6, s = 3, h = 5, y = 3)
```

 $M_{M_sINF_H_Y}$ 

## **Arguments**

lambda	Mean arrival rate
mu	Mean service rate
S	Number of servers
h	Population size
У	Number of replacements

#### Value

Returns the next information of a M/M/s/∞/H/Y model:

rho	Constant coefficient: $\lambda/\rho$
barrho	Traffic intensity: $\bar{\rho}$
barlambda	Effective arrival rate: $\bar{\lambda}$
cn	Coefficients used in the computation of $P_n$ : $C_r$
p0	Probability of empty system: $P_0$
1	Number of customers in the system: $L$
lq	Number of customers in the queue: $L_q$
W	Waiting time in the system: $\boldsymbol{W}$
wq	Waiting time in the queue: $W_q$
eff	System efficiency: $Eff = W/(W - W_q)$

# See Also

```
\label{loss} Other Analitical Models: {\tt ClosedJacksonNetwork}; {\tt M\_M\_1\_INF\_H}; {\tt M\_M\_1\_K}; {\tt M\_M\_1\_K}; {\tt M\_M\_S\_INF\_H}; {\tt M\_M\_S\_K}; {\tt M\_M\_S}; {\tt OpenJacksonNetwork}
```

```
#A bank has 5 ATMs. Occasionally one ot them is #damaged until one of the two hired technicians #repairs it. It is known that the mean time to repair #follows an exponential distribution with mean 10 #minutes, while the distribution of time an ATM #is run until it breaks down it is also exponential #with mean 2 hours. The bank has an ATM extra to #replace a damaged one.

M_M_S_INF_H_Y(lambda=1/2, mu=60/10, s=2, h=5, y=1)
```

 $M_{-}M_{-}S_{-}K$  27

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Obtains the main characteristics of a M/M/S/k queueing model

### **Description**

Obtains the main characteristics of a M/M/S/k queueing model

## Usage

```
M_M_S_K(lambda = 3, mu = 6, s = 2, k = 3)
```

#### **Arguments**

lambda	Mean arrival rate
mu	Mean service rate
S	Number of servers
k	Maximun size of the queue

#### Value

Returns the next information of a M/M/S/K model:

rho	Constant coefficient: $\lambda/\rho$
barrho	Traffic intensity: $\bar{\rho}$
barlambda	Effective arrival rate: $\bar{\lambda}$
cn	Coefficients used in the computation of $P_n$ : $C_n$
pks	Probability of having $K+s$ customers in the system: $P_{K+s}$
p0	Probability of empty system: $P_0$
1	Number of customers in the system: ${\cal L}$
lq	Number of customers in the queue: $L_q$
W	Waiting time in the system: $W$
wq	Waiting time in the queue: $W_q$
eff	System efficiency: $Eff = W/(W - W_q)$

# See Also

```
\label{lem:other-analitical-Models:ClosedJacksonNetwork; M_M_1_INF_H; M_M_1_K; M_M_1; M_M_INF; M_M_S_INF_H_Y; M_M_S_INF_H; M_M_S; OpenJacksonNetwork
```

```
#A workstation with three processors
#runs programs with CPU time following
#an exponential distribution with mean 3 minutes.
#The programs arrive to the workstation following
#a Poisson process with an intensity of 15
#programs per hour.
#The workstation has a limited memory and only
#one program is allowed to wait if the processor
```

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```
#is busy.

M_M_S_K(lambda=15, mu=60/3, s=3, k=1)
```

no\_distr

Defines an empty object representing the inexistence of a distribution.

## **Description**

Defines an empty object representing the inexistence of a distribution.

## Usage

```
no_distr()
```

OpenJacksonNetwork Obtains the main characteristics of an Open Jackson network model

# **Description**

Obtains the main characteristics of an Open Jackson network model

## Usage

```
OpenJacksonNetwork(lambda = c(20, 30), mu = c(100, 25), s = c(1, 2), p = matrix(c(0.2, 0.25, 0.1, 0), nrow = 2, ncol = 2))
```

# Arguments

lambda	Vector of arrival rates at each node
mu	Vector of mean service rates
S	Vector with the number of servers at each node
р	Routing matrix, where $p_{ij}$ is the routing probability from node i to node j

# Value

Returns the next information of an Open Jackson network model:

rho	Traffic intensity: $\rho$
1	Vector with the number of customers in the nodes: $L$
lq	Vector with the number of customers in the queue at each node: $L_q$
W	Vector with the waiting time in each node: $W$
wq	Vector with the waiting time in the queue at each node: $W_q$
lt	Number of customers in the network: $L_{Total}$
lqt	Number of customers in all the queues: $L_{qTotal}$
wt	Total waiting time in the network: $W_{Total}$
wqt	Total waiting time in all the queues: $W_{qTotal}$
eff	System efficiency: $Eff = W/(W - W_q)$

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#### See Also

```
\label{loss} Other Analitical Models: {\tt ClosedJacksonNetwork}; {\tt M\_M\_1\_INF\_H}; {\tt M\_M\_1\_K}; {\tt M\_M\_1\_K}; {\tt M\_M\_S\_INF\_H}; {\tt M\_M\_S\_INF\_H}; {\tt M\_M\_S\_INF\_H}; {\tt M\_M\_S\_K}; {\tt M\_M\_S}
```

## **Examples**

```
#Two servers receive a number of tasks per minute;
#20 tasks per minute in the case of the first
#server and 30 tasks per minute in the second one.
#The unique processsor in the first server can manage
#100 tasks per minute, while the two processors in the
#second server only can manage 25 task per minute.
#When a task is close to finish in the server 2, it creates
#a new task in the server 1 with a probability of 25%,
#the task ends in the other case.
#The tasks that ends in the server 1 creates a new one
#in the same server the 20% of the times and creates
#a new one in the server 2 the 10% of the times, ending
#in other case.
OpenJacksonNetwork(lambda=c(20, 30),
                   mu=c(100, 25),
                   s=c(1,2),
                   p=matrix(c(0.2,0.1,
                              0.25,0), 2, byrow = TRUE))
```

OpenNetwork

Obtains the main characteristics of an Open Network model by simulation

### **Description**

Obtains the main characteristics of an Open Network model by simulation

# Usage

```
OpenNetwork (arrivalDistribution = c(Exp(20), Exp(30)), serviceDistribution = c(Exp(100), Exp(25)), s = c(1, 2), p = matrix(c(0.2, 0.25, 0.1, 0), nrow = 2, ncol = 2), staClients = 100, transitions = 1000, historic = FALSE, nsim = 10, nproc = 1)
```

# Arguments

```
arrivalDistribution
```

Vector indicating the arrival distribution at each node (Each element must be an object of S4-class distr defined in **distr** package or the no\_distr() object)

serviceDistribution

Vector indicating the service distribution at each node (Each element must be an object of S4-class distr defined in **distr** package)

S Vector of servers in each node

p Routing matrix, where  $p_{ij}$  is the routing probability from node i to node j

staClients Number of customers used in the stabilization stage

30 P0i

transitions	Number of transitions between nodes used in the simulation stage
historic	Parameter to activate/deactivate the historic information
nsim	Number of simulations
nproc	Processors used in the simulation.

## Value

Returns the next information of an Open network model:

pn	Vector of steady-state probabilities of having n customers in the system: $P_n$
1	Vector of expected number of customers in the nodes: $L$
lq	Vector of expected number of customers in the queues of the nodes: $\mathcal{L}_q$
lqt	Expected number of customers in all the queues: $L_{qTotal}$
W	Vector of expected waiting times in the nodes: $W$
wq	Vector of expected waiting time in the queues of the nodes: $\boldsymbol{W}_q$
eff	System efficiency: $Eff = W/(W - W_q)$
rho	Traffic intensity: $\rho$
historic	Optional parameter that stores the evolution of $L$ , $L_q$ , $W$ and $W_q$ , Customers in the system, Rho and Elapsed time during the simulation.

#### See Also

```
Other SimulatedModels: ClosedNetwork; G_G_1_INF_H; G_G_1_K; G_G_1; G_G_INF; G_G_S_INF_H_Y; G_G_S_INF_H; G_G_S_K; G_G_S
```

# **Examples**

```
OpenNetwork (arrivalDistribution = c(Exp(20), no\_distr()), serviceDistribution = c(Exp(100), Exp(25)), s = c(1,2), p = matrix(c(0.2, 0.25, 0.1, 0), nrow=2, ncol=2), staClients = 10, transitions = 100, nsim = 100
```

P0i Steady-state probability of 0 customers in the system on the node i of an Open Jackson Network.

## **Description**

Returns the value of the probability of having 0 customers at node i of an Open Jackson Network.

## Usage

```
P0i(net, i)
## S3 method for class 'OpenJackson'
P0i(net, i)
```

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# **Arguments**

 $\text{net} \hspace{1cm} Network$ 

i Node. Index starts in 1.

## **Details**

P0i.OpenJackson implements the method for an Open Jackson Network model

#### Value

 $P_{0,i}$ 

# **Examples**

```
#Probability of having 0 customers on the node 2
P0i(OpenJacksonNetwork(), 2)
```

Ρi

Steady-state probability of n customers at node i of a network.

# Description

Returns the value  $P_i(n)$  in the node i of a Closed Jackson Network

# Usage

```
Pi(net, n, node)
## S3 method for class 'ClosedJackson'
Pi(net, n, node)
## S3 method for class 'SimulatedNetwork'
Pi(net, n, node)
```

# Arguments

net Closed Jackson Network

n Customers node Node

#### **Details**

 ${\tt Pi.ClosedJackson}\ implements\ the\ method\ for\ a\ Closed\ Jackson\ Network\ model$ 

 $\verb"Pi.Simulated Network" implements the method for a Simulated Network model \\$ 

## Value

 $P_n$  in the selected node

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## **Examples**

```
#Probability of having 0 customers on node 2
Pi(ClosedJacksonNetwork(), 0, 2)

#It is possible obtain multiple probabilities
#for a node at once.
Pi(ClosedJacksonNetwork(), 0:2, 2)
```

```
plot.MarkovianModel
```

Shows the main graphics of the parameters of a Markovian Model

# Description

Shows the main graphics of the parameters of a Markovian Model

# Usage

```
## S3 method for class 'MarkovianModel'
plot(x, t = list(range = seq(x$out$w, x$out$w * 3,
   length.out = 100)), n = c(0:5), only = NULL, graphics = "ggplot2", ...)
```

# Arguments

X	Markovian Model
t	range for drawing the waiting plots
n	range for drawing the probabilities plot
only	Allow to only show the waiting plots or the probabilites plots. Must be NULL, "t" or "n" $$
graphics	library used to draw the plots
	Further arguments

#### **Details**

 $\verb|plot.MarkovianModel| implements the function for an object of class MarkovianModel|.$ 

```
plot.SimulatedModel
```

#Shows a plot of the evolution of a variable during the simulation ##

## **Description**

#Shows a plot of the evolution of a variable during the simulation ##

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#### Usage

```
## S3 method for class 'SimulatedModel'
plot(x, minrange = 1, maxrange, var = "L",
    graphics = "ggplot2", depth = maxrange - minrange, ...)

## S3 method for class 'SimulatedNetwork'
plot(x, minrange = 1, maxrange, var = "L",
    graphics = "ggplot2", depth = maxrange - minrange, nSimulation = NULL,
    ...)

## S3 method for class 'list'
plot(x, minrange = 1, maxrange, var = "L",
    graphics = "ggplot2", depth = maxrange - minrange + 1, nSimulation = 1,
    showMean = TRUE, showValues = TRUE, ...)
```

#### **Arguments**

X	Simulated Model #
minrange	Number of customer needed to establish the start of the plot #
maxrange	Number of customer needed to establish the end of the plot #
var	This variable indicates the parameter of the queue to show in graphic (L, Lq, W, Wq, Clients, Intensity) $\#$
graphics	Type of graphics: "graphics" use the basic R plot and "ggplot2" the library ggplot2 #
depth	Number of points printed in the plot #
	Further arguments passed to or from other methods. #
nSimulation	Only used when the var param is equal to "Clients". Selects one of the multiple simulations to show the evolution of the Clients. #
showMean	Shows the mean of all the simulations
showValues	Shows the values of all the simulations

# **Details**

```
plot.SimulatedModel implements the function for an object of class SimulatedModel. plot.SimulatedNetwork implements the function for an object of class SimulatedNetwork. plot.list implements the function for an object of class list
```

Рn

Steady-state probability of having n customers in the system

### **Description**

Returns the probability of having n customers in the given queueing model

# Usage

```
Pn(qm, n)
```

34 Pn

### **Arguments**

qm Queueing model

Number of customers. With OpenJacksonNetwork objects must be a vector with same length as nodes. With ClosedJacksonNetwork objects also the sum the vector must be equal to the number of customers in the network.

Value

 $P_n$ 

## Methods (by class)

- MarkovianModel: Implements the method for a Markovian model
- M\_M\_1: Implements the method for a M/M/1 queueing model
- M\_M\_S: Implements the method for a M/M/s queueing model
- M\_M\_1\_K: Implements the method for a M/M/1/K queueing model
- M\_M\_S\_K: Implements the method for a M/M/s/K queueing model
- M\_M\_1\_INF\_H: implements the method for a M/M/1/∞/H queueing model
- M\_M\_S\_INF\_H: Implements the method for a M/M/s/∞/H queueing model
- M\_M\_S\_INF\_H\_Y: Implements the method for a M/M/s/\infty/H/Y queueing model
- M\_M\_INF: Implements the method for a M\_M\_INF queueing model
- OpenJackson: Implements the method for a Open Jackson Network model
- ClosedJackson: Implements the method for a Closed Jackson Network model
- $\bullet$  SimulatedModel: Implements the method for a Simulated model

```
#Probability of having one customer in the
#system
Pn(M_M_S(), 1)
Pn(M_M_INF(), 1)
#You can also get multiple probabilities
#at once
Pn(M_M_1_INF_H(), 0:5)
Pn(M_M_S_K(), 1:3)
#With networks must be a vector with
#same length as nodes
#Probability of having 0 customers in
#the node 1, and 2 customers in node 2
Pn(OpenJacksonNetwork(), c(0, 2))
#Probability of having 1,2,0, and 0
#customers in nodes 1,2,3 and 4 respectively
Pn(ClosedJacksonNetwork(), c(1,2,0,0))
```

Qn 35

Qn

Steady-state probability of finding n customers in the system when a new customer arrives

## **Description**

Returns the probability of having n customers in the system at the moment of the arrival of a customer.

# Usage

```
Qn(qm, n)
```

#### **Arguments**

qm Queueing model
n Customers

Value

 $Q_n$ 

### Methods (by class)

- MarkovianModel: Implements the default method (generates a message)
- M\_M\_1\_K: Implements the method for a M/M/1/K queueing model
- M\_M\_S\_K: Implements the method for a M/M/S/K queueing model
- M\_M\_1\_INF\_H: Implements the method for a M/M/1/\infty/H queueing model
- M\_M\_S\_INF\_H: Implements the method for a M/M/s/∞/H queueing model
- M\_M\_S\_INF\_H\_Y: Implements the method for a M/M/s/ $\infty$ /H with Y replacements queueing model

```
#Probability of having one customer in the
#queue
Qn(M_M_1_K(), 1)
Qn(M_M_S_INF_H(), 1)

#You can also get multiple probabilities
#at once
Qn(M_M_1_INF_H(), 0:5)
Qn(M_M_S_K(), 1:3)
```

qqcompggplot2

Q-Q Plot using the package ggplot2

# Description

Q-Q Plot using the package ggplot2

# Usage

```
qqcompggplot2(lfitdata)
```

## **Arguments**

```
lfitdata a list of fitted data
```

#### See Also

 $\label{thm:compggplot2} Other \ Distribution Analysis: \ \texttt{cdfcompggplot2}; \ dens \ compggplot2; \ fit \ \texttt{Data}; \ goodness \ Fit; \ summary \ Fit$ 

```
summary.SimulatedModel
```

Shows basic statistical information of the variable

# Description

Shows basic statistical information of the variable

#### Usage

```
## S3 method for class 'SimulatedModel'
summary(object, var = "l", ...)
```

# Arguments

object SimulatedModel

var Main characteristic of an queue model

... Further argumets

# **Details**

 $\verb|summary.Simulated Model| implements the function for an object of class Simulated Model.$ 

summaryFit 37

summaryFit	Shows three plots: The histogram and theoretical densities, the empirical and theoretical CDF's and the Q-Q plot

## **Description**

Shows three plots:The histogram and theoretical densities, the empirical and theoretical CDF's and the Q-Q plot

# Usage

```
summaryFit(lfitdata, graphics = "ggplot2", show = "all")
```

# Arguments

lfitdata a list of fitted data

graphics Type of graphics: "graphics" uses the basic R plot and "ggplot2" the library

ggplot2

show Select what plots to show. Can be: "all", "dens" for the histogram, "cdf" for the

CDF's or "qq" for the Q-Q-plot

# See Also

 $\label{thm:compggplot2} Other \ Distribution Analysis: \ \texttt{cdfcompggplot2}; \ \texttt{denscompggplot2}; \ \texttt{fitData}; \ \texttt{goodnessFit}; \ \texttt{qqcompggplot2}$