

# Question Paper

1. Surfaces  $\phi(x, y, z) = C_1$  and  $\psi(x, y, z) = C_2$ , are orthogonal if :

A.  $\nabla \phi \cdot \nabla \psi = 0$

B.  $(\nabla \phi, \nabla \psi) = 0$

C.  $\nabla \phi \cdot \nabla \psi = 0$

D.  $\nabla \phi \cdot \nabla \psi = 0$

2. Gradient of a scalar function  $\phi(x, y, z)$  is :

A.  $\nabla \phi$

B.  $\nabla^2 \phi$

C.  $\nabla \cdot \phi$

D. None of the above.

3. Let  $F = xi + yj + zk$  and  $r = |r|$ , then :

A.  $r = F$

B.  $r = F/r$

C.  $r = rF$

D.  $r = r/F$

4. Divergence of vector field  $F = xi + 2yj - zk$  is:

A. 5

B. 10

C. 0

D. 20

5. For the scalar function  $f$ ,  $\text{div}[\text{grad } f]$  is equal to :

A.  $\nabla^2 f$

B.  $\nabla f$

C.  $\nabla \cdot f$

D. None of the above.

6. If  $F = xi + yj + zk$ , then  $\nabla \cdot F =$

A. 0

B. 3

C. 1

D. 3

7. If  $F = (x+3)i + (y-2z)j + (x+nz)k$  is solenoidal, then the value of  $n$  is :

A. 2

B. 3

- C. 0
- D. -1

8. The curl of a vector function  $F=(y^2z)i$  at a point (1,2,3) is:

- A. 0
- B.  $-3j$
- C.  $3j$
- D. 0

9. If  $dy/dx = (x+y+1)/(x+y+1)$ , then it is reduced to homogeneous by :

- A.  $x+y=v+1$
- B.  $x+y=v$
- C.  $x-y=v$
- D.  $x+y+1=v$

10. For  $dy/dx = x^2/y$ , (A) linear in x (B) linear in y (C) non-linear in x (D) none of the above

- A. linear in x
- B. linear in y
- C. non-linear in x
- D. none of the above

11. If  $z = 3+iy$ ,  $\bar{z} = 3-i$ , then real part of  $z \bar{z}$ , is

- A.  $9-y^2$
- B.  $9+y^2$
- C.  $9-y$
- D.  $9+y$

12.  $\text{Arg}(z)$  at  $z=0$  is:

- A. 0
- B. not defined
- C.  $<$
- D.  $< \pi$

13. If  $z=1-i$ , then conjugate of conjugate of  $z$  is :

- A.  $1+i$
- B.  $1-i$
- C.  $1+i$
- D.  $1-i$

14. If  $z=x+iy$ , then  $z+\bar{z}$  is

- A.  $x$

- B.  $2x$
- C. 2
- D.  $2x+i2y$

15. If  $z=2.4+3i$ , then modulus of  $z$  is :

- A. 13
- B. 5
- C. " 13
- D. " 5

16. Imaginary part of  $z$  is, where  $z = x+iy$

- A.  $x$
- B.  $y$
- C.  $x$
- D.  $y$

17. If  $x+y = 5$ , then:

- A.  $x=1, y=2$
- B.  $x=2, y=3$
- C.  $x=3, y=2$
- D.  $x=3, y=2$

18. The differential equation  $d^2y/dx^2 + 3dy/dx + 2y=0$  is:

- A. linear
- B. non-linear
- C. linear with constant coefficients
- D. none of the above

19. A differential equation is ordinary if it has :

- A. one dependent variable
- B. one independent variable
- C. both (A) and (B)
- D. none of the above

20. Differential equation  $Mdx+Ndy=0$  is exact iff':

- A. " $M/' y = N/' x$
- B. " $M/' x = N/' y$
- C. " $M/' x = -N/' y$
- D. " $M/' y = -N/' x$

21.  $(y-\cos x)+(x+\sin y)dy/dx=0$  is:

- A. exact ODE

- B. not exact ODE
- C. linear in y
- D. linear in x

22. General solution of  $(d^2y/dx^2)-4y=0$  is:

- A.  $y=c_1 e^{2x} + c_2 e^{-2x}$
- B.  $y=c_1 e^{2x} + c_2 e^{2x}$
- C.  $y=c_1 e^0$
- D.  $y=c_1 e^{\{.0}$

23. Integrating factor of  $dy/dx+Py=Q$  is:

- A.  $e^{\int P dx}$
- B.  $e^{\int Q dx}$
- C.  $e^{\int P dx}$
- D. None of the above

24. Fourier series uses which domain representation of signals ?

- A. Time domain
- B. Frequency domain
- C. Both (A) and (B)
- D. None of the above

25. Solution of  $d^2y/dx^2=1$  is:

- A.  $y=x+c$
- B.  $y=x$
- C.  $y=x^2+c$
- D.  $y=e^0$

26. The equation  $dy/dx = 1+y$  can be transformed to linear by rule :

- A.  $dy/dx = 1+y$
- B.  $dy/dx = 1+y$
- C.  $dy/dx = 1+y$
- D.  $dy/dx = 1+y$

27. If  $dy/dx = 1+y/1-x$ , then its solution is:

- A.  $\tan^{-1} y = \tan^{-1} x + c$
- B.  $\tan^{-1} y = x+c$
- C.  $y = e^{2x} + 0$
- D.  $1+y = e^0$

28. If  $f(x,y)=x^2+y^2+2$ , then  $f(x,y)$  is:

- A. homogeneous

- B. homogeneous of degree 0
- C. non-homogeneous of degree 2
- D. non-homogeneous

29.  $\lim_{n \rightarrow \infty} [(1+1/n)^n]$  is linear if :

- A.  $n=2$
- B.  $n=1$
- C.  $n=0$
- D.  $n=0$

30. For equation  $d^2y/dx^2 + 2dy/dx + y = x$ , integrating factor is :

- A.  $x+1$
- B.  $(x+1)^2$
- C.  $e^x$
- D.  $e^{-x}$

31. A vector field is rotational if:

- A.  $\nabla \times F = 0$
- B.  $\nabla \cdot F = 0$
- C.  $\nabla \cdot F = 0$
- D. None of the above

32. If  $F = yzi + zj + xyk$  and  $F = \nabla \phi$  is :

- A.  $xyz + c$
- B.  $xyz + c$
- C.  $xyz + c$
- D.  $xyz + c$

33. Conjugate of the complex number  $(6+5i)$  is:

- A.  $6-5i$
- B.  $6-5i$
- C.  $6+5i$
- D.  $6+5i$

34. Value of  $(i)^{100}$  is equal to:

- A. 1
- B.  $i$
- C.  $-1$
- D.  $-i$

35. Find the particular integral of  $(D^2-4)y=1$ :

- A.  $-1/4$

- B.  $1/4$
- C. 1
- D. -1

36. Find the PI of  $(D^2+4)y=\cos 2x$  :

- A.  $(x/4)\sin 2x$
- B.  $\cos 2x$
- C.  $\sin 2x$
- D.  $x\sin 2x$

37. Particular integral of  $(D^2-1)y=x$  is:

- A.  $-x$
- B.  $x$
- C.  $-x$
- D.  $x$

38. Solution of  $(D^2+1)y=0$  is :

- A.  $c \cdot \cos x + c \cdot \sin x$
- B.  $c \cdot \cos x + c \cdot \sin x$
- C.  $c \cdot \cos x - c \cdot \sin x$
- D. Both (B) and (C)

39. If  $f(x)$  is discontinuous at  $x=1$  in  $[a,b]$  then  $\lim_{x \rightarrow 1} f(x)$  is:

- A.  $\lim_{x \rightarrow 1} \{ f(x) + \lim_{x \rightarrow 1} z f(x) \}$
- B.  $\lim_{x \rightarrow 1} f(x)$
- C.  $\lim_{x \rightarrow 1} f(x)$
- D. None of the above

40. If  $d^2y/dx^2 = x$ , then general solution is:

- A.  $y = x^3/6 + c \cdot x + c$ ,
- B.  $y = x^3/6$
- C.  $y = x^3 + c$
- D.  $y = x + c$

41. If  $y = ce^{2x}$  is a particular solution of the differential equation is :

- A.  $dy/dx = y$
- B.  $dy/dx = y$
- C.  $dy/dx = y$
- D.  $dy/dx = y$

42. Which of the following is ODE ?

- A.  $y = dx$

B.  $dy=dx$

C.  $x=y$

D.  $y=x$

43. Order of differential equation  $x^2 \frac{d^2z}{dx^2} + y^2 \frac{d^2z}{dy^2} = 0$  is:

A. 2

B. 1

C. not defined

D. None of the above

44. If  $z = 1+i$  and  $\arg(z) = \theta$ , then  $\arg(z^2) =$

A.  $2+2i$

B.  $2-2i$

C.  $-2+2i$

D.  $-2-2i$

45. If  $f(x)$  is periodic in  $[-\pi, \pi]$ , then Fourier coefficient  $a_n$  is

A.  $\frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \cos nx \, dx$

B.  $\frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \sin nx \, dx$

C.  $\frac{1}{\pi} \int_{-\pi}^{\pi} f(x) \cos nx \, dx$

D. None of the above

46. Operator form of  $\frac{d^3y}{dx^3} + \frac{dy}{dx} + y = 0$  is:

A.  $D^3 + D + 1 = 0$

B.  $(D^3 + D + 1)y = 0$

C.  $D^3 + D + y = 0$

D. None of the above

47. If  $z=1+i$ ,  $\bar{z}=1-i$ , then  $z \bar{z}$  is:

A. 2

B. 1

C. i

D. 2

48. Euler's formula for  $b^{\text{TM}}$  in Fourier series in  $[a, b]$  is:

A.  $\frac{2}{b-a} \int_a^b f(x) \cos(n\pi x) \, dx$

B.  $\frac{2}{b-a} \int_a^b f(x) \sin(n\pi x) \, dx$

C.  $\frac{1}{b-a} \int_a^b f(x) \sin(n\pi x) \, dx$

D.  $\frac{1}{b-a} \int_a^b f(x) \cos(n\pi x) \, dx$