Assignment 2

Advanced Algorithms 1 (7081) --- Spring 2021

Due Friday, February 12 by the end of the day

The **leader** of each group is to upload a .cpp file with the **source code** for your C++ program as well as a file with **output for a sample run**. For ease of grading, all the C++ code for your program should be included in a **single** file and designed using the C++ Visual Studio Platform. It should be well-commented and the output user-friendly. You may also write the program in Python instead of C++ if you prefer.

Textbook reference. RSA discussed in Chapter 1 and the Miller-Rabin primality testing algorithm discussed in Chapter 5 of the textbook *Algorithms: Special Topics*.

Topics covered: RSA, modular exponentiation, changing bases, GCD, extended Euclid GCD, Miller-Rabin prime-testing algorithm.

Write a C++ program that involves implementing the RSA cryptosystem. In practice for the encryption to be secure and to handle larger messages you would need to utilize a class for large integers. However, for this assignment you can use built-in types to store integers, e.g., unsigned long long int.

Also, rather than using the ASCII table for this assignment use BEARCATII, which restricts the characters to the blank character and the lower-case letters of the alphabet as follows:

blank character is assigned the value 0. A, ..., Z are assigned the values 1, ..., 26, respectively.

The message M will be represented by replacing each character in the message with its assigned integer base 27. For example, the message M = ``TEST'' will be represented as

$$N = 2051920$$

Translating this to decimal we obtain:

$$D = 20 + 19*27 + 5*27^2 + 20*27^3 = 397838$$

Note that to convert back to base 27, we simply apply the algorithm we discussed in class, i.e., the least significant digit (rightmost) is obtained by performing the operations D mod 27 and performing a recursive call with D/27. For the example above we obtain,

397838 / 27, $397838 \mod 27 = 14734$, 20

- \rightarrow 14734 / 27, 14734 mod 27, 20 = 545, 19, 20
- \rightarrow 545/27, 545 mod 20, 19, 20 = 20, 5, 19, 20 = N

Find primes p and q by choosing positive integers at random and testing for primality using **Miller-Rabin** probabilistic algorithm.

Your program should prompt the user to input a positive integer representing the public key e. If the user enters a number that is not relatively prime to n = pq, then have the user reenter and keep doing this until e and n are coprime, i.e., $gcd(e, \varphi(n)) = 1$. Also prompt the user to enter the message M (as a character string). For handing purposes, run your program with M = "TEST". Output p, q, n, M, C, P where C is the encrypted message, i.e., cyber text, and P is the decrypted message, i.e., plaintext. If your program is working correctly then M should be equal to P.