

## Simple LR(SLR) Parser:-

$$S \rightarrow AA$$

$$A \rightarrow aA1b$$

string : aabb

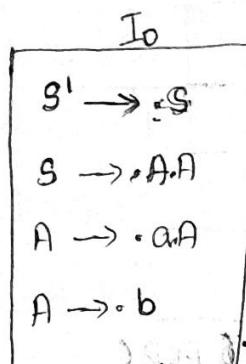
## Augmented Grammar:-

$$\underline{S'} \rightarrow S$$

$$S \# \rightarrow AA\#$$

$$A \rightarrow aA$$

$$A \rightarrow b$$



I<sub>1</sub>  
 $S' \rightarrow S.$

I<sub>2</sub>  
 $S \rightarrow A \cdot A$   
 $A \rightarrow \cdot AA$   
 $A \rightarrow \cdot b$

I<sub>3</sub>  
 $A \rightarrow a \cdot A$   
 $A \rightarrow \cdot aA$   
 $A \rightarrow \cdot b$

I<sub>5</sub>  
 $S \rightarrow AA\#$

I<sub>6</sub>  
 $A \rightarrow aA.$

I<sub>2</sub>  
 $S \rightarrow A \cdot A$   
 $A \rightarrow \cdot AA$   
 $A \rightarrow \cdot b$

I<sub>4</sub>  
 $A \rightarrow b.$

## Parsing Table

	Action			Goto	
	a	b	\$	A	S
0	$S_3$	$S_4$	*	2	1
1			Accept		
2	$S_3$	$S_4$		5	
3	$S_3$	$S_4$		6	
4	$\gamma_3$	$\gamma_3$	$\gamma_3$		

	Action			goto	
	a	b	\$	N	S
5.	$\gamma_1$	$\gamma_1$	$\gamma_1$		
6.	$\gamma_2$	$\gamma_2$	$\gamma_2$		

Stack	INPUT	Action	
<u>0</u>	<u>aabb\$</u>	shift	
0 $\alpha_3$	<u>abb\$</u>	shift	
0 $\alpha_3\alpha_3$	<u>bb\$</u>	shift	(POP 2 elements)
0 $\alpha_3\alpha_3b\gamma_4$	<u>b\$</u>	Reduce A $\rightarrow b$	(POP 2 elements)
0 $\alpha_3\alpha_3A\gamma_5$	<u>b\$</u>	Reduce A $\rightarrow \alpha A$	(POP 2 elements)
0 $\alpha_3\alpha_3A\gamma_5$	<u>b\$</u>	Reduce A $\rightarrow \alpha A$	(POP 2 elements)
<u>0 A <math>\gamma_2</math></u>	<u>b\$</u>	shift	(POP 1 elements)
0 A $\gamma_2$	<u>\$</u>	reduce A $\rightarrow b$	(POP 1 elements)
0 A $\gamma_2$	<u>\$</u>	reduce $\theta \rightarrow AA$	(POP 2 elements)
<u>0 \$ !</u>	<u>\$</u>	Accept	

$$\textcircled{2} \quad E \rightarrow E + T \mid T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E) \mid id$$

Augmented Grammar:-

$$\underline{E' \rightarrow E}$$

$$E \rightarrow E + T \textcircled{1}$$

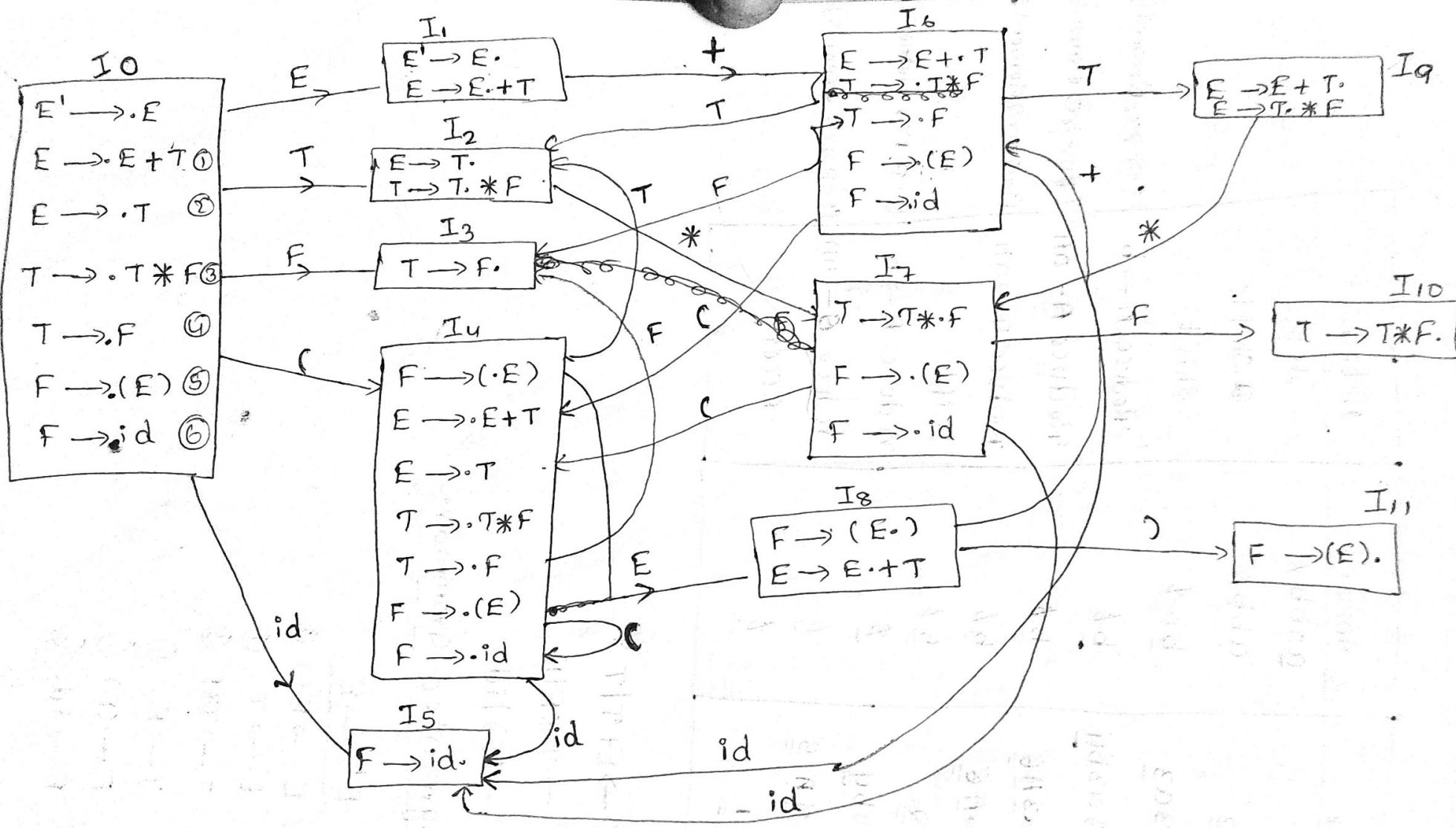
$$E \rightarrow T \textcircled{2}$$

$$T \rightarrow T * F \textcircled{3}$$

$$T \rightarrow F \textcircled{4}$$

$$F \rightarrow (E) \textcircled{5}$$

$$F \rightarrow id. \textcircled{6}$$



	Action						Goto		
	+	*	(	)	id	\$	E	T	F
0			$s_4$			$s_5$	1	2	3
1	$s_6$						Accept		
2	$\gamma_2$	$s_7$		$\gamma_2$			$\gamma_2$		
3	$\gamma_4$	$\gamma_4$		$\gamma_4$			$\gamma_4$		
4			$s_4$		$s_5$		8	2	3
5	$\gamma_6$	$\gamma_6$		$\gamma_6$			$\gamma_6$		
6			$s_4$		$s_5$			9	3
7			$s_4$		$s_5$				10
8	$s_6$			$s_{11}$					
9	$\gamma_1$	$s_7$		$\gamma_1$			$\gamma_1$		
10	$\gamma_3$	$\gamma_3$		$\gamma_3$			$\gamma_3$		
11	$\gamma_5$	$\gamma_5$		$\gamma_5$			$\gamma_5$		

	First	Follow
E	{+, *, (, id}	\${, +, )}
T	{*, (, id}	\${, +, *})}
F	{(, id}	\${, +, *)}

stack	input	Action
0	<u>id + id \$</u>	shift
0 id \$	<u>+ id \$</u>	reduce $F \rightarrow id$
0 F \$	<u>+ id \$</u>	reduce $T \rightarrow F$
0 T \$	<u>+ id \$</u>	reduce $E \rightarrow T$
0 E \$	<u>+ id \$</u>	shift
0 E 1	<u>id \$</u>	shift
0 E 1 + 6	<u>\$</u>	reduce $F \rightarrow (E)$
0 E 1 + 6 F \$	<u>\$</u>	reduce $T \rightarrow F$

0 E1 + B1 T0

0 E = 1

\$

reduce  $E \rightarrow E + T$

Accept.

Construct an SLR Parser for the given grammar

$$S \rightarrow CC$$

$$C \rightarrow CC \mid d$$

Parse the string : cedd

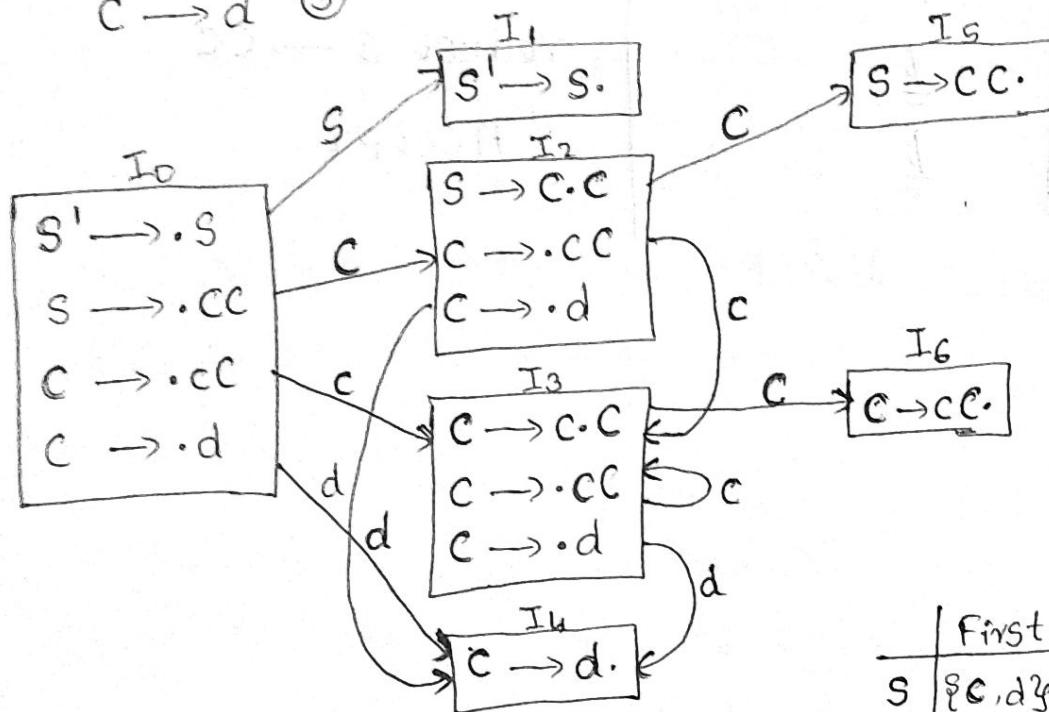
Augmented Grammar:-

$$S' \rightarrow S$$

$$S \rightarrow CC \quad ①$$

$$C \rightarrow cC \quad ②$$

$$C \rightarrow d \quad ③$$



	First	Follow
S	{c, d}*	{\$, \$}
C	{c, d}*	{c, d, \$}

	c	d	\$	AS	C
0	$s_3$	$s_4$			1 2
1				Accept	
2	$s_3$	$s_4$			5
3	$s_3$	$s_4$			6
4	$\gamma_3$	$\gamma_3$	$\gamma_3$		
5			$\gamma_1$		
6	$\gamma_2$	$\gamma_2$	$\gamma_2$		

Stack	Input	Action
<u>0</u>	<u>ccdd\$</u>	shift
0 <u>C3</u>	<u>cdd\$</u>	shift
0C3 <u>C3</u>	<u>dd\$</u>	shift
0C3 <u>C3d\$</u>	<u>d\$</u>	reduce $C \rightarrow d$
0C3 <u>C3C\$</u>	<u>d\$</u>	reduce $C \rightarrow CC$
0 <u>C3C\$</u>	<u>d\$</u>	reduce $C \rightarrow CC$
<u>0C2</u>	<u>d\$</u>	shift
0 <u>C2d\$</u>	<u>\$</u>	reduce $C \rightarrow d$
0 <u>C2C\$</u>	<u>\$</u>	reduce $S \rightarrow CC$
<u>0S1</u>	<u>\$</u>	Accept

# Compiler Design

## ① Operator grammar:-

$$E \rightarrow E + T$$

$$E \rightarrow T$$

$$T \rightarrow T * F \mid F$$

$$F \rightarrow (E)$$

$$F \rightarrow id$$

Ans:-

Step-1:-

Rules for Leading:-

①  $A \rightarrow \alpha a B$  if  $\boxed{\alpha \rightarrow \epsilon \mid \text{Single NT}}$

$$\text{Leading}(A) = a$$

②  $A \rightarrow \alpha a B$  if  $\boxed{\alpha \rightarrow \text{NT}}$

$$\text{Leading}(A) = (\text{Leading}(\alpha))$$

$$E \rightarrow E + T$$

$$\text{Leading}(E) = \{+, \text{Leading}(T)\} = \{+, *, (, )\}$$

$$E \rightarrow T$$

$$\text{Leading}(T) = \{* \}, \text{Leading}(F) = \{*, (, )\}$$

$$T \rightarrow T * F$$

$$\text{Leading}(F) = \{ (, id \} \}$$

$$T \rightarrow F$$

$$F \rightarrow (E)$$

$$F \rightarrow id$$

Rules for Trailing:-

①  $A \rightarrow a B \beta$  if  $\boxed{B \rightarrow \epsilon \mid \text{Single NT}}$

$$\text{Leading}(A) = \text{Trailing}$$

$$\text{Trailing}(A) = \beta$$

②  $A \rightarrow a B \beta$  if  $\boxed{B \rightarrow \text{NT}}$

$$\text{Trailing}(A) = \text{Trailing}(B)$$

$$\text{Trailing}(E) = \{ +, \text{Trailing}(T)\} = \{ +, *, ), id \}$$

$$\text{Trailing}(T) = \{ *\}, \text{Trailing}(F) = \{ *, ), id \}$$

$$\text{Trailing}(F) = \{ ), id \}$$

Step-2:-

Operator grammer Precedence table :-

\* it have two rules

Rule-1:-

$\$ < \text{Leading}(S) \& \text{Trailing}(S) > \$$

$\therefore S \rightarrow NT$

Rule-2:-

(a) if  $x_i \notin T \rightarrow x_i = x_{i+1}$

(b) if  $x_i \notin T \rightarrow x_i = x_{i+2}$

(c) if  $x_i \in T \& x_{i+1} \in NT, x_i \leftarrow \text{Leading}(x_{i+1})$

(d) if  $x_i \in NT \& x_{i+1} \in T, \text{Trailing}(x_{i+1}) > x_{i+1}$

Now,  $x_1$  ~~पहला अक्षर~~.

$E \rightarrow E + T$

Here c, d Condition will statutied

(1) trailing(E)  $\rightarrow +$

$\{ +, *, ), id \} \rightarrow +$

(2)  $+ < \text{Leading}(T)$

$+ < \{ +, *, (, id \}$

$T \rightarrow T * F$

Here c, d Condition will statutied

(3) trailing(T)  $\rightarrow *$

$\{ *, ), id \} \rightarrow *$

$\$ \rightarrow \text{Trailing}(S)$

(4)  $* < \text{Leading}(F)$

$* < \{ (, id \}$

~~Trailing~~

$\text{Trailing}(S) < f$

$F \rightarrow CE$

here b, C & id condition will statitcal

⑤  $C \stackrel{?}{=}$

⑥  $C \leftarrow \text{Leading}(CE)$

$C \leftarrow \{ +, *, (, id \}$

⑦ Trailing(CE)  $\Rightarrow$

$\{ +, *, ), id \} \Rightarrow )$

id \* id

	+	*	(	)	id	\$
+	$\cdot >$	$\cdot <$	$\cdot <$	$\cdot >$	$\cdot <$	$\cdot >$
*	$\cdot >$	$\cdot >$	$\cdot <$	<del><math>\cdot &gt;</math></del>	$\cdot <$	$\cdot >$
(	$\cdot <$	$\cdot <$	$\cdot <$	$\cdot \div$	$\cdot <$	$\cdot c$
)	$\cdot >$	$\cdot >$	$c$	$\cdot >$	$c$	$\cdot >$
id	$\cdot >$	$\cdot >$	$c$	$\cdot >$	$c$	$\cdot >$
\$	$\cdot <$	$\cdot <$	$\cdot <$	$c$	$\cdot <$	accept

C	<	<	<	=	<id.	e
)	>	>	c	>		
id	>	>	e	>		
\$	L1	L1	e			

stack	relation	input	Action
\$	\$ < id	id + id + \$	shift
\$ id	id > +	+ id + id	Rede pop
\$	\$ < +	+ id + id	shift
\$ +	+ < id	id + id	shift
\$ + id	id > *	* id	POP
\$ +	+ < *	* id	shift
\$ + *	* < id	id	shift
\$ + * id	id > \$	\$	POP
\$ + *	* > \$	\$	POP
\$ +	+ \$	\$	POP
\$	\$	\$	accept

String  $\rightarrow$  id + id \* id

Stack	Relation	INPUT	ACTION
\$.	$\beta \leftarrow id$	id + id * id \$	shift
\$ id	$id \beta \rightarrow +$	+ id * id \$	<del>Rede</del> pop
\$	$\beta \leftarrow +$	+ id * id \$	shift
\$ +	$+ \beta \leftarrow id$	id * id \$	shift
\$ + id	$id \beta \rightarrow *$	* id \$	POP
\$ +	$+ \beta \leftarrow *$	* id \$	shift
\$ + *	$* \beta \leftarrow id$	id \$	shift
\$ + * id	$id \beta \rightarrow \$$	\$	POP
\$ + *	$* \beta \rightarrow \$$	\$	POP
\$ *	$* \beta \rightarrow \$$	\$	POP
\$		\$	accept