

## Knowledge Based Agents:-

- The central component of a knowledge-based agent is its knowledge base, or KB.

- A knowledge base is a set of sentences.

- knowledge Representation language:-

- Each sentence is expressed in a language called a knowledge Representation language and represents some assertion about the world.

- Inference:-

There is a way to add new sentences to the knowledge base is TELL and to query what is known ASK.

TELL:- A way to add new sentences to the knowledge base.

ASK: A way to query what is known.

Both tasks may involve INFERENCE that is, deriving new sentences from old.

In LOGICAL AGENTS, inference must obey the fundamental requirement that when one asks a question of the knowledge base, the answer should follow from what has been told to the knowledge base previously.

### \* Knowledge Based Agent program:-

function KB-AGENT (percept) returns an action

static: KB, a knowledge base,

t, a counter, initially 0, indicating time

TELL(KB, MAKE-PERCEPT-SENTENCE  
CG  
(percept))

action  $\leftarrow$  ASK(KB, MAKE-ACTION-QUERY  
(t))

TELL(KB, MAKE-ACTION-SENTENCE(action  
t))

t  $\leftarrow$  t + 1

return action.

Like all our agents, it takes a percept as input and returns an action.

- The agent maintains a knowledge base, KB, which may initially contain some background knowledge.
- first, it TELLS the knowledge base what it perceives.
- second, it ASK the knowledge base what action it should perform.
- third, the agent records its choice with TELL and executes the action.

#### • MAKE - PERCEPT - SENTENCE:-

— takes a percept and a time and return a sentence asserting that the agent perceived the given percept at the given time.

#### • MAKE - ACTION - QUERY:-

— takes a time as input and returns a sentence that asks what action should be done at the current time.

• MAKE-ACTION-SENTENCE:  
constructs a sentence asserting  
that the chosen action was executed

Knowledge level:-

The knowledge-based agent is  
not an arbitrary program for calculating  
actions.

Implementation level:-

—e.g.: an automated taxi might have  
the goal of dropping a passenger to  
Main Country and might know that  
it is in San Francisco and that the  
Golden Gate Bridge is the only  
link b/w the two locations.

## (a) The Wumpus world environment-

The Wumpus world is a cave consisting of rooms connected by passageways.

Working somewhere in the cave is the Wumpus, a beast that eats anyone who enters its room.

, the Wumpus can be shot by an agent but the agent has only one arrow.

Some rooms contain bottomless pits that will trap anyone who wanders into these rooms.

. The only mitigating feature of living in this environment is the possibility of finding a heap of gold.

Although the Wumpus world is rather tame by modern computer game standards , it makes an excellent test bed environment for intelligent agents.

• Michael Grentz was the first to suggest this.

	stench	breeze	PIT
3	wumpus	breeze green (gold)	PIP
2		breeze	
1	start	breeze	PIT
	2	3	4

WUMPUS world.

The precise definition of the task environment is given by the PEAS description.

- performance measure: +1000 for picking up the gold, -1000 for falling into a pit or being eaten by the wumpus, -1 for each action taken and -10 for using up the arrow.
- environment: A 4x4 grid of rooms.

The agent always starts in the square labeled facing to the right.

The locations of the gold and the wumpus are chosen randomly, with a uniform distribution; from the squares other than the start square.

### ACTUATORS:-

- the agent can move forward, turn left by  $90^\circ$ , or turn right by  $90^\circ$ .
- The agent dies a miserable death miserable death if it enters a square containing a pit or alive wumpus.

### SENSORS:-

The agent has five sensors, each of which gives a single bit of information.

- 1. In the square directly adjacent to a pit, the agent will perceive a breeze
- 2. In the square directly adjacent to a wumpus, the agent will perceive a stench.

- In the square containing the wumpus and in the directly adjacent square the agent will perceive a stench.
- In the square directly adjacent to a pit, the agent will perceive a breeze.

3. In the square where the gold is, the agent will perceive a glitter.

4. When an agent walks into a wall, it will perceive a bump.

5. When the wumpus is killed it emits a woeful scream that can be perceived anywhere in the cave.

1,4	2,4	3,4	4,4	PA- agent	1,4	2,4	3,4	4,4
1,3	2,3	3,3	4,3	B = Breeze	1,3	2,3	3,3	4,3
1,2 OK	2,2	3,2	4,2	G = Glitter	1,2 OK	2,2 P?	3,2	4,2
1,1 OK	2,1 OK	3,1	4,1	ok = safe square	1,1 OK	2,1 OK	3,1 P?	4,1
				P = pit S = stench ch				

v = visited  
w = wumpus

→ The first step taken by the agent in the wumpus world.

- The initial situation, after percept [none, none, none, none, none].

b) After an move, with percept [None, Breeze, None, None, None]

from the fact that there was no stench or breeze in [1,1], the agent can infer that [1,2] and [2,1] are free of danger. They are marked with an ok to indicate this.

A cautious agent will move only a square that it knows is OK.

1,4	2,4	3,4	4,4
1,3 W	2,3	3,3 B	4,3
1,2 A OK	2,2 OK	3,2 V	4,2
1,1 OK	2,1 VOK	3,1 P?	4,1

A = agent

B = breeze

G = glitter, gold

OK = safe square

P = pit

S = stench

V = visited

W = wumpus.

1,4	2,4 P?	3,4 VOK	4,4
1,3 A G B	2,3 G P?	3,3 P?	4,3
1,2 V OK	2,2 V OK	3,2 V P?	4,2
1,1 V OK	2,1 V OK	3,1 V P?	4,1

-Two later stages in the progress of the agent.

third

(a) After the ~~first~~ move, with percept [stench, none, none, none, none].

(b) After the fifth move, with percept [stench, breeze, glitter, none, none].

## LOGIC:-

- knowledge bases consists of sentences.
- These sentences are expressed according to the syntax of the representation language, which specifies what the sentences that are well formed.
- The syntax is clear enough in ordinary arithmetic

" $x+y=4$ " is a well-formed sentence,  
whereas " $x2y + =$ " is not.

## Semantics:

- A logic must also define the semantics of the language.
- Semantics means "meaning" of sentence in logic; the definition is more precise.  
for eg " $x+y=4$ " is true in a world where  $x$  is 2 and  $y$  is 2, but false in a world where  $x$  is 1 and  $y$  is 1.

## Entailment:

Entailment means that one thing follows from another.

Relation of logical entailment b/w sentences is involved that a sentence follows logically from another sentence.

- KB = a ~~know~~ knowledge base KB entails sentence  $\alpha$  if and only if  $\alpha$  is true in all worlds where KB is true,

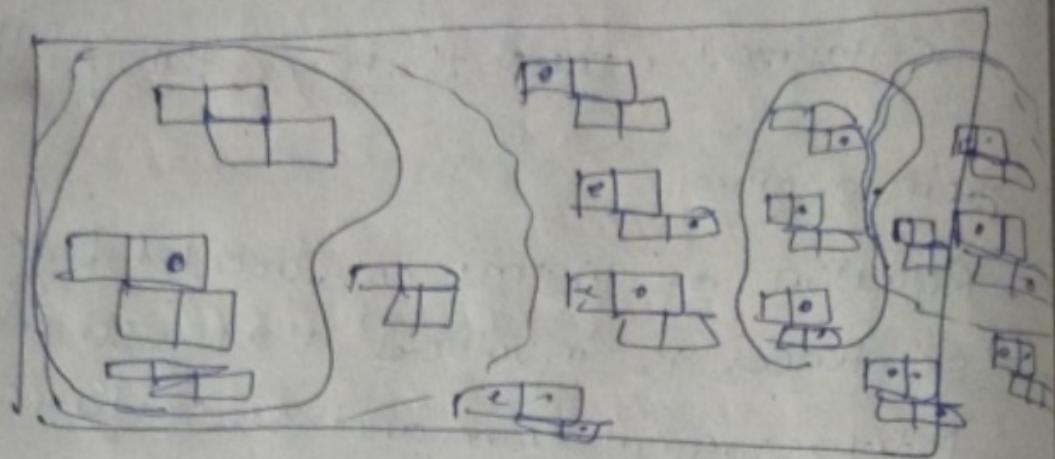
e.g.  $x+y = u$  entails  $u = x+y$ .

## Model:-

• logicians typically think in terms of models ; which are formally structured , world with respect to which truth can be evaluated.

$m$  is a model of a sentence  $\alpha$   
if  $\alpha$  is true in  $m$ .

$M(\alpha)$  is the set of all models of  $\alpha$ .



### Conclusion:-

- the KB is false in models that contradict what the agent knows - for eg, the KB is false in any model in which  $[1,2]$  contains a pit, because there is no breeze in  $[1,1]$ .
- Now let us consider two possible conclusions:
- $\alpha_1 = \text{"There is no pit in } [1,2]\text{"}$
- $\alpha_2 = \text{"There is no pit in } [2,2]\text{"}$
- ~~In every~~ In every model in which KB is true,  $\alpha_1$  is also true.
- Hence,  $\text{KB} \not\models \alpha_2$  so the agent cannot conclude that there is no pit in  $[2,2]$

## PROPOSITIONAL LOGIC

3) propositional logic is the simplest logic.

The syntax of propositional logic and its semantics - the truth of sentences is determined.

Syntax - The syntax of propositional logic defines the allowable sentences.

The atomic sentences - the indivisible syntactic elements consist of a single proposition symbol.

### Rules:-

i. uppercase names are used for symbols

(ie) P, Q, R and so on.

ii. Name are arbitrary.

### Complex sentences-

Complex sentences are constructed from simpler sentences using logical connections. There five connectives.

- If  $s$  is a sentence,  $\neg s$  is a sentence (negation)
- If  $s_1$  and  $s_2$  are sentences,  $s_1 \wedge s_2$  is a sentence (conjunction)
- If  $s_1$  and  $s_2$  are sentences,  $s_1 \vee s_2$  is a sentence (disjunction)
- If  $s_1$  and  $s_2$  are sentences,  $s_1 \Rightarrow s_2$  is a sentence (implication).
- If  $s_1$  and  $s_2$  are sentences,  $s_1 \Leftrightarrow s_2$  is a sentence (biconditional / if ~~AND~~ ON IF)

### BNF (Backus-Naur form),

The fig 3.4 shows about the BNF grammar of sentence in propositional logic.

Sentence  $\rightarrow$  Atomic sentence | complex sentence.

Atomic sentence  $\rightarrow$  true | false | symbol

Symbol  $\rightarrow$  P | Q | R | ...

Complex sentence  $\rightarrow$   $\neg$  sentence.

(sentence ||| sentence)

(sentence  $\vee$  sentence)

(sentence  $\Rightarrow$ , sentence)

(sentence  $\Leftrightarrow$  sentence)

every sentence constructed with binary connectives must be enclosed in parentheses.

This ensure that we have to write

$((A \wedge B) \Rightarrow C)$  instead of  $A \wedge B \Rightarrow C$

order of precedence for the connecting is similar to the precedence used in arithmetic.

for eg:-  $a b + c$  is read as  $(a b) + c$  rather than  $a(b+c)$  because multiplication has higher precedence than addition.

The order of precedence in propositional logic

$\neg$

The order of precedence in propositional logic (from highest to lower)  $\neg, \wedge, \vee, \Rightarrow, \Leftrightarrow$ .

- Hence, the sentence  $\neg P \vee Q \wedge R \Rightarrow S$  is equivalent to the sentence  $(\neg P) \vee (Q \wedge R) \Rightarrow S$ .
- Precedence does not resolve ambiguity in sentences such as  $A \wedge B \wedge C$ , which could be read as  $((A \wedge B) \wedge C)$  or as  $(A \wedge (B \wedge C))$ . These two readings mean the same thing according to the semantics.

### Semantics:

- The semantics defines the rules for determining the truth of a sentence with respect to a particular model.
- In propositional logic, a model simply ~~fixes~~ fixes the truth value, true or false for every proposition symbol.
- for eg:- if the sentences in the knowledge base make use of the proposition symbols  $P_{1,2}$ ,  $P_{2,1}$  and  $P_{3,1}$  then one possible model is.

$m_1 = \{P_{1,2} = \text{false}, P_{2,12} = \text{true}, P_{3,12} = \text{true}\}$

### Atomic sentences:-

Atomic sentences are easy:

- true is true in every model and false is false in every model.

- The truth value of every other proposition symbol must be specified directly in the model.

- For eg. in the model  $m_1$  gives earlier,  $P_{1,2}$  is false.

### Complex sentences:-

for any sentences  $s$  and any model  $m$ , the sentence  $-s$  is true in  $m$  if and only if  $s$  is false in  $m$ .

P	Q	$\neg P$	$P \wedge Q$	$P \vee Q$	$P \Rightarrow Q$	$P \Leftrightarrow Q$
F	F	T	F	F	T	T
F	T	T	F	T	T	F
T	F	F	F	T	F	F
T	T	F	T	T	T	T

Using the above fig 3.5, truth values of any sentence  $S$  can be computed with respect to any model in by a simple process of recursive evaluation.

e.g.:  $P_{1,2} \quad P_{2,2} \quad P_{3,1}$   
 $f \quad T \quad f$

#### 4) FIRST-ORDER LOGIC

fol, a representation language of knowledge which is powerful than propositional logic.

- (ic) Boolean logic: fol is an expressive
- It follows procedural approach
  - It derive facts from other facts
  - (ir) dependent

first-order logic (like natural lang.)

assuming the world contains:-

⇒ Noun - refers to objects.

e.g.: name, place, thing.

- verb refers to relations.
  - some relations are functions.
  - Relation has only one value.
- functions have many values assigned to it:

it:

- objects: people, houses, numbers, colors, baseball games, wars.
- properties: red, round, prime, small
- relations: bigger than, part of, comes b/w..
- functions: father of, best friend, one more than, plus, ...

e.g.:

1. "Evil King John ruled England in 1200"

objects: John, England, 1200; Relation:  
ruled; properties: evil, king.

2. "One plus two equals three"

object: one, two, three, one plus  
two; relation: equals;

function: plus. ("one plus two" is  
a name for the object that is

obtained by applying the function "plus" to the objects "one" and "two". Three is another name for this object.)

3. "Squares neighboring the Wumpus are smelly"

Object: Wumpus, squares; property: Smelly; Relation: neighboring.

### Ontological commitment:-

The primary difference b/w propositional and first-order logic lies in the ontological commitment made by each language - that is, what it assumes about the nature of reality. Special purpose logic make faster ontological commitment.

### Temporal logic:-

It assumes that fast hold at particular times and that those time (intervals) are ordered (consequent).

### High order logic:-

It is more expressive than FOL. It allows one to make assertions about all relations.

## Epistemological Commitments:

— A logic that allows the possible state of knowledge that it allows with respect to each fact. In first order logic, a sentence represents a fact and the agent believes the sentence to be true, believes it to be false or has no opinion.

## Ontological Commitment and Epistemological commitment of different logics:-

### Logics

language	ontological commitment (what exists in the world)	epistemological commitment
propositional logic	fact	T/f un known
first-order logic	fact, object, relations	T/f un known
temporal logic	fact, object, relations, time	T/f un known
probability theory	fact	degree of belief [0,1] un known
fuzzy logic	fact with degree of truth	interval value

## 5) SITUATION CALCULUS:

- The situation calculus is a logic formalism designed for representing and reasoning about dynamical domain
- McCarthy, Hayes 1969.
- Reiter 1991
- in first-order logic, sentences are either true or false and stay that way. Nothing is corresponding to any sort of change.
- sit calc represents changing scenario as a set of S<sub>OL</sub> formulae.
- A domain is encoded in S<sub>OL</sub> by three kind of formulae.
  - Action precondition axioms and action effects axioms.
  - successor state axioms, one for each fluent.
  - the foundation axioms of the situation calculus.

## situation calculus: an example.

### world:-

- robot
- items
- locations( $x, y$ )
- moves around the world.
- picks up or drops items.
- Some items are too heavy for the robot to pick up.
- Some items are fragile so that they break when they are dropped.
- robot can repair any broken item that it is holding.

### actions:-

- move( $(x,y)$ ): robot is moving to a new location( $x_1, y_1$ )
- pick up( $o$ ): robot picks up an object  $o$ .
- drop( $o$ ): robot drops the object  $o$  that holds

### - situations:-

- Initial situation  $s_0$ : no actions have occurred
- A new situation resulting from the performance of an action  $a$  in  $s_0$ .  
situation  $s_1$  is denoted using the function  $symbol do(a,s)$

### fluents:- "properties of the world"

#### • Relational fluents.

- statements whose truth value may change.
- They take a situation as a final argument.

### - Action precondition axioms:-

- some actions may not be executable in a given situation
- $\text{pos}(a,s)$ : special binary predicate.

## Action effect Axioms

specify the effect of an action  
on the fluents

examples:-

• poss (pick up(o), s)  $\rightarrow$  is-carrying  
(o, do(pick up(o), s))

• poss (drop(o), s)  $\wedge$  fragile(o)  $\rightarrow$  broken  
(o, do(drop(o), s)).

• is that enough? No, because  
of the frame problems.

## ⑧ Building A knowledge Base:-

knowledge engineering projects vary widely in content, scope, and difficulty, but all such projects include the following steps:

### 1. Identify the task:-

The knowledge engineer must delineate (ie) describe the range of questions that the knowledge base will support and the kinds of facts that will be available for each problem instance.

### 2. Assemble the relevant knowledge:-

The knowledge engineer might already be an expert in the domain to extract what this knowledge.

3. decide on a vocabulary of predicates, functions and constants:-

Translate the important domain-level concepts into logic-level names

4. encode general knowledge about the domain

The knowledge engineer writes down the axioms for all the vocabulary terms (ie) enabling the expert to check the content.

5. encode a description of the specific problem instance:

It will involve writing simple atomic sentences about instances of concepts that are already part of the ontology.

6. pose queries to the inference procedure and get answers:-

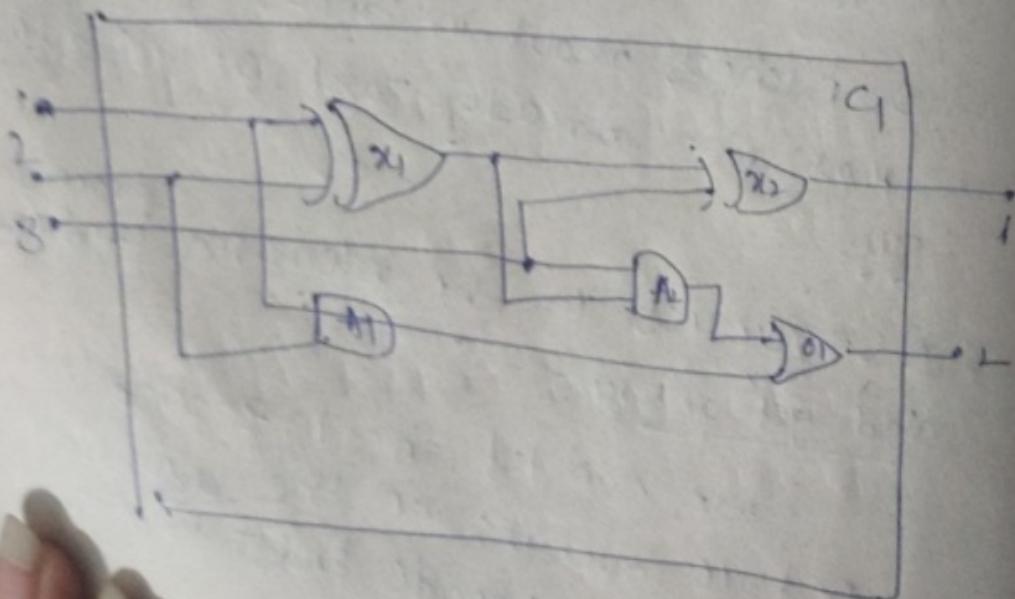
We can let the inference procedure operate on the axioms and problem-specific facts to derive

The facts we are interested in knowl-  
+ ledge the knowledge base:-

To understand this seven-step  
process better, we now apply it to an  
extended example the domain of  
electronic circuits.

#### 4) The electronic circuits Domain:-

We will develop an ontology and  
knowledge base that allow us to  
reason about digital circuits of  
the kind shown.



The first two inputs are the two bits to be added and the third input is a carry bit.

The circuit contains two XOR gates, two AND gates and one OR gate.

We follow the seven-step process for knowledge engineering.

### 1. Identify the task:-

- Does the circuit actually add properly? (Circuit verification).

### 2. Assemble the relevant knowledge:-

- composed of wires and gates; types of gate (AND, OR, XOR, NOT)

- irrelevant: size, shape, color, cost of gates.

### 3. Decide on a vocabulary:-

Type ( $x_1$ ) = XOR

Type ( $x_1$ , XOR)

XOR ( $x_1$ )

4. encode general knowledge of the domain

$\neg t_1, t_2 \text{ connected } (t_1, t_2) \Rightarrow \text{signal}(t_1) = \text{signal}(t_2)$

$\therefore \forall t \text{ signal}(t) = 1 \vee \text{signal}(t) = 0$

$\neg 1 \neq 0$

$\neg t_1, t_2 \text{ connected } (t_1, t_2) (\neg) \text{ connect} (t_2, t_1)$

$\neg \forall g \text{ Type}(g) = \text{OR} \Rightarrow \text{Signal}(\text{out}(1, g)) = 1 \Leftrightarrow \exists n \text{ signal}(\text{in}(n, g))$

$\neg \forall \text{Type}(g) = \text{AND} \Rightarrow \text{Signal}(\text{out}(1, g)) = 0 \Leftrightarrow \exists n \text{ signal}(\text{in}(n, g)) = 0$

$\neg \forall \text{Type}(g) = \text{XOR} \Rightarrow \text{Signal}(\text{out}(1, g)) = 1 \Leftrightarrow \text{signal}(\text{in}(1, g)) \neq \text{signal}(\text{in}(2, g))$

$\neg \forall \text{Type}(g) = \text{NOT} \Rightarrow \text{Signal}(\text{out}(1, g)) \neq \text{Signal}(\text{in}(1, g))$

5. Encode the specific problem instance

$$\rightarrow \text{Type}(x_1) = \text{XOR} \quad \text{Type}(x_2) = \text{XOR}$$

$$\rightarrow \text{Type}(A_1) = \text{AND} \quad \text{Type}(A_2) = \text{AND}$$

$$\rightarrow \text{Type}(O_1) = \text{OR}.$$

: pose querying to the inference procedure

what are the possible sets of values  
of all the terminals for the  
adder circuit

$i_{1r}, i_{12}, i_{13}, o_1, o_2$  signal (in(1,c1))

$i_1 \wedge \text{signal}(\text{in}(2,c1)) = i_{12} \wedge \text{signal}$

(in(3,c1)) =  $i_{13} \wedge \text{signal}(\text{out}(1,c1))$

$= o_1 \wedge \text{signal}(\text{out}(2,c1)) = 1.$

7. debug the knowledge base may  
have omitted assertion like  $1 \neq 0$

suddenly, the system will  
be unable to prove any outputs  
for the circuit, except for input  
cases 000 and 110.

8)

### Truth maintenance System

Many of the inferences drawn by a knowledge representation system, will have only default status, rather than being absolutely certain.

- This process is called belief revision
- Truth maintenance systems (TMS) have been developed as a means of implementing Non-Monotonic Reasoning Systems.

#### Basically TMS:-

- all do some form of dependency directed backtracking.
- assertions are connected via a network of dependencies.

#### Justification-Based Truth Maintenance System (JFTMS)

This is a simple TMS in that it does not know anything about the structure of assertions themselves.

- AN IN-LIST - which supports beliefs held.

- AN OUT-LIST - which supports beliefs not held.

### Logic-based (LTMs)

Similar to ~~JTMS~~ JTMS except

- note assume nodes no relationship among them except ones explicitly stated in justifications.

- if this happens new has to be reconstructed.

### Assumption-Based TMS (ATMs)

- JTMS and LTMS provide a single line of reasoning at a time and back track when needed - depth first search.

- ATMs maintain alternative paths in parallel - breadth-first search
- Backtracking is avoided at the expense of maintaining multiple contexts

## Resolution:-

In 1930, the German mathematician Kurt Gödel proved the first completeness theorem for first-order logic showing that any entailed sentence has a finite proof.

- The theorem states that a logical system that includes the principle of induction without which very little of discrete mathematics can be constructed - is necessarily incomplete.
- Resolution-based theorem provers have been applied widely to derive mathematical theorems, including several for which no proof was known previously.
  - Conjunctive normal form for first-order logic.
  - The resolution inference rule.
  - Completeness of resolution.
  - Dealing with equality.

- Resolution Strategy.
- Theorem Prover.

Conjunctive normal form for first-order logic:-

First-order resolution requires that sentences be in conjunctive normal form (CNF) - that is, a conjunction of clauses, where each clause is a disjunction of literals.

$$\neg \forall x \text{American}(x) \wedge \neg \text{weapon}(y)) \wedge \text{sees}$$

$$(x, y, z) \wedge \neg \text{hostile}(z) \Rightarrow \neg \text{criminally}$$

Becomes in CNF

$$\neg \text{American}(x) \vee \neg \text{weapon}(y) \vee \neg \text{sees}$$

$$(x, y, z) \vee \neg \text{hostile}(z) \vee \neg \text{criminally}(z)$$

1. Eliminate biconditionals and implications:

$$\neg \forall x (\neg \forall y \neg \text{animal}(y) \vee \text{loves}(x, y))$$

$$\vee [\exists y \text{ loves}(y, x)]$$

2. Move  $\neg$  inwards -

$\neg \forall x P$  becomes  $\exists x \neg P$

$\neg \exists x P$  becomes  $\forall x \neg P$

The transforms are -

$\neg \forall x [\exists y \neg (\neg \text{animal}(y) \vee \text{loves}(x, y))] \vee$   
 $[\exists y \text{ loves}(y, x)]$

$\neg \forall x [\exists y \neg P(\text{Animal}(y)) \wedge \neg \text{loves}(x, y)] \vee$   
 $[\exists y \text{ loves}(y, x)]$

$\neg \forall x [\exists y \text{ animal}(y) \wedge \neg \text{loves}(x, y)] \vee$   
 $[\exists y \text{ loves}(y, x)].$

3. Standardize variables:-

for sentences like  $(\forall x P(x)) \vee (\exists x Q(x))$  which use the same variable name twice, change the name of one of the variables.

$\neg \forall x [\exists y \text{ animal}(y) \wedge \neg \text{loves}(x, y)] \vee$   
 $[\exists z \text{ loves}(z, x)]$

#### 4. Skolemize:-

- A more general form of existential instantiation.

$$\neg \forall x [\text{Animal}(A) \wedge \neg \text{Loves}(x, A)] \vee \text{Love}_y \\ (B, x)$$

#### 5. Drop universal quantifiers:-

- At this point, all remaining variables must be universally quantified.

$$\neg \text{Animal}(f(x)) \wedge \neg \text{Loves}(x, f(x)) \vee \text{Love}_y \\ (G_1(x), x)$$

#### 6. Distribute $\neg$ over $\vee$ :-

$$[\neg \text{Animal}(f(x)) \vee \text{Loves}(G_1(x), x)] \wedge$$

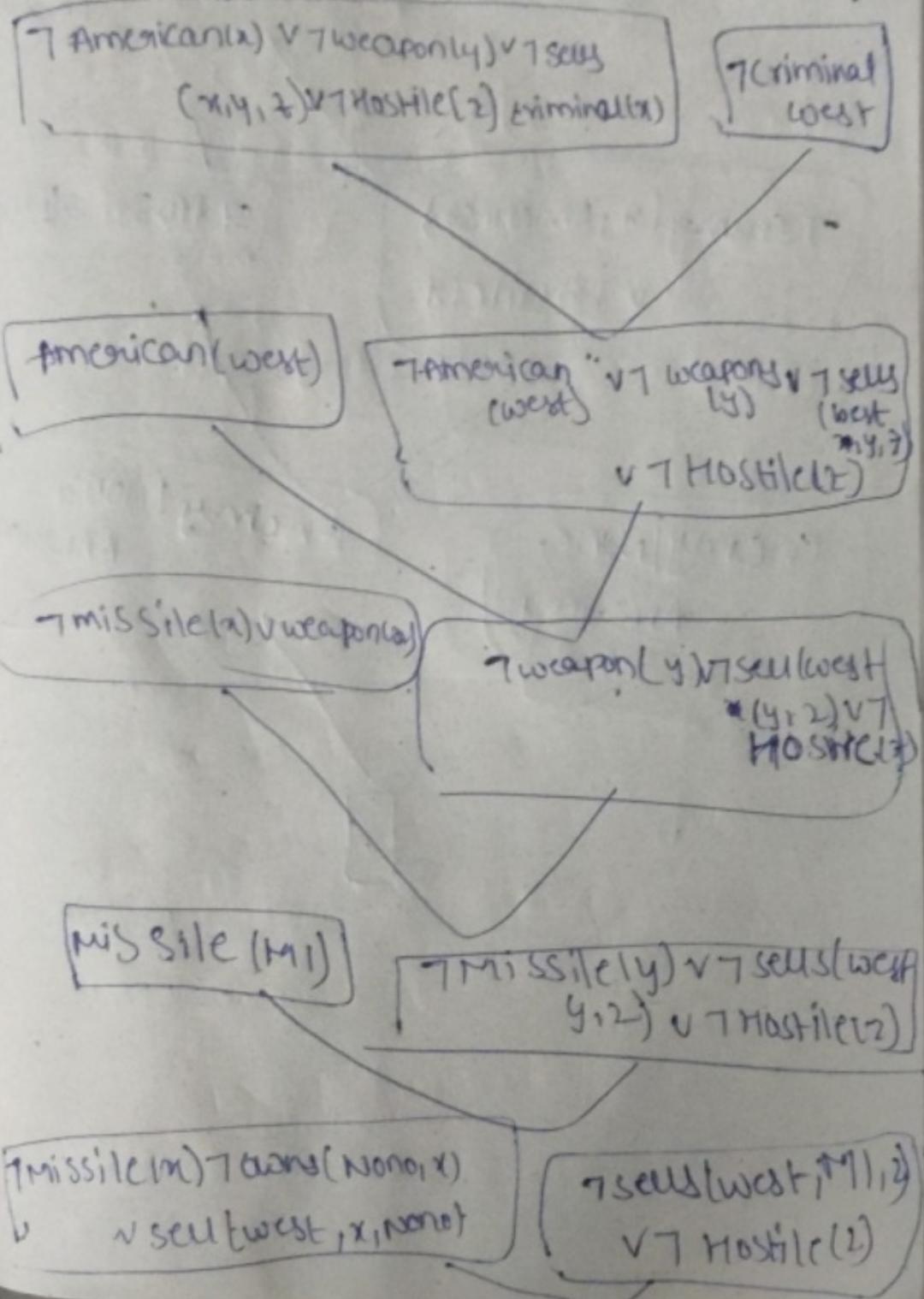
$$[\neg \text{Loves}(x, f(x)) \vee \text{Loves}(G_1(x), x)]$$

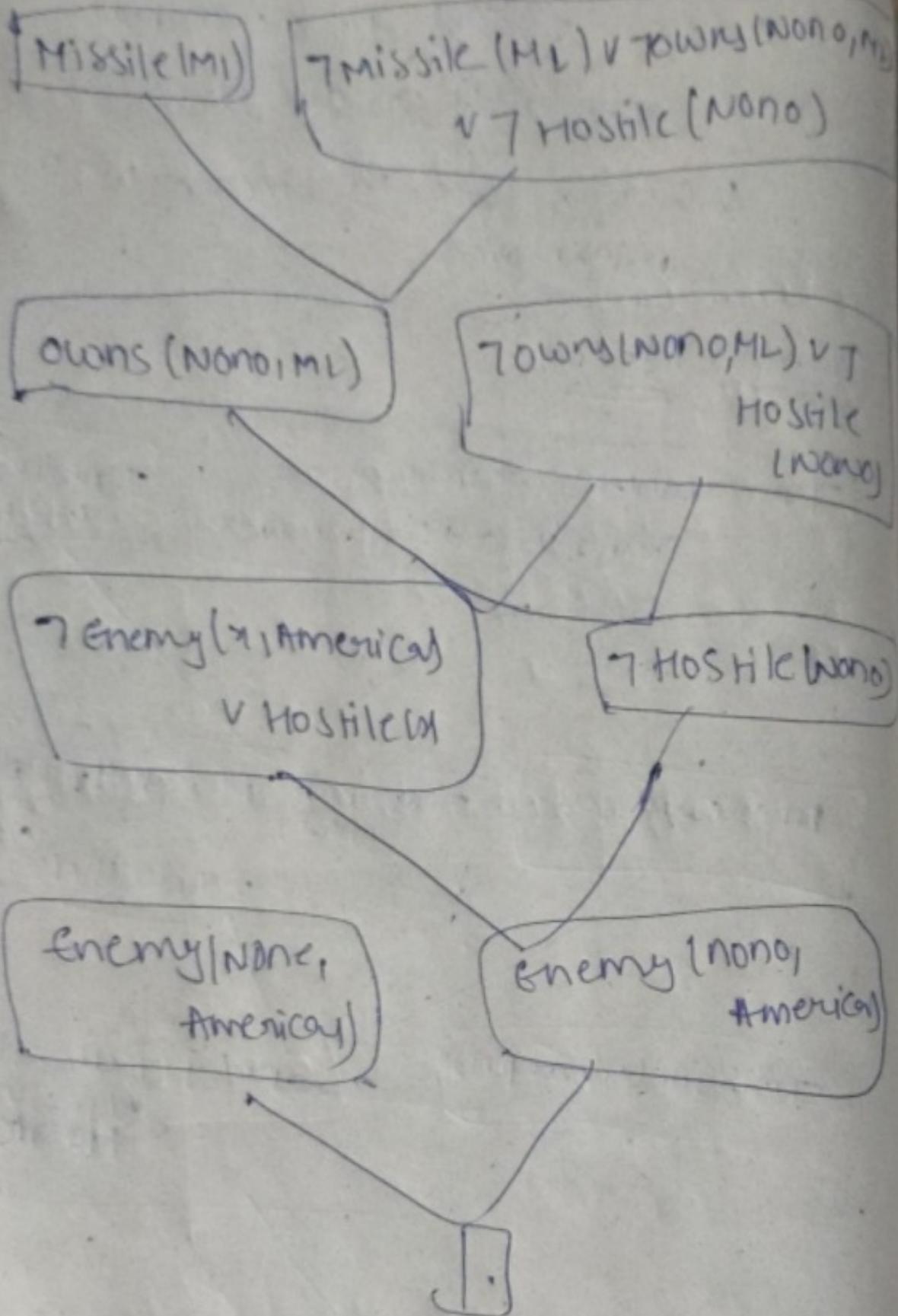
This step may also require flattening out nested conjunctions and disjunctions.

1.  $f(x)$  refers to the animal potentially owned by  $x$

2.  $g(x)$  refers to someone who might love  $x$ .

Example:- Pg = 44.





18) FORWARD AND BACKWARD  
CHAINING

forward chaining is one of the two main methods of reasoning when using an inference engine and can be described logically as repeated application of modus ponens.

1. If  $x$  croaks and  $x$  eats flies -

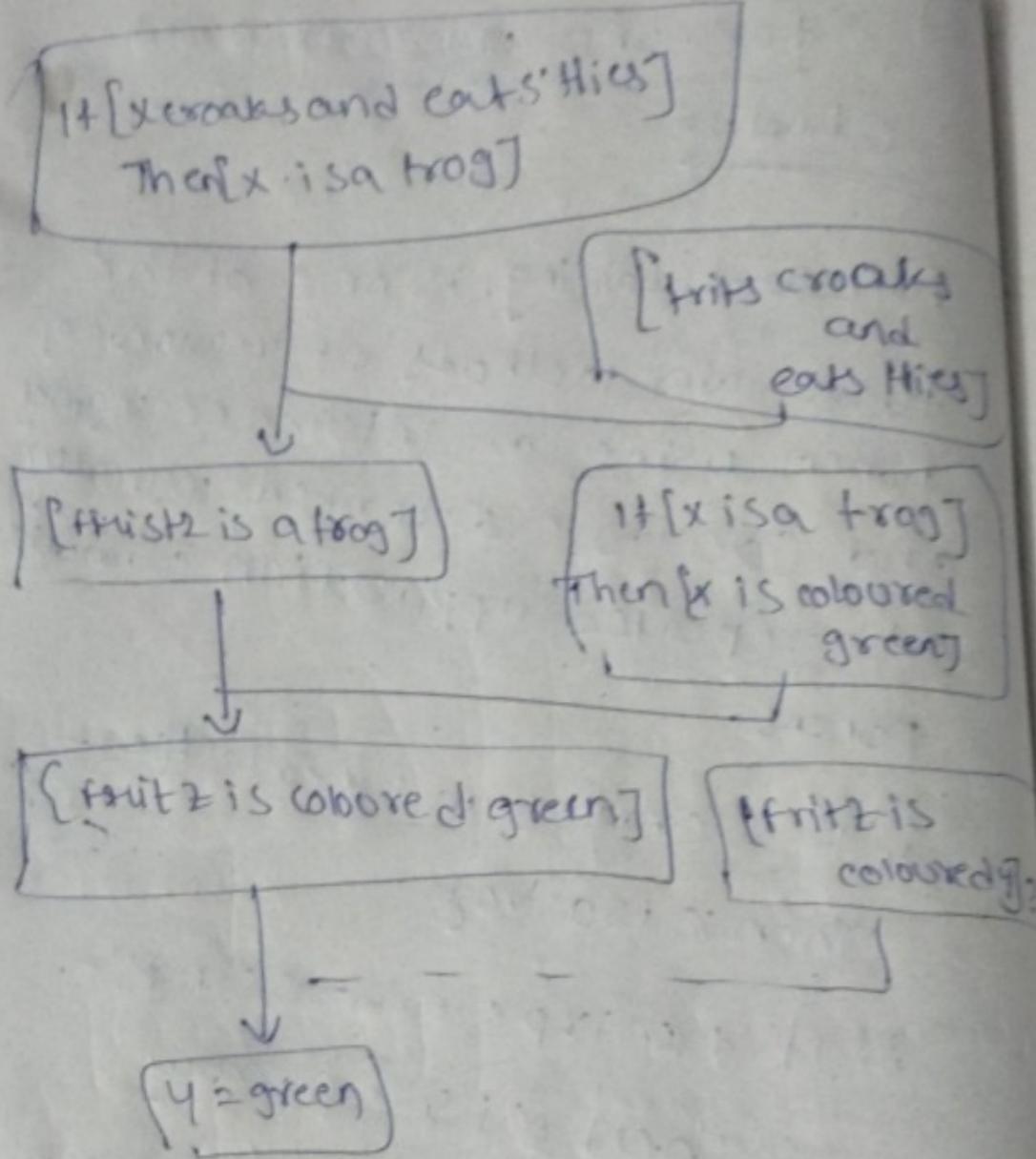
Then  $x$  is a frog.

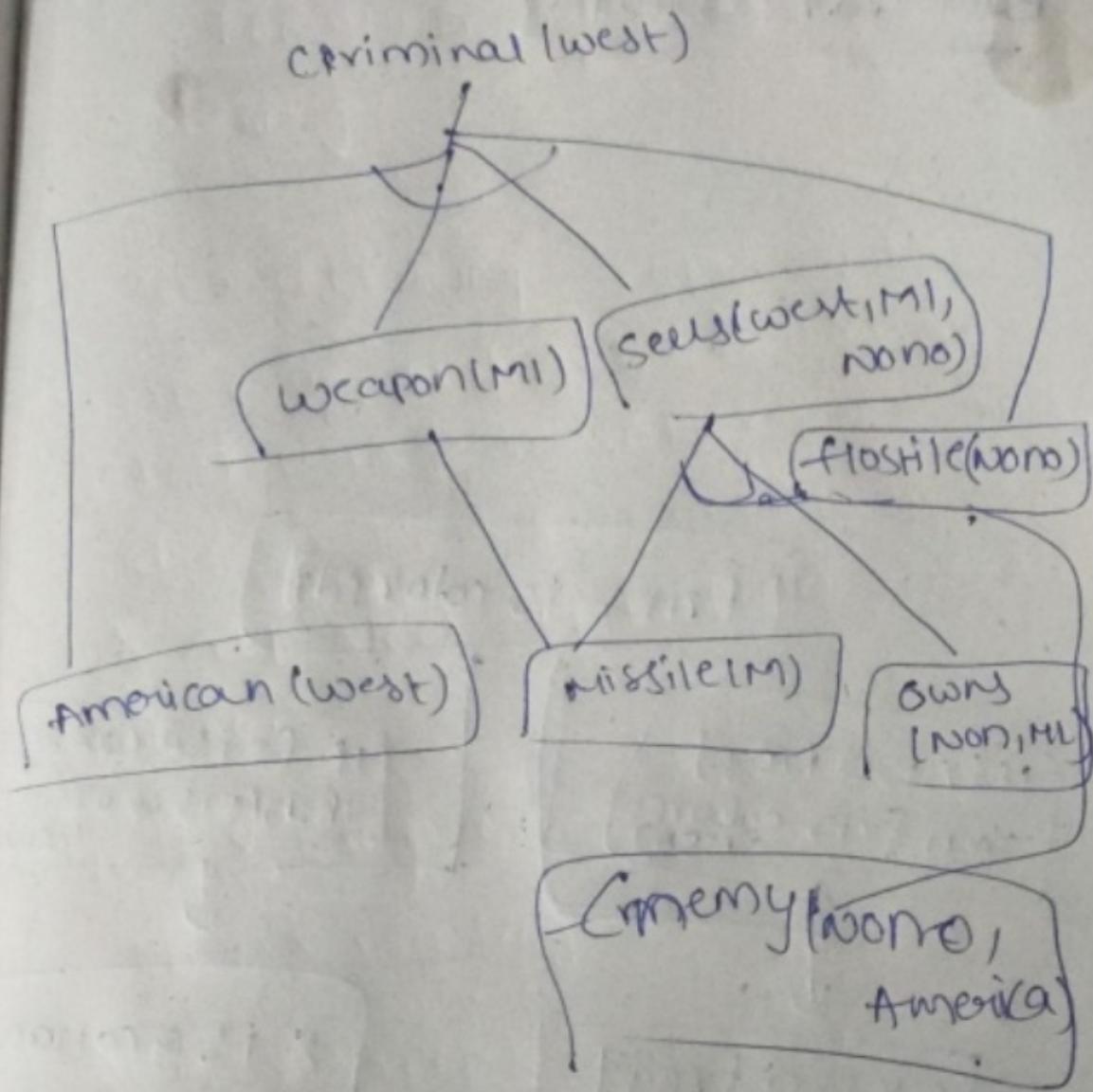
2. If  $x$  chirps and  $x$  sings -

Then  $x$  is a canary

3. If  $x$  is a frog - Then  $x$  is green

4. If  $x$  is a canary - Then  $x$  is yellow





~~function~~

## Backward chaining

