



SATHYABAMA

INSTITUTE OF SCIENCE AND TECHNOLOGY
(DEEMED TO BE UNIVERSITY)

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SCHOOL OF COMPUTING

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DEPARTMENT OF BIOTECHNOLOGY

DEPARTMENT OF BIOMEDICAL ENGINEERING

UNIT – III - PROJECTION OF SOLIDS – SMEA1102

PROJECTION OF SOLIDS

Introduction:

A solid has three dimensions, the length, breadth and thickness or height. A solid may be represented by orthographic views, the number of which depends on the type of solid and its orientation with respect to the planes of projection. Solids are classified into two major groups.

- (i) Polyhedral, and
- (ii) Solids of revolution

POLYHEDRAL

A polyhedral is defined as a solid bounded by plane surfaces called faces. They are: (i) Regular polyhedral (ii) Prisms and (iii) Pyramids

Regular Polyhedral

A polyhedron is said to be regular if its surfaces are regular polygons. The following are some of the regular polyhedral.

SOLIDS

To understand and remember various solids in this subject properly, those are classified & arranged in to two major groups.

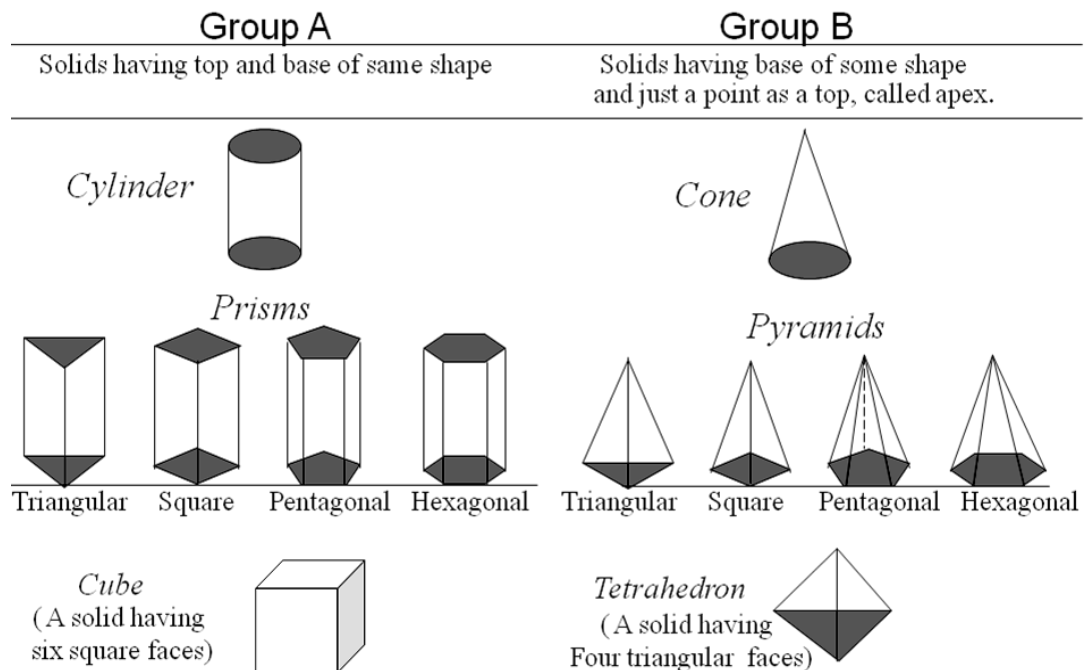


Figure 3.1

Prisms: A prism is a polyhedron having two equal ends called the bases parallel to each other. The two bases are joined by faces, which are rectangular in shape. The imaginary line passing through the centers of the bases is called the axis of the prism. A prism is named after the shape of its base. For example, a prism with square base is called a square prism, the one with a pentagonal base is called a pentagonal prism, and so on (Fig) The nomenclature of the prism is given in Fig.3.1

Tetrahedron: It consists of four equal faces, each one being an equilateral triangle.

Hexahedron (cube): It consists of six equal faces, each a square.

Octahedron: It has eight equal faces, each an equilateral triangle.

Dodecahedron: It has twelve regular and equal pentagonal faces.

Icosahedrons: It has twenty equal, equilateral triangular faces.

Pyramids: A pyramid is a polyhedron having one base, with a number of isosceles triangular faces, meeting at a point called the apex. The imaginary line passing through the center of the base and the apex is called the axis of the pyramid.

Dimensional parameters of different solids.

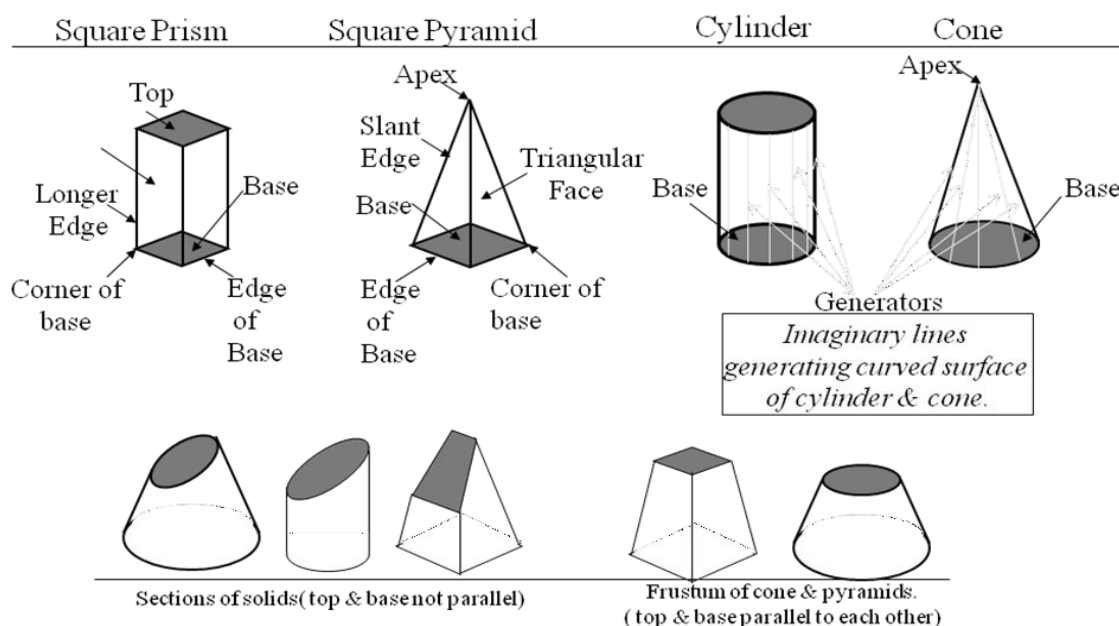


Figure 3.2

The pyramid is named after the shape of the base. Thus, a square pyramid has a square base and pentagonal pyramid has pentagonal base and so on. The nomenclature of a pyramid is shown in Fig.3.2.

Types of Pyramids:

There are many types of Pyramids, and they are named after the shape of their base.

These are Triangular Pyramid, Square Pyramid, Pentagonal pyramid, hexagonal pyramid and tetrahedron

Solids of Revolution: If a plane surface is revolved about one of its edges, the solid generated is called a solid of revolution. The examples are (i) Cylinder, (ii) Cone, (iii) Sphere.

Frustums and Truncated Solids: If a cone or pyramid is cut by a section plane parallel to its base and the portion containing the apex or vertex is removed, the remaining portion is called frustum of a cone or pyramid.

Prisms Position of a Solid with Respect to the Reference Planes: The position of solid in space may be specified by the location of either the axis, base, edge, diagonal or face with the principal planes of projection. The following are the positions of a solid considered.

- Axis perpendicular to HP
- Axis perpendicular to VP
- Axis parallel to both the HP and VP
- Axis inclined to HP and parallel to VP
- Axis inclined to VP and parallel to HP
- Axis inclined to both the Planes (VP. and HP)

The position of solid with reference to the principal planes may also be grouped as follows:

- Solid resting on its base.
- Solid resting on anyone of its faces, edges of faces, edges of base, generators, slant edges, etc.
- Solid suspended freely from one of its corners, etc.

1. Axis perpendicular to one of the principal planes:

When the axis of a solid is perpendicular to one of the planes, it is parallel to the other. Also, the projection of the solid on that plane will show the true shape of the base.

When the axis of a solid is perpendicular to H.P, the top view must be drawn first and then the

front view is projected from it. Similarly when the axis of the solid is perpendicular to V.P, the front view must be drawn first and then the top view is projected from it.

Problem is solved in three steps:
 STEP 1: ASSUME SOLID STANDING ON THE PLANE WITH WHICH IT IS MAKING INCLINATION.
 (IF IT IS INCLINED TO HP, ASSUME IT STANDING ON HP)
 (IF IT IS INCLINED TO VP, ASSUME IT STANDING ON VP)
 IF STANDING ON HP - IT'S TV WILL BE TRUE SHAPE OF IT'S BASE OR TOP:
 IF STANDING ON VP - IT'S FV WILL BE TRUE SHAPE OF IT'S BASE OR TOP.
 BEGIN WITH THIS VIEW:
 IT'S OTHER VIEW WILL BE A RECTANGLE (IF SOLID IS *CYLINDER OR ONE OF THE PREMS*):
 IT'S OTHER VIEW WILL BE A TRIANGLE (IF SOLID IS *CONE OR ONE OF THE PYRAMIDS*):
 DRAW FV & TV OF THAT SOLID IN STANDING POSITION:
 STEP 2: CONSIDERING SOLID'S INCLINATION (AXIS POSITION) DRAW IT'S FV & TV.
 STEP 3: IN LAST STEP, CONSIDERING REMAINING INCLINATION, DRAW IT'S FINAL FV & TV.

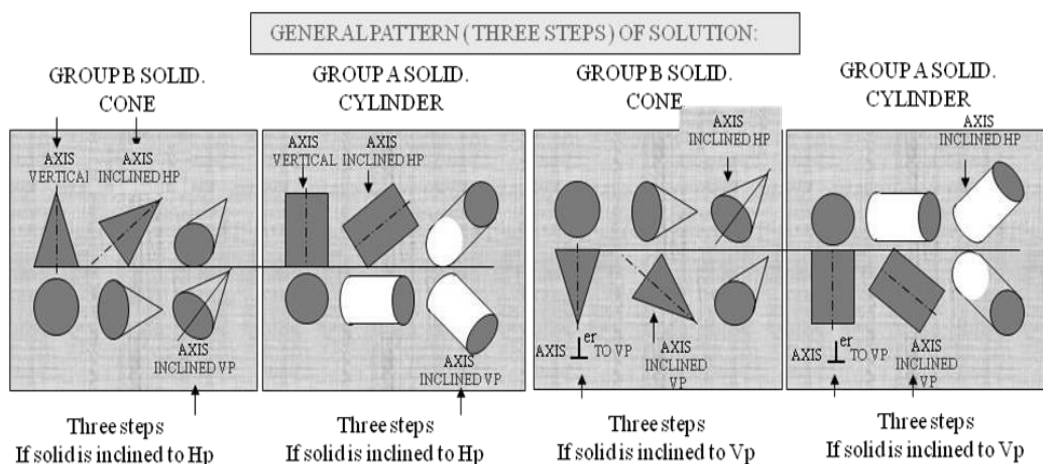


Figure 3.3

Simple Problems:

When the axis of solid is perpendicular to one of the planes, it is parallel to the other. Also, the projection of the solid on that plane will show the true shape of the base. When the axis of a solid is perpendicular to H.P, the top view must be drawn first and then the front view is projected from it. Similarly when the axis of the solid is perpendicular to V.P, the front view must be drawn first and then the top view is projected from it.

Axis perpendicular to HP

Problem:

A Square Pyramid, having base with a 40 mm side and 60mm axis is resting on its base on the HP. Draw its Projections when (a) a side of the base is parallel to the VP. (b) A side of the base is inclined at 30° to the VP and (c) All the sides of base are equally inclined to

the VP.

Solution:

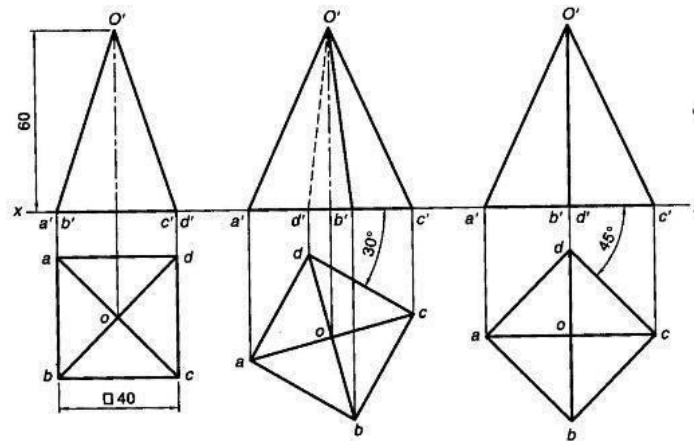


Figure 3.4

Axis perpendicular to VP

Problem:

A pentagonal Prism having a base with 30 mm side and 60mm long Axis, has one of its bases in the VP. Draw its projections when (a) rectangular face is parallel to and 15 mm above the HP (b) A rectangular face perpendicular to HP and (c) a rectangular face is inclined at 45° to the HP **Solution:**

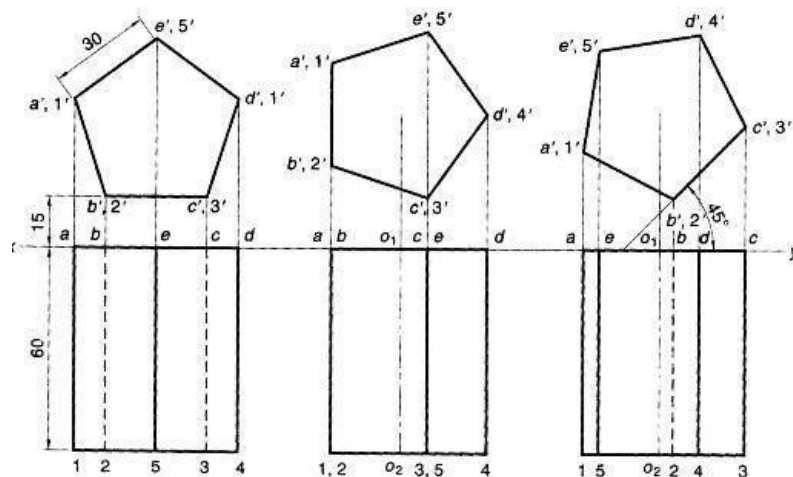


Figure 3.5

Axis inclined to HP and parallel to VP

Problem:

A Hexagonal Prism having a base with a 30 mm side and 75 mm long axis, has an edge its base on the HP. Its axis is parallel to the VP and inclined at 45° to the HP. Draw its projections?

Solution:

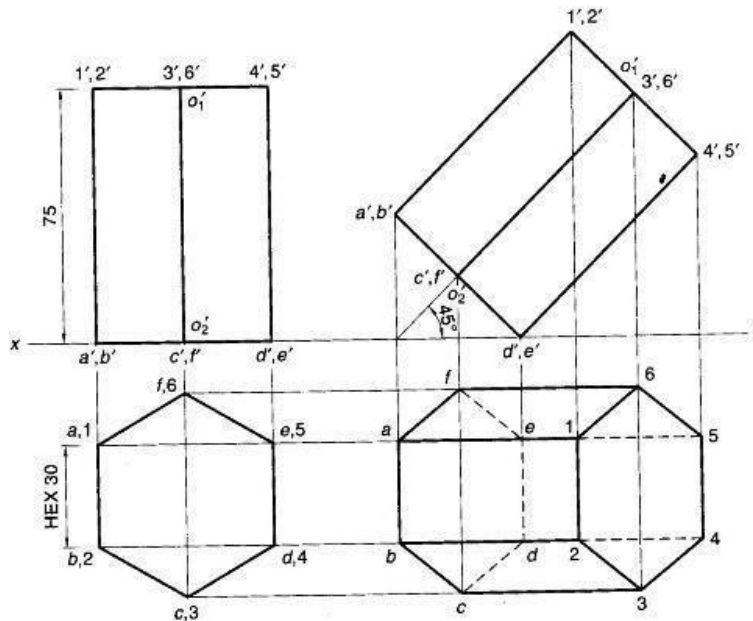


Figure 3.6

Problem:

A cube of 50 mm long edges is so placed on HP on one corner that a body diagonal is parallel to HP and perpendicular to VP. Draw its projections.

Solution Steps:

- Assuming standing on HP, begin with TV, a square with all sides equally inclined to xy. Project Fv and name all points of FV & TV.
- Draw a body-diagonal joining c' with $3'$ (This can become Parallel to xy)
- From $1'$ drop a perpendicular on this and name it p'
- Draw 2nd Fv in which $1'-p'$ line is vertical means $c'-3'$ diagonal must be horizontal. Now as usual project TV.
- In final TV draw same diagonal is perpendicular to VP as said in problem. Then as usual project final FV.

Solution:

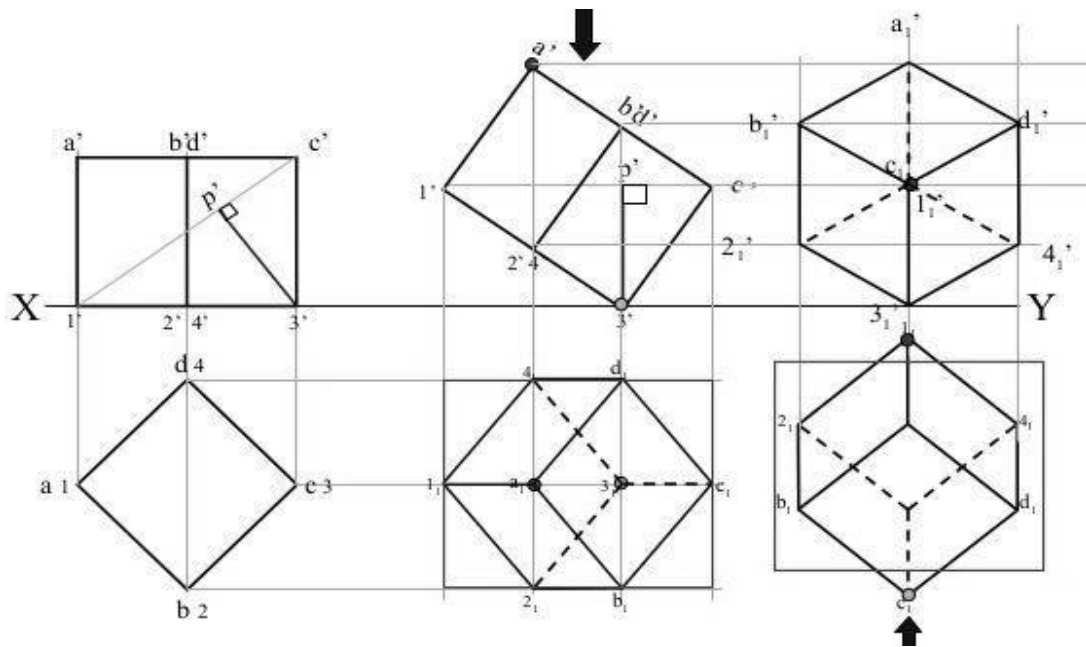


Figure 3.7

Problem:

A cone 40 mm diameter and 50 mm axis is resting on one of its generator on HP which makes 30° inclinations with VP. Draw it's projections?

Solution Steps:

- Resting on HP on one generator, means lying on HP
- Assume it standing on HP.
- It's TV will show True Shape of base(circle)
- Draw 40mm dia. Circle as TV& taking 50 mm axis project FV. (a triangle)
- Name all points as shown in illustration.
- Draw 2nd FV in lying position I.e. o'e' on xy. And project its TV below xy.
- Make visible lines dark and hidden dotted, as per the procedure.
- Then construct remaining inclination with VP (generator o₁e₁ 30° to xy as shown) & project final FV.

Solution:

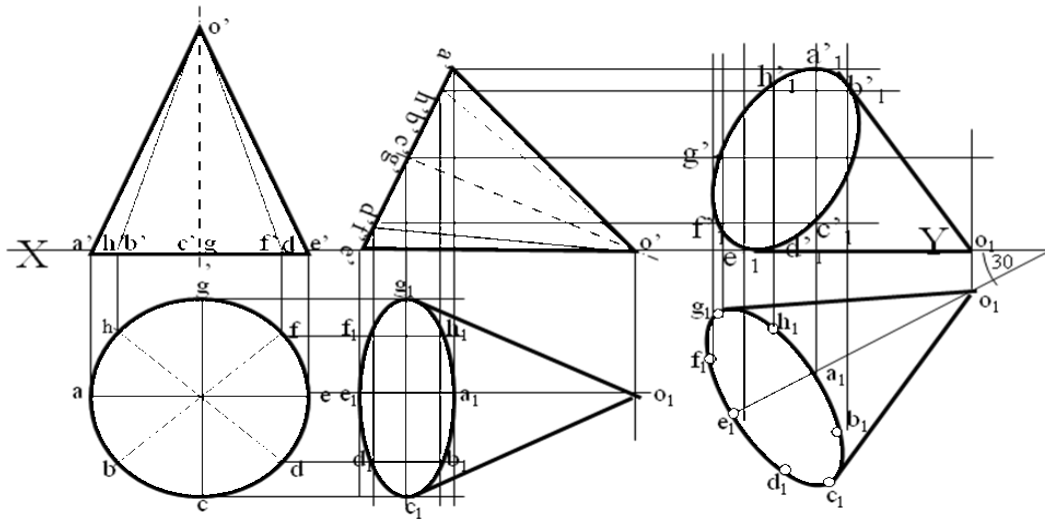


Figure 3.8

Problem

A cube of 50 mm long edges is so placed on HP on one corner that a body diagonal through this corner is perpendicular to HP and parallel to VP. Draw its views.

Solution:

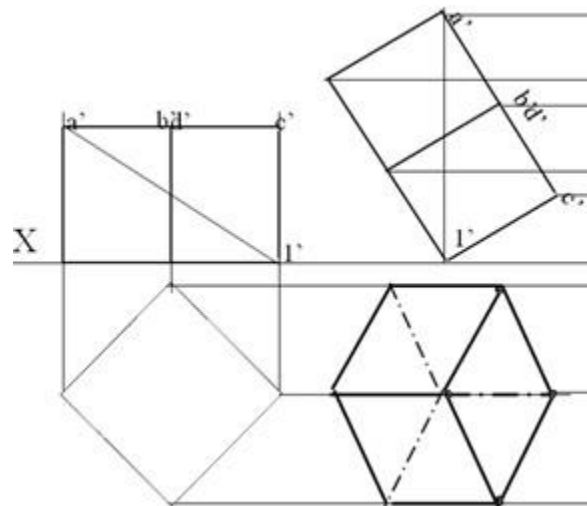


Figure 3.9

Solution Steps:

- Assuming it standing on HP begin with TV, a square of corner case.

- Project corresponding FV & name all points as usual in both views.
- Join $a'l'$ as body diagonal and draw 2nd FV making it vertical (l' on xy)
- Project its TV drawing dark and dotted lines as per the procedure.
- With standard method construct Left-hand side view. (Draw a 45° inclined Line in Tv region (below xy). Project horizontally all points of Tv on this line and reflect vertically upward, above xy . After this, draw horizontal lines, from all points of Fv, to meet these lines. Name points of intersections and join properly. For dark & dotted lines locate observer on left side of Fv as shown.)

Problem:

A circular cone, 40 mm base diameter and 60 mm long axis is resting on HP, on one point of base circle such that its axis makes 45° inclination with HP and 40° inclination with VP. Draw its projections.

Solution:

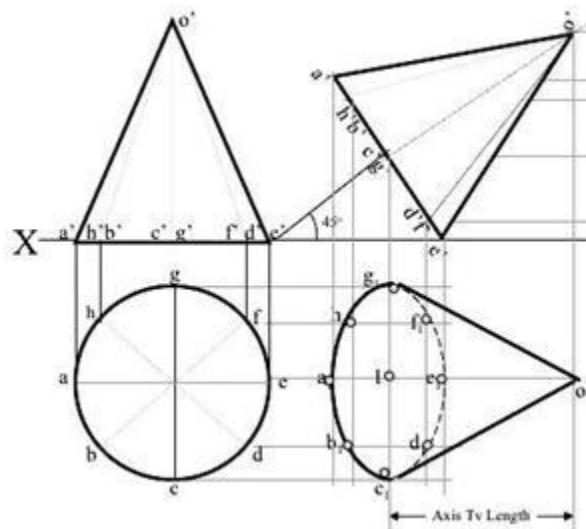


Figure 3.10

Problem

A hexagonal prism, having a base with a 30mm side and an 80mm long axis, rests on one of its base edges in the H.P such that the axis is inclined at 30° to the HP and 45° to the VP. Draw its projections?

Solution:

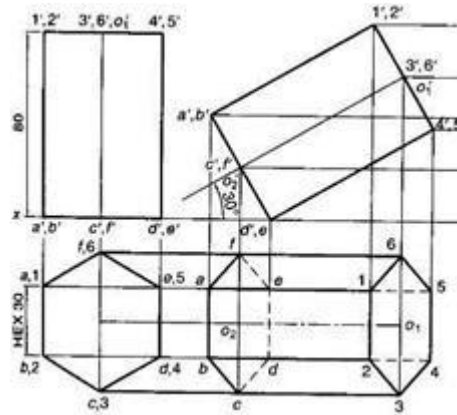


Figure 3.11

Tips & Shortcuts:

1. Axis inclined to HP and Parallel to VP → have to solve in two stages Stage (i) assume axis perpendicular to HP then draw Top and Front view

Stage (ii) Tilt the Front view according to given angle. Then project all the points will get Final Top view

2 Axis inclined to VP and Parallel to HP → have to solve in two stages Stage(i) assume axis perpendicular to VP then draw front and Top view

Stage (ii) Tilt the Top view according to given angle. Then project all the points will get Final Front view