ASSIGNMENT 2

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Download all python codes from

https://github.com/vishwahurakadli/EE3900/blob/main/Assignment_2/EE3900_Assignment_2.ipynb

and latex-tikz codes from

https://github.com/vishwahurakadli/EE3900/blob/main/Assignment_2/EE3900_Assignment_2.tex

1 Problem

(Matrix-2.52)
If
$$\mathbf{A} = \begin{pmatrix} -2\\4\\5 \end{pmatrix}$$
, $\mathbf{B} = \begin{pmatrix} 1,3,-6 \end{pmatrix}$, verify that $(\mathbf{A}\mathbf{B})^{\mathsf{T}} = \mathbf{B}^{\mathsf{T}}\mathbf{A}^{\mathsf{T}}$

2 Solution

Calculating transpose of matrix multiplication on LHS

Matrix multiplication of AB is given by

$$\mathbf{AB} = \begin{pmatrix} -2\\4\\5 \end{pmatrix} (1,3,-6) \tag{2.0.1}$$

$$\implies \mathbf{AB} = (-2 \times 1 + 4 \times 3 + 5 \times (-6)) = (-20)$$
(2.0.2)

As there is only one element in matrix AB and it is square matrix, therefore transpose of matrix AB is AB itself

$$(\mathbf{A}\mathbf{B})^{\mathsf{T}} = (-20) \tag{2.0.3}$$

Calculating multiplication of transpose of matrices Transpose of matrices

$$\mathbf{A}^{\top} = \begin{pmatrix} -2, 4, 5 \end{pmatrix} \tag{2.0.4}$$

$$\mathbf{B}^{\top} = \begin{pmatrix} 1\\3\\-6 \end{pmatrix} \tag{2.0.5}$$

Now

$$\mathbf{B}^{\mathsf{T}}\mathbf{A}^{\mathsf{T}} = (1 \times -2 + 3 \times 4 + (-6) \times 5) (2.0.6)$$

$$\mathbf{B}^{\mathsf{T}}\mathbf{A}^{\mathsf{T}} = (-20) \tag{2.0.7}$$

$$\implies (\mathbf{A}\mathbf{B})^{\mathsf{T}} \tag{2.0.8}$$

Therefore $(\mathbf{A}\mathbf{B})^{\mathsf{T}} = \mathbf{B}^{\mathsf{T}}\mathbf{A}^{\mathsf{T}}$