

$$e^{[s]t} = \begin{bmatrix} e^{[w]t} & I\theta + (1-\cos\theta)[w] + \theta\sin\theta[w^2] \\ 0 & 1 \end{bmatrix}$$

$$w = \underline{\omega} \quad \theta = \sqrt{\text{mag.}}$$

$$e^{[w]t} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} + \sin(\theta)[w] + (1-\cos\theta)[w^2]$$

$$w = \begin{bmatrix} 0 \\ 0 \\ \omega_2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \quad \theta = \omega_2$$

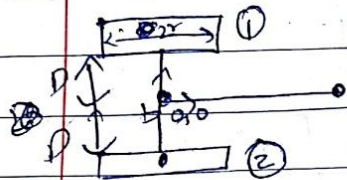
$$[w] = \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$e^{[w]t} = I + \sin(\omega_2) \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} + (1-\cos(\omega_2)) \begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \times \omega_3 + (1-\cos(\omega_3)) \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} + \omega_3 - \sin(\omega_3) \begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$e^{j\omega_2 t} = \begin{vmatrix} \cos(\omega_2 t) & -\sin(\omega_2 t) \\ \sin(\omega_2 t) & \cos(\omega_2 t) \end{vmatrix} \begin{pmatrix} \frac{V_n \sin(\omega_3 t) - V_y}{\omega_3} + \frac{V_y \cos(\omega_3 t)}{\omega_3} \\ \frac{V_n - V_n \cos(\omega_3 t) + V_y \sin(\omega_3 t)}{\omega_3} \end{pmatrix}$$

0 0 1



$$T_{b1}(0, 0, D)$$

$$T_{b2}(0, 0, -D)$$

$$A_{b1} =$$

$$\begin{bmatrix} 1 & 0 & 0 \\ D & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$A_{1b} =$$

$$\begin{bmatrix} 1 & 0 & 0 \\ -D & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$A_{b2} =$$

$$\begin{bmatrix} 1 & 0 & 0 \\ -D & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$A_{2b} =$$

$$\begin{bmatrix} 1 & 0 & 0 \\ D & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$V_1 = A_{1b} V_b \quad V_2 = A_{2b} V_b$$

$$V_b = \begin{bmatrix} \theta \\ v_x \\ v_y \end{bmatrix}$$

$$V_1 = \begin{bmatrix} \theta \\ v_{x1} \\ v_{y1} \end{bmatrix}$$

$$\begin{bmatrix} \theta \\ v_{x1} \\ v_{y1} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ -D & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \times \begin{bmatrix} \theta \\ v_x \\ v_y \end{bmatrix}$$

$$\begin{bmatrix} \dot{\theta} \\ \dot{r} u_1 \\ 0 \end{bmatrix} = \begin{bmatrix} \dot{\theta} \\ -\cancel{D\dot{\theta}} + v_n \\ v_y \end{bmatrix}$$

$$u_1 = \frac{-D\dot{\theta} + v_n}{r}$$

$$\begin{bmatrix} u_1 \\ 0 \end{bmatrix} = \begin{bmatrix} -\frac{D}{r} & \frac{1}{r} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \dot{\theta} \\ v_n \\ v_y \end{bmatrix}$$

$$\begin{bmatrix} u_2 \\ 0 \end{bmatrix} = \begin{bmatrix} \frac{D}{r} & \frac{1}{r} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \dot{\theta} \\ v_n \\ v_y \end{bmatrix}$$

$$\begin{bmatrix} u_1 \\ u_2 \end{bmatrix} = \frac{1}{r} \begin{bmatrix} -D & 1 & 0 \\ D & 1 & 0 \end{bmatrix} \begin{bmatrix} \dot{\theta} \\ v_n \\ v_y \end{bmatrix}$$