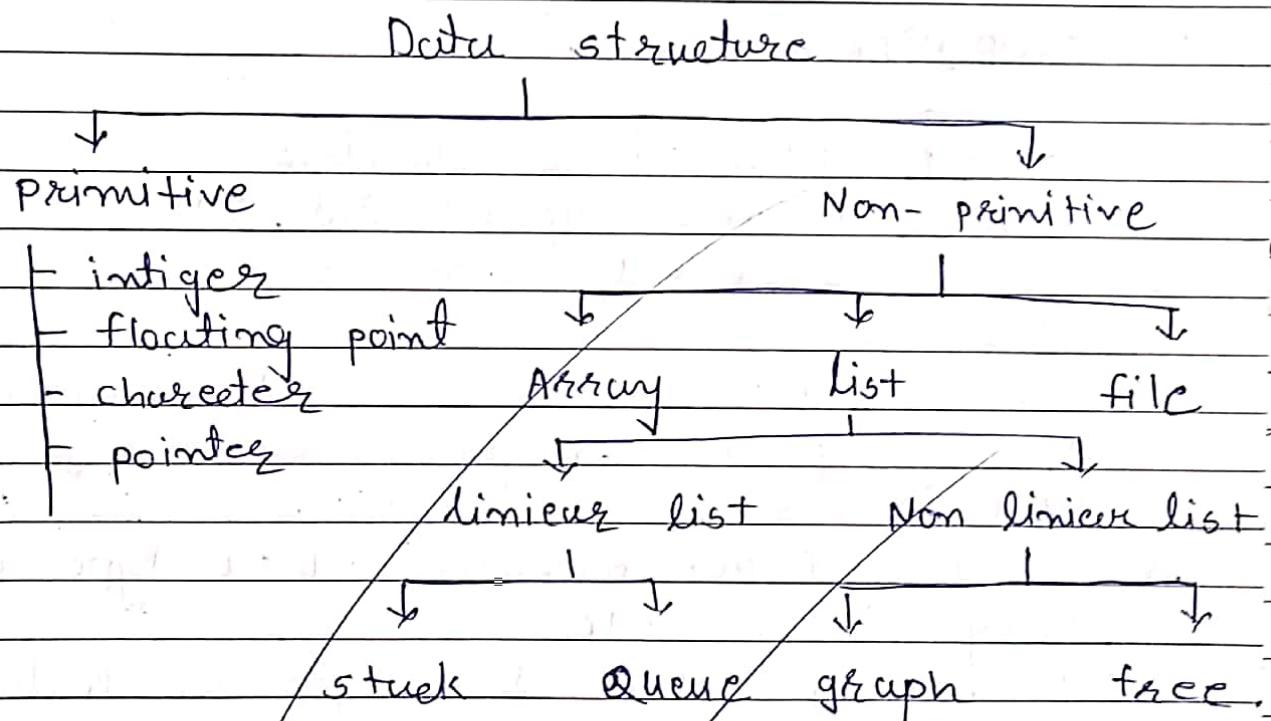


B

ASSIGNMENT - I

- Q) Define data structure, list out types of data structure and explain them in brief. Differentiate the following terms primitive & Non-primitive data structure. linear and Non-linear data structure.
- ⇒ Data structure is representation of the logical relationship existing between individual element of data.



⇒ Data structure are normally divided into two broad categories.

- 1) primitive data structure
- 2) Non-primitive data structure.

primitive data structure

- ⇒ primitive data structure are basic structures and are directly operated upon by machine instructions.
- ⇒ primitive data structure have different representation on different computers
- ⇒ Integer , float , character & pointers are examples of primitive data structure.
- ⇒ These data types are available in most programming languages as built in type.
 - Integer
 - float
 - character
 - pointer

Non-primitive data structure

- ⇒ These are more sophisticated data structures
- ⇒ These are derived from primitive data structure.
- ⇒ The non-primitive data structure comprises of a group of homogeneous or heterogeneous data items.
- ⇒ Examples of Non primitive data type are array , list , file etc.
- ⇒ A non-primitive data type is further divided into linear & Non-linear data structure.
 - Array
 - list
 - file

Linear Data Structure:

- ⇒ A data structure is said to linear, if its elements are connected in linear fashion by means of logically or in sequence memory location.
- ⇒ There are two ways to represent a linear data structure in memory.
 - static memory allocated
 - Dynamic memory allocation.
- ⇒ The possible operation on linear data structure are: Traversal, Deletion, insertion, searching, sorting, & Merging.
- ⇒ Examples of linear data structure are stack and queue.

Non linear data structure:

- ⇒ Non-linear data structures are those data structure in which data items are not arranged in sequence.
- ⇒ Examples of Non-linear data structure are tree and graph.

2) Discuss best case, average case and worst case time analysis with example.

Best case Analysis

⇒ In the best case analysis we calculate lower bound on running time of an algorithm we must know the case that causes min no of operation to be executed. in the linear search problem the best case occurs when x is present at the first location. the number of operation in worst case is const. so time complexity is the best case

Average case Analysis

⇒ In average case analysis, we take all possible inputs and calculate computing time for all of the input. sum all the calculated values and divide the sum by total number of inputs we must know distribution of cases. for the linear search problem, let us assume that all cases are uniformly distributed, so we sum all the cases and divide the sum by (nH) .

Worst case Analysis:

⇒ In the worst case analysis, we calculated upper bound on running time of an algorithm we must know the case that causes maximum number of operation to be executed. for linear search. the worst case happens when the element to be searched is not present in the array, when x is

not present, the search loop function compares it with all the elements of array one by one. Therefore, the worst case time complexity of linear search would be $O(n)$.

3) what does abstract data type mean?

- ⇒ An abstract datatype is the way we look at the data structure, focusing on what it does and ignoring how it does its job. The word "abstract" in the contrast of data structures means considered apart from the detailed specification or implementation.
- ⇒ In C, an abstract data type can be considered without regard to its implementation. It can be thought of as a description of the data structure with a list of operations that can be performed on the data within the structure.
- ⇒ The end-user is not concerned about how the details of how the methods carry out their tasks. They are only aware of the method that are available to them and are only concerned about calling those methods and getting the results. They are not concerned about how they work.

4) Write an algorithm to implement PUSH POP & CHANGE operations on stack.

PUSH algorithm.

1) [check for stack overflow]

if ($\text{TOP} \geq N$)

then write ('STACK OVERFLOW')
Return

2) [TOP Increment]

$\text{TOP} \leftarrow \text{TOP} + 1$

3) [Insert element]

$s[\text{TOP}] \leftarrow x$

4) [finished]

Return

POP algorithm.

1) [check for underflow on stack]
if $\text{TOP} = 0$

then write ('STACK UNDERFLOW ON POP')
take action in response to underflow
exit.

2) [pointer decrementation]

$\text{TOP} \leftarrow \text{TOP} - 1$

3) [Return former top element of stack]
Return ($s[\text{TOP} + 1]$)

CHANGE algorithm

- 1) [check for stack underflow]
if $\text{TOP} - i + 1 \leq 0$
then write ('STACK UNDERFLOW ON
CHANGE')
 - 2) [change i^{th} element from top of stack]
 $s[\text{TOP} - i + 1] \leftarrow x$
 - 3) [finished]
Return.
- 5) convert infix to prefix / postfix format
showing stack status after every step in
tabular form.

i) $((A+B)*C-D^E^F * G))$ postfix

Next check content of stack Notation
RPN

((-	-
*	((-	-
A	((A	-	-
+	((+)	A	
B	((+B	A	
)	((AB+	1
*	((*	AB+	1
C	((*C	AB+	1
-	((-)	AB+C*	1
D	((-D	AB+C*	1

Next char	content of stack	polish notation	Rank
^	C - ^	A B + C * D	2
E	C - ^ E	A B + C * D	2
^	C - ^ ^	A B + C * D E	3
(C - ^ ^ (A B + C * D E	3
F	C - ^ ^ (F	A B + C * D E	3
*	C - ^ ^ (*	A B + C * D E F	4
G	C - ^ ^ (* G	A B + C * D E F	4
)	C - ^ ^	A B + C * D E F G *	4
)	-	A B + C * D E F G * ^ ^ -	2

ii) $((A + B * D + F / (E F + G * D)) + C)$ postfix

Next char.	Content of stack	polish notation	Rank.
((-	-
(((-	-
A	((A	-	-
+	((+	A	1
B,	((+ B	A	1
*	((+ B *	AB +	1
D	((+ B * D	AB +	1
+	((+ D	AB +	1
E	((+ D + E	AB + D *	1
/	((+ D + E /	AB + D * E	2
(((+ D + E / (AB + D * E	2
F	((+ D + E / F	AB + D * E F	2
+	((+ D + E / F +	AB + D * E F	3
G	((+ D + E / F + G	AB + D * E F F	3
*	((+ D + E / F + G *	AB + D * E F F G	4
)	((+ D + E / F + G *	AB + D * E F F G	4
)	C + I	AB + D * E F F G D * +	3

$$\begin{array}{lll}
 + & (+ AB + D * E F G D * + I +) & \\
 C & (+ C AB + D * E F G D * + I +) & \\
) & - AB + D * E F G D * + I + C + &
 \end{array}$$

iii) $A \mid B \& C + D * E \mid F - G + H$ prefix

\Rightarrow After inventing expression $\# H + G - F \mid E * D + C$
 $\& B \mid A \#$

Neat char	content of stacks	polish Notation	Rank
#	#	-	-
H	# H	-	-
+	# +	H	1
G	# + G	H	1
-	# -	H G +	1
F	# - F	H G +	1
I	# - I	H G + F	2
E	# - I E	H G + F	2
*	# - * E	H G + F E I	2
D	# - * D	H G + F E I	2
+	# +	H G + F E I D * -	1
C	# + C	H G + F E I D * -	1
\$	# + C \$	H G + F E I D * - C	2
B	# + C \$ B	H G + F E I D * - C	2
/	# + /	H G + F E I D * - C B \$	2
A	# + / A	H G + F E I D * - C B \$ A +	2
#	-	H G + F E I D * - C B \$ A +	1

prefix : $+ \mid n \& BC - * D \mid E F + G H$

iv) $a - b * c + d + e * f / g$ prefix.
 $\Rightarrow \# g f e c d + * - + a b -$

Next char	content of stack	polish Notation	Rank
#	#	-	-
g	# g	-	-
f	# f	g	1
*	# *	gf	1
c	# * c	gf	1
+	# +	gf +	1
d	# + d	gf +	1
*	# + *	gf +	1
c	# + * c	gf + c	2
l	# + l	gf + cl	2
b	# + l b	gf + cl b	2
-	# -	gf + cl b -	2
a	# - a	gf + cl b - a	1
#	-	gf + cl b - a -	1
prefix	$\Rightarrow - a + b * c d * e f g$		

v) $((A - (B + C)) * D) + (E + F))$ - postfix

Next ch	com of stack	polish Notation	Rank
((-	-
)	11	-	-
(111	-	-
A	111 A	-	-
-	111 -	A	-
C	111 - C	A	1
B	111 - C B	A	1
+	111 - C +	A B	1
F	111 - C + F	A B	2

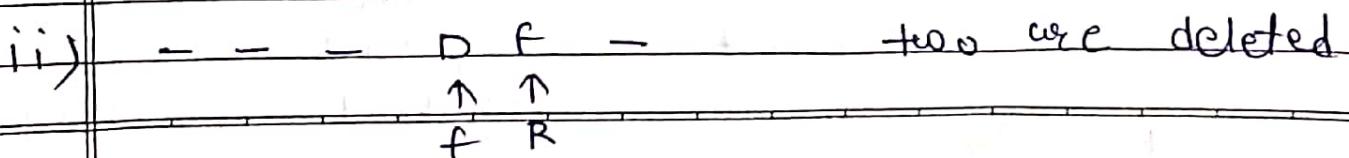
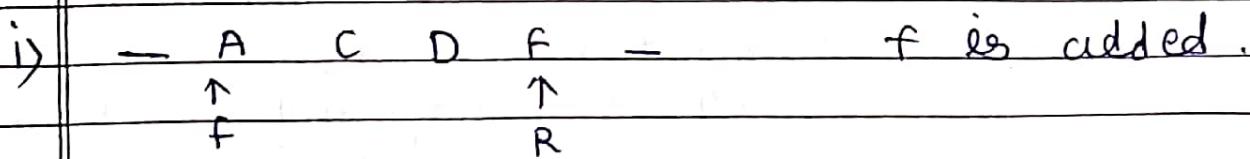
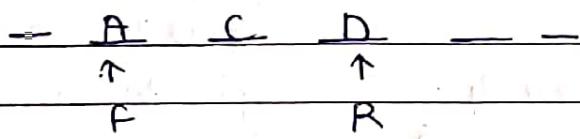
)	((-	A B C +	2
)	((A B C + -	1
*	((*	A B C + -	1
D	((* D	A B C + -	1
)	(A B C + - D *	1
\$	(\$	A B C + - D *	1
C	(\$ (A B C + - D *	1
E	(\$ (E	A B C + - D *	1
+	(\$ (@ +	A B C + - D * E	2
F	(\$ (+ F	A B C + - D * E	2
)	(\$	A B C + - D * E F T	2
)	-	A B C + - D * E F T + \$	1

6) Consider the following queue, where queue is a circular queue having 6 memory cells.
 front = 2 , Rear = 4

Queue : — A C D — —

Describe queue in following operation take place

- i) F is added
- ii) Two letters are deleted
- iii) R is added.
- iv) S is added.
- v) one letter is deleted.



iii) $_ _ - D F \frac{R}{\uparrow}$ R is added.
 f R

iv) $S - - D F R$ S is added.
 ↑ ↑
 R f

v) $S - - - f R$ one is deleted.
 ↑ ↑
 R f

7) Write an algorithm for evaluation of postfix expression & calculate the following expression showing status of stack in tubular form.

i) $S \ 4 \ 6 \ + \ * \ 4 \ 9 \ 3 \ / \ + \ *$

char scanned	content of stack	operation on stack	operation
S	S	push S	
4	S, 4	push 4	
6	S, 4, 6	push 6	
+	S, 10	pop 6, 4 $6 + 4 = 10$	
:		push 10	
*	50	pop 10, S $10 * 5 = 50$	
4	50, 4	push 4	
9	50, 4, 9	push 9	
3	50, 4, 9, 3	push 3	
/	50, 4, 3	pop 3, 9 $9 / 3 = 3$	
+	50, 7	push 3	
*	350	pop 4, 3 $3 + 4 = 7$	
		push 7	
		pop 7, 50 $50 * 7 = 350$	
		push 350	

ii) $7 \ 5 \ 2 \ + \ * \ 4 \ 1 \ 1 \ + \ 1 \ -$

char scanned	content of stack	operation on stack	operation
7	7	push 7	-
5	7, 5	push 5	-
2	7, 5, 2	push 2	-
+	7, 7	pop 2, 5 push 7	$2 + 5 = 7$
*	49	pop 7, 7 push 49	$7 * 7 = 49$
4	49, 4	push 4	
1	49, 4, 1	push 1	
1	49, 4, 1, 1	push 1	
+	49, 4, 1, 2	pop 1, 1 push 2	$1 + 1 = 2$
1	49, 2	pop 4, 2 push 2	$4 / 2 = 2$
-	47	pop 2, 49 push 47	$49 - 2 = 47$

iii) $2 \$ 3 + 5 * 2 \$ 2 - 6 / 6 \Rightarrow 23 \$ 522 \$ * + 661 -$

char	content of stack	operation ^{in stack}	operation
2	2	push 2	
3	2, 3	push 3	
\$	8	pop 2, 3 push 8	$2^3 = 8$
5	8, 5	push 5	
2	8, 5, 2	push 2	
2	8, 5, 2, 2	push 2	
\$	8, 5, 4	pop 2, 2 push 4	$2^2 = 4$

*	4, 120	pop 4, 5	4 * 5 = 20
+	28	push 20 pop 6, 120	20 + 6 = 26
G	28, G	push 28 push G	
G	28, G, G	push G	
/	28, 1, 1	pop G, 6 push 1	6 / 6 = 1
-	27	pop 28, 1 push 27	28 - 1 = 27

9) Write an algorithm to perform various operations (insert, delete, display) for simple queue.

Q INSERT

1) [overflow]

if $R \geq N$

then write ('OVERFLOW')

Return.

2) [Increment REAR pointer]

$R \leftarrow R + 1$

3) [Insert element] $\alpha[R] \leftarrow y$

4) [Is front pointer properly set?]

if $F = 0$

then $F \leftarrow 1$ Return.

Q DELETE or

1) [Underflow]

if $F = 0$

then write ('UNDERFLOW')
Return (0)

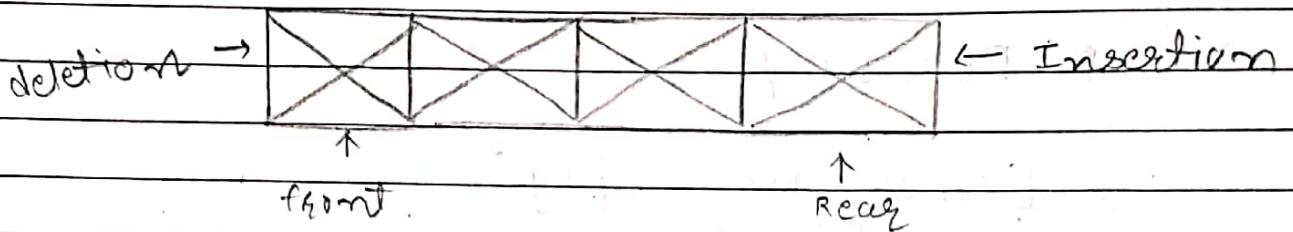
- 2) [Decrement element] $y \leftarrow a[F]$
- 3) [queue empty?] if $F = R$
then $F \leftarrow R \leftarrow 0$
else $F \leftarrow F + 1$
- 4) [Return element]
Return y

Q DISPLAY :-

- 1) [check for empty]
if $F > R$
then write ('queue is empty')
- 2) [Display content]
for ($i = FRONT ; i \leq REAR ; i++$)
write ($a[i]$)
- 3) [Return statement]
Return.
- 10) compare simple queue vs circular queue. write an algorithm to implement insert / delete operation into a circular queue using array representation of queue.

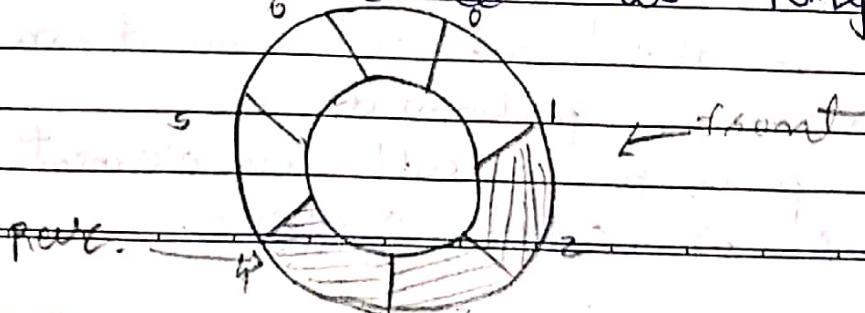
Queue \rightarrow It follows FIFO pattern
 \rightarrow front is the end of queue from where deletion is performed.
 \rightarrow Rear is the end of queue from where insertion is performed.
 \rightarrow The process to add an element in a queue is called enqueue.

- The process of removal of an element in a queue is called Dequeue.
- The familiar traditional examples of a queue is checkout line at supermarket cash registers where the first person in the line is usually the first to checkout.



Circular Queue → A more suitable method of representing simple queue which prevents an excessive use of memory to arrange the element $a[1]$, $a[2]$... $a[n]$ in a called circular fashion with $a[1]$ following $a[n]$, this is called circular queue.

- Circular queue is a linear data structure. It follows FIFO principle.
- In circular queue, the last node is connected back to the first node to make a circle.
- Circular linked list follow the first FIFO.
- Elements are added at the rear end & the elements are deleted from the front end of queue.
- Both the front & the rear pointer point to the beginning of array.
- It is also called as 'Ring buffer'.



consider a circular queue: F is at 2, R is at 4, queue - A C D - -

- i) F is added
- ii) two letters are deleted
- iii) R is added
- iv) S is added
- v) one is deleted.

- A C D - -
 ↑ ↑
 F R

F is added : - A C D F -
 ↑ ↑
 F R

two deleted : - - - D F -
 ↑ ↑
 F R

R added : - - - D F R
 ↑ ↑
 F R

S added : S - - D F R
 ↑ ↑ *
 R F

one is deleted : S - - - F R
 ↑ ↑
 R F

Q) briefly explain various applications of stack.

→ Recursion

→ keeping track of function calls.

→ evaluation of expression

→ Reversing character.

→ servicing hardware interrupts

→ solving combinatorial problems using backtracking.

expression evaluation.

→ stack is used to evaluate prefix, postfix, infix

expression conversion.

→ An expression can be represented in prefix, postfix, notation.

Infix expression: it is the general notation used for representing expression.

prefix expression :- operators are followed by operands

ex. infix :- a + b c

= postfix :- abc +

prefix :- + abc

All infix operations will be converted into postfix notation with the help of stack in any problem.

posting:-

→ Many compilers use a stack for parsing the syntax of expression program stacks etc. before transferring into the stack and then bestly invoked function will return the value by popping the stack.

function calls

→ A stack is useful for the operating system to store local variables used inside a for block so that they can be discarded once the control comes out of for block.

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