

Assignment - 2

1) What is image processing?

- It is a method to perform some operations on an image, in order to get an enhanced image or to extract some useful informations from it.

- It is a type of signal processing in which input is an image and output may be image or characteristics/features associated with that image.

- It basically includes the following three steps:

- Importing the image via image acquisition tools;
- Analysing and manipulating the image;
- Output in which result can be altered image or report that is based on image analysis.

2) Explain the key stages in Digital Image Processing.

Ans- There are mainly three types of steps for digital image processing as discussed earlier.

- Now, if we talk about phases of digital Image processing.

I. **ACQUISITION** - It could be as simple as being given an image which is in digital form.

- The main work involves:
 - a) Scaling
 - b) Color conversion (RGB to Gray or vice-versa)
- 2. IMAGE ENHANCEMENT - It is amongst the simplest and most appealing in areas of Image Processing it is also used to extract some hidden details from an image and is subjective.
- 3. IMAGE RESTORATION - It also deals with appealing of an image but it is objective.
- 4. COLOR IMAGE PROCESSING - It deals with pseudocolor and full color image processing color models are applicable to digital image processing.
- 5. WAVELETS & MULTI-RESOLUTION PROCESSING - It is foundation of representing images in various degrees.
- 6. IMAGE COMPRESSION - It involves in developing some functions to perform this operation. It mainly deals with image size or res.
- 7. MORPHOLOGICAL PROCESSING - It deals with tools for extracting image components that are useful in the representation & description of shape.

8. **SEGMENTATION PROCEDURE** - It includes partitioning an image into its constituent parts or objects. Autonomous segmentation is the most difficult task in Image Processing.

9. **REPRESENTATION & DESCRIPTION** - It follows output of segmentation stage, choosing a representation is only the part of solution for transforming raw data into processed data.

10. **OBJECT DETECTION AND RECOGNITION** - It is a process that assigns a label to an object based on its descriptor.

3) Write difference between Enhancement and Restoration.

- The difference between Enhancement and Restoration is given below:

- Enhancement:

- Largely a **subjective** process
- Prior knowledge about the degradation is not a must (sometimes no degradation is involved)
- Procedures are heuristic and take advantage of the psychophysical aspects of human visual system.

- Restoration:

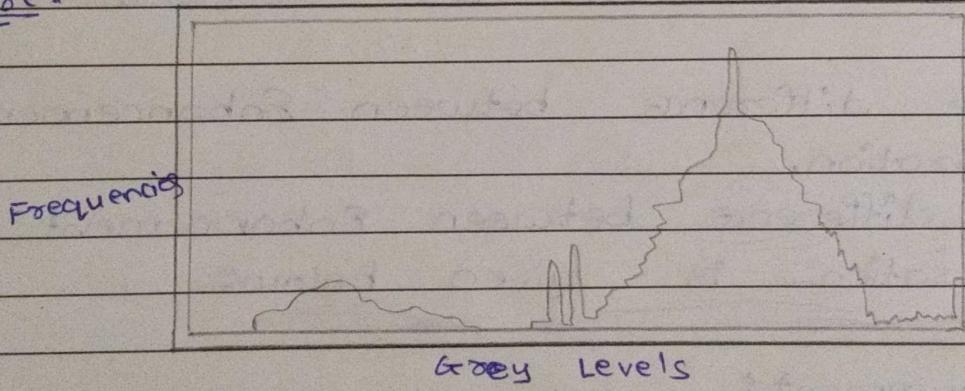
- More an objective process
- Images are degraded.
- Tries to recover the image by using the knowledge about the degradation.

4) Explain Image Histograms and Histogram Stretching with example.

- Image Histogram:

- The histogram of an image shows us the distribution of grey levels in image.
- Massively useful in image processing especially in segmentation.

Figure:



- Histogram Image Stretching:

- One way to increase the dynamic range is by using a technique known as histogram stretching.
- In the method, we do not alter the basic shape of the histogram, but we spread it so as to cover the entire dynamic range.

$$S = T(\gamma) = \frac{S_{\max} - S_{\min}}{R_{\max} - R_{\min}} (R - R_{\min}) + S_{\min}$$

Remember

$\hookrightarrow S_{\max}$ = Max grey level of output image

$\hookrightarrow S_{\min}$ = Min " " " "

$\hookrightarrow \gamma_{\max}$ = Max " " " input "

$\hookrightarrow \gamma_{\min}$ = Min " " " input "

→ Example: $R_{\min} = 2, R_{\max} = 6, S_{\min} = 0, S_{\max} = 7, \gamma = [2, 6]$

Put the given value in eqn

$$S = \frac{7 - 0}{6 - 2} (\gamma - 2) + 0$$

$$S = \frac{7}{4} (\gamma - 2) \Rightarrow \gamma = 2: S = \frac{7}{4} (2 - 2) = 0$$

$$\Rightarrow \gamma = 3: S = \frac{7}{4} (3 - 2) = 1.75 \approx 2$$

$$\Rightarrow \gamma = 4: S = \frac{7}{4} (4 - 2) = 3.5 \approx 4$$

$$\Rightarrow \gamma = 5: S = \frac{7}{4} (5 - 2) = 5.25 \approx 5$$

$$\Rightarrow \gamma = 6: S = \frac{7}{4} (6 - 2) = 7$$

- Here, are all the slope value at different range.

5) Explain Arithmetic Mean Filter with example.

Ans - An arithmetic mean filter operation on an image removes short tailed noise such as uniform and gaussian type noise from the image at the cost of blurring the image.

- It is defined as the average of all pixels within a local region of an image.
- It is defined as:

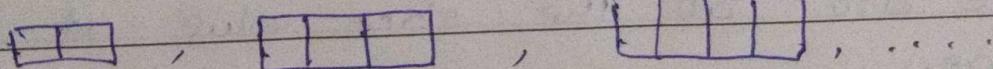
$$\bar{x} = \frac{1}{n} (x_1 + \dots + x_n)$$

- Pixels that are included in the averaging operation are specified by a mask.

- The larger the filtering mask becomes the more predominant the ~~but~~ blurring becomes and less high spatial frequency detail that remains in the image.

• Example: 3, 9, 4, 52, 3, 8, 6, 2, 2, 9

Step 1 1st take windowing size,
we can take any size for windowing



Step 2

Normal: 3, 9, 4, 52, 3, 8, 6, 2, 2, 9

○ Padding: [0|3|9] [3|9|4] [9|4|52] ... [2|9|0]

- Replication:

3	3	9
---	---	---

3	9	4
---	---	---

 ...

2	9	9
---	---	---
- Trimming:

3	9	4
---	---	---

9	4	52
---	---	----

 ...

2	2	9
---	---	---

- There are different kinds mean filters all of which exhibit slightly different behaviour:

- ↳ Geometric Mean
- ↳ Harmonic Mean
- ↳ Contraharmonic Mean

6) Explain an Order Statistics Filters with example.

- Spatial filters that are based on ordering the pixel values that make up the neighbourhood operated on by the filter

- Useful spatial filters include,
 - Median filter
 - Max and Min filter
 - Midpoint filter
 - Alpha trimmed mean filter

- Median Filter

$$\hat{f}(x, y) = \text{median}_{(s, t) \in S_{xy}} \{g(s, t)\}$$

- Excellent at noise removal, without the smoothing effects that can occur with

other smoothing filters.
Particularly good when salt and pepper noise is present.

Example $\hat{f}(x,y) = \text{median}(\text{ges}, 3)$
 $3, 9, 4, 52, 3, 8, 6, 2, 2, 9$

(i) Replication:-

$$\boxed{3 \ 3 \ 9} = 3$$

$$\boxed{3 \ 9 \ 4} \rightarrow \boxed{3 \ 4 \ 9} = 4$$

$$\boxed{9 \ 4 \ 52} \rightarrow \boxed{4 \ 9 \ 52} = 9$$

$$\boxed{4 \ 52 \ 3} \rightarrow \boxed{3 \ 4 \ 52} = 4$$

$$\boxed{52 \ 3 \ 8} \rightarrow \boxed{3 \ 8 \ 52} = 8$$

$$\boxed{3 \ 8 \ 6} \rightarrow \boxed{3 \ 6 \ 8} = 6$$

$$\boxed{8 \ 6 \ 2} \rightarrow \boxed{2 \ 6 \ 8} = 6$$

$$\boxed{6 \ 2 \ 2} \rightarrow \boxed{2 \ 2 \ 6} = 2$$

$$\boxed{2 \ 2 \ 9} \rightarrow \boxed{2 \ 2 \ 9} = 2$$

$$\boxed{2 \ 9 \ 9} = 9$$

$$\boxed{3 \ 4 \ 9 \ 4 \ 8 \ 6 \ 6 \ 2 \ 2 \ 9}$$

(ii) Padding:

$$\boxed{0 \ 3 \ 9} = 3$$

$$\boxed{2 \ 9 \ 0} \rightarrow \boxed{0 \ 2 \ 9} = 2$$

$$\boxed{3 \ 4 \ 9 \ 4 \ 8 \ 6 \ 6 \ 2 \ 2 \ 2}$$

(iii) Trimming

↳ without effect boundary value

$$\boxed{3 \ 4 \ 9 \ 4 \ 8 \ 6 \ 6 \ 2 \ 2 \ 9}$$

- Max and Min Filter

↳ Max Filter

$$\hat{f}(x, y) = \max_{(s, t) \in S_{xy}} \{g(s, t)\}$$

↳ Min Filter

$$\hat{f}(x, y) = \min_{(s, t) \in S_{xy}} \{g(s, t)\}$$

- Max filter is good for pepper noise and min is good for salt noise.

Example: 3, 9, 5, 52, 8, 6, 2, 2, 9

(i) Replication

	max	min	mid
[3 3 9]	= 4	3	$3.5 \approx 5$
[3 9 4]	= 9	3	6
[9 5 52]	= 52	5	28
[5 52 3]	= 52	3	$27.5 \approx 28$
[52 3 8]	= 52	3	≈ 28
[3 8 1 8]	= 8	8	≈ 6
[8 6 2]	= 8	2	≈ 5
[6 2 2]	= 6	2	≈ 6
[2 2 9]	= 9	2	≈ 6
[2 9 9]	= 9	2	≈ 6

max : [4 9 52 52 52 8 8 6 9 9]

min : [3 3 4 3 3 3 2 2 2 2]

(ii) Trimming :

$$[3 3 9] = 3 \quad 3 = 3$$

$$[2 2 9] = 9 \quad 9 = 9$$

max : [3 9 52 52 52 8 8 6 9 3]
min : [3 3 4 3 3 3 2 2 2 9]

(iii) Padding: [0 3 9] = 9 0 = 5

$$[2 9 0] = 9 \quad 0 = 5$$

max : [9 9 52 52 52 8 8 6 9 3 9]

min : [0 3 4 3 3 3 2 2 2 0]

- Midpoint Filter

$$\hat{f}(x, y) = \frac{1}{2} \left[\max_{(s, t) \in S_{xy}} \{g(s, t)\} + \min_{(s, t) \in S_{xy}} \{g(s, t)\} \right]$$

Good for random Gaussian and uniform noise.

(i) Replication:

$$\text{midpoint} = [5 | 6 | 28 | 28 | 28 | 6 | 5 | 6 | 6 | 6]$$

(ii) Trimming:

$$\text{midpoint} = [3 | 6 | 28 | 28 | 28 | 6 | 5 | 6 | 6 | 9]$$

(iii) Padding:

$$\text{midpoint} = [5 | 6 | 28 | 28 | 28 | 6 | 5 | 6 | 6 | 5]$$

- Alpha - Trimmed Mean Filter

$$\hat{f}(x, y) = \frac{1}{mn-d} \sum_{(s, t) \in S_{xy}} g_x(s, t)$$

- We can delete the $d/2$ lowest and $d/2$ highest grey levels.
- So $g_x(s, t)$ represents the remaining $mn - d$ pixels

7) Explain Discrete Fourier Transform (DFT).

- The DFT is one of the most popular tools in digital signal processing which enables us to find the spectrum of a finite-duration signal.
- There are many circumstances in which we need to determine the frequency content of a time-domain signal.
- For example, we may have to analyze the spectrum of the output of an LC oscillator to see how much noise is present in the produced sine wave.
- The DFT of $f(x,y)$ for $x=0,1,2,\dots,M-1$ and $y=0,1,2,\dots,N-1$, denoted by $F(u,v)$ is given by the equation

$$F(u,v) = \sum_{x=0}^{M-1} \sum_{y=0}^{N-1} f(x,y) e^{-j2\pi ux/M + vy/N}$$

for $u=0,1,2,\dots,M-1$ and $v=0,1,2,\dots,N-1$

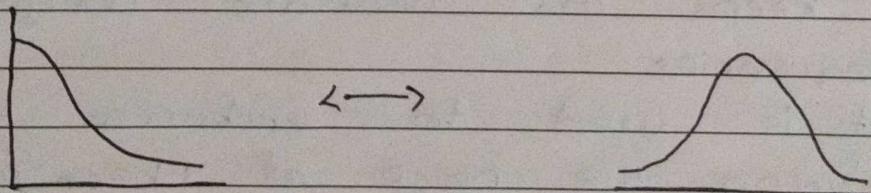
- The DFT of a two dimensional image can be visualised by showing the spectrum of the image component frequencies.
- Inverse DFT :- It is really important to note that the Fourier transform is completely reversible

$$f(x,y) = \frac{1}{MN} \sum_{u=0}^{M-1} \sum_{v=0}^{N-1} F(u,v) e^{j2\pi(ux/M+vy/N)}$$

Q1 Explain the major Filter Categories.

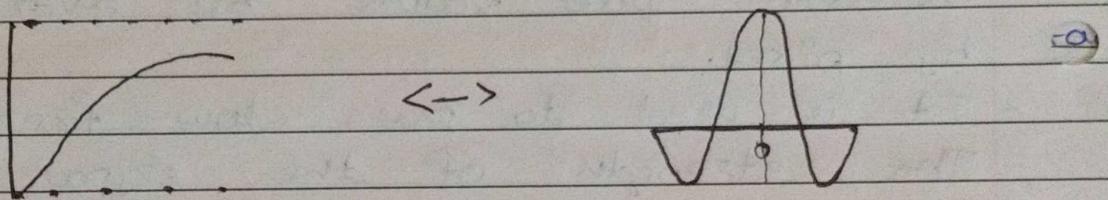
→ Typically, filters are classified by examining their properties in the frequency domain.

- **Low-Pass**: A low-pass filter is the basis for most smoothing methods. An image is smoothed by decreasing the disparity between pixel values by averaging near by pixel.
 - It is used to pass low-frequency signals
 - The strength of the signal is reduced & frequencies which are passed is higher than the cutoff frequency.
 - The amount of strength reduced for each frequency depends on the design of the filters.
 - Smoothing is low pass operation in the frequency domain.
 - Preserve low frequencies, useful for noise suppression.

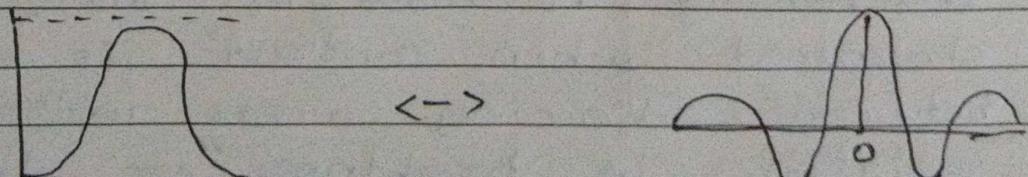


- **High-Pass**: It is the basis for most sharpening methods. An image is sharpened when contrast is enhanced between adjoining areas with little variation in brightness or darkness.

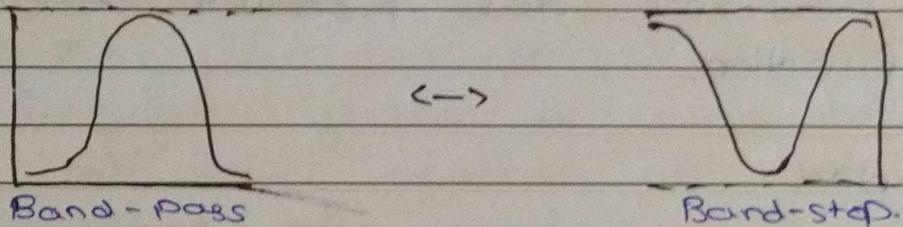
- Sharpening is a highpass operation in the frequency domain.
- It also has standard forms such as Ideal highpass filter, Butterworth highpass filter, Gaussian highpass filter,
- Preserves high frequencies - useful for edge detection.



- Band-Pass Filter: It is a device that passes frequencies within a certain range & rejects (alters) frequencies outside that range.
- It is useful when the general location of the noise in the frequency domain is known.
- It removes the very low frequency & the very high frequency components that means it keeps the moderate range band of frequencies.
- It is used to enhances edges while reducing the noise at the same time.
- Preserves frequencies within a certain band.



- Band-Stop Filters: It is also known as band rejection filters.
- It is a filter that passes most frequencies unaltered, but attenuates those in a specific range to very low levels.
- It is the opposite of a band-pass filter.
- A notch filter is a band-stop filter with a narrow stopband (high Q factors).
- It is useful when the general location of the noise in the frequency domain is known.



- A band reject filter blocks frequencies within the chosen range & lets frequencies outside of the range pass through.
- Q. Discuss the filtering correlation and filtering convolution.
- Filtering Correlation: It is a process of moving a filter mask often referred to as kernel over the image & computing the sum of products at each location.
- Correlation is the function of displacement of filter.
- In other words, the first value of the

correlation corresponds to zero displacements of the filter, the second value corresponds to one unit of displacement & so on

- The equation of correlation is defined as follows.

$$g(x, y) = \sum_{s=a}^a \sum_{t=b}^b w(s, t) f(x+s, y+t)$$

$$g = w \cdot f$$

- It performs dot product between weights & function.

- Example:

original	value	output
2 2 2 3	1 -1 -1	5 10 10 15
2 1 3 3	1 2 -1	3 4 6 11
2 2 1 2	1 1 1	7 11 4 9
1 3 2 2	Mask	-5 4 4 5

- The correlation operation in 2D is very straight forward. This also helps us achieve two very popular properties.

1) Translational Invariance
2) Locality

- It has a limitation or characteristic property

that when it is applied on a discrete unit impulse, yields a result that is a copy of the filters but ~~is not~~ related by an angle of 180 degrees.

- **Filtering Convolution**: It is very similar to the correlation operation but has a slight difference.
 - In convolution operation, the kernel is first flipped by an angle of 180 degrees & is then applied to the image.
 - The fundamental property of convolution is that convolving a kernel with a discrete unit impulse yields a copy of the kernel at the location of the impulse.
 - The equation of convolution is defined as follows:

$$g(x, y) = \sum_{s=-a}^b \sum_{t=-b}^b w(s, t) f(x-s, y-t)$$

$$g = w * f$$

- It performs cross product between weight & function.

- Example :-

1	-1	-1
1	2	-1
1	1	1

convolution kernel

w

Rotate
180°

1	1	1
-1	2	1
-1	-1	1

(Mask)

2	2	2	3
2	1	3	3
2	2	1	2
1	3	2	2

original

5	4	3	-2
9	6	14	5
11	7	6	5
9	12	8	5

output Image

Step=1

$$\begin{aligned}
 & 2(2) + 2(1) + (-2) + 1 \\
 & = 4 + 2 - 2 + 1 \\
 & = \boxed{5}
 \end{aligned}$$

- The same proportion of Translational Invariance & Locality are followed by convolution operation as well.