

# CSCI 516 - Fundamental Concepts in Computing and Machine Organization

## Homework Assignment 4

Due on 11/08/2022 (Tuesday), 11:55PM

### Requirement

- You need to do your assignment independently.
- You need to submit ".pdf" file which contains your solutions to D2L

### Questions

Perform each of the following computation using IEEE-754 single precision and IEEE-754 double precision representation. Clearly show all the steps.

[Method: Convert each of the decimal values to IEEE-754 single precision representation. Perform IEEE-754 computation (addition or multiplication) and convert the IEEE-754 single precision result back to decimal value. Repeat the above method for each computation using IEEE-754 double precision representation].

1.  $-2.25 + 15 =$

2.  $-7.5 * 3.25 =$

1.  $-2.25 + 15 = 12.75$

Convert 2.25 to binary.

$$(2)_{10} = (10)_2$$

$$(.25)_{10} = .25 \times 2 = 0.5 \rightarrow 0$$
$$\quad \quad \quad \downarrow$$
$$\quad \quad \quad \rightarrow 0.5 \times 2 = 1$$

$$2.25 = (10.01)_2$$

$$(15)_{10} = (1111)_2$$

IEEE - 754 format:

Sign	Exponent	Mantissa
1bit	8 bits	23 bits

-2.25

number is negative Sign = 1

$(10.01)_2$  is  $\underbrace{1.001}_{\text{Mantissa}} \times 2^1 \rightarrow \text{exponent}$

IEEE exponent = Exponent + Bias

IEEE exponent =  $1 + 127 = 128 = (10000000)_2$

IEEE-754 format:

1	1000 0000	001 0000 0000 0000 0000 0000
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15

number is positive Sign = 0

$(1111.0)$  is  $\underbrace{1.111}_{\text{Mantissa}} \times 2^3 \rightarrow \text{Exponent}$

IEEE exponent =  $3 + 127 = 130 = (10000010)_2$

IEEE-754 format:

0	1000 0010	111 0000 0000 0000 0000 0000
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15 - 2.25

$$2^3 > 2^1$$

$$15: 1.111\ 0000\ 0000\ 0000\ 0000\ 0000 \times 2^3$$

$$-2.25: -0.010\ 0100\ 0000\ 0000\ 0000\ 0000 \times 2^3$$

$$1.111\ 0000\ 0000\ 0000\ 0000\ 0000 \times 2^3$$

$$1.101\ 1100\ 0000\ 0000\ 0000\ 0000 \times 2^3$$

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$$1.100\ 1100\ 0000\ 0000\ 0000\ 0000 \times 2^3$$

## IEEE - 754 format

0	1000 0010	10001100 0000 0000 0000 0000
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$$2. -7.5 \times 3.25 = -24.375$$

IEEE - 754 single precision:

$$-1.1110000\ 0000\ 0000\ 0000 \times 2^2 = -7.5$$

$$+1.1010000\ 0000\ 0000\ 0000 \times 2^1 = 3.25$$

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$$-11.0000110000\ 0000\ 0000\ 0000 \times 2^3$$

$$-1.1000011000000000\ 0000\ 0000 \times 2^4$$

$$= -24.375$$

IEEE - 754 double precision:

$$-1.1110000000\ 0000\ 0000\ 0000 \times 2^2 = -7.5$$

$$+1.1010000000\ 0000\ 0000\ 0000 \times 2^1 = 3.25$$

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$$-11.0001100000\ 0000\ 0000\ 0000 \times 2^3$$

$$-1.100001100000\ 0000\ 0000\ 0000 \times 2^4$$

$$= -24.375$$