

Assignment No. 6: Multi-way Trees

Transforms between different representations

Allocated time: 2 hours

Implementation

The correct and efficient implementation of linear complexity algorithms is required for transforming multi-way trees between the following representations:

R1: *Parent representation:* for each index, the value in the vector represents the parent's index, e.g.: $\Pi = \{2, 7, 5, 2, 7, 7, -1, 5, 2\}$

R2: *Multi-way tree representation:* each node contains the key and a vector of child nodes.

R3: *Binary representation:* each node contains the key and two pointers, one to the first child and the second to the right sibling (e.g., the next sibling).

Therefore, you need to define transformation **T1** from the parent representation (**R1**) to the multi-way tree representation (**R2**), and then the transformation **T2** from the multi-way tree representation (**R2**) to the binary representation (**R3**). For all representations (**R1**, **R2**, **R3**), you need to implement the Pretty Print (**PP**) display (see page 2).

Define the data structures. You can use intermediate structures (e.g., additional memory).

Requirements

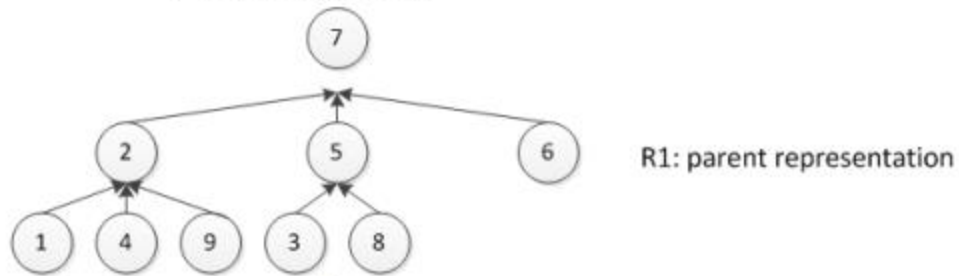
1. **Pretty-print for R1 (5p)**
2. **Correct implementation for T1 and pretty-print for R2 (1p) + T1 in linear time (1p)**
3. **Correct implementation for T2 and pretty-print for R3 (2p) + T2 in linear time (1p)**

The correctness of the algorithms should be demonstrated using the example from **R1** (Π). Use Pretty Print for all three representations.

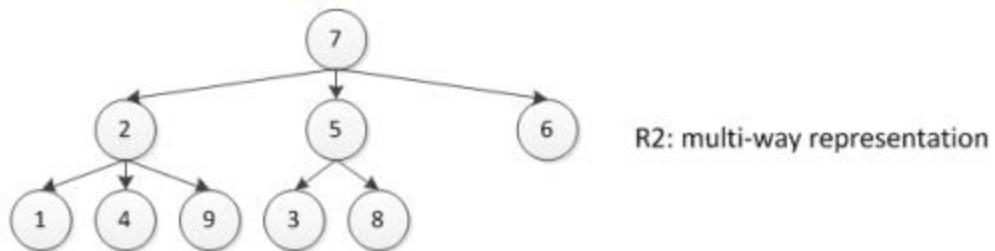
Explain the data structures you used for representations **R2** and **R3**.

Analyse the time and space efficiency of the two transformations. Did you achieve $O(n)$? Did you use additional memory?

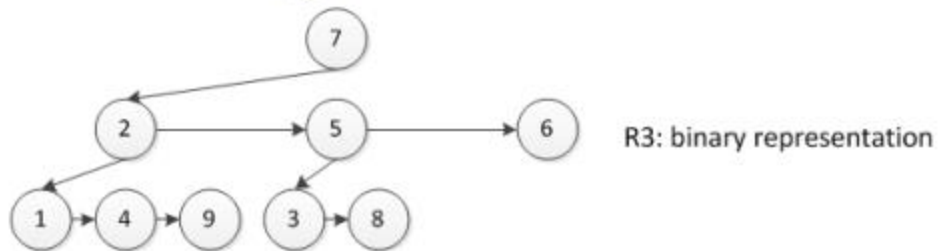
Input (R1): $\Pi = \{2, 7, 5, 2, 7, 7, -1, 5, 2\}$
 1 2 3 4 5 6 7 8 9



$T1: \text{parent} \rightarrow \text{multi-way}$



$T2: \text{multi-way} \rightarrow \text{binary}$



$PP: \text{pretty_print}(\text{binary})$

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7
 2
   1
   4
   9
 5
   3
   8
 6
  
```

Pretty print