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Space and time efficient Binomial Coefficient

Write a function that takes two parameters n and k and returns the value of Binomial Coefficient C(n, k). For example, your function should return 6 for n = 4 and k = 2, and it should return 10 for n = 5 and k = 2.

We have discussed a $O(n^*k)$ time and O(k) extra space algorithm in this post. The value of C(n, k) can be calculated in O(k) time and O(1) extra space.

```
C(n, k) = n! / (n-k)! * k!
= [n * (n-1) * .... * 1] / [ ( (n-k) * (n-k-1) * .... * 1) * ( k * (k-1) * .... * 1 ) ]
After simplifying, we get
C(n, k) = [n * (n-1) * .... * (n-k+1)] / [k * (k-1) * .... * 1]
Also, C(n, k) = C(n, n-k) // we can change r to n-r if r > n-r
```

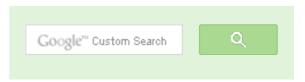
Following implementation uses above formula to calculate C(n, k)

```
// Program to calculate C(n ,k)
#include <stdio.h>

// Returns value of Binomial Coefficient C(n, k)
int binomialCoeff(int n, int k)
{
   int res = 1;

      // Since C(n, k) = C(n, n-k)
      if ( k > n - k )
        k = n - k;

      // Calculate value of [n * (n-1) *---* (n-k+1)] / [k * (k-1) *----
```





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```
for (int i = 0; i < k; ++i)
        res *= (n - i);
        res /= (i + 1);
    return res;
/* Drier program to test above function*/
int main()
    int n = 8, k = 2;
    printf ("Value of C(%d, %d) is %d ", n, k, binomialCoeff(n, k) );
    return 0;
Value of C(8, 2) is 28
```

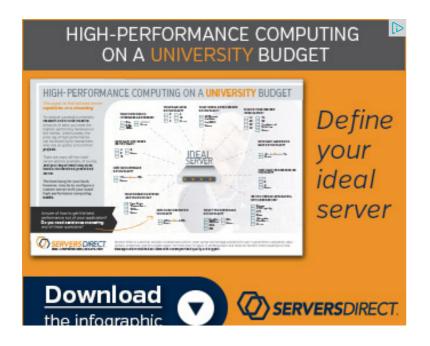
Time Complexity: O(k) Auxiliary Space: O(1)

This article is compiled by Aashish Barnwal and reviewed by GeeksforGeeks team. Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above.



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Alok Kumar • a month ago

Good to know, but not practical. In most of the cases overflow is certain.





K.kaushik • 11 months ago

The above program gives negative result for 100 C 15 or 100 C 18 or 100 C 19 C 20 or 100 C 25. Why this strange behaviour?

/* Paste your code here (You may **delete** these lines **if not** writing co







GeeksforGeeks → K.kaushik • 11 months ago

The reason for negative values seems to be integer overflow. The proc



geekguy → GeeksforGeeks · 11 months ago
Use Java's BigInteger!:)

Easiest Solution!

^ ~ ·



Aashish → K.kaushik • 11 months ago

This is because 100 C 15 > 100 C 25. The former shows the negative Please do some paper work.

^ V ·



Anuj Siroi → Aashish • 11 months ago

How is 100 C 15 > 100 C 25 ?? If so then

100 C 15 > 100 C 25

=> 100! / 15! * 85! > 100! /25! * 75!

=> 15! * 85! < 25! * 75!

=> 85 * 84 * * 76 < 25 * 24 * * 16

Is it possible ????



K.kaushik → Aashish • 11 months ago

yes obviously 10 C 15 < 10 C 25. So 10 C 25 may show negati 15 is showing negative, not 10 C 25. In java iterative implement



Abhi You live US or India?

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kzs please provide solution for the problem...

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 $tree::Root_to_leaf_path_given_sum(tree...$

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GOPI GOPINATH @admin Highlight this sentence "We can easily...

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hour ago

newCoder3006 If the array contains negative numbers also. We...

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ualatype a#uosionga#uos insteau oi a#uosinta#uos. Dut still i positive. Please clear the confusion.

A .



Aashish → K.kaushik • 11 months ago

Apologies. Please see the updated comment.

^ V ·



Swapnil • 2 years ago

Just a small error. You can't define int inside for(). you need to define it before t

/* Paste your code here (You may **delete** these lines **if not** writing $c\iota$



Aashish → Swapnil • 2 years ago

According to c-99 standard, you can define a variable inside loops also Check here: https://ideone.com/pOWZM

A | V .



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