

Dynamic Programming | Set 21 (Variations of LIS)

We have discussed Dynamic Programming solution for Longest Increasing Subsequence problem in [this](#) post and a $O(n\log n)$ solution in [this](#) post. Following are commonly asked variations of the standard [LIS problem](#).

1. Building Bridges: Consider a 2-D map with a horizontal river passing through its center. There are n cities on the southern bank with x -coordinates $a(1) \dots a(n)$ and n cities on the northern bank with x -coordinates $b(1) \dots b(n)$. You want to connect as many north-south pairs of cities as possible with bridges such that no two bridges cross. When connecting cities, you can only connect city i on the northern bank to city i on the southern bank.

```

8      1      4      3      5      2      6      7
<---- Cities on the other bank of river---->
-----
<----- River----->
-----
1      2      3      4      5      6      7      8
<----- Cities on one bank of river----->
```

Source: [Dynamic Programming Practice Problems](#). The link also has well explained solution for the problem.

2. Maximum Sum Increasing Subsequence: Given an array of n positive integers. Write a program to find the maximum sum subsequence of the given array such that the integers in the subsequence are sorted in increasing order. For example, if input is $\{1, 101, 2, 3, 100, 4, 5\}$, then output should be $\{1, 2, 3, 100\}$. The solution to this problem has been published [here](#).

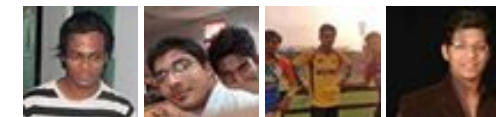
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3. The Longest Chain You are given pairs of numbers. In a pair, the first number is smaller with respect to the second number. Suppose you have two sets (a, b) and (c, d), the second set can follow the first set if $b < c$. So you can form a long chain in the similar fashion. Find the longest chain which can be formed. The solution to this problem has been published [here](#).

4. Box Stacking You are given a set of n types of rectangular 3-D boxes, where the i^{th} box has height $h(i)$, width $w(i)$ and depth $d(i)$ (all real numbers). You want to create a stack of boxes which is as tall as possible, but you can only stack a box on top of another box if the dimensions of the 2-D base of the lower box are each strictly larger than those of the 2-D base of the higher box. Of course, you can rotate a box so that any side functions as its base. It is also allowable to use multiple instances of the same type of box.

Source: [Dynamic Programming Practice Problems](#). The link also has well explained solution for the problem.

Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above.

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GeeksforGeeks

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triveni • 9 days ago

i need to know program for num of nodes,connectivity,deletion of node.(the nu
for ex:the tree having 4 node after delet the num of node should be same)

^ | v .



xxmajia • 5 months ago

THANKS a lot

^ | v .



Mandeep • a year ago

[sourcecode language="java"]

```

/*
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 * and open the template in the editor.
 */
package DynaProg;

/**
 *
 * @author Pardeep
 */
public class buildingbridge {
    public static void main(String ar[]){

        int cr[]={8,1,4,3,5,2,6,7};
        int oth[]={1,2,3,4,5,6,7,8};
        int othpos[]=new int[cr.length];
        for(int i=0;i<oth.length;i++) //find the occurence of oth[] element in cr[]
        {

```

[see more](#)

^

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▼

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GeeksforGeeks · 2 years ago

@Deep & @kalyan: The Box Stacking problem is also a variation of LIS proble
maximum height stack.

1) We sort the boxes according to their increasing base areas (only a smaller
another box).

2) After sortina the boxes. the problem is same as LIS.

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By not sorting the boxes, the problem is same as LRS.

$H(i)$ = Maximum possible stack height with box i at top of stack

$H(i) = \{ \text{Max} (H(j)) + \text{height}(i) \}$ where $j < i$. If there is no such j then $H(i) = \text{height}(i)$

To get overall maximum height, we need to return $\text{max}(H(i))$ where $0 < i < n$

AdChoices 

[► Variations](#)

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We will soon publish it as a separate post.

^ | v .



kalyan · 2 years ago

can u explain the box stacking problem pls ..

^ | v .



deep · 2 years ago

on the given link i am not getting The Box Stacking problem. can anyone explain

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