

Total number of possible Binary Search Trees with n keys

Total number of possible Binary Search Trees with n different keys = Catalan number $C_n = \frac{(2n)!}{(n+1)!n!}$

See references for proof and examples.

References:

http://en.wikipedia.org/wiki/Catalan_number



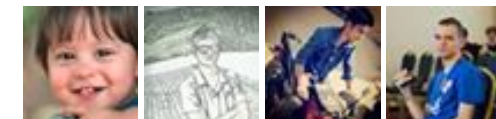
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atiq • 6 months ago

No. of Binary trees(it can be structurally similar and different) out of N nodes is

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Tao → atiq • 7 days ago

I agree. Catalan(N) is the number of binary trees built from the array[1..N]. Each permuted array can build Catalan(N) binary trees. Thus, the total

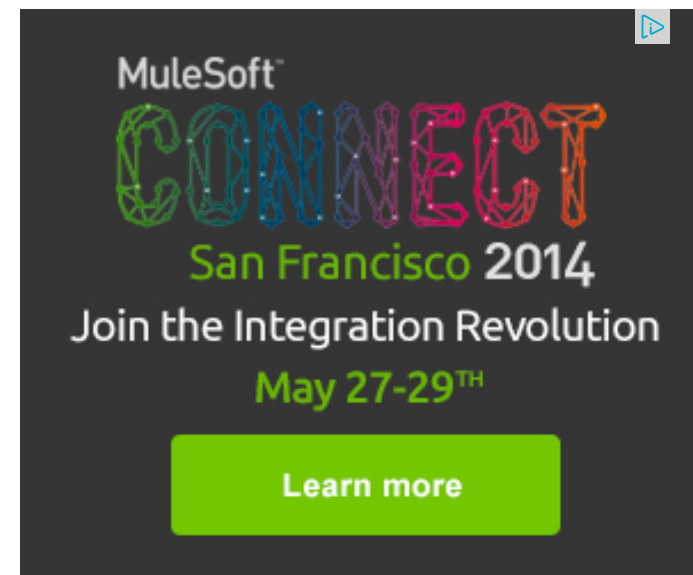
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Pawan Kumar • 9 months ago

I think catalan no. C_n is total no of possible binary tree with n nodes. but in case of binary search tree total no. of possible bst(s) follows the recursive formula $T(n) = \sum_{i=0}^{n-1} T(i) * T(n-i-1)$

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$$t(n) = \sum_{i=1}^n t(i-1) t(n-i)$$
 sum over $i=1$ to n .

correct me if I m wrong.

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Kong • 9 months ago

It should be $(2n)!/((n+1)!*n!)$ because above expression will evaluate to $((2n)!/$

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GeeksforGeeks • 10 months ago

@All:

The above fact is correct. The number of possible Binary Search Trees with n

Number of structurally different binary trees is also a catalan numbers.

They both are different types of questions, but their result is same.

In first, we are given n different keys and we want to know the number of ways
Let us take few examples.

keys[] = {1, 2, 3}, we can organize them in 5 ways: two trees with 1 as root + 1
root.

Take more examples, and you will see pattern of catalan numbers. See questi

In second, we want to know structurally different trees with n nodes, we are not
For $n = 3$, there can be 5 trees. The expression for this will be same as the ex

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aspire → GeeksforGeeks • 9 months ago

Can you please explain the difference between nodes and keys?

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affizerv Your example has two 4s on row 3, that's why it...

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RVM Can someone please elaborate this Qs from above...

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@meya Working solution for question 2 of 4f2f round....

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sandeep void rearrange(struct node *head) {...

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Neha I think that is what it should return as, in...

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Asap · 10 months ago

I think its binary tree

<http://cs.lmu.edu/~ray/notes/b...>

<http://stackoverflow.com/quest...>

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subhasish · a year ago

It is number if Binary trees not Binary *Search* Trees

1 ^ | v · Reply · Share ›



wgpshashank · a year ago

hi , please update the post that Cn will number of fully binary trees not simple I

```
/* Paste your code here (You may delete these lines if not writing c
```

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geek4u · 4 years ago

What about binary trees? how many binary trees are possible with n nodes?

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veera reddy → [geek4u](#) · 3 years ago

The number of structurally different Binary Trees with n nodes is Catal:

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if we don't consider the structure then total number of possible

(n)

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