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Greedy Algorithms | Set 3 (Huffman Coding)

Huffman coding is a lossless data compression algorithm. The idea is to assign variable-legth codes to input characters, lengths of the assigned codes are based on the frequencies of corresponding characters. The most frequent character gets the smallest code and the least frequent character gets the largest code.

The variable-length codes assigned to input characters are Prefix Codes, means the codes (bit sequences) are assigned in such a way that the code assigned to one character is not prefix of code assigned to any other character. This is how Huffman Coding makes sure that there is no ambiguity when decoding the generated bit stream.

Let us understand prefix codes with a counter example. Let there be four characters a, b, c and d, and their corresponding variable length codes be 00, 01, 0 and 1. This coding leads to ambiguity because code assigned to c is prefix of codes assigned to a and b. If the compressed bit stream is 0001, the de-compressed output may be "cccd" or "ccb" or "acd" or "ab".

See this for applications of Huffman Coding.

There are mainly two major parts in Huffman Coding
1) Build a Huffman Tree from input characters.
2) Traverse the Huffman Tree and assign codes to characters.

Steps to build Huffman Tree
Input is array of unique characters along with their frequency of occurrences and output is Huffman Tree.

1. Create a leaf node for each unique character and build a min heap of all leaf nodes (Min Heap is used as a priority queue. The value of frequency field is used to compare two nodes in min heap. Initially, the least frequent character is at root)

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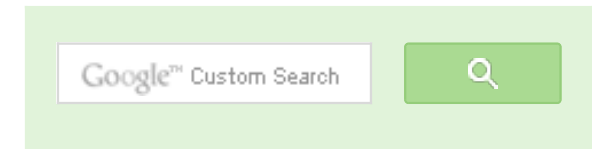
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2. Extract two nodes with the minimum frequency from the min heap.

3. Create a new internal node with frequency equal to the sum of the two nodes frequencies. Make the first extracted node as its left child and the other extracted node as its right child. Add this node to the min heap.

4. Repeat steps#2 and #3 until the heap contains only one node. The remaining node is the root node and the tree is complete.

Let us understand the algorithm with an example:

```
character    Frequency
    a            5
    b            9
    c            12
    d            13
    e            16
    f            45
```

Step 1. Build a min heap that contains 6 nodes where each node represents root of a tree with single node.

Step 2 Extract two minimum frequency nodes from min heap. Add a new internal node with frequency 5 + 9 = 14.
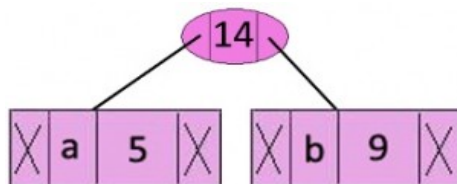
Now min heap contains 5 nodes where 4 nodes are roots of trees with single element each, and one heap node is root of tree with 3 elements

```
character          Frequency
      c                12
      d                13
 Internal Node         14
      e                16
      f                45
```

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Step 3: Extract two minimum frequency nodes from heap. Add a new internal node with frequency 12 + 13 = 25
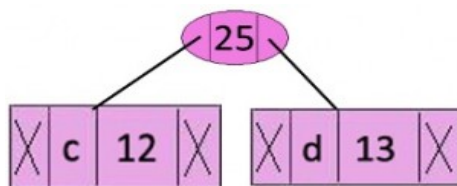
Now min heap contains 4 nodes where 2 nodes are roots of trees with single element each, and two heap nodes are root of tree with more than one nodes.

```
character           Frequency
Internal Node          14
        e              16
Internal Node          25
        f              45
```

Step 4: Extract two minimum frequency nodes. Add a new internal node with frequency 14 + 16 = 30
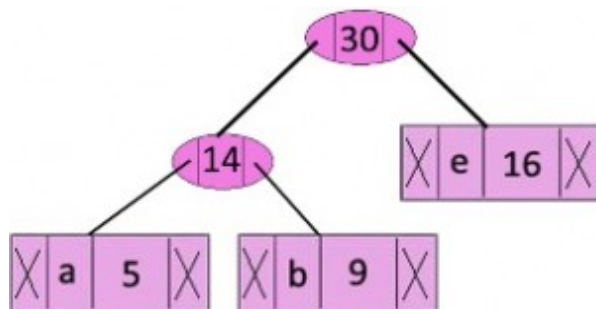
Now min heap contains 3 nodes.

```
character           Frequency
Internal Node          25
Internal Node          30
        f              45
```

Step 5: Extract two minimum frequency nodes. Add a new internal node with frequency 25 + 30 = 55

Now min heap contains 2 nodes.

```
character      Frequency
     f            45
Internal Node    55
```

Step 6: Extract two minimum frequency nodes. Add a new internal node with frequency 45 + 55 = 100
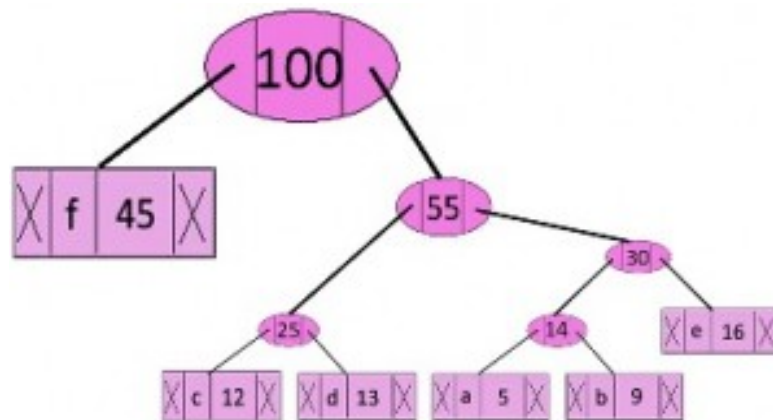
Now min heap contains only one node.

```
character      Frequency
Internal Node    100
```

Since the heap contains only one node, the algorithm stops here.

Steps to print codes from Huffman Tree:
Traverse the tree formed starting from the root. Maintain an auxiliary array. While moving to the left child, write 0 to the array. While moving to the right child, write 1 to the array. Print the array when a leaf node is encountered.
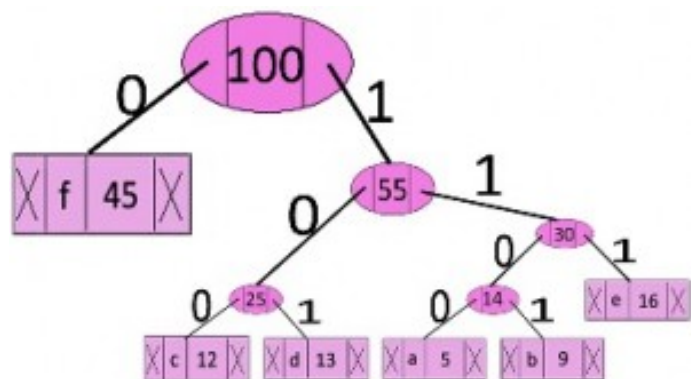
The codes are as follows:

```
character    code-word
    f            0
    c           100
    d           101
    a          1100
    b          1101
    e           111
```

```c
// C program for Huffman Coding
#include <stdio.h>
#include <stdlib.h>

// This constant can be avoided by explicitly calculating height of Hu
#define MAX_TREE_HT 100

// A Huffman tree node
struct MinHeapNode
{
    char data;  // One of the input characters
    unsigned freq;  // Frequency of the character
    struct MinHeapNode *left, *right; // Left and right child of this
};

// A Min Heap:  Collection of min heap (or Hufmman tree) nodes
struct MinHeap
{
    unsigned size;     // Current size of min heap
    unsigned capacity;   // capacity of min heap
    struct MinHeapNode **array;  // Attay of minheap node pointers
};
```

```c
// A utility function allocate a new min heap node with given characte
// and frequency of the character
struct MinHeapNode* newNode(char data, unsigned freq)
{
    struct MinHeapNode* temp =
          (struct MinHeapNode*) malloc(sizeof(struct MinHeapNode));
    temp->left = temp->right = NULL;
    temp->data = data;
    temp->freq = freq;
    return temp;
}

// A utility function to create a min heap of given capacity
struct MinHeap* createMinHeap(unsigned capacity)
{
    struct MinHeap* minHeap =
          (struct MinHeap*) malloc(sizeof(struct MinHeap));
    minHeap->size = 0;  // current size is 0
    minHeap->capacity = capacity;
    minHeap->array =
      (struct MinHeapNode**)malloc(minHeap->capacity * sizeof(struct Mi
    return minHeap;
}

// A utility function to swap two min heap nodes
void swapMinHeapNode(struct MinHeapNode** a, struct MinHeapNode** b)
{
    struct MinHeapNode* t = *a;
    *a = *b;
    *b = t;
}

// The standard minHeapify function.
void minHeapify(struct MinHeap* minHeap, int idx)
{
    int smallest = idx;
    int left = 2 * idx + 1;
    int right = 2 * idx + 2;

    if (left < minHeap->size &&
        minHeap->array[left]->freq < minHeap->array[smallest]->freq)
      smallest = left;

    if (right < minHeap->size &&
        minHeap->array[right]->freq < minHeap->array[smallest]->freq)
      smallest = right;
```

```c
        if (smallest != idx)
        {
            swapMinHeapNode(&minHeap->array[smallest], &minHeap->array[idx
            minHeapify(minHeap, smallest);
        }
}

// A utility function to check if size of heap is 1 or not
int isSizeOne(struct MinHeap* minHeap)
{
    return (minHeap->size == 1);
}

// A standard function to extract minimum value node from heap
struct MinHeapNode* extractMin(struct MinHeap* minHeap)
{
    struct MinHeapNode* temp = minHeap->array[0];
    minHeap->array[0] = minHeap->array[minHeap->size - 1];
    --minHeap->size;
    minHeapify(minHeap, 0);
    return temp;
}

// A utility function to insert a new node to Min Heap
void insertMinHeap(struct MinHeap* minHeap, struct MinHeapNode* minHeap
{
    ++minHeap->size;
    int i = minHeap->size - 1;
    while (i && minHeapNode->freq < minHeap->array[(i - 1)/2]->freq)
    {
        minHeap->array[i] = minHeap->array[(i - 1)/2];
        i = (i - 1)/2;
    }
    minHeap->array[i] = minHeapNode;
}

// A standard funvtion to build min heap
void buildMinHeap(struct MinHeap* minHeap)
{
    int n = minHeap->size - 1;
    int i;
    for (i = (n - 1) / 2; i >= 0; --i)
        minHeapify(minHeap, i);
}

// A utility function to print an array of size n
```

```c
void printArr(int arr[], int n)
{
    int i;
    for (i = 0; i < n; ++i)
        printf("%d", arr[i]);
    printf("\n");
}

// Utility function to check if this node is leaf
int isLeaf(struct MinHeapNode* root)
{
    return !(root->left) && !(root->right) ;
}

// Creates a min heap of capacity equal to size and inserts all charac
// data[] in min heap. Initially size of min heap is equal to capacity
struct MinHeap* createAndBuildMinHeap(char data[], int freq[], int siz
{
    struct MinHeap* minHeap = createMinHeap(size);
    for (int i = 0; i < size; ++i)
        minHeap->array[i] = newNode(data[i], freq[i]);
    minHeap->size = size;
    buildMinHeap(minHeap);
    return minHeap;
}

// The main function that builds Huffman tree
struct MinHeapNode* buildHuffmanTree(char data[], int freq[], int size
{
    struct MinHeapNode *left, *right, *top;

    // Step 1: Create a min heap of capacity equal to size.  Initially
    // modes equal to size.
    struct MinHeap* minHeap = createAndBuildMinHeap(data, freq, size);

    // Iterate while size of heap doesn't become 1
    while (!isSizeOne(minHeap))
    {
        // Step 2: Extract the two minimum freq items from min heap
        left = extractMin(minHeap);
        right = extractMin(minHeap);

        // Step 3:  Create a new internal node with frequency equal to
        // sum of the two nodes frequencies. Make the two extracted no
        // left and right children of this new node. Add this node to
        // '$' is a special value for internal nodes, not used
        top = newNode('$', left->freq + right->freq);
```

```c
            top->left = left;
            top->right = right;
            insertMinHeap(minHeap, top);
    }

    // Step 4: The remaining node is the root node and the tree is com
    return extractMin(minHeap);
}

// Prints huffman codes from the root of Huffman Tree.  It uses arr[]
// store codes
void printCodes(struct MinHeapNode* root, int arr[], int top)
{
    // Assign 0 to left edge and recur
    if (root->left)
    {
        arr[top] = 0;
        printCodes(root->left, arr, top + 1);
    }

    // Assign 1 to right edge and recur
    if (root->right)
    {
        arr[top] = 1;
        printCodes(root->right, arr, top + 1);
    }

    // If this is a leaf node, then it contains one of the input
    // characters, print the character and its code from arr[]
    if (isLeaf(root))
    {
        printf("%c: ", root->data);
        printArr(arr, top);
    }
}

// The main function that builds a Huffman Tree and print codes by tra
// the built Huffman Tree
void HuffmanCodes(char data[], int freq[], int size)
{
    //  Construct Huffman Tree
    struct MinHeapNode* root = buildHuffmanTree(data, freq, size);

    // Print Huffman codes using the Huffman tree built above
    int arr[MAX_TREE_HT], top = 0;
    printCodes(root, arr, top);
}
```

```
// Driver program to test above functions
int main()
{
    char arr[] = {'a', 'b', 'c', 'd', 'e', 'f'};
    int freq[] = {5, 9, 12, 13, 16, 45};
    int size = sizeof(arr)/sizeof(arr[0]);
    HuffmanCodes(arr, freq, size);
    return 0;
}
```

```
f: 0
c: 100
d: 101
a: 1100
b: 1101
e: 111
```

Time complexity: O(nlogn) where n is the number of unique characters. If there are n nodes, extractMin() is called 2*(n – 1) times. extractMin() takes O(logn) time as it calles minHeapify(). So, overall complexity is O(nlogn).

If the input array is sorted, there exists a linear time algorithm. We will soon be discussing in our next post.

Reference:

http://en.wikipedia.org/wiki/Huffman_coding

This article is compiled by Aashish Barnwal and reviewed by GeeksforGeeks team. Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above.

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Thank You Sir,
Your printCodes function in the code helped me complete my project....

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sas · 5 months ago

superb work sir

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vishal · 7 months ago

nice solution

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Ajay · 9 months ago

In swapNodes() function
struct MinHeapNode* t = *a;

should be
struct MinHeapNode t = *a;

⌃ | ⌄ ·

JV · 9 months ago

why is this called as greedy algo.

In practical case do we need to maintain the table with symbol and code for de
huffman tree can be deleted once we get the codes for all the symbols

2 ⌃ | ⌄ ·

its_dark · 10 months ago

how the huffman coding is a grredy algo??

```
/* Paste your code here (You may delete these lines if not writing cc
```

Abhishek Choudhery · 10 months ago

Also could you please explain, how is this GREEDY Algo?
And if we could use DP here?

∧ | ∨ ·

Abhishek Choudhery · 10 months ago

Why have double pointers been used for swapMinHeapNode function?

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srinivas · a year ago

very well explained and coded!

∧ | ∨ ·

a2 · 2 years ago

Awesome !

∧ | ∨ ·

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