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## Dynamic Programming | Set 19 (Word Wrap Problem)

Given a sequence of words, and a limit on the number of characters that can be put in one line (line width). Put line breaks in the given sequence such that the lines are printed neatly. Assume that the length of each word is smaller than the line width.

The word processors like MS Word do task of placing line breaks. The idea is to have balanced lines. In other words, not have few lines with lots of extra spaces and some lines with small amount of extra spaces.

The extra spaces includes spaces put at the end of every line except the last one. The problem is to minimize the following total cost.

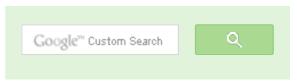
Cost of a line = (Number of extra spaces in the line)^3 Total Cost = Sum of costs for all lines

For example, consider the following string and line width M = 15"Geeks for Geeks presents word wrap problem"

Following is the optimized arrangement of words in 3 lines Geeks for Geeks presents word wrap problem

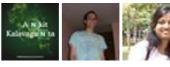
The total extra spaces in line 1, line 2 and line 3 are 0, 2 and 3 respectively. So optimal value of total cost is 0 + 2\*2 + 3\*3 = 13

Please note that the total cost function is not sum of extra spaces, but sum of cubes (or square is also used) of extra spaces. The idea behind this cost function is to balance the spaces among





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lines. For example, consider the following two arrangement of same set of words:

- 1) There are 3 lines. One line has 3 extra spaces and all other lines have 0 extra spaces. Total extra spaces = 3 + 0 + 0 = 3. Total cost = 3\*3\*3 + 0\*0\*0 + 0\*0\*0 = 27.
- 2) There are 3 lines. Each of the 3 lines has one extra space. Total extra spaces = 1 + 1 + 1 = 3. Total cost = 1\*1\*1 + 1\*1\*1 + 1\*1\*1 = 3.

Total extra spaces are 3 in both scenarios, but second arrangement should be preferred because extra spaces are balanced in all three lines. The cost function with cubic sum serves the purpose because the value of total cost in second scenario is less.

### Method 1 (Greedy Solution)

The greedy solution is to place as many words as possible in the first line. Then do the same thing for the second line and so on until all words are placed. This solution gives optimal solution for many cases, but doesn't give optimal solution in all cases. For example, consider the following string "aaa bb cc ddddd" and line width as 6. Greedy method will produce following output.

aaa bb CC ddddd

Extra spaces in the above 3 lines are 0, 4 and 1 respectively. So total cost is 0 + 64 + 1 = 65.

But the above solution is not the best solution. Following arrangement has more balanced spaces. Therefore less value of total cost function.

aaa

bb cc

ddddd

Extra spaces in the above 3 lines are 3, 1 and 1 respectively. So total cost is 27 + 1 + 1 = 29.

Despite being sub-optimal in some cases, the greedy approach is used by many word processors like MS Word and OpenOffice.org Writer.

### Method 2 (Dynamic Programming)

The following Dynamic approach strictly follows the algorithm given in solution of Cormen book.

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First we compute costs of all possible lines in a 2D table Ic[][]. The value Ic[i][j] indicates the cost to put words from i to j in a single line where i and j are indexes of words in the input sequences. If a sequence of words from i to j cannot fit in a single line, then lc[i][j] is considered infinite (to avoid it from being a part of the solution). Once we have the Ic[][] table constructed. we can calculate total cost using following recursive formula. In the following formula, C[j] is the optimized total cost for arranging words from 1 to j.

$$c[j] = \begin{cases} 0 & \text{if } j = 0, \\ \min_{1 \le i \le j} (c[i-1] + lc[i,j]) & \text{if } j > 0. \end{cases}$$

The above recursion has overlapping subproblem property. For example, the solution of subproblem c(2) is used by c(3), C(4) and so on. So Dynamic Programming is used to store the results of subproblems. The array c[] can be computed from left to right, since each value depends only on earlier values.

To print the output, we keep track of what words go on what lines, we can keep a parallel p array that points to where each c value came from. The last line starts at word p[n] and goes through word n. The previous line starts at word p[p[n]] and goes through word p[n] - 1, etc. The function printSolution() uses p[] to print the solution.

In the below program, input is an array I[] that represents lengths of words in a sequence. The value I[i] indicates length of the ith word (i starts from 1) in theinput sequence.

```
// A Dynamic programming solution for Word Wrap Problem
#include <limits.h>
#include <stdio.h>
#define INF INT MAX
// A utility function to print the solution
int printSolution (int p[], int n);
// l[] represents lengths of different words in input sequence. For ex-
// 1[] = {3, 2, 2, 5} is for a sentence like "aaa bb cc ddddd". n is
// l[] and M is line width (maximum no. of characters that can fit in
void solveWordWrap (int l[], int n, int M)
    // For simplicity, 1 extra space is used in all below arrays
    // extras[i][i] will have number of extra spaces if words from i
```







```
// to j are put in a single line
int extras[n+1][n+1];
// lc[i][j] will have cost of a line which has words from
// i to i
int lc[n+1][n+1];
// c[i] will have total cost of optimal arrangement of words
// from 1 to i
int c[n+1];
// p[] is used to print the solution.
int p[n+1];
int i, j;
// calculate extra spaces in a single line. The value extra[i][j]
// indicates extra spaces if words from word number i to j are
// placed in a single line
for (i = 1; i <= n; i++)</pre>
    extras[i][i] = M - l[i-1];
    for (j = i+1; j <= n; j++)
        extras[i][j] = extras[i][j-1] - 1[j-1] - 1;
// Calculate line cost corresponding to the above calculated extra
// spaces. The value lc[i][j] indicates cost of putting words from
// word number i to j in a single line
for (i = 1; i <= n; i++)</pre>
    for (j = i; j <= n; j++)
        if (extras[i][j] < 0)
            lc[i][j] = INF;
        else if (j == n && extras[i][j] >= 0)
            lc[i][i] = 0;
        else
            lc[i][j] = extras[i][j]*extras[i][j];
// Calculate minimum cost and find minimum cost arrangement.
// The value c[j] indicates optimized cost to arrange words
// from word number 1 to j.
c[0] = 0;
for (j = 1; j <= n; j++)
```





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#### AdChoices [>

- Word Wrap
- ▶ Microsoft Word

```
c[j] = INF;
        for (i = 1; i <= j; i++)
            if (c[i-1] != INF && lc[i][j] != INF && (c[i-1] + lc[i][j]
                c[j] = c[i-1] + lc[i][j];
                p[j] = i;
    printSolution(p, n);
int printSolution (int p[], int n)
    int k;
    if (p[n] == 1)
        k = 1;
    else
        k = printSolution (p, p[n]-1) + 1;
    printf ("Line number %d: From word no. %d to %d \n", k, p[n], n);
    return k;
// Driver program to test above functions
int main()
    int 1[] = {3, 2, 2, 5};
    int n = sizeof(l)/sizeof(l[0]);
    int M = 6;
    solveWordWrap (l, n, M);
    return 0;
Output:
Line number 1: From word no. 1 to 1
Line number 2: From word no. 2 to 3
Line number 3: From word no. 4 to 4
```

Time Complexity: O(n^2)

Auxiliary Space: O(n^2) The auxiliary space used in the above program cane be optimized to O(n) (See the reference 2 for details)

AdChoices [>

- Word Text
- Office for Word
- ▶ Word Program

AdChoices [>

- ► Algorithm
- ► Solution Space
- ► Solution Series

#### References:

http://en.wikipedia.org/wiki/Word\_wrap

Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above.

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dave • 3 months ago

your code doesn't work optimally with this test data {1,2,3,1,1} M=6 the ans



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""The last line starts at word p[n] and goes through word n. The previous line s word p[n] - 1, etc."

shouldn't the previous line start at p[p[n]-1], instead of p[p[n]]??

In the example given above,

n=4, p[4]=4 ==> p[p[4]]=4 and the previous line doesn't start at 4th word obvio

Correct me if I am wrong.

**^ \ \ ·** 



raghson • 11 months ago

In the explanation, it is mentioned that the previous line starts from p[p[n]] till pl till p[n]-1.

A .



magnet • 11 months ago

In solveWordwrap function after extras[n+1][n+1] in comment line it should be lc[i][j] instead of extras[i][j]..thnx :)



GeeksforGeeks → magnet • 11 months ago

Thanks for pointing this out. We have updated the comment.

^ V ·



abhishek08aug • 11 months ago

Intelligent:D



**Kumar** • a year ago

In the greedy approach,

We can do some thing like that

- 1> Sort the words based on their length
- 2> run the above mentioned greedy algorithm

for eg: aaa bb cc ddddd

after step 1 ddddd aaa bb cc after step 2 ddddd aaa bb cc

will it work? Let me know your opinion or counter example.

/\* Paste your code here (You may **delete** these lines **if not** writing co



Guest → Kumar • 5 months ago

you can't sort the words dude! it is not allowed...you can't change the s A | V .



pavi → Kumar · a year ago

This will not work because the words are from a paragraph and sorting completely distort the meaning of paragraph.

Please see the question in CLRS for more detail.

Second way of looking at it is: Question says sequence of words. And means "order matters". Hence you cannot sort, 'coz that will break the

Hope this clarifies your doubt :)





Kumar → pavi • a year ago

Thanks Pavi... I didn't realize the basic of Text Editor :D

/\* Paste your code here (You may **delete** these lines  ${\bf if}$ 



aryan • 2 years ago

How would you make sure that the line is also fully(left and right) justified?





kartik → aryan · 2 years ago

I can think of following two step process to justify left and right.

- 1) Run the above given DP algo to balance extra spaces among lines.
- 2) Now for each line equally distribute the extra spaces between words







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