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Dynamic Programming | Set 15 (Longest Bitonic Subsequence)

Given an array arr[0 ... n-1] containing n positive integers, a subsequence of arr[] is called Bitonic if it is first increasing, then decreasing. Write a function that takes an array as argument and returns the length of the longest bitonic subsequence.

A sequence, sorted in increasing order is considered Bitonic with the decreasing part as empty. Similarly, decreasing order sequence is considered Bitonic with the increasing part as empty.

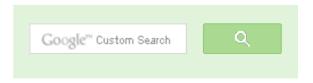
Examples:

```
Input arr[] = \{1, 11, 2, 10, 4, 5, 2, 1\};
Output: 6 (A Longest Bitonic Subsequence of length 6 is 1, 2, 10, 4, 2, 1)
Input arr[] = \{12, 11, 40, 5, 3, 1\}
Output: 5 (A Longest Bitonic Subsequence of length 5 is 12, 11, 5, 3, 1)
Input arr[] = \{80, 60, 30, 40, 20, 10\}
Output: 5 (A Longest Bitonic Subsequence of length 5 is 80, 60, 30, 20, 10)
```

Source: Microsoft Interview Question

Solution

This problem is a variation of standard Longest Increasing Subsequence (LIS) problem. Let the input array be arr[] of length n. We need to construct two arrays lis[] and lds[] using Dynamic Programming solution of LIS problem. lis[i] stores the length of the Longest Increasing subsequence ending with arr[i]. Ids[i] stores the length of the longest Decreasing subsequence starting from arr[i]. Finally, we need to return the max value of lis[i] + lds[i] - 1 where i is from 0





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to n-1.

Following is C++ implementation of the above Dynamic Programming solution.

```
/* Dynamic Programming implementation of longest bitonic subsequence p.
#include<stdio.h>
#include<stdlib.h>
/* lbs() returns the length of the Longest Bitonic Subsequence in
    arr[] of size n. The function mainly creates two temporary arrays
   lis[] and lds[] and returns the maximum lis[i] + lds[i] - 1.
   lis[i] ==> Longest Increasing subsequence ending with arr[i]
   lds[i] ==> Longest decreasing subsequence starting with arr[i]
int lbs( int arr[], int n )
  int i, j;
   /* Allocate memory for LIS[] and initialize LIS values as 1 for
      all indexes */
  int *lis = new int[n];
  for ( i = 0; i < n; i++ )</pre>
      lis[i] = 1;
  /* Compute LIS values from left to right */
  for ( i = 1; i < n; i++ )
     for ( j = 0; j < i; j++ )
         if ( arr[i] > arr[j] && lis[i] < lis[j] + 1)</pre>
            lis[i] = lis[j] + 1;
   /* Allocate memory for lds and initialize LDS values for
      all indexes */
  int *lds = new int [n];
  for ( i = 0; i < n; i++ )
      lds[i] = 1;
   /* Compute LDS values from right to left */
  for (i = n-2; i >= 0; i--)
     for (j = n-1; j > i; j--)
         if ( arr[i] > arr[j] && lds[i] < lds[j] + 1)</pre>
            lds[i] = lds[j] + 1;
  /* Return the maximum value of lis[i] + lds[i] - 1*/
  int max = lis[0] + lds[0] - 1;
  for (i = 1; i < n; i++)
```



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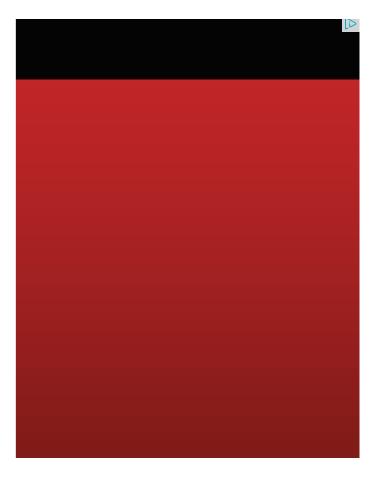
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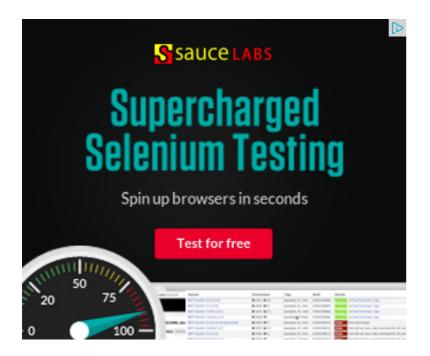
```
if (lis[i] + lds[i] - 1 > max)
         max = lis[i] + lds[i] - 1;
   return max;
/* Driver program to test above function */
int main()
  int arr[] = {0, 8, 4, 12, 2, 10, 6, 14, 1, 9, 5, 13, 3, 11, 7, 15};
  int n = sizeof(arr)/sizeof(arr[0]);
  printf("Length of LBS is %d\n", lbs( arr, n ) );
  getchar();
  return 0;
Output:
```

Length of LBS is 7

Time Complexity: O(n^2) Auxiliary Space: O(n)

Please write comments if you find anything incorrect, or you want to share more information about the topic discussed above





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Siddharth Rajpal • 10 months ago

Hello, This is an O(n) solution:

For example we're given an array and we need to find the longest bitonic of O(n):

Array[n] -> original array, Answer[n]-> The bitonic sequence including that eler

- 1. set answer[0]=1; answer[1]=2;.
- 2. For all elements from i=2 to n-1 do.
- a) if (array[i-1]>array[i-2]) then answer[i]=answer[i-1]+1; (because it is an incre obviously be a part of that bitonic solution.
- b) else if (array[i]<array[i-1]) then answer[i]=answer[i-1]+1; (because it is an de will obviously be a part of that bitonic solution if it less than the previous eleme
- c) else answer[i]=2; because only the previous element and the current eleme

Now traverse the answer[] to find the max value and that will be your answer.



Ujjwal • 10 months ago

```
For the example :-
arr = \{ 3, 1, 2, 4, 7, 8, 6 \}
longest sequence should be 6 (1,2,4,7,8,6)
But above algo gives maximum length as 5..!!
How did this happen.??
```

namit maheshwari • 10 months ago

hour ago

newCoder3006 If the array contains negative numbers also. We...

Find subarray with given sum · 1 hour ago

newCoder3006 Code without using while loop. We can do it...

Find subarray with given sum · 1 hour ago

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```
public static void main(String args[]){
      int i,j;
       int max[] = new int[a.length];
       max[0] = 1;
       boolean inc[] = new boolean[a.length];
       inc[0] = true;
       for(i=0;i<a.length;i++){</pre>
             for(j=0;j<i;j++){
                     if(((inc[j] && a[i]>a[j])||(!inc[j] &
                            max[i] = max[j]+1;
                            inc[i] = inc[j];
                     else if(inc[j] && a[i]<a[j] && max[i]
                            inc[i] = false;
```

see more





Kapil → namit maheshwari • 10 months ago

You can save the O(n) space for array by using inc and dec

```
/* Paste your code here (You may delete these lines if not wri
*/
#include<stdio.h>
#include<stdlib.h>
#include<iostream>
#include<limits.h>
using namespace std;
```

```
#define n 6
int main(void)
        int A[n]={80,60,30,40,20,10};
        int i, j, maxi=INT_MIN, dec, inc, L[n];
        for(i=0;i<n;i++)
        L[i]=1;
```

see more





AMIT • 11 months ago

why din't you use nlogn LIS to make it o(nlogn)???

A .



xxmajia → AMIT · 3 months ago

because the BFS way to archive nlogn may not end with the A[i] eleme **^ V** •



GeeksforGeeks • a year ago

A sequence, sorted in increasing order is considered Bitonic with the decreasing decreasing order sequence is considered Bitonic with the increasing part as e

1 ^ | ~ .



Karry Rawani • a year ago

What if all elements of the array are in increasing order only

A .



Nikhil Gupta • a year ago

In this Method you don't need to traverse the sequence two times

current phase of bitonic sequence i.e. whether it's still increasing or it is now ir

```
/* Paste your code here (You may delete these lines if not writing co
#include<stdio.h>
#include<iostream>
#include<vector>
#define F first
#define S second
using namespace std;
vector<pair<int,int> >dp;
int arr[100];
int main()
{
```

see more



Nikhil Gupta • a year ago

In this Method you don't need to traverse the sequence two times We are storing two things in dp... first is the length of the bitonic sequence end current phase of bitonic sequence i.e. whether it's still increasing or it is now ir

#include #include #include #define F first #define S second using namespace std;

```
vector<pair >qp;
int arr[100];
int main()
int i,j,n;
int max=0;
cin>>n;
see more
A .
```



rajat rastogi • a year ago

This should be solved in O(nlogn) time now it is question which is combination and longest decreasing subsequence.

A | V .



algobard • 2 years ago

Just a minor edit - you guys haven't freed lis and lds before returning max.

A | V .



Akash ⋅ 2 years ago

No need to allocate separate memory for both lis and lds. We could manage in issues.

```
int longestBitonic(int a[], int size) {
       int dp[size], i, j, max = 1;
      dp[0] = 1;
       for(i=1;i<size;i++) {</pre>
               dp[i] = 1;
               for(j=i-1;j>=0;j--) {
                       if((dp[i]<dp[j]+1) && a[i]>a[j]) {
                                dp[i] = dp[j]+1;
```

```
if(dp[i]>max) {
                max = dp[i];
dp[size-1] = 1;
```

see more

1 ~ | ~ .



Jagat → Akash • a year ago

On a closer looks, I'm afraid I don't think it works. You'll end up adding which in the following case will fail.

You'll end up finding a mountain range when all you need to find is a hil Expected answer: 3

Your solution: 6 (Erroneous stmt: LBS[1] = LBS[3] + LIS[1] - 1) A .



Jagat → Akash • a year ago **Brilliant!**

^ V ·



Manish ⋅ 2 years ago

I dont think below statements are requirement while computing the LIS and LD case for any index if we get the number which in increasing (from left) or decre the below statements is always true so need to check it again. Am I right?

$$lis[i] < lis[j] + 1$$

$$Ids[i] < Ids[j] + 1$$

lohith • 2 years ago

^ V .

```
public class longestBiotonicSubsequence {
        public static void main(String str[]){
                int array[] = {1, 11, 2, 10, 4, 5, 2, 1};
                 BiotonicObj b =calculateLongest(array, 0, array.length-:
            System.out.println(b.length);
        }
        public static BiotonicObj calculateLongest(int[] array,int state
                 if(start<end){</pre>
                         int i=start;
```

see more



The King • 2 years ago

This can also be solved simply by using longest increasing sub sequence and Store longest_increasing[i] stores values of longest increasing sub sequence Store longest_decreasing[i] stores values of longest decreasing sub sequence Longest bitonic[i]=longest decreasing[i] + longest decreasing[i] then find max in Longest bitonic

A | V .



The King → The King • 2 years ago

Longest bitonic[i]=longest decreasing[i] + longest decreasing[i] -1

Looks like the owner has used the same method:(A | V .



Aseem • 2 years ago

The examples are wrong. In 2nd and 3rd example, Outputs shown are strictly



Aseem → Aseem • 2 years ago

Please take a closer look at the problem statement. Especially the folic "A sequence, sorted in increasing order is considered Bitonic with the decreasing order sequence is considered Bitonic with the increasing p A .



Gang · 2 years ago

LIS has an O(n*log(n)) solution. So I think this one should be solveble in O(n*log(n)) demonstrated in the following code.

```
template<typename citer>
void LIS(citer begin, citer end, function<void (typename citer::value)</pre>
  typedef vector<typename citer::value_type> lut_t;
  lut_t lut;
 for (citer i = begin; i != end; ++i)
    lut_t::iterator p = upper_bound(lut.begin(), lut.end(), *i);
    if (p == lut.end())
```

lut.push_back(*i); else

see more

^ V ·



Ratan • 2 years ago

Does the question says that the sequence first need to increase and then dec presented here does not seems to do so..... correct me if i am wrong.

/* Paste your code here (You may **delete** these lines **if not** writing co



kartik → Ratan • 2 years ago

Please take a closer look at the problem statement and solution. It says increasing, then decreasing. Not vice versa.

A | V .



Duke • 2 years ago simply rocking:)



Venki · 2 years ago

Second loop should start from (n-2), as it saves one extra iteration.

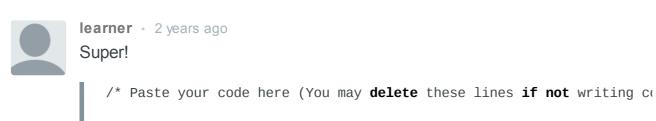
A .



GeeksforGeeks → Venki • 2 years ago

Thanks for suggesting the optimization. We have changed it to start from

A .



^ V ·



rajeev · 2 years ago Awesome:) ^ V ·





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