
**PHILADELPHIA
MIXING
SOLUTIONS**



**MIXING
SOLUTIONS
LIMITED**

The Role of Mixing in Fast, Competitive Chemical Reactions

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FOR PDF OF PRESENTATION.....



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AGENDA

Is mixing important?

CSTR design and operation:

- Assumption of “perfect back mixing”
- By-passing

Chemical reactions:

- Simple vs. competitive
- Mixing issues and reduction of yield on scale-up

Timescales of mixing and reaction:

- Damkohler number

Agitator design for fast, competitive chemical reactions

Examples

Conclusions

IMPORTANCE OF MIXING



Smith, ChERD., 1990:

- US chemical industry loses \$ 10^{10} each year due to poor mixing:
 - 1 % increase in yield $\rightarrow \sim \$ 10^6$
 - One day of down time $\rightarrow \sim \$ 10^6$

Examples:

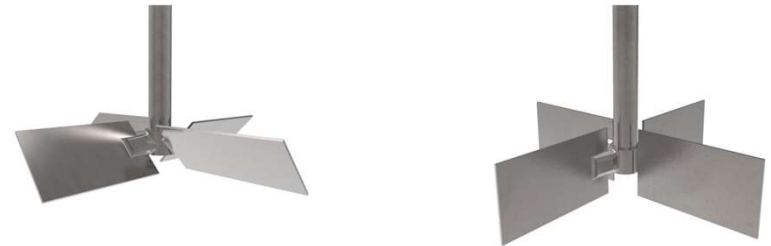
- Lower than expected yields in chemical reactions
- Longer than expected batch / cycle times
- Stagnation, fouling and build-up of solids
- Solids settled on base of vessel
- Poor mass transfer – any multiphase system
- Poor heat transfer
- Others.....?

IMPELLER TYPES

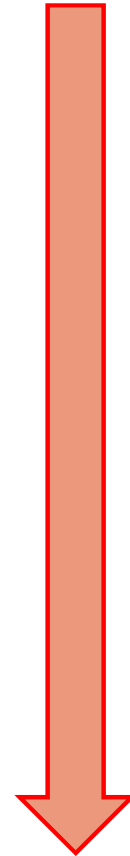
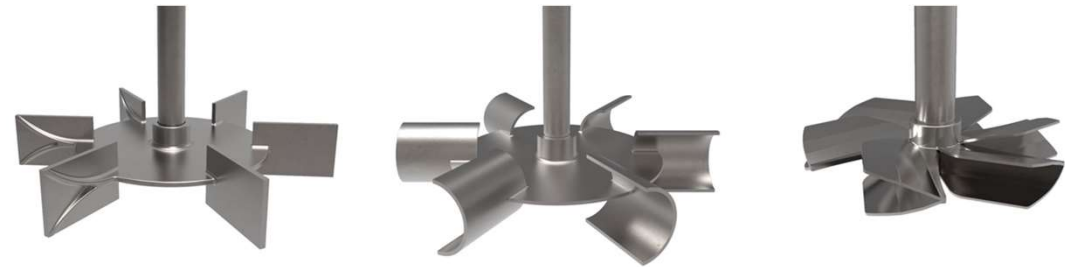
Hydrofoils
“Low shear”
“High efficiency”



Pitched and flat blade turbines
“Mixed flow”



Disc turbines
“High shear”
“Low efficiency”



Increasing “shear” (Ducoste et al., AIChEJ, 1997)

PROCESS RESULT



Mix components to promote chemical reaction:

- Semi-batch and continuous

Minimize side reactions:

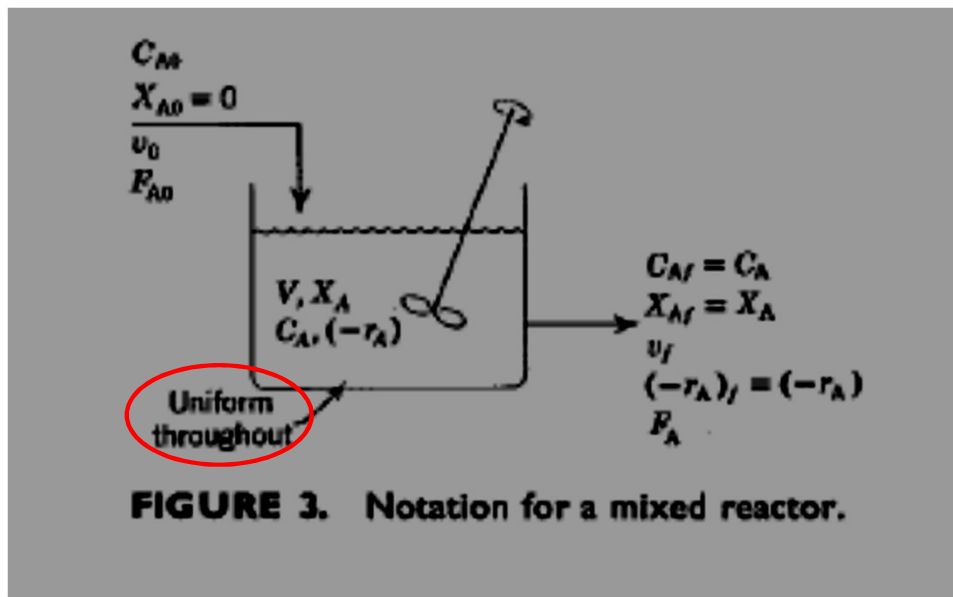
- Formation of by-products
- Waste of raw materials
- Increased separation and disposal costs

Minimize scale-up issues:

- Change in yield on scale-up:
 - Including molecular weight distribution (polymerization); particle size distribution and crystal polymorph (crystallization or precipitation); etc.

PERFECTLY MIXED REACTOR

“The CSTR is normally run at steady state, and is usually operated so as to be quite well mixed”, (Fogler, Elements of Chemical Reaction Engineering 2nd Ed., 1992)



From Levenspiel, “Chemical Reaction Engineering. 2nd Ed., 1972

Assume that exit composition is same as reactor contents

IDEAL CSTR

If vessel is perfectly back mixed composition of fluid leaving vessel is equal to composition in the vessel

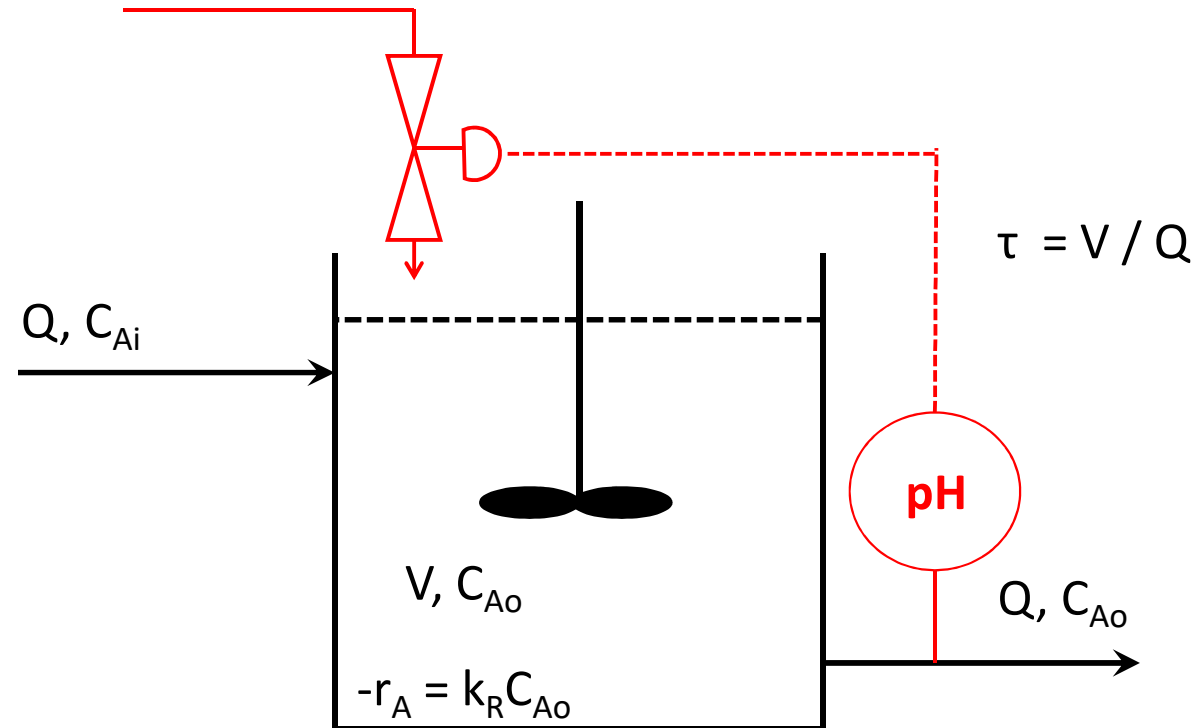
Assumption made in the design of systems for pH control in WWT

Rule-of-thumb, vessel is back mixed if:

$$\tau = \Omega \theta$$

$$5 < \Omega < 10$$

Reagent



$$C_{Ao} = \frac{C_{Ai}}{(1 + k_R \tau)}$$

$$X = 1 - \frac{1}{(1 + k_R \tau)}$$

RTD – PERFECT BACK MIXING

If vessel is “perfectly back mixed” residence time distribution (RTD) can be analytically calculated

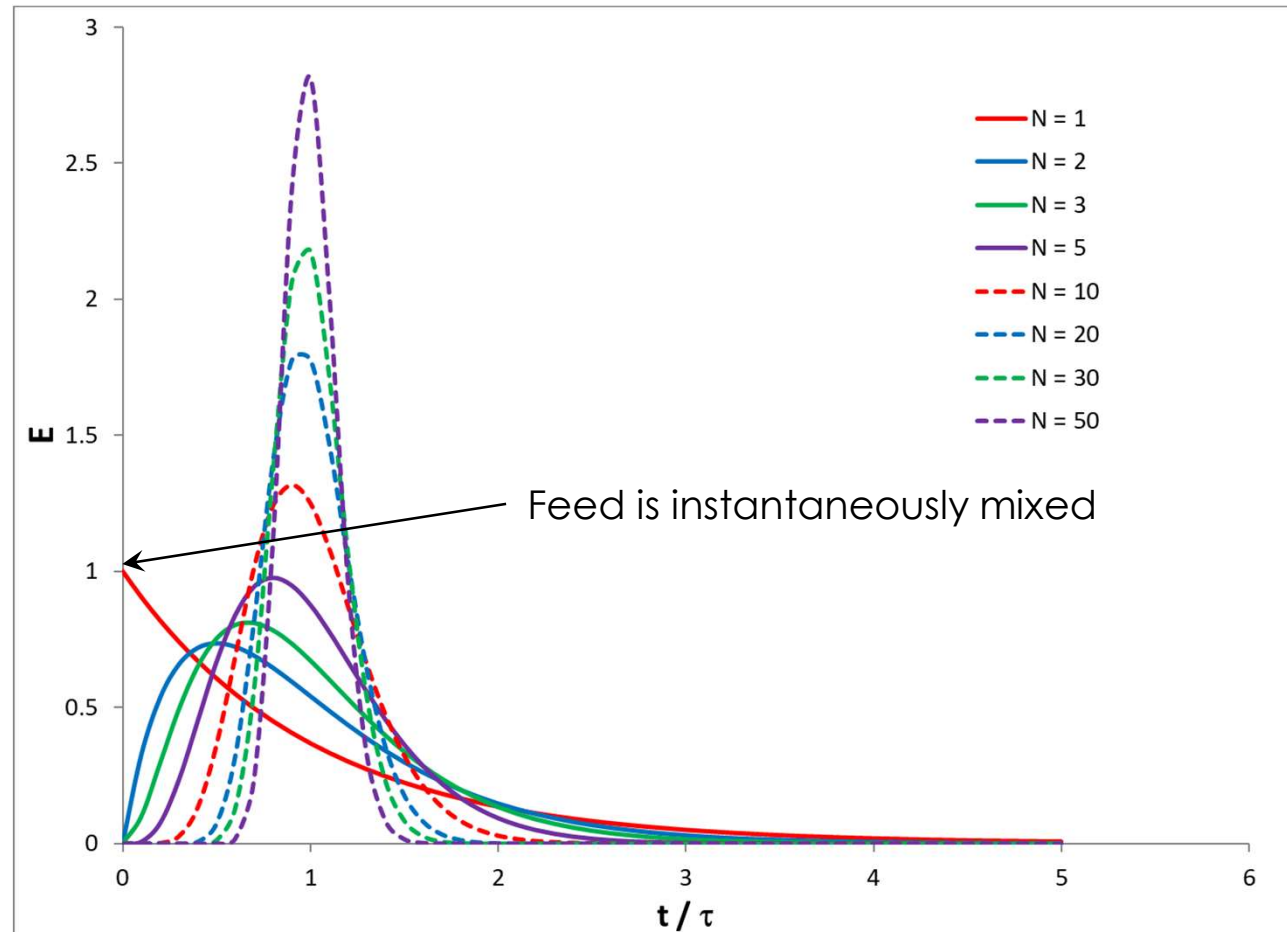
Can be combined with reaction kinetics to estimate conversion

Increasing number of tanks-in-series approximates plug flow

Slow reaction rates – compared to mixing rates

Vessel contents are homogeneous in space and time

When does assumption fail?



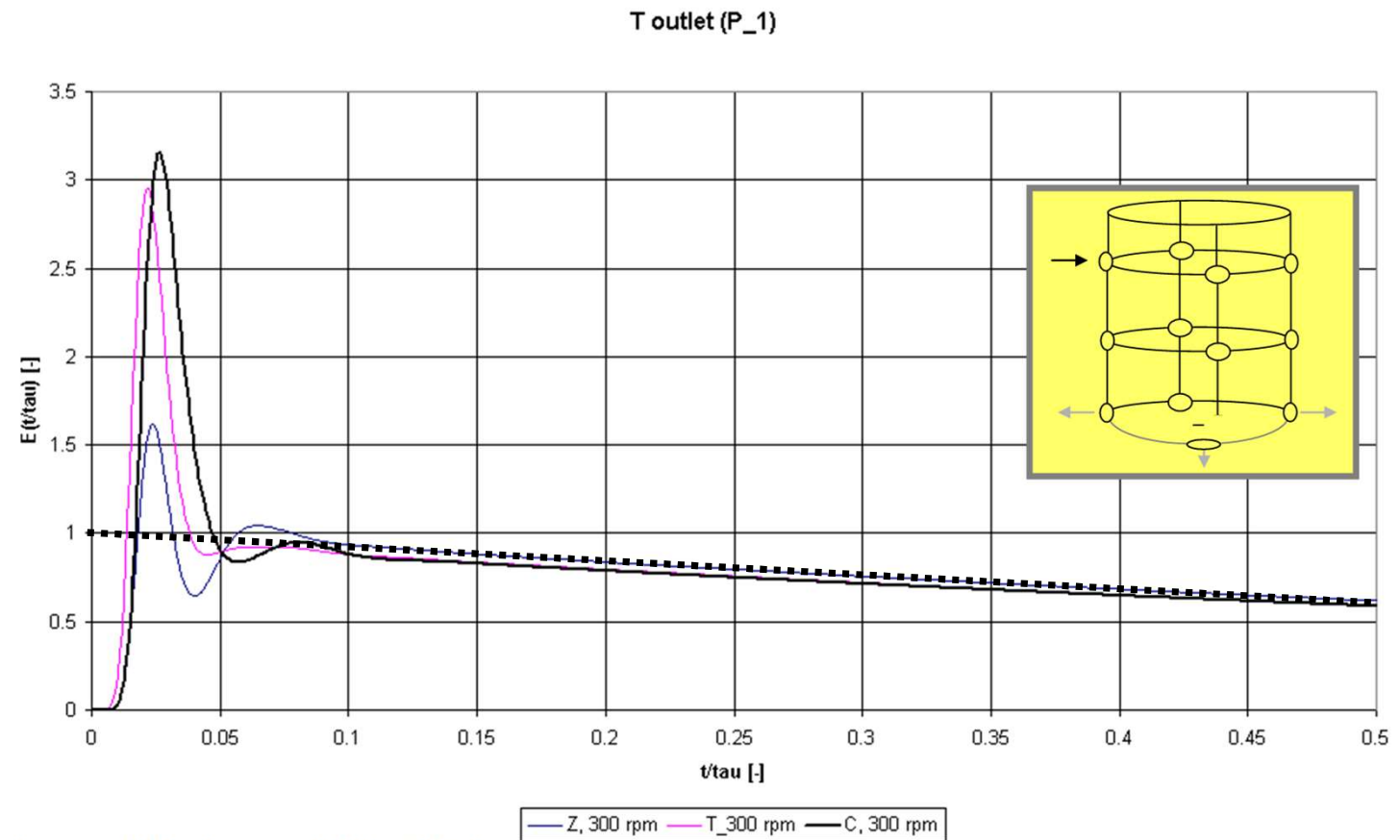
CSTR – RTD & BY-PASSING

Some material leaves early –compared to prediction of “perfect back mixing”

Therefore that material is under-converted

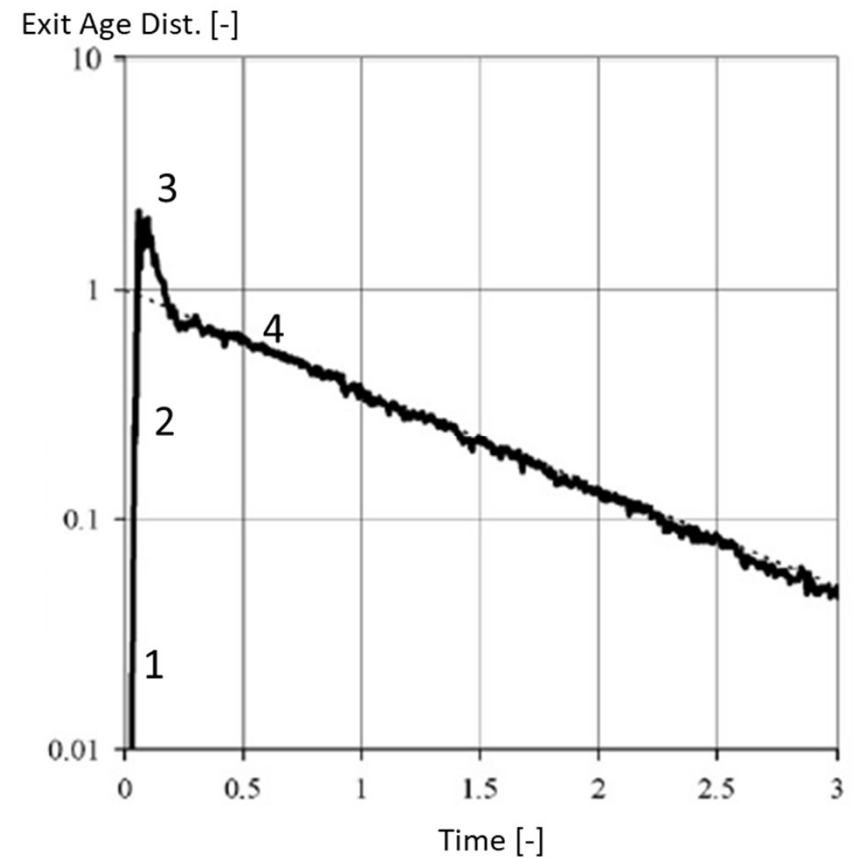
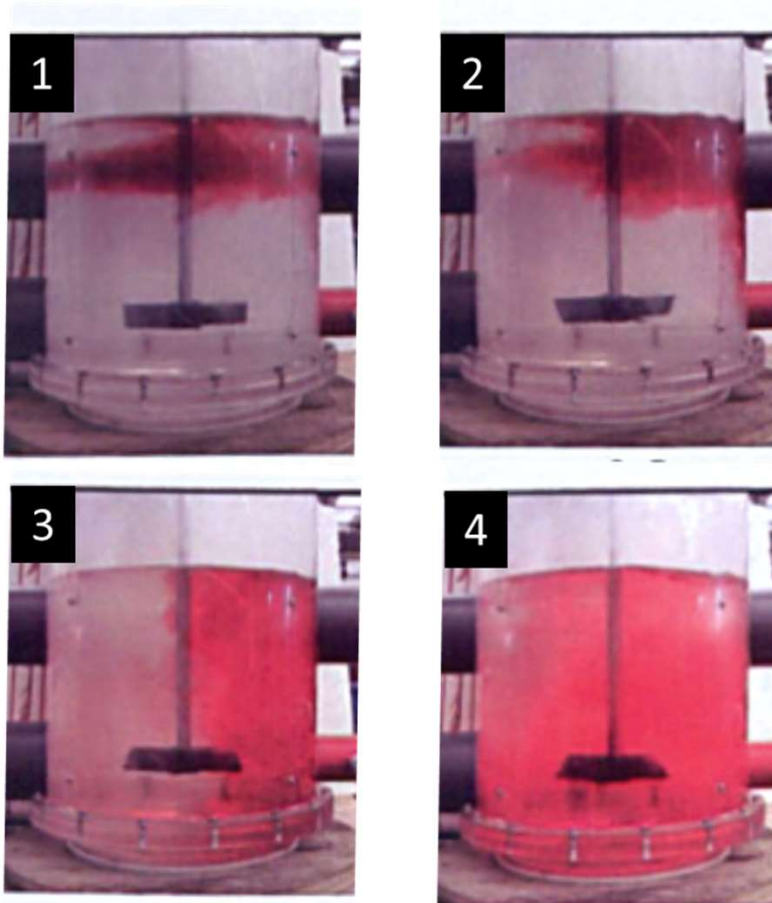
Spent less time than expected in reactor

Need to eliminate by-passing



Jones, *PhD Thesis*, KCL, 2004

BY-PASSING



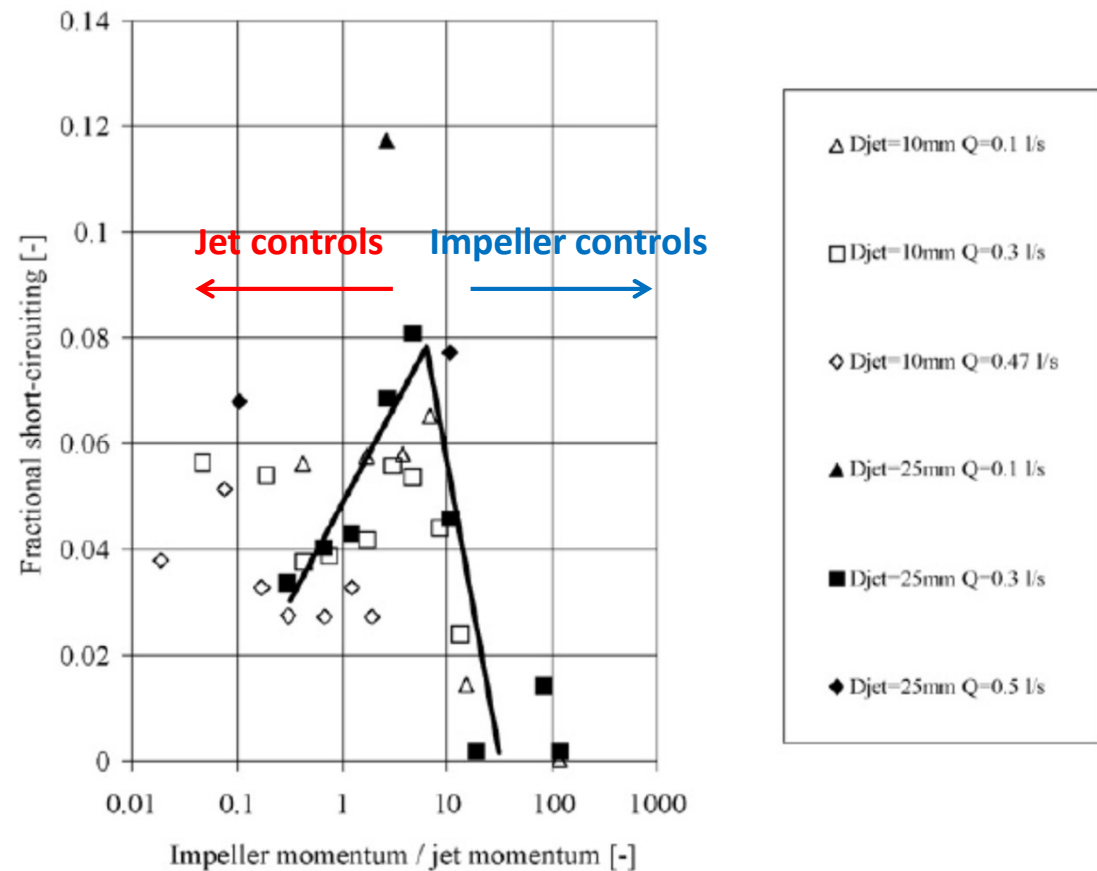
Jones et al., ChERD., 2009

MOMENTUM RATIO

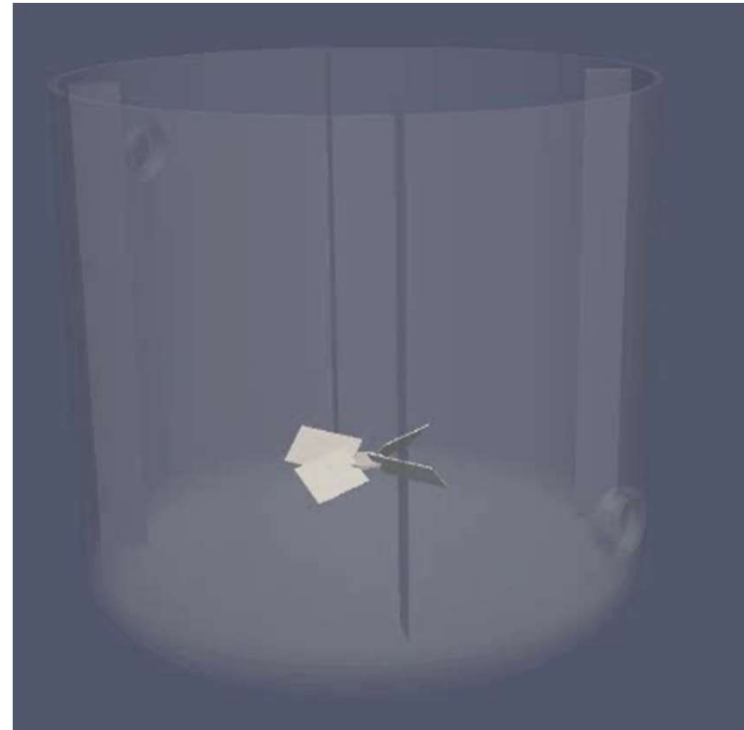
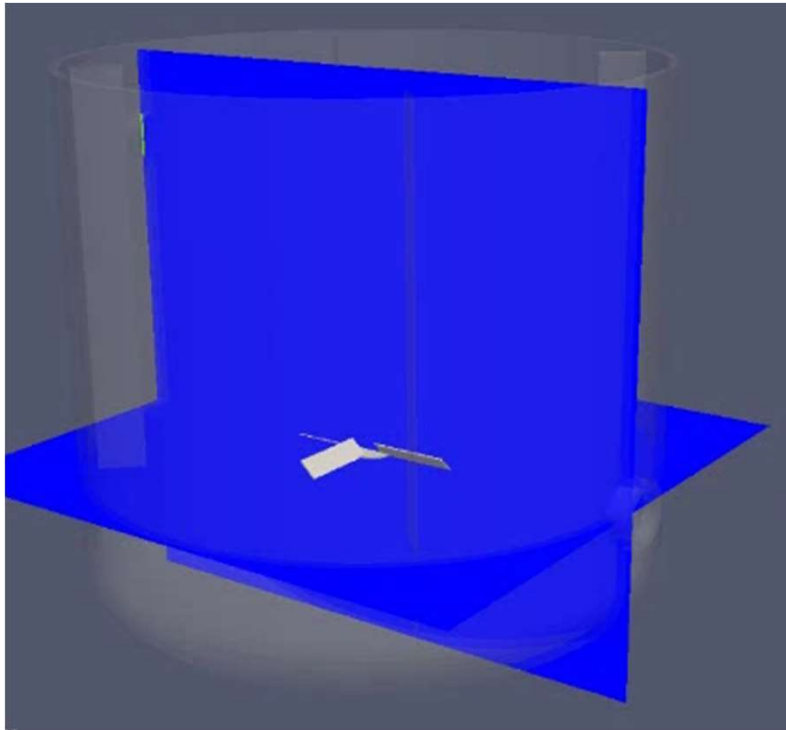
Need flow generated by impeller
to control flow patterns in vessel

Ratio of impeller flow momentum to
feed jet momentum determines
operating regime

Also need to consider location and
direction of feed

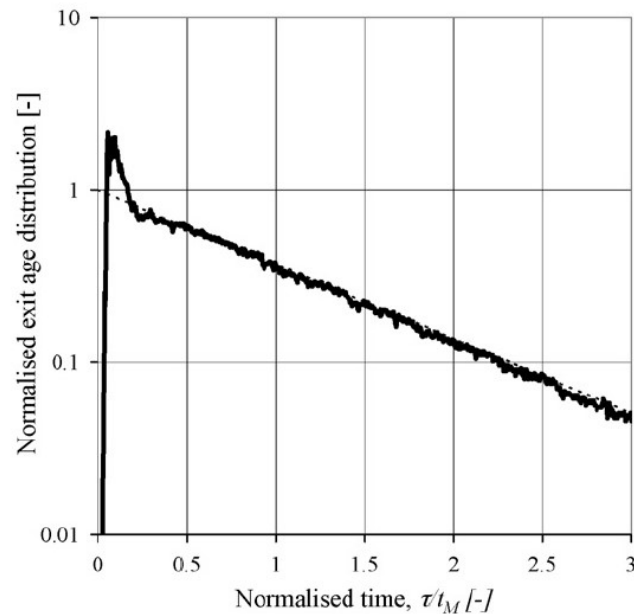


CFD MODELLING



Modelling case from Jones et al: $D_{PBT} = 0.1 \text{ m}$, $D_{jet} = 0.025 \text{ m}$, $Q = 0.3 \text{ l/s}$, $N = 1 \text{ s}^{-1}$

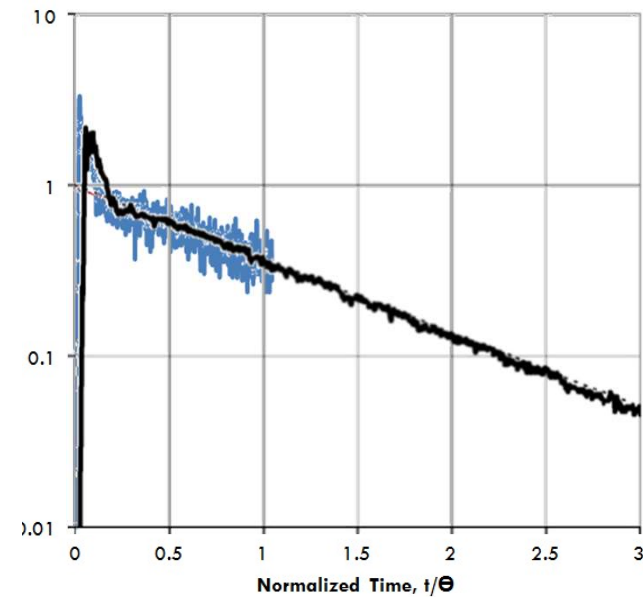
EXPERIMENT & MODEL



Jones et al., 2009

Measured θ : 68.9 s

Exit Age Dist.

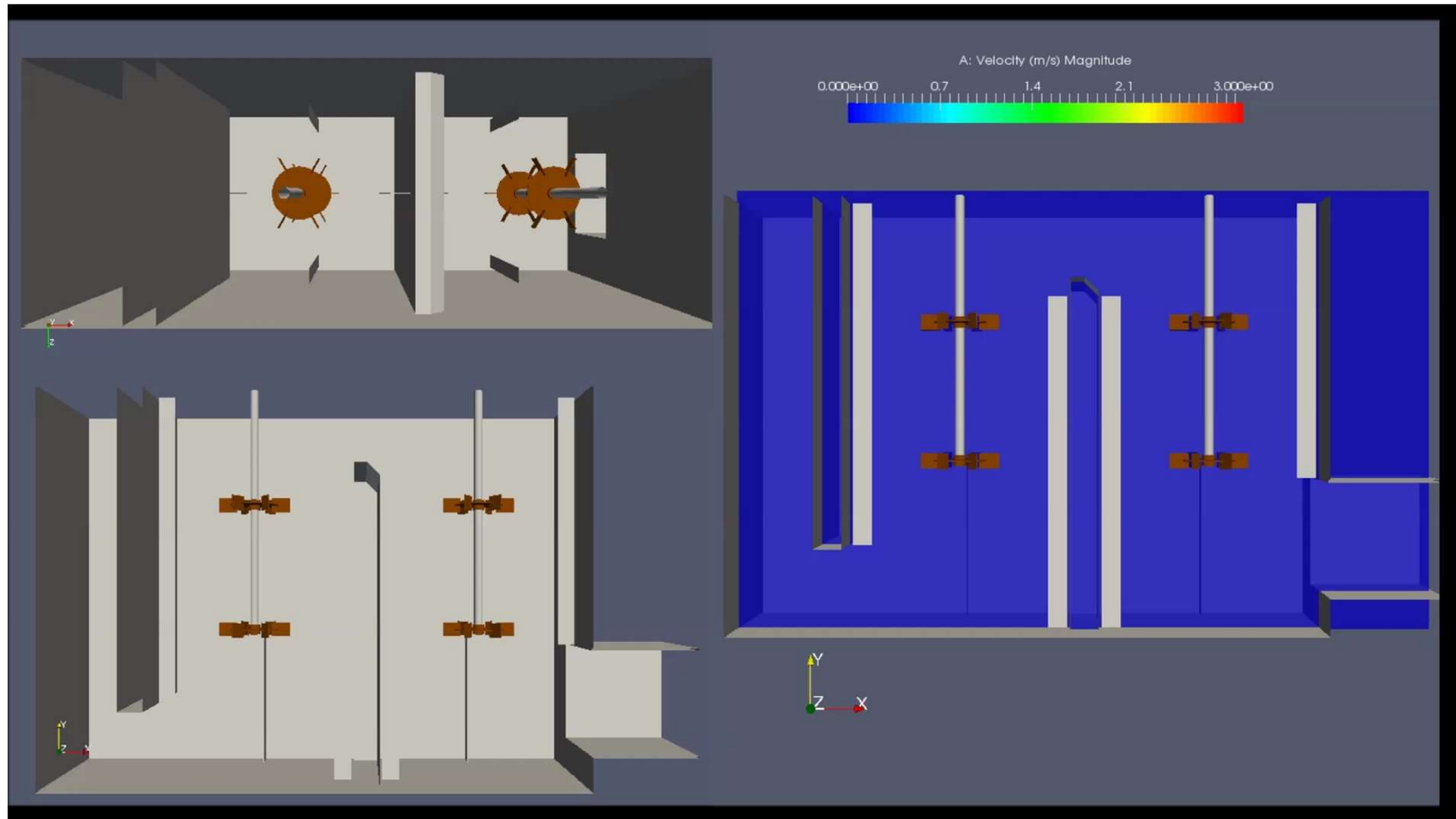


LES-CFD Prediction

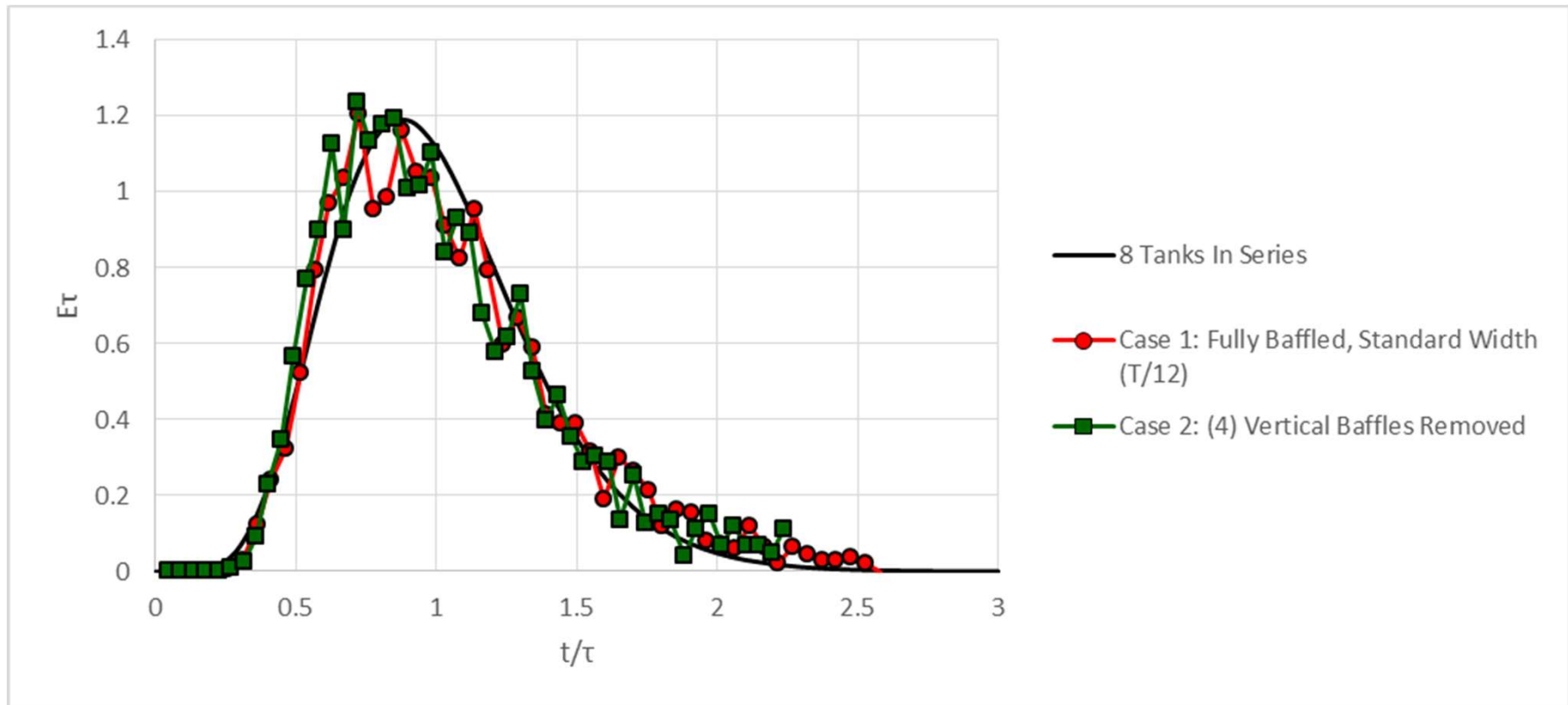
Predicted θ : 68.5 s

No need to run model for $\sim 5 \times \tau$

WATER TREATMENT RAPID MIX TANK



RTDs - ~8 TANKS IN SERIES

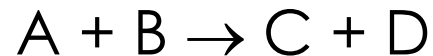


TYPES OF REACTION



Some reactions are fast (“instantaneous”) and some reactions are competitive

Simple, non-competitive reaction:



A = HCl

B = NaOH

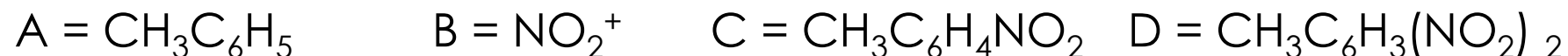
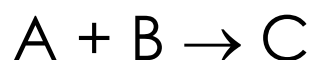
C = NaCl

D = H₂O

The Rate of Mixing has no influence on the outcome of the reaction

TYPES OF REACTION

Many (valuable) reactions are competitive:



Example:

- Want to make mononitro-toluene
- Dinitro-toluene is a possible by-product
- So is trinitro-toluene

ASSUMPTION OF PERFECT MIXING



Timescale of the reaction must be longer than Blend Time:

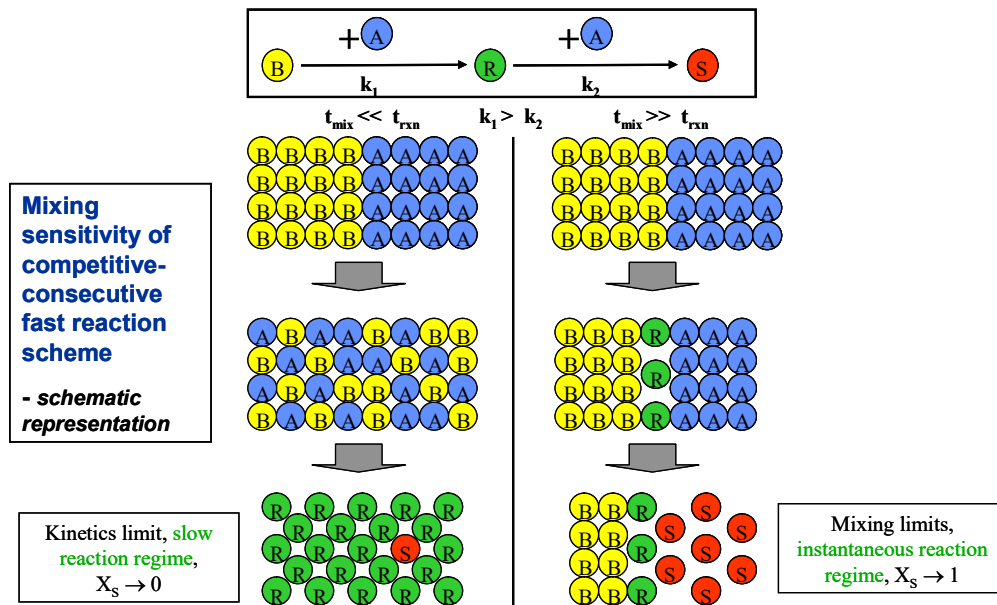
- Assumption of perfect mixing is valid
- Outcome of reaction is determined by kinetics

In a turbulent stirred tank, the blend time is generally in the order to 10's of seconds

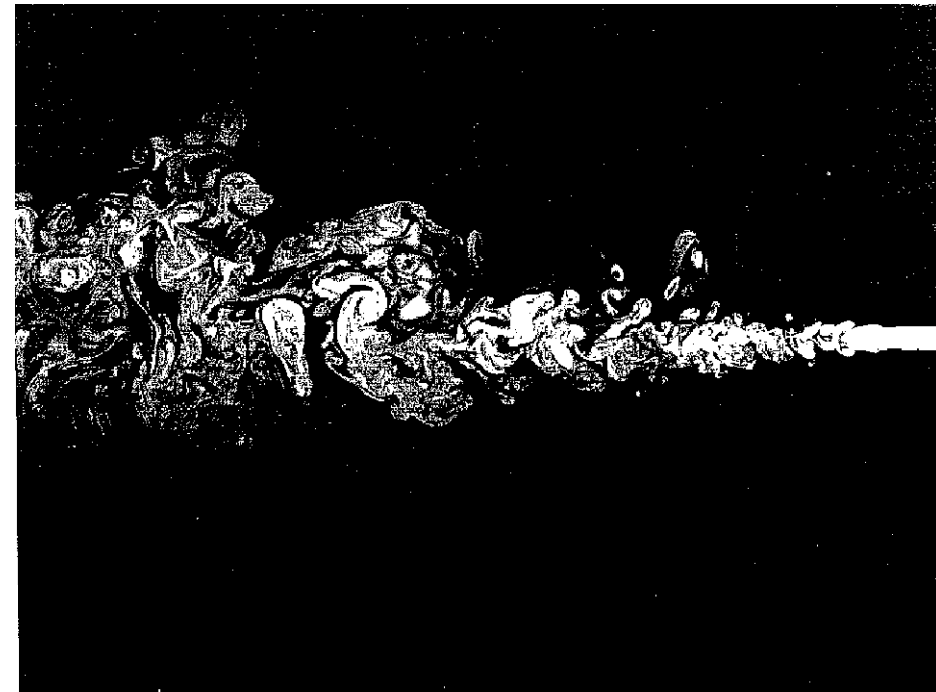
If Half-Life of Reaction is greater than ~60 seconds, then reactor is perfectly mixed (as far as reactants are concerned)

So what is the problem?

MIXING ON MICRO-SCALE

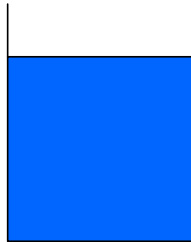


Mixing sensitivity from Hannon *et al.*, MIXING XVII, 1999



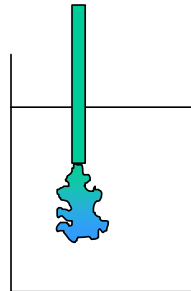
Scales of mixing from Dimotakis *et al.*, Proc. XV Int Symp Fluid Dyn, 1981

TIMESCALES OF MIXING



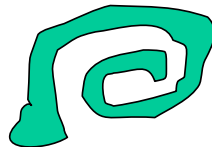
Macro-mixing:

- scale of the tank
- blend time



Meso-mixing:

- scale of the feed zone
- dispersion of feed plume



10 μ m

Micro-mixing:

- smallest scales of turbulence
- diffusion time

MIXING TIMESCALES



Macromixing → at scale of the vessel:

- Time for vessel contents to become homogeneous
- Blend time

Micromixing → at scale of smallest turbulent eddies:

- Deformation of fluid elements (vortex stretching, engulfment)
- Diffusion

Mesomixing → at scale of feed plume:

- Turbulent exchange of fresh feed with surrounding fluid
- Erosive reduction in scale of “blobs” of feed

MESO-MIXING

Meso-mixing Time (Bourne *et al.*):

- Semi-batch or continuous reactor - adding B to A
- Time for “plume” of B to be dispersed in A by local turbulence

More complicated than micro-mixing:

- Time is dependent on local mixing conditions and feed rate of B

$$t_M = 2\left(\frac{L_C^2}{\varepsilon}\right)^{1/3} = 2\left(\frac{q_B}{U\varepsilon}\right)^{1/3}$$

Local energy dissipation rate and mean velocity at feed location

REACTION TIMESCALE

Reaction Time is determined by:

- Rate constant.
- Concentration(s).

In a perfectly mixed environment:

$$t_R = \frac{1}{r_R} = \frac{1}{k_R C(A)C(B)}$$

In a poorly mixed environment:

$$t_R = \frac{1}{r_R} = \frac{1}{k_R C(A)C_0(B)}$$

If mixing is too slow, reaction occurs between concentrations at the feed location where $C(B) = C_0(B)$:

- Reaction rate is faster than predicted based on “good” mixing.
- More by-product will form.

DAMKOHLER NUMBER

$$Da = \frac{r_{\text{React}}}{r_{\text{Mix}}} = \frac{t_{\text{Mix}}}{t_{\text{React}}}$$

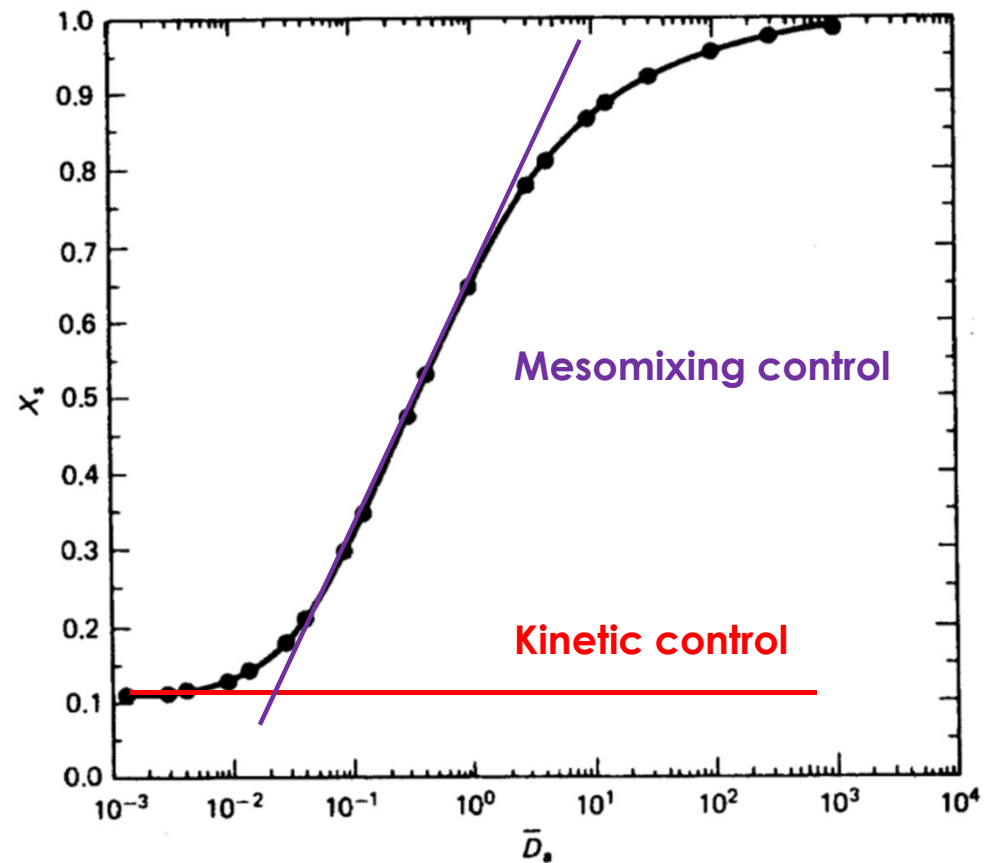
$$r_{\text{Mix}} \gg r_{\text{React}}$$

$$Da \ll 1$$

Kinetically controlled

If chemistry (kinetics)
are fixed:

$$Da \propto t_{\text{Mix}}$$



SCALE-UP CONSIDERATIONS



Feed location

Addition rate of B:

- Batch / feed time

Impeller type

FEED LOCATION – DIP PIPES



Feed at location of highest mixing and energy dissipation rate:

- Into the impeller zone

Effect has been well characterized and reported

Care must be taken in the mechanical design of the pipe:

- Flow induced vibration → fatigue failures

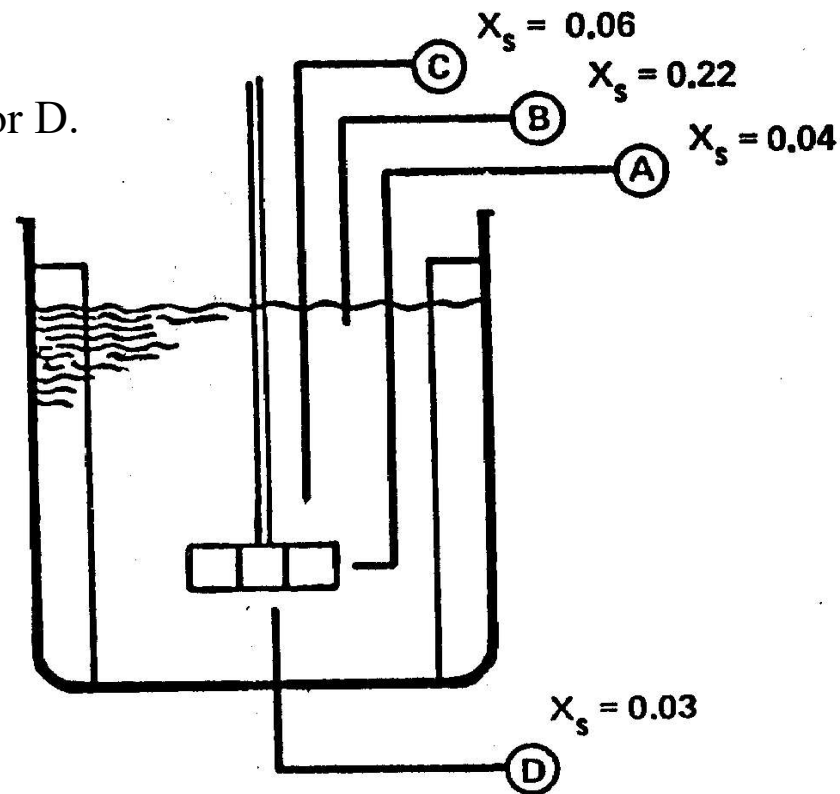
What happens if feed of B shuts off?

- Will reactor contents migrate into feed pipe?
- May have to feed above liquid surface for safety reasons

What happens if dip tube plugs?

EFFECT OF FEED LOCATION

Location B makes
6 -7 x more waste
than Locations A or D.



EFFECT OF FEED RATE

At low feed rates, micro-mixing controls:

- Engulfment of small-scale eddies
- Feed jet is dispersed quickly

As feed rate, q_B , increases mechanism changes:

- Dispersion of feed jet takes longer than engulfment

A critical feed time (or feed rate) can be identified:

- $t > t_{\text{CRIT}}$ Micro-mixing controls
- $t < t_{\text{CRIT}}$ Meso-mixing controls

EFFECT OF FEED RATE

Identify and operate at
“knee-of-curve” (compare to
Damkohler plot)

In order to operate in micro-mixing
(kinetic) regime:

- Increase feed time:
 - Reduce production
- Increase agitation:
 - Power input

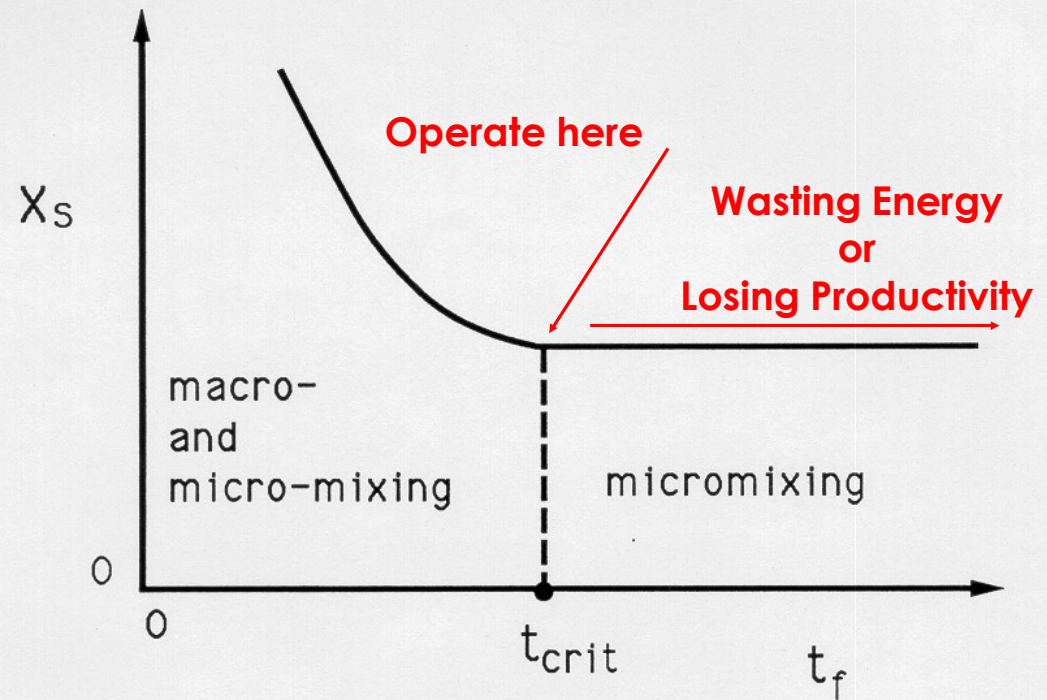


Fig.1 Product distribution (X_s) as a function of feed time (t_f) for a semi-batch reactor

Baldyga *et al.*, Chem Eng Sci, 1993

FEED RATE

Reduce feed time – move from micro to meso-mixing control:

- Yield of desired product reduced
- Plume of B cannot be dispersed fast enough by local mixing rate

Understanding this aspect of mixing and reaction is critical to successful scale-up:

- Long feed times achievable in lab combined with high impeller speed
- Feed time in plant dictated by required production rate

“Ream-Out”:

- What if higher production rate is required (sold out)?
- Need shorter feed time



Feature Report

Mixing:

Impeller Performance in Stirred Tanks

Characterizing mixer impellers on the basis of power, flow, shear and efficiency

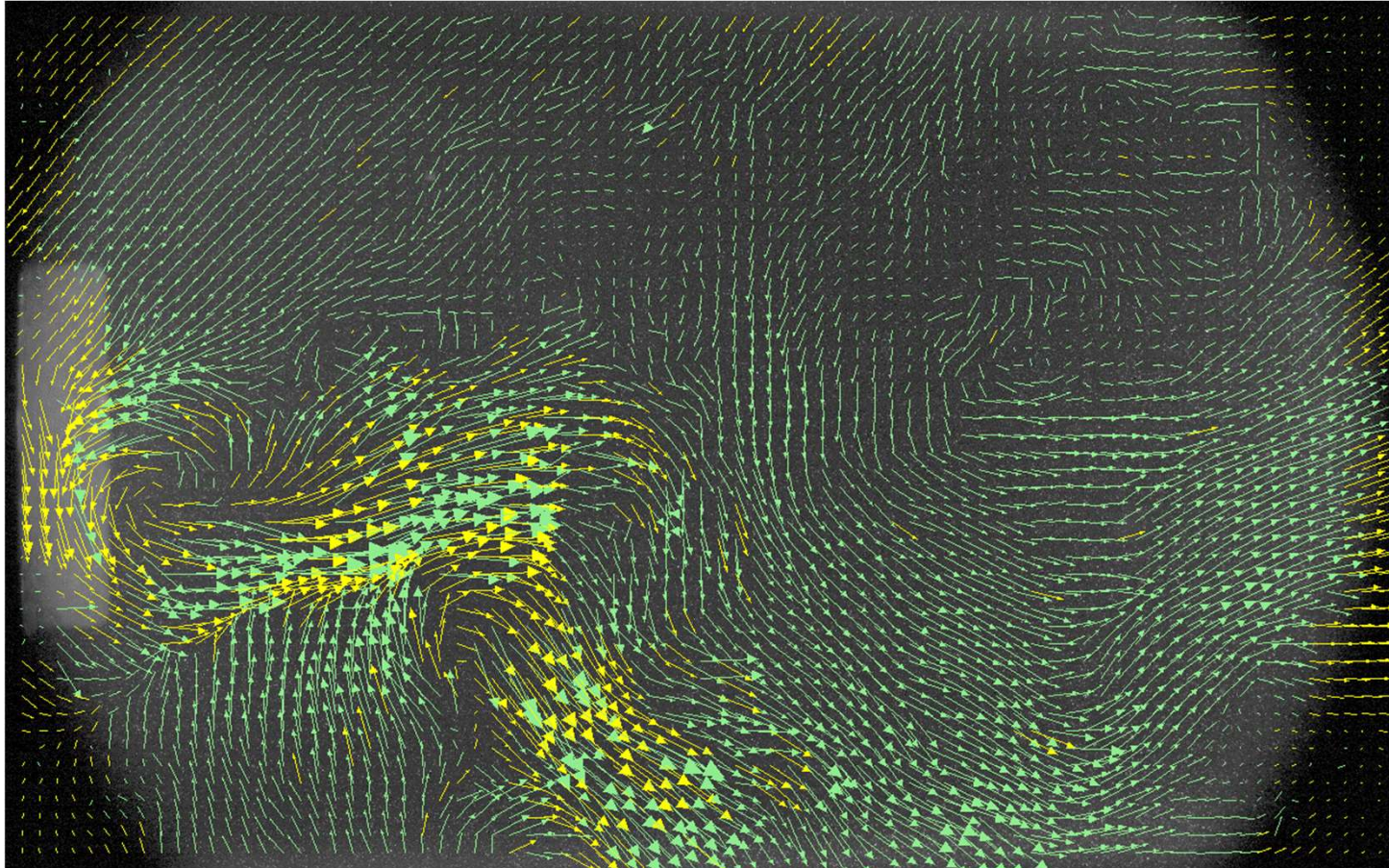
**Richard K.
Grenville
and Jason J.
Giacomelli**
Philadelphia Mixing
Solutions Ltd.
**Gustavo Padron
and David A. R.
Brown**
BHR Group

Mixing has been defined as “the application of mechanical motion in order to create fluid dynamic effects that achieve a desired process result” [1]. The process result is the objective of the vessel operator and will be a transformation of the ingredients fed to the vessel into a product. The goal of the equipment supplier will be to understand the role of mixing in promoting the

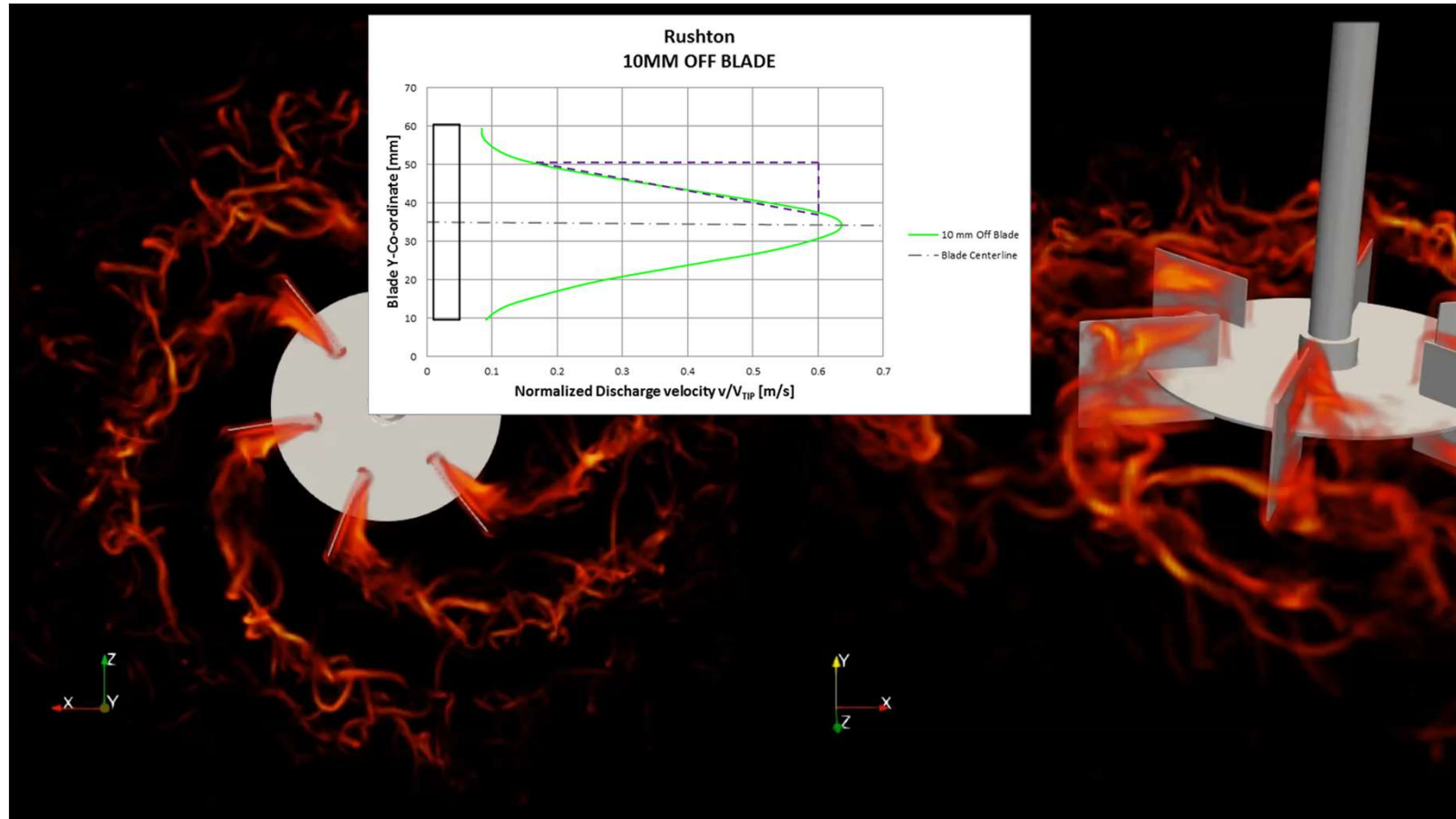
NOMENCLATURE

A Constant in Equation (30)
 A_{DIS} Discharge area for primary flow from impeller
 D Impeller diameter
 d_{32} Sauter mean droplet size
 Fl Flow or pumping number ($= Q/(ND^3)$)
 K Ratio ($= \varepsilon_{MAX}/\bar{\varepsilon}$)
 k_{MAX} Maximum kinetic energy in trailing vortex
 l_0 Diameter of trailing vortex
 N Impeller rotational speed

RUSHTON: PIV → TRAILING VORTEX



RUSHTON: CFD → TRAILING VORTEX



IMPELLER TYPE AND DIAMETER



Easy to estimate mean energy dissipation rate (or power input per unit volume):

$$\bar{\varepsilon} = \frac{P}{M} = \frac{P_0}{\pi/4} N^3 D^2 \left(\frac{D}{T}\right)^3$$

B does not experience “mean” conditions

Dissipation is highest in trailing vortex at tip of impeller blades

LOCAL TKEDR AT FEED LOCATION



If dip pipe is used, feeding into impeller suction and vortex behind blade feed will “feel” maximum TKEDR where:

$$\epsilon_{\max} = K \bar{\epsilon}$$

K has been calculated previously:

$$K = 0.82 \frac{x}{Po^{1/4}} \left(\frac{T}{D}\right)^3$$

OPTIMIZING REACTOR OPERATION



Maximize local energy dissipation rate and mean velocity at feed point:

- High power input from motor
- Correct choice of impeller

Use dip pipe to feed into impeller zone

Choose appropriate q_B :

- If necessary, divide feed by using multiple dip pipes

Can reaction rate be slowed?

- Lower temperature? Dilution?

EXAMPLE

Di-Acid + Base \rightarrow Mono-Acidic Product (P) + Water

Mono-Acidic Product + Base \rightarrow Inert By-product (W) + Water

Reaction products are equally soluble:

- Cannot be easily separated

Product sold as solution of P in water.:

- W is inert in product
- Sold on basis of concentration of P

Mixture is diluted to make product:

- Higher P : W ratio \rightarrow more dilution water added.

LAB STUDIES

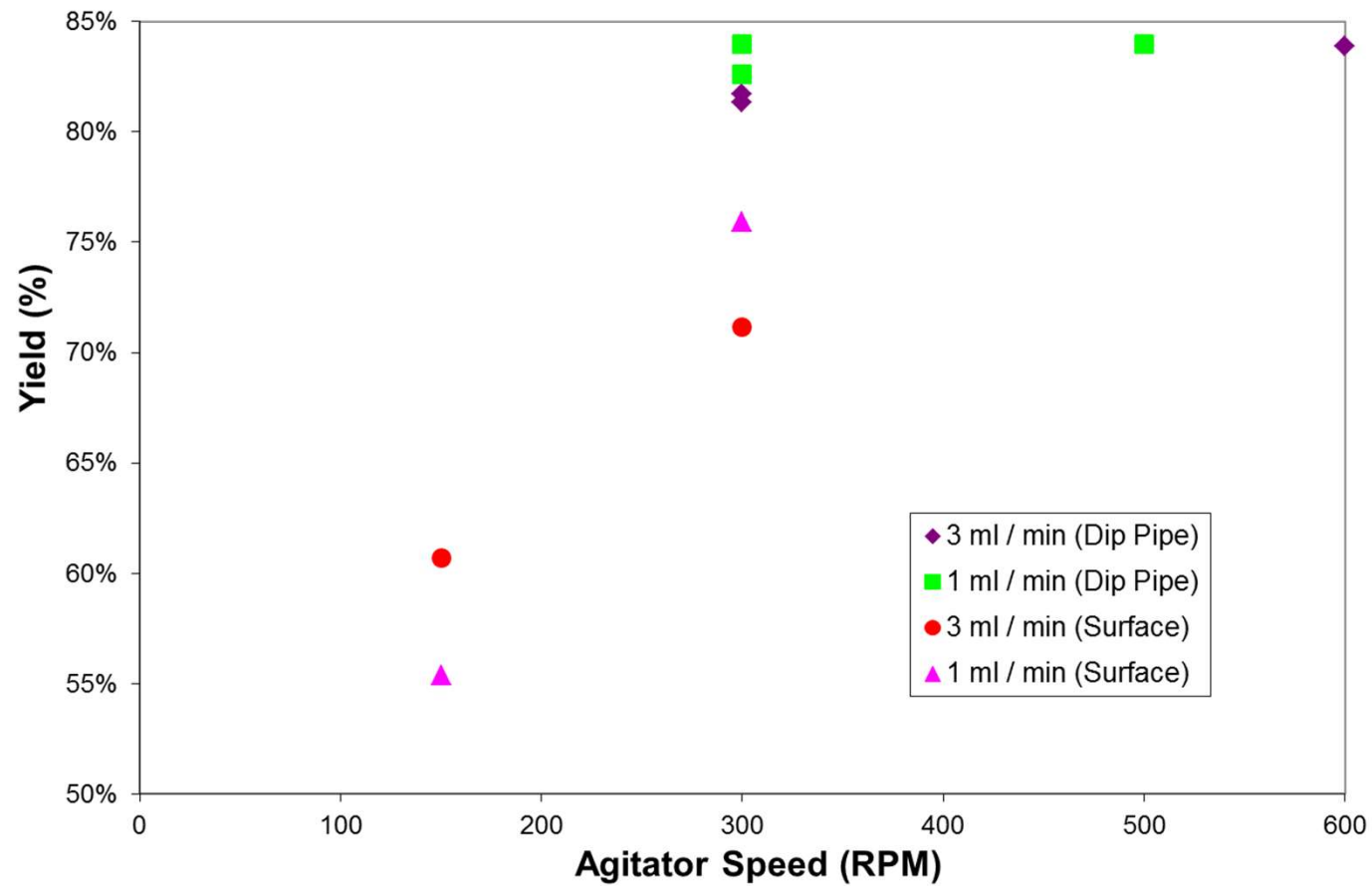
Tests carried out at lab-scale in Hood

If mixing is slow product loses “quality”

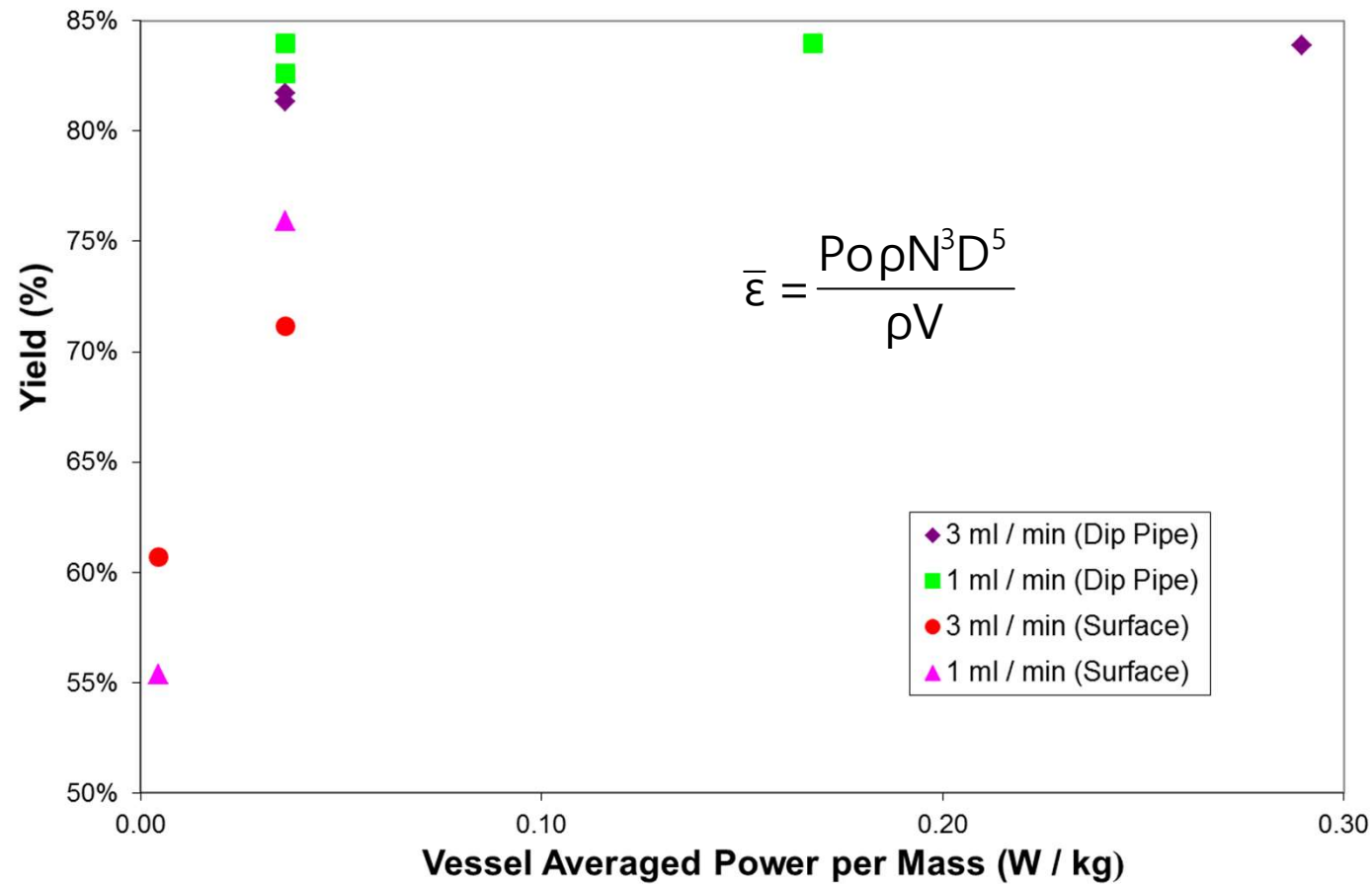
Conditions:

- 1 litre vessel ($T = 99$ mm) with single Hydrofoil ($D = 54$ mm)
- Feed rate, $q = 1$ and 3 ml / min
- Impeller speed = $150 - 600$ RPM
- Feed at surface and at impeller tip (through dip pipe)

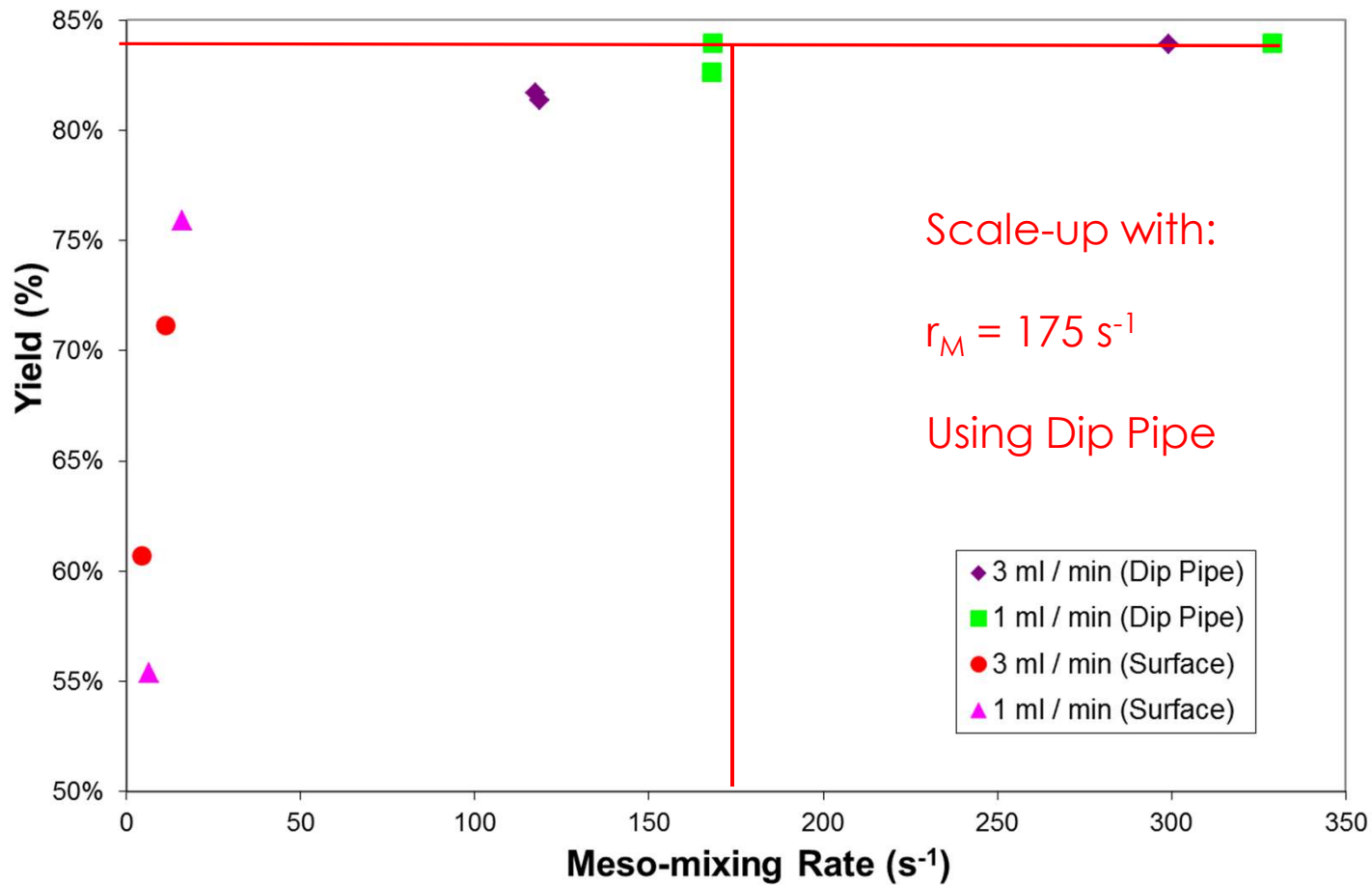
YIELD vs SPEED



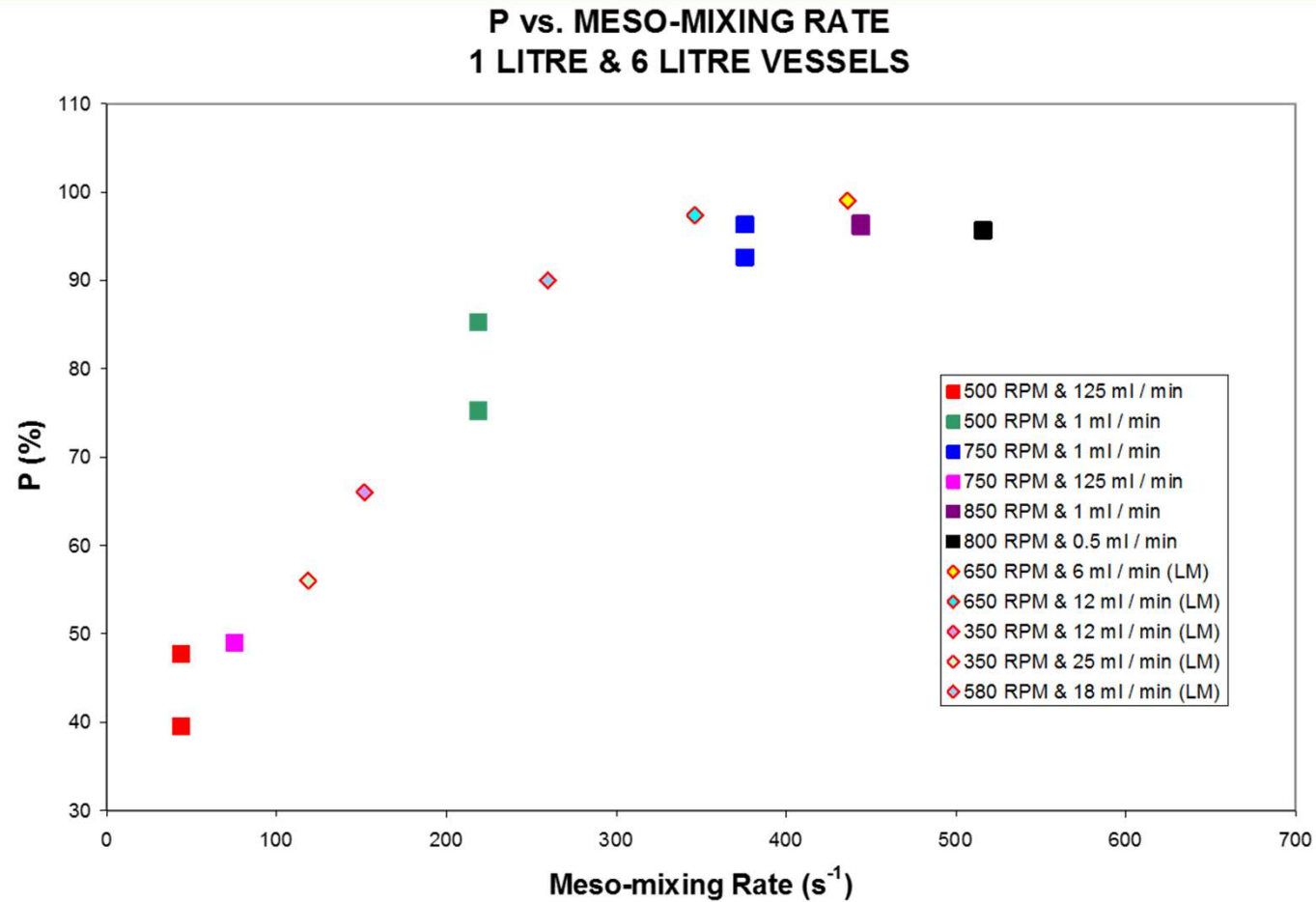
YIELD vs AVG POWER PER MASS



YIELD vs MESO-MIXING RATE



YIELD vs MESO-MIXING RATE (2)



CONCLUSIONS

Mixing is rarely an issue for:

- Simple reactions
- Slow reactions

Yield of fast, competitive reactions is determined by mixing rate at feed location

In industrial reactors mesomixing timescale controls

Scale-up on constant Damkohler number

Must encourage chemists to run batches that “fail” at lab-scale:

- Find the “knee-of-the-curve”

Alternative chemistry?