

# **Deep Reinforcement Learning**

Deep learning

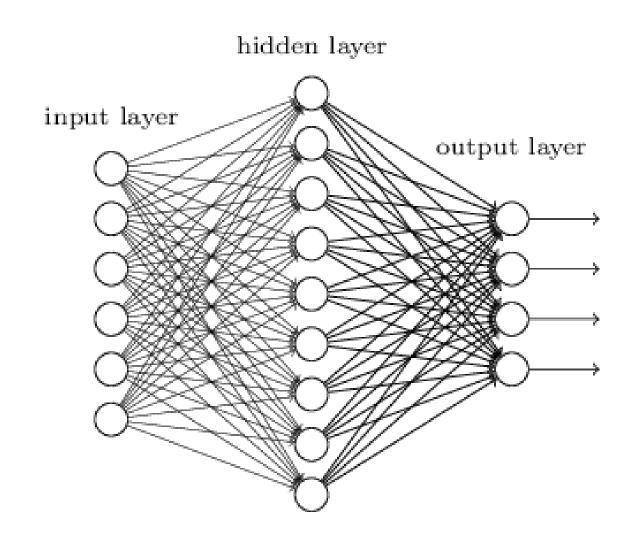
Julien Vitay

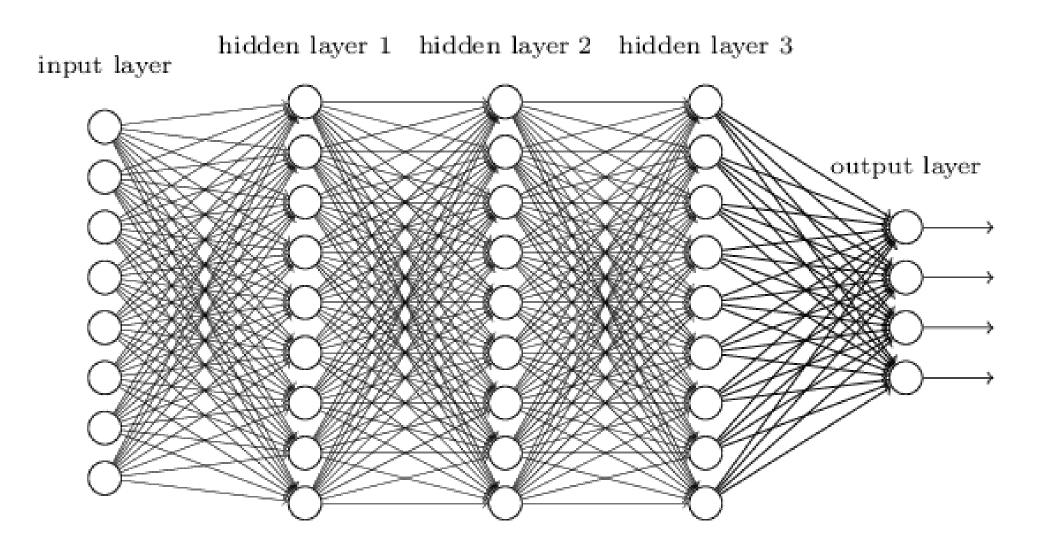
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1 - Artificial neural networks

#### **Artificial neural networks**

• An artificial neural network (ANN) is a cascade of fully-connected (FC) layers of artificial neurons.





• Each layer k transforms an input vector  $\mathbf{h}_{k-1}$  into an output vector  $\mathbf{h}_k$  using a weight matrix  $W_k$ , a bias vector  $\mathbf{b}_k$  and an activation function f().

$$\mathbf{h}_k = f(W_k imes \mathbf{h}_{k-1} + \mathbf{b}_k)$$

• Overall, ANNs are **non-linear parameterized function estimators** from the inputs x to the outputs y with parameters  $\theta$  (all weight matrices and biases).

$$\mathbf{y} = F_{ heta}(\mathbf{x})$$

#### **Loss functions**

- ANNs can be used for both regression (continuous outputs) and classification (discrete outputs) tasks.
- In supervised learning, we have a fixed training set  $\mathcal{D}$  of N samples  $(\mathbf{x}_t, \mathbf{t}_i)$ , where  $t_i$  is the desired output or target.

#### • Regression:

- ullet The output layer uses a **linear** activation function: f(x)=x
- The network minimizes the **mean square error** (mse) of the model on the training set:

$$\mathcal{L}( heta) = \mathbb{E}_{\mathbf{x}, \mathbf{t} \in \mathcal{D}}[||\mathbf{t} - \mathbf{y}||^2]$$

#### • Classification:

- The output layer uses the **softmax** operator to produce a probability distribution:  $y_j = rac{e^{z_j}}{\sum_k e^{z_k}}$
- The network minimizes the **cross-entropy** or **negative log-likelihood** of the model on the training set:

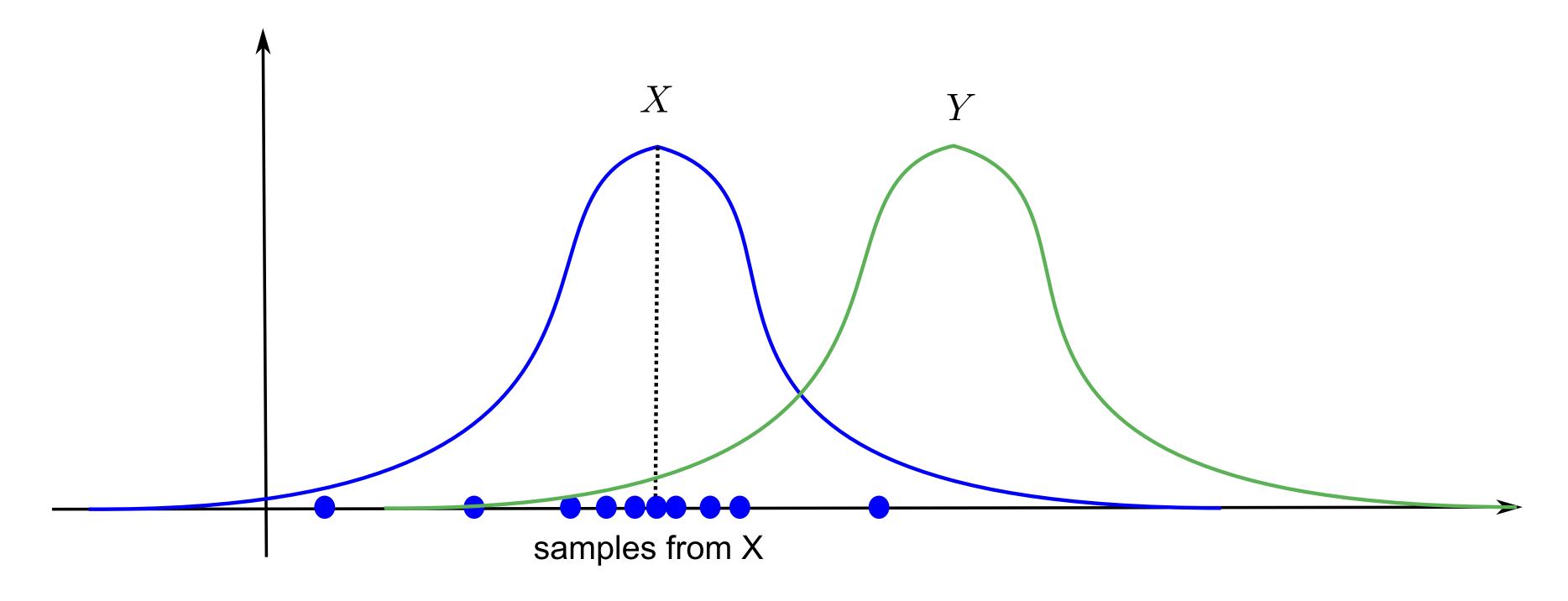
$$\mathcal{L}( heta) = \mathbb{E}_{\mathbf{x}, \mathbf{t} \in \mathcal{D}}[-\mathbf{t} \, \log \mathbf{y}]$$

### **Cross-entropy**

ullet The cross-entropy between two probability distributions X and Y measures their similarity:

$$H(X,Y) = \mathbb{E}_{x\sim X}[-\log P(Y=x)]$$

- ullet Are samples from X likely under Y?
- Minimizing the cross-entropy makes the two distributions equal almost anywhere.

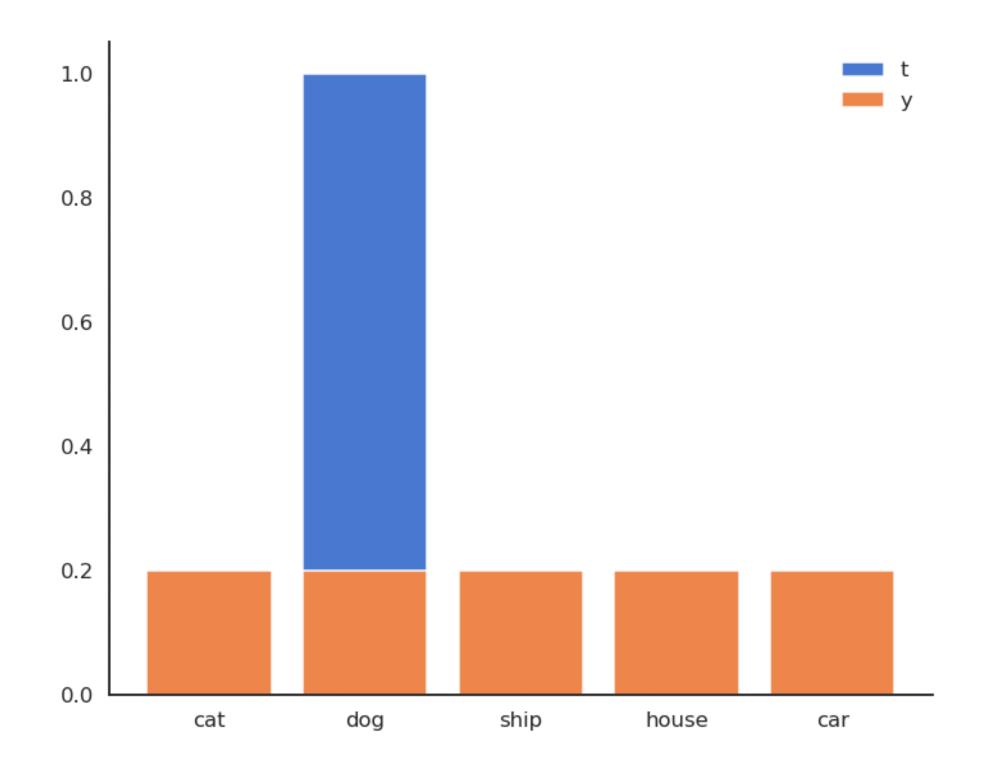


### **Cross-entropy**

ullet In supervised learning, the targets  $oldsymbol{t}$  are fixed **one-hot encoded vectors**.

$$\mathcal{L}( heta) = \mathbb{E}_{\mathbf{x}, \mathbf{t} \in \mathcal{D}}[-\sum_{j} t_{j} \, \log y_{j}]$$

• But it could be any target distribution.



### Backpropagation

• In both cases, we want to minimize the loss function by applying **Stochastic Gradient Descent** (SGD) or a variant (Adam, RMSprop).

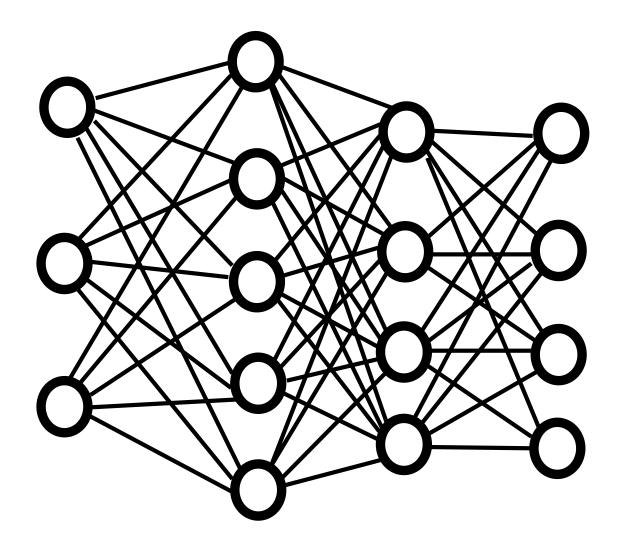
$$\Delta heta = -\eta \, 
abla_{ heta} \mathcal{L}( heta)$$

- The question is how to compute the **gradient of the loss function** w.r.t the parameters  $\theta$ .
- For both the mse and cross-entropy loss functions, we have:

$$abla_{ heta} \mathcal{L}( heta) = \mathbb{E}_{\mathcal{D}}[-(\mathbf{t}-\mathbf{y})\,
abla_{ heta}\,\mathbf{y}]$$

- There is an algorithm to compute efficiently the gradient of the output w.r.t the parameters: **backpropagation** (see Neurocomputing).
- In deep RL, we do not care about backprop: tensorflow or pytorch do it for us.

### **Components of neural networks**

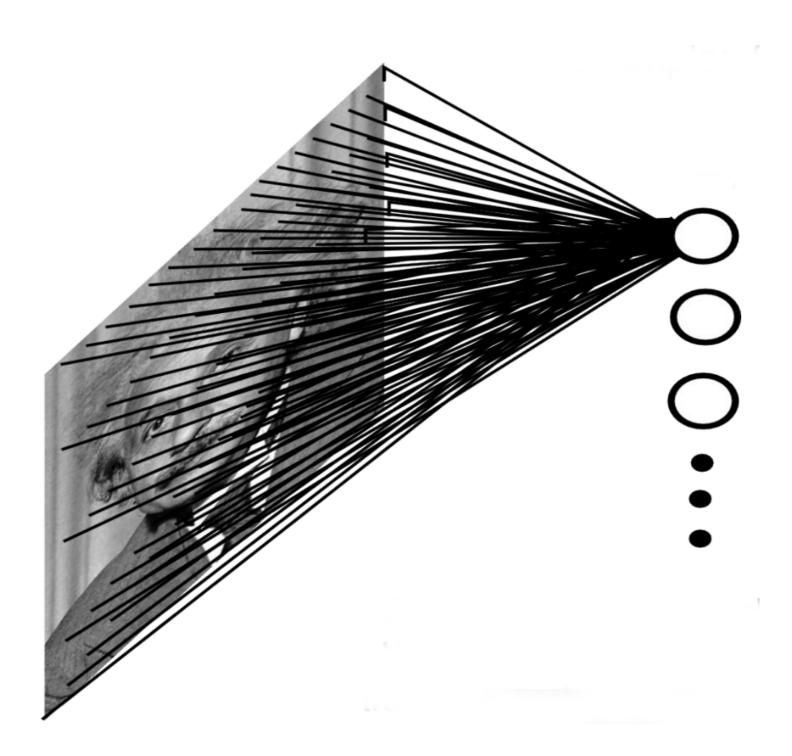


- There are three aspects to consider when building a neural network:
- 1. Architecture: how many layers, what type of layers, how many neurons, etc.
  - Task-dependent: each RL task will require a different architecture. Not our focus.
- 2. Loss function: what should the network do?
  - Central to deep RL!
- 3. **Update rule** how should we update the parameters  $\theta$  to minimize the loss function? SGD, backprop.
  - Not really our problem, but see natural gradients later.

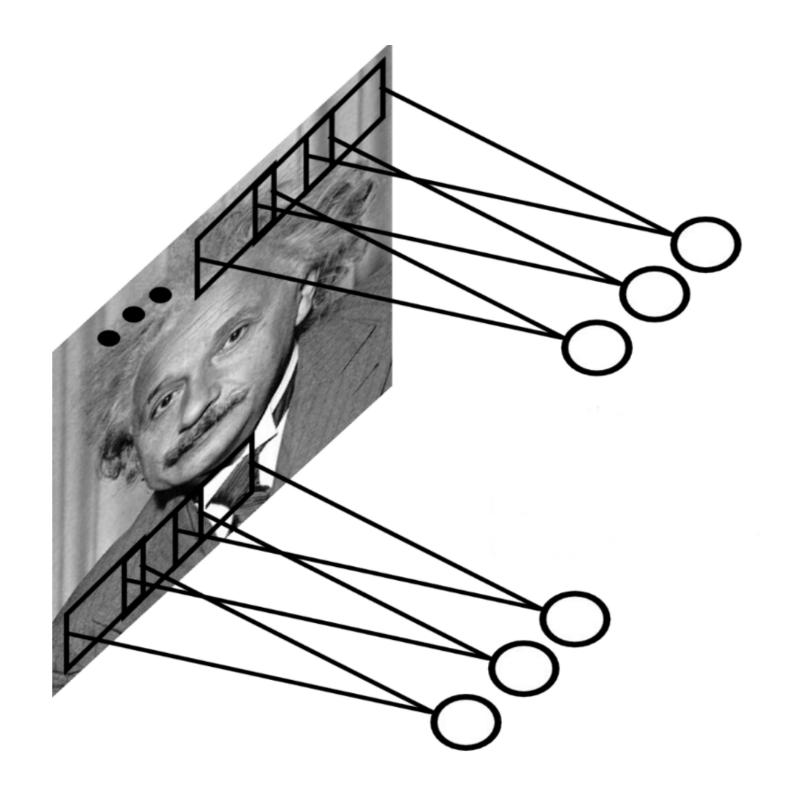
2 - Convolutional neural networks

## **Convolutional layers**

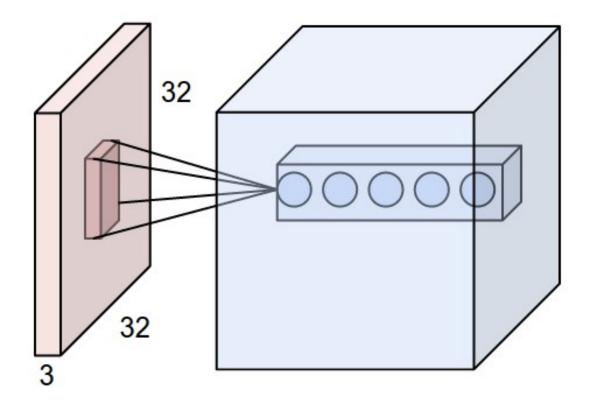
- When using images as inputs, **fully-connected networks** (FCN) would have too many weights:
  - Slow.
  - Overfitting.

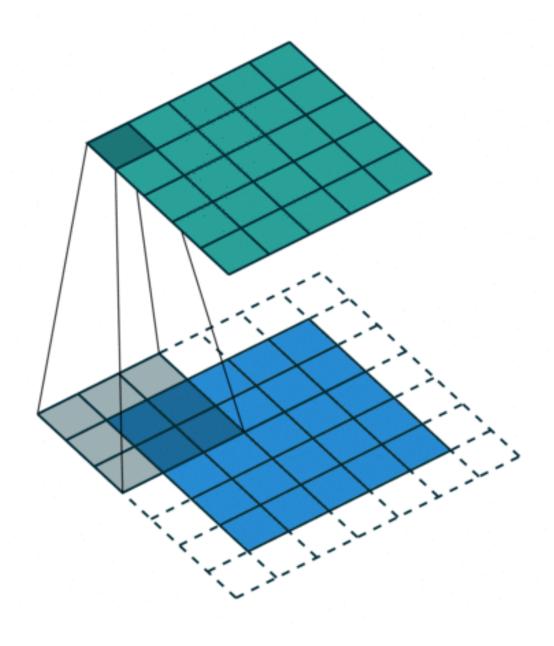


- **Convolutional layers** reduce the number of weights by **reusing** weights at different locations.
  - Principle of a convolution.
  - Fast and efficient.



### **Convolutional layers**

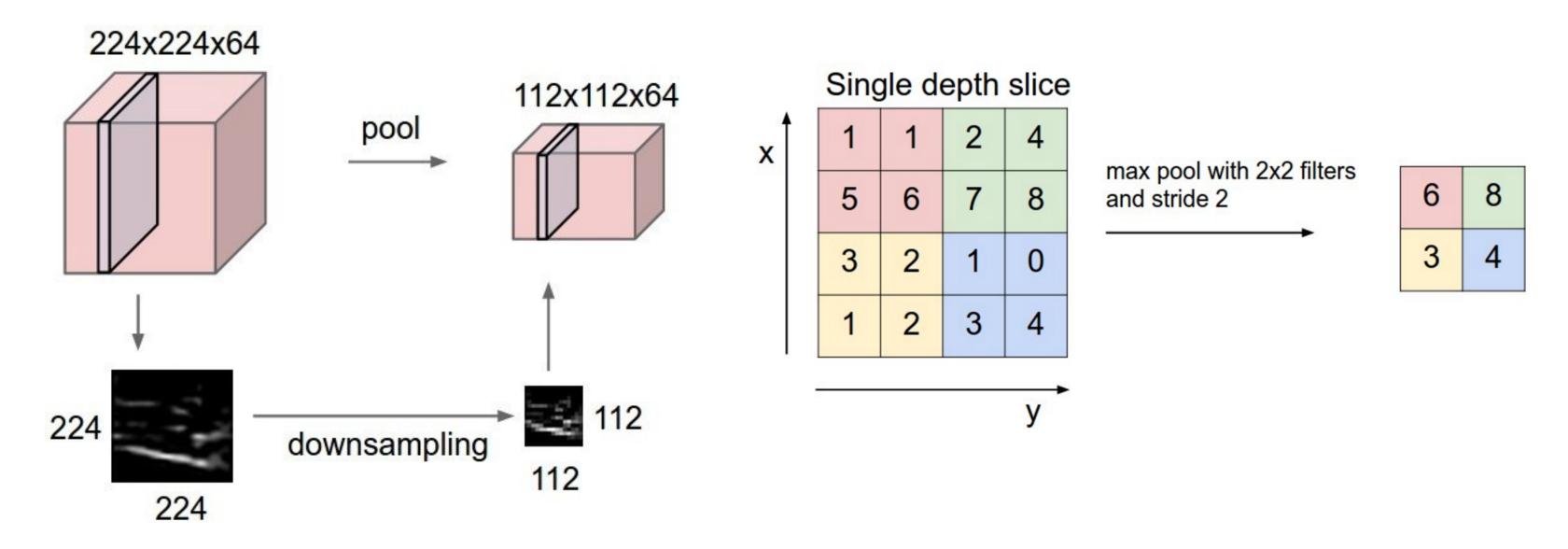




Source: https://github.com/vdumoulin/conv\_arithmetic

- A convolutional layer extracts features of its inputs.
- d filters are defined with very small sizes (3x3, 5x5...).
- Each filter is convoluted over the input image (or the previous layer) to create a **feature map**.
- The set of d feature maps becomes a new 3D structure: a **tensor**.
- If the input image is 32x32x3, the resulting tensor will be 32x32xd.
- The convolutional layer has only very few parameters: each feature map has 3x3 values in the filter and a bias, i.e. 10 parameters.
- The convolution operation is **differentiable**: backprop will work.

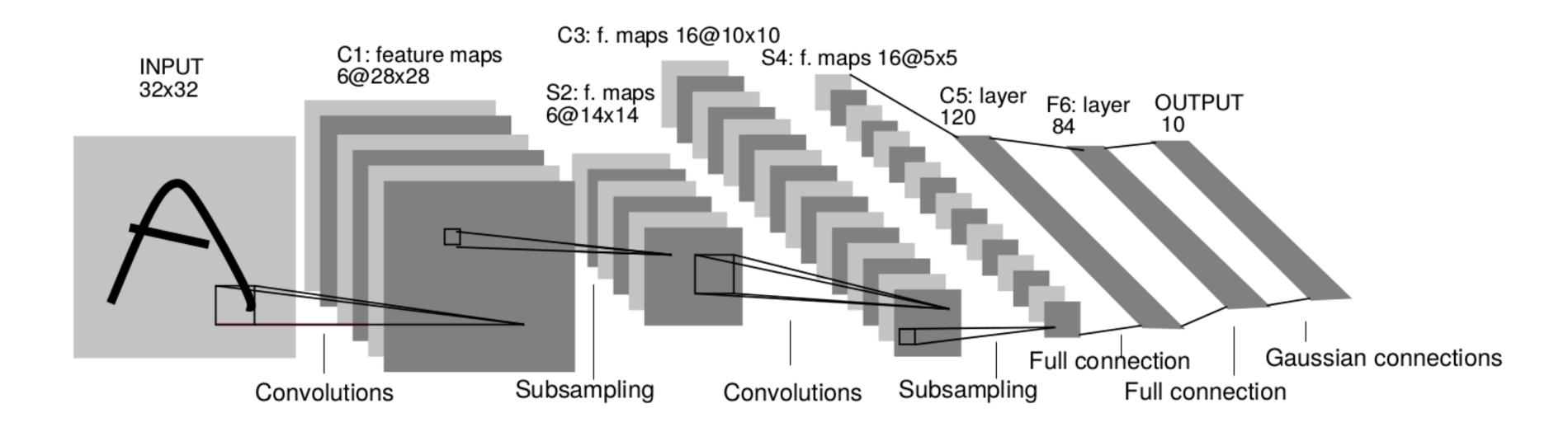
### **Max-pooling**



Source: http://cs231n.github.io/convolutional-networks/

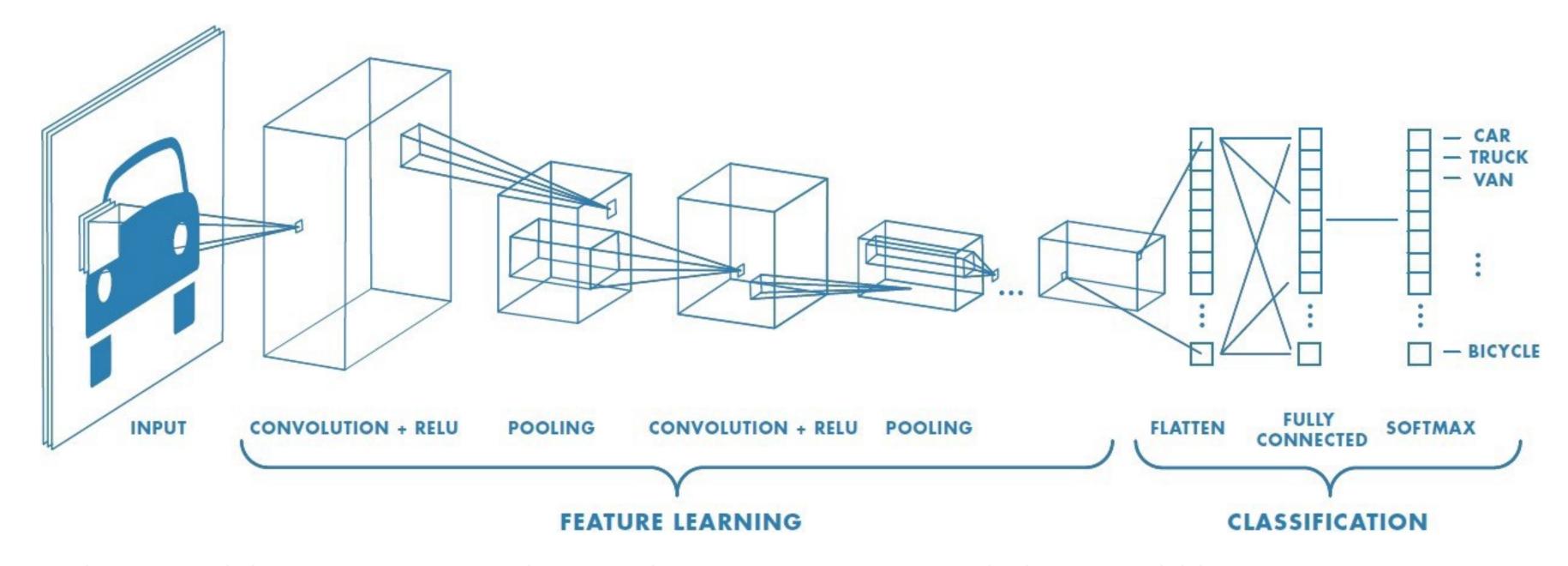
- The number of elements in a convolutional layer is still too high. We need to reduce the spatial dimension of a convolutional layer by **downsampling** it.
- For each feature, a **max-pooling** layer takes the maximum value of a feature for each subregion of the image (mostly 2x2).
- Pooling allows translation invariance: the same input pattern will be detected whatever its position in the input image.
- Max-pooling is also differentiable.

#### **Convolutional neural networks**



- A **convolutional neural network** (CNN) is a cascade of convolution and pooling operations, extracting layer by layer increasingly complex features.
- The spatial dimensions decrease after each pooling operation, but the number of extracted features increases after each convolution.
- One usually stops when the spatial dimensions are around 7x7.
- The last layers are fully connected. Can be used for regression and classification depending on the output layer and the loss function.
- Training a CNN uses backpropagation all along: the convolution and pooling operations are differentiable.

#### **Convolutional neural networks**



Source: https://towardsdatascience.com/a-comprehensive-guide-to-convolutional-neural-networks-the-eli5-way-3bd2b1164a53

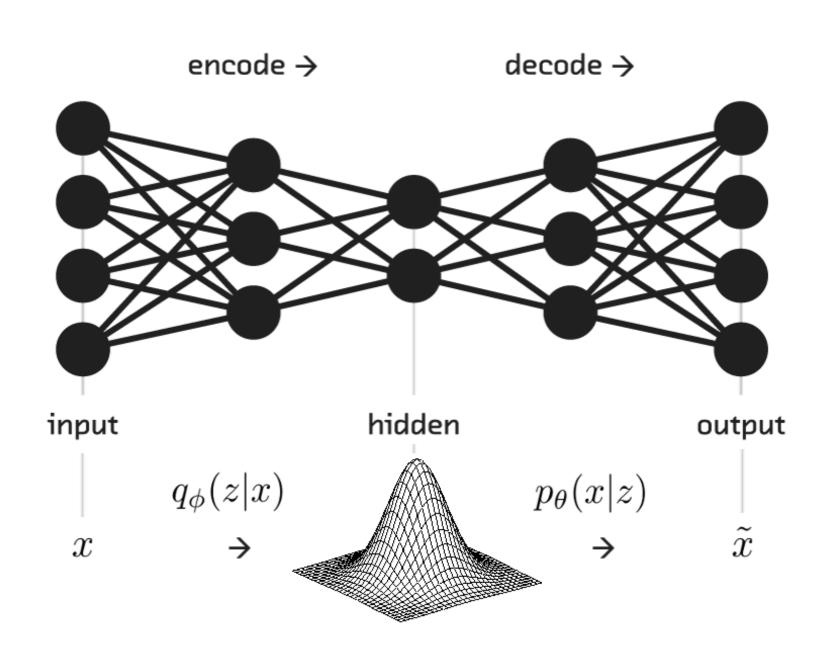
• The only thing we need to know is that CNNs are non-linear function approximators that work well with images.

$$\mathbf{y} = F_{ heta}(\mathbf{x})$$

- The conv layers extract complex features from the images through learning.
- The last FC layers allow to approximate values (regression) or probability distributions (classification).

## 3 - Autoencoders

#### Autoencoders



- The problem with FCN and CNN is that they **extract features** in supervised learning tasks.
  - Need for a lot of annotated data (image, label).
- Autoencoders allows unsupervised learning:
  - They only need inputs (images).
- Their task is to **reconstruct** the input:

$$\mathbf{y} = \mathbf{\tilde{x}} pprox \mathbf{x}$$

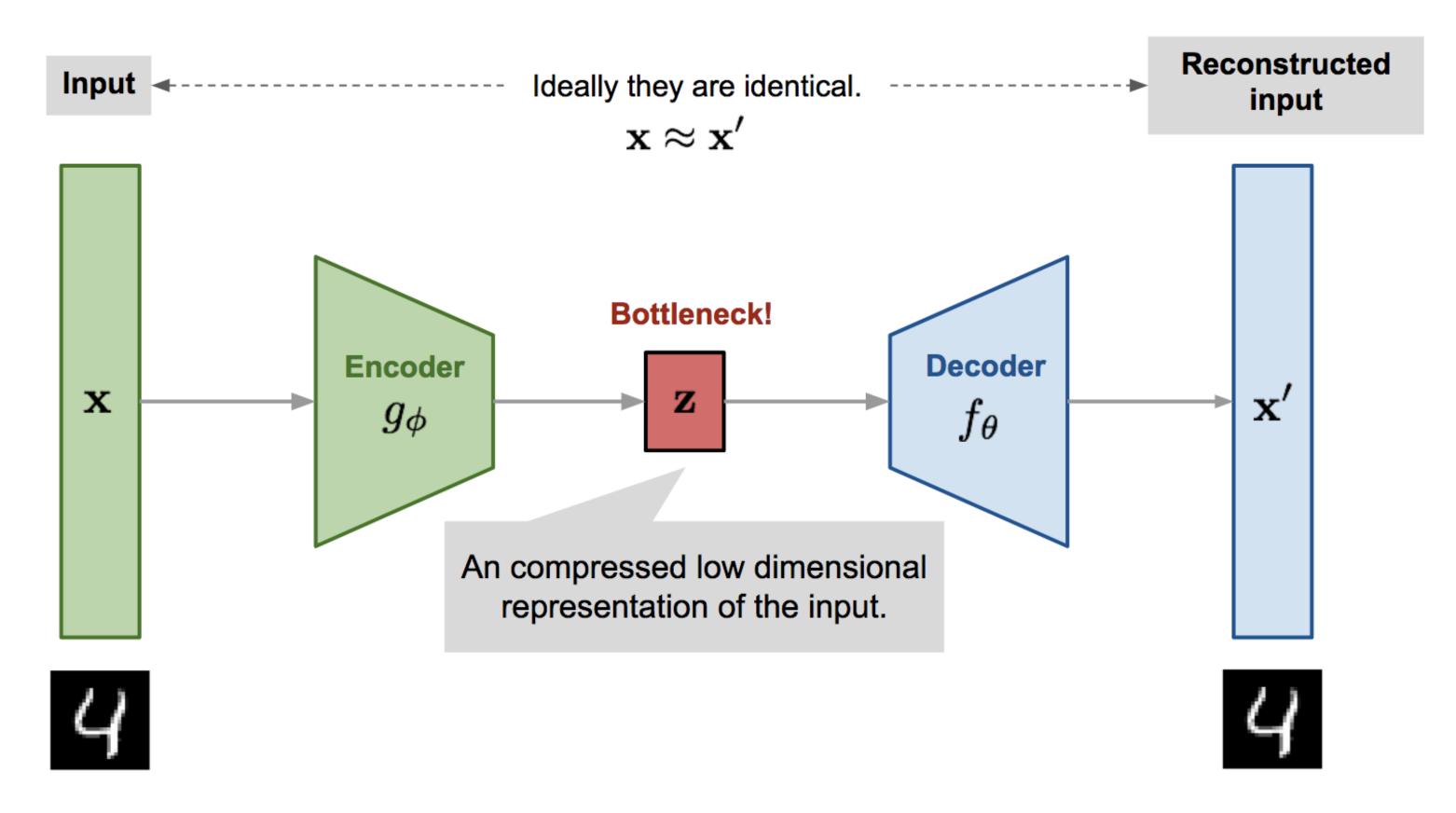
• The reconstruction loss is simply the mse between the input and its reconstruction.

$$\mathcal{L}_{ ext{autoencoder}}( heta) = \mathbb{E}_{\mathbf{x} \in \mathcal{D}}[||\mathbf{ ilde{x}} - \mathbf{x}||^2]$$

Apart from the loss function, they are trained as regular NNs.

#### Autoencoders

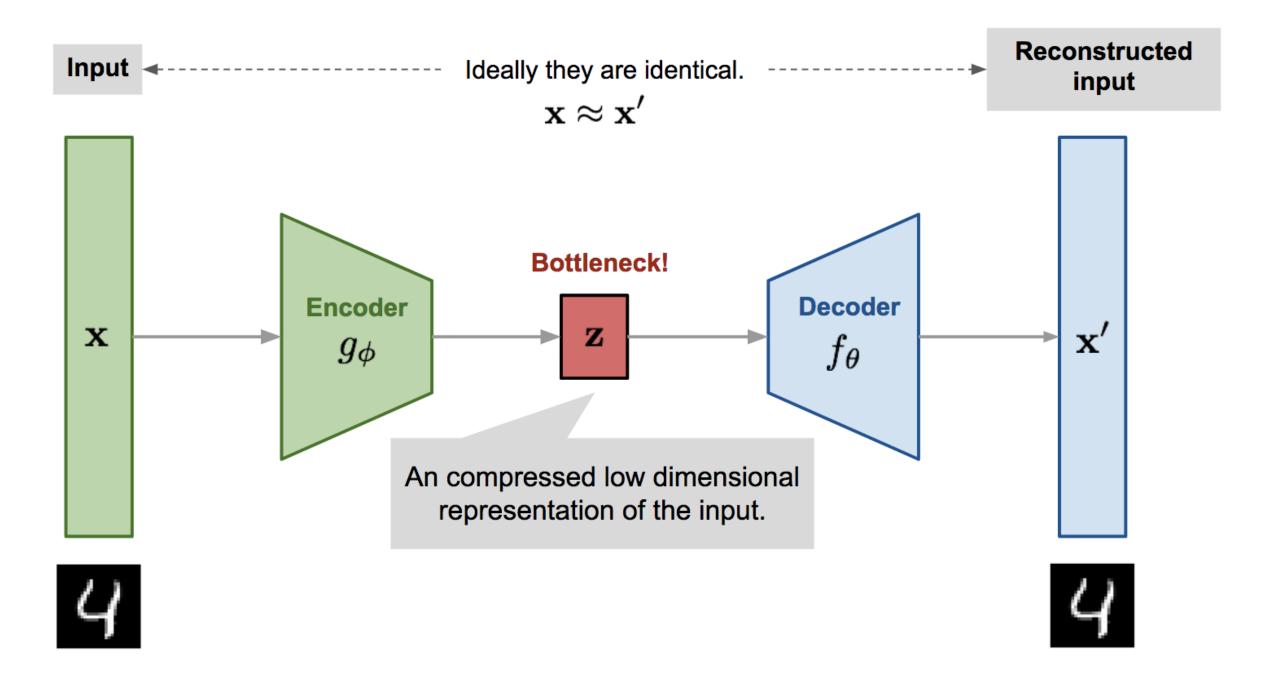
- Autoencoders consists of:
  - the **encoder**: from the input **x** to the **latent space z**.
  - the **decoder**: from the latent space z to the reconstructed input  $\tilde{x}$ .



Source: https://lilianweng.github.io/lil-log/2018/08/12/from-autoencoder-to-beta-vae.html

#### Autoencoders

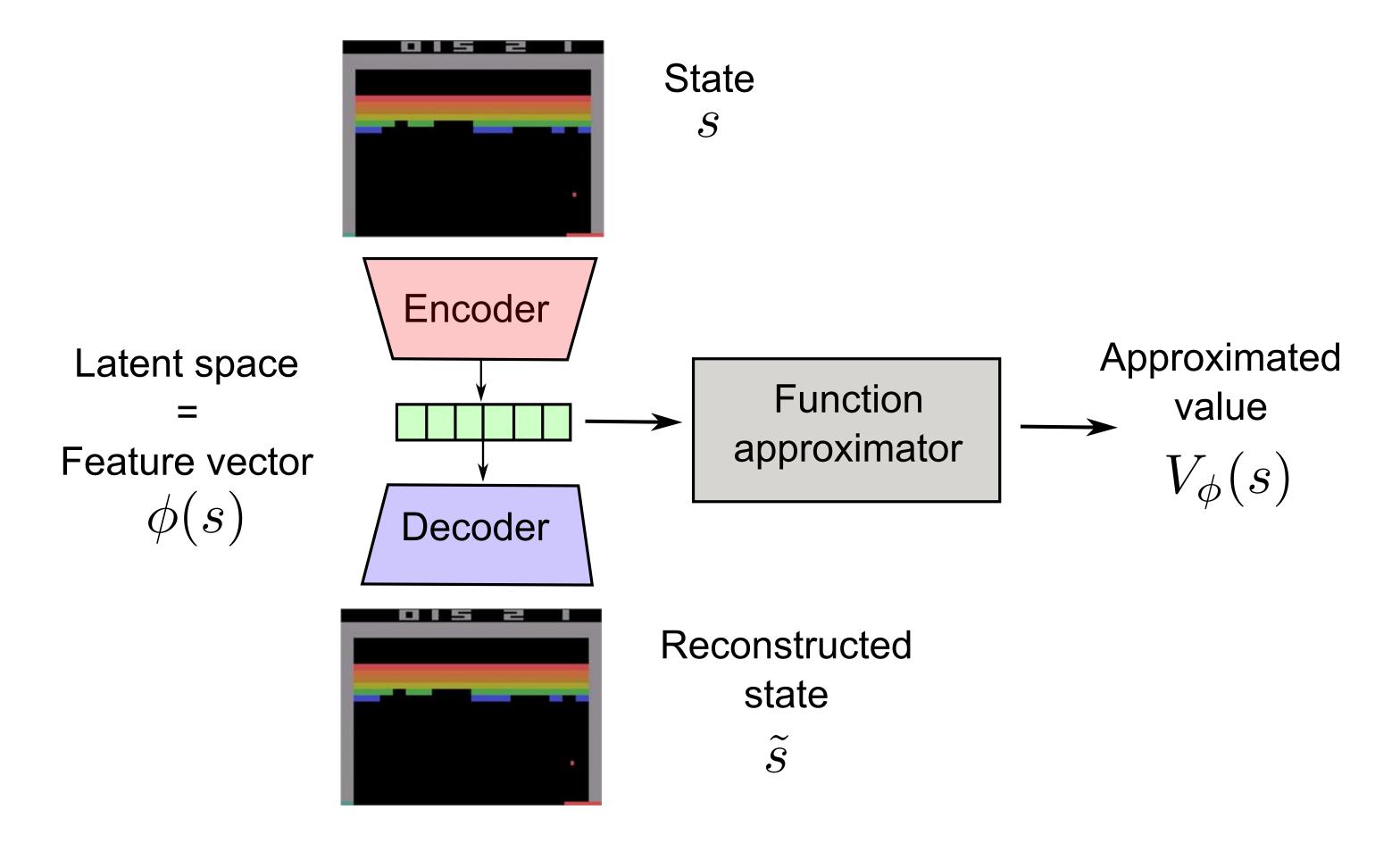
- The latent space z is a compressed representation (bottleneck) of the inputs x.
- It has to learn to compress efficiently the inputs without losing too much information, in order to reconstruct the inputs.
  - Dimensionality reduction.
  - Unsupervised feature extraction.



Source: https://lilianweng.github.io/lil-log/2018/08/12/from-autoencoder-to-beta-vae.html

### **Autoencoders in deep RL**

- In deep RL, we can construct the feature vector with an autoencoder.
- The autoencoder can be trained offline with a random agent or online with the current policy (auxiliary loss).



ullet FCN, CNN and AE are **feedforward neural networks**: they transform an input old x into an output old y:

$$\mathbf{y} = F_{ heta}(\mathbf{x})$$

• If you present a sequence of inputs  $\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_t$  to a feedforward network, the outputs will be independent from each other:

$$\mathbf{y}_0 = F_{ heta}(\mathbf{x}_0)$$

$$\mathbf{y}_1 = F_{\theta}(\mathbf{x}_1)$$

• • •

$$\mathbf{y}_t = F_{ heta}(\mathbf{x}_t)$$

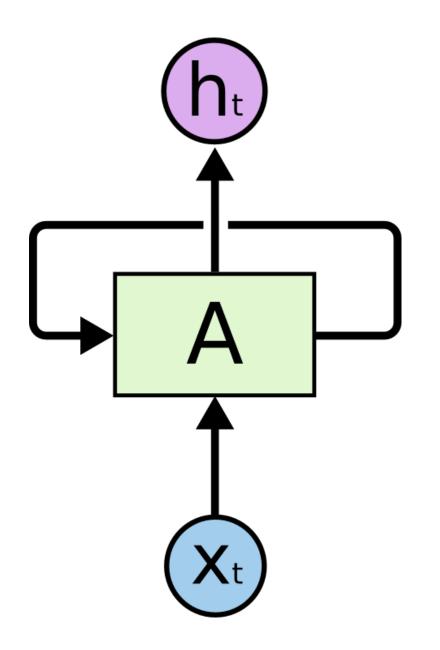
• The output  $\mathbf{y}_t$  does **not** depend on the history of inputs  $\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_{t-1}$ .

- This not always what you want.
- ullet If your inputs are frames of a video, the correct response at time t might also depend on previous frames.



Source: https://srirangatarun.wordpress.com/2018/07/09/video-frame-prediction-with-keras/

- The task of the NN could be to explain what happens at each frame.
- As we saw, a single frame is often not enough to predict the future (Markov property).

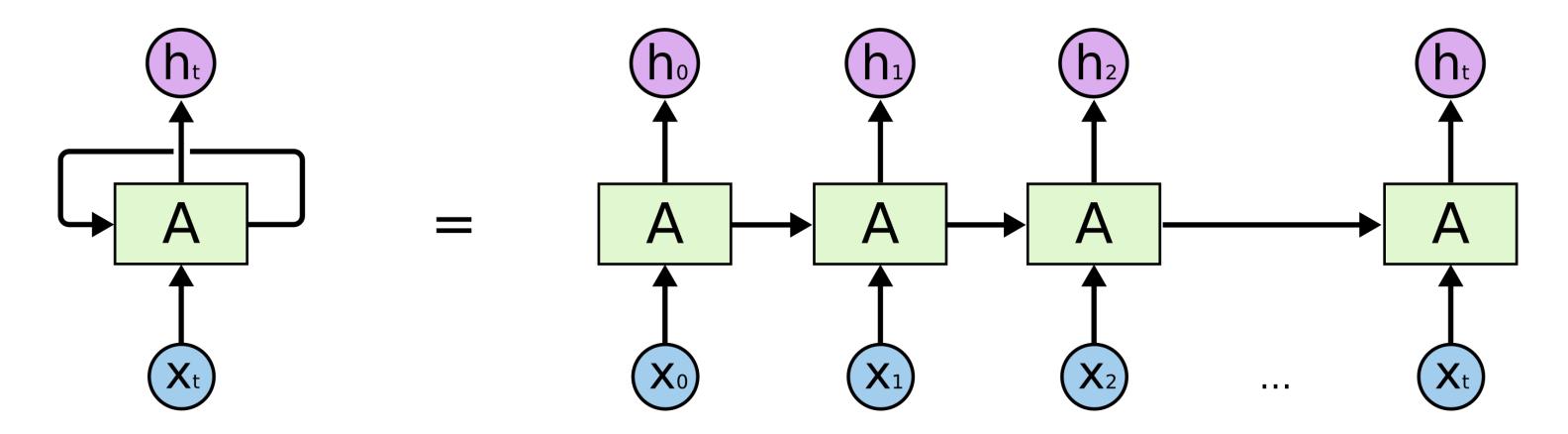


- A recurrent neural network (RNN) uses it previous output as an additional input (context).
- ullet All vectors have a time index t denoting the time at which this vector was computed.
- The input vector at time t is  $\mathbf{x}_t$ , the output vector is  $\mathbf{h}_t$ :

$$\mathbf{h}_t = f(W_x imes \mathbf{x}_t + W_h imes \mathbf{h}_{t-1} + \mathbf{b})$$

Source: C. Olah

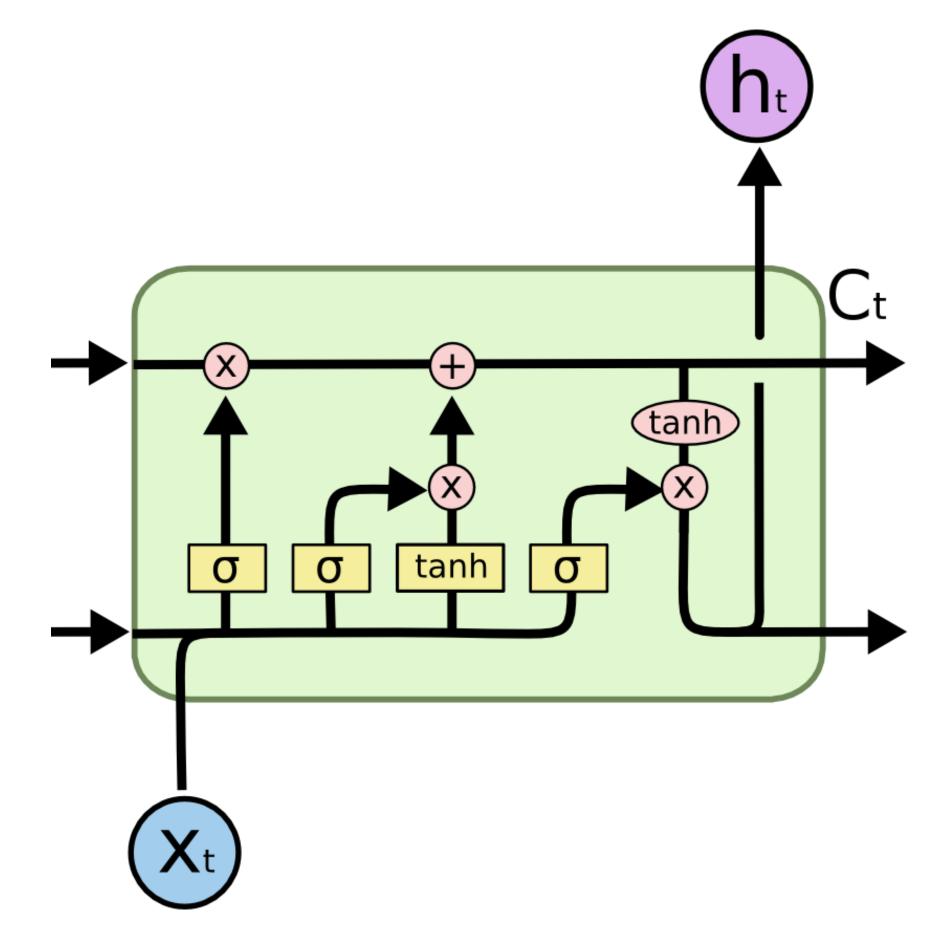
- The input  $\mathbf{x}_t$  and previous output  $\mathbf{h}_{t-1}$  are multiplied by **learnable weights**:
  - ullet  $W_x$  is the input weight matrix.
  - $W_h$  is the recurrent weight matrix.



Source: C. Olah

- This is equivalent to a deep neural network taking the whole history  $\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_t$  as inputs, but reusing weights between two time steps.
- The weights are trainable using **backpropagation through time** (BPTT).
- A RNN can learn the **temporal dependencies** between inputs.

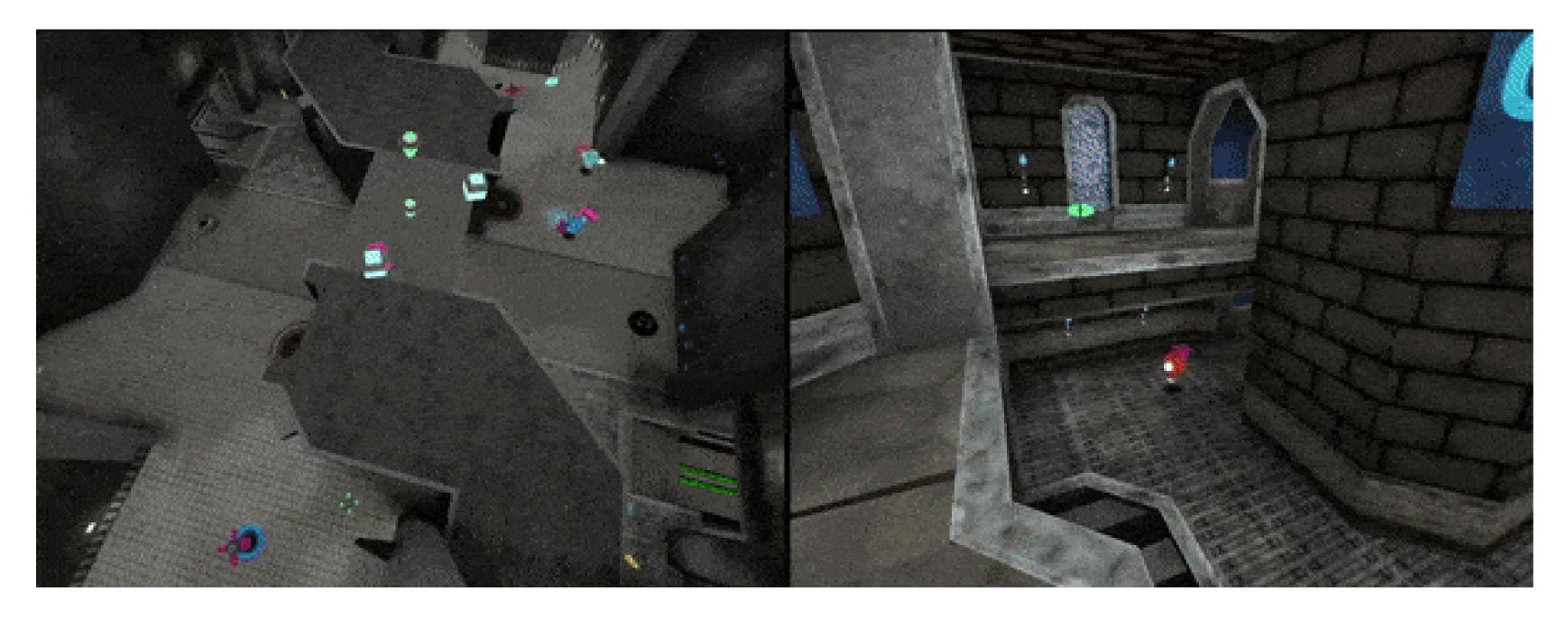
#### LSTM cell



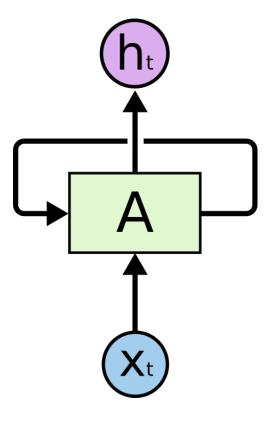
Source: C. Olah

- A popular variant of RNN is LSTM (long short-term memory).
- In addition to the input  $\mathbf{x}_t$  and output  $\mathbf{h}_t$ , it also has a **state** (or **memory** or **context**)  $\mathbf{C}_t$  which is maintained over time.
- It also contains three multiplicative gates:
  - The **input gate** controls which inputs should enter the memory.
  - The **forget gate** controls which memory should be forgotten.
  - The output gate controls which part of the memory should be used to produce the output.

#### RNN in RL



Source: https://deepmind.com/blog/article/capture-the-flag-science



- An obvious use case of RNNs in deep RL is for POMDP (partially observable MDP).
- If the individual states  $s_t$  do not have the Markov property, the output of a LSTM does:
  - The output of the RNN is a representation of the complete history  $s_0, s_1, \ldots, s_t.$
- We can apply RL on the output of a RNN and solve POMDPs for free!