

Deep Reinforcement Learning

Deep learning

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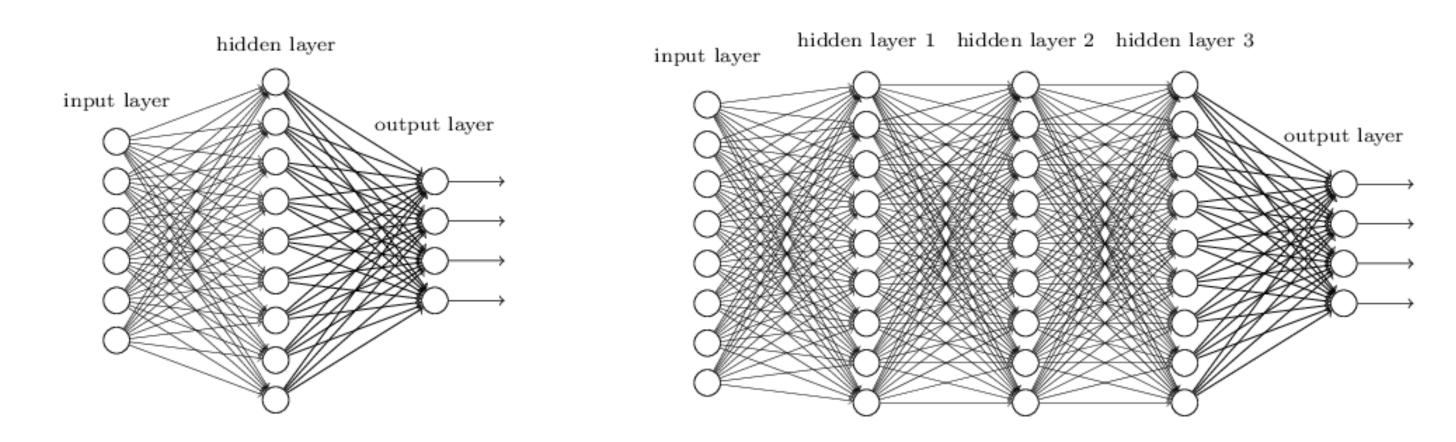
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https://tu-chemnitz.de/informatik/KI/edu/deeprl

1 - Artificial neural networks

Artificial neural networks

• An artificial neural network (ANN) is a cascade of fully-connected (FC) layers of artificial neurons.



• Each layer k transforms an input vector \mathbf{h}_{k-1} into an output vector \mathbf{h}_k using a weight matrix W_k , a bias vector \mathbf{b}_k and an activation function f().

$$\mathbf{h}_k = f(W_k imes \mathbf{h}_{k-1} + \mathbf{b}_k)$$

• Overall, ANNs are **non-linear parameterized function estimators** from the inputs x to the outputs y with parameters θ (all weight matrices and biases).

$$\mathbf{y} = F_{ heta}(\mathbf{x})$$

Loss functions

- ANNs can be used for both regression (continuous outputs) and classification (discrete outputs) tasks.
- In supervised learning, we have a fixed training set \mathcal{D} of N samples $(\mathbf{x}_t, \mathbf{t}_i)$, where t_i is the desired output or target.
- Regression:
 - ullet The output layer uses a **linear** activation function: f(x)=x
 - The network minimizes the **mean square error** (mse) of the model on the training set:

$$\mathcal{L}(heta) = \mathbb{E}_{\mathbf{x}, \mathbf{t} \in \mathcal{D}}[||\mathbf{t} - \mathbf{y}||^2]$$

- Classification:
 - The output layer uses the **softmax** operator to produce a probabilty distribution: $y_j = rac{e^{z_j}}{\sum_k e^{z_k}}$
 - The network minimizes the **cross-entropy** or **negative log-likelihood** of the model on the training set:

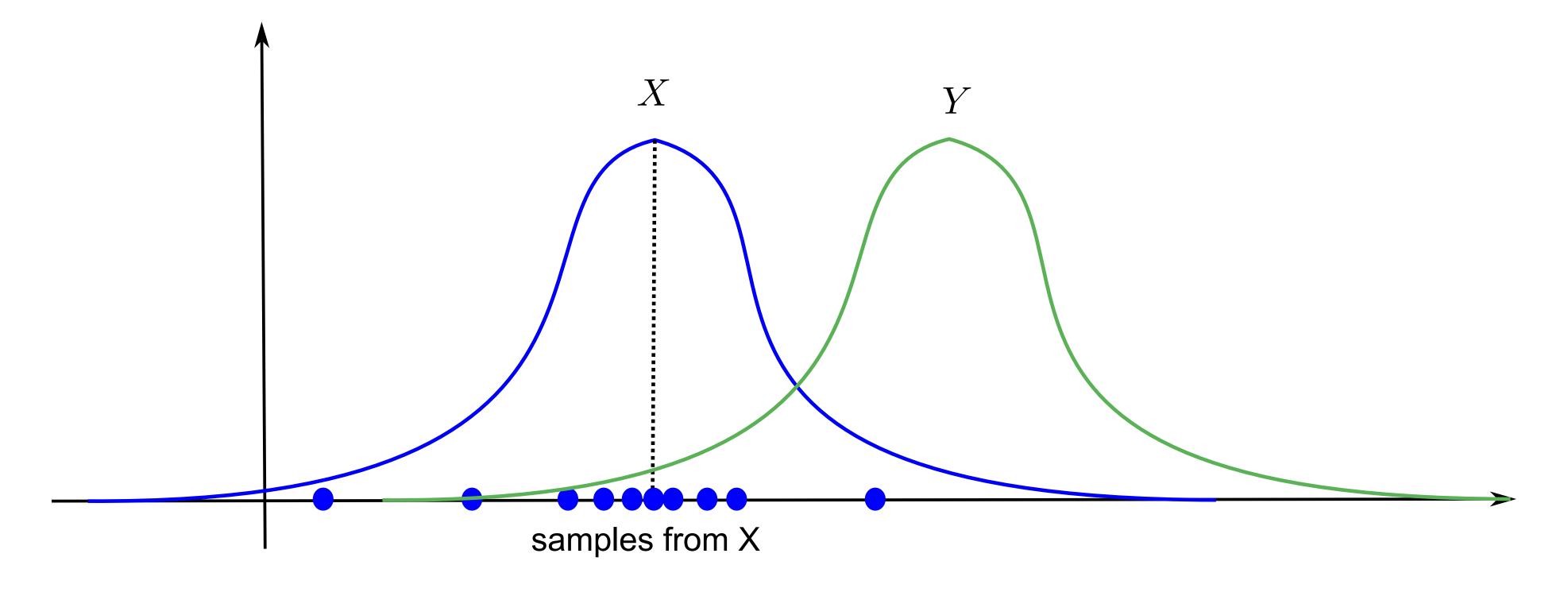
$$\mathcal{L}(heta) = \mathbb{E}_{\mathbf{x}, \mathbf{t} \in \mathcal{D}}[-\mathbf{t} \, \log \mathbf{y}]$$

Cross-entropy

ullet The cross-entropy between two probability distributions X and Y measures their similarity:

$$H(X,Y) = \mathbb{E}_{x\sim X}[-\log P(Y=x)]$$

- ullet Are samples from X likely under Y?
- Minimizing the cross-entropy makes the two distributions equal almost anywhere.

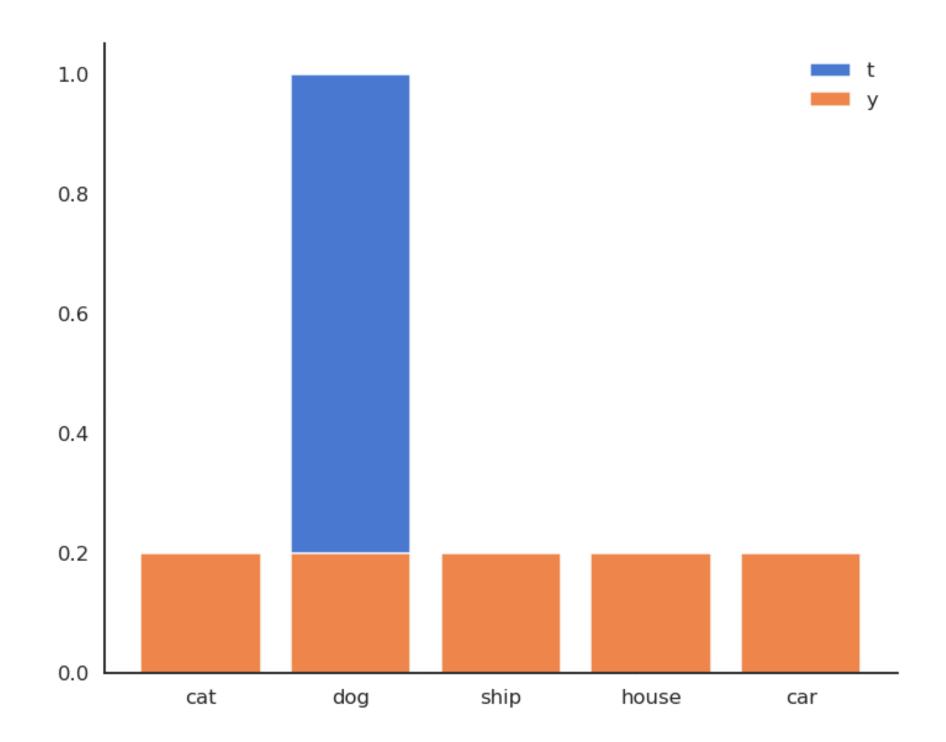


Cross-entropy

ullet In supervised learning, the targets ${f t}$ are fixed **one-hot encoded vectors**.

$$\mathcal{L}(heta) = \mathbb{E}_{\mathbf{x},\mathbf{t}\in\mathcal{D}}[-\sum_{j}t_{j}\,\log y_{j}]$$

But it could be any target distribution.



Backpropagation

• In both cases, we want to minimize the loss variant by applying **Stochastic Gradient Descent** (SGD) or a variant (Adam, RMSprop).

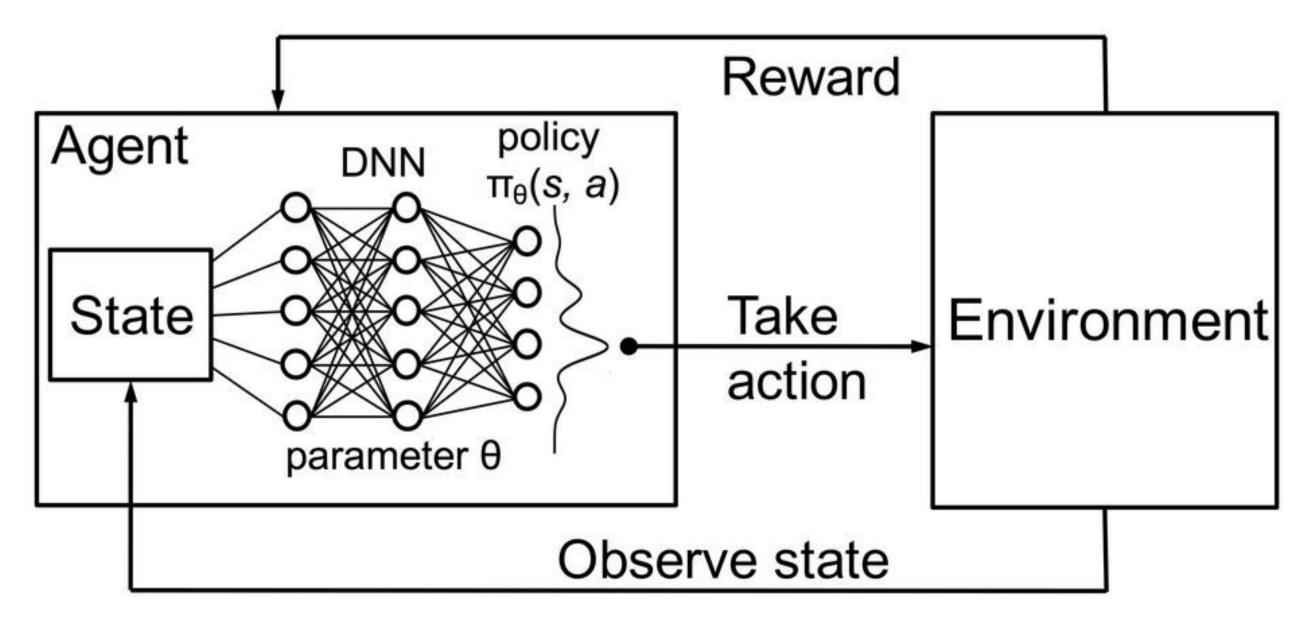
$$\Delta heta = -\eta \,
abla_{ heta} \mathcal{L}(heta)$$

- The question is how to compute the **gradient of the loss function** w.r.t the parameters θ .
- For both the mse and cross-entropy loss functions, we have:

$$abla_{ heta} \mathcal{L}(heta) = \mathbb{E}_{\mathcal{D}}[-(\mathbf{t} - \mathbf{y}) \,
abla_{ heta} \, \mathbf{y}]$$

- There is an algorithm to compute efficiently the gradient of the output w.r.t the parameters: **backpropagation** (see Neurocomputing).
- In deep RL, we do not care about backprop: tensorflow or pytorch do it for us.

Components of neural networks

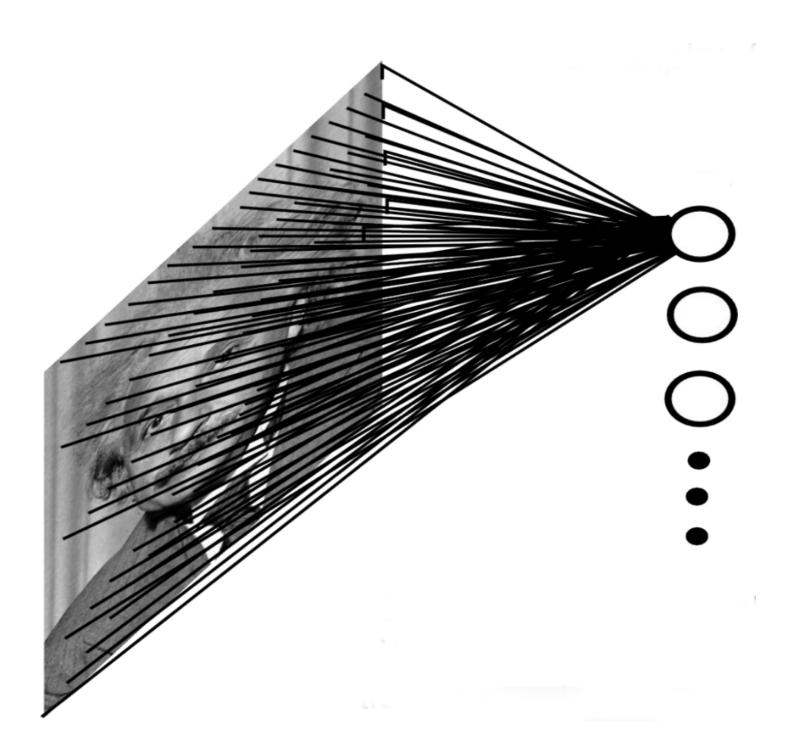


- There are three aspects to consider when building a neural network:
- 1. Architecture: how many layers, what type of layers, how many neurons, etc.
 - Task-dependent: each RL task will require a different architecture. Not our focus.
- 2. Loss function: what should the network do?
 - Central to deep RL!
- 3. **Update rule** how should we update the parameters θ to minimize the loss function? SGD, backprop.
 - Not really our problem, but see natural gradients later.

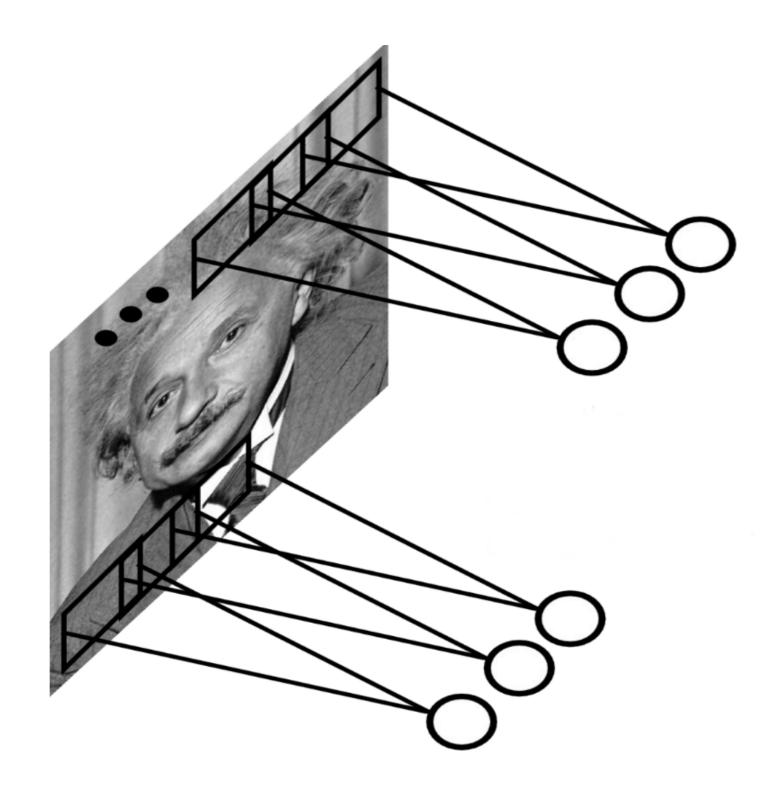
2 - Convolutional neural networks

Convolutional layers

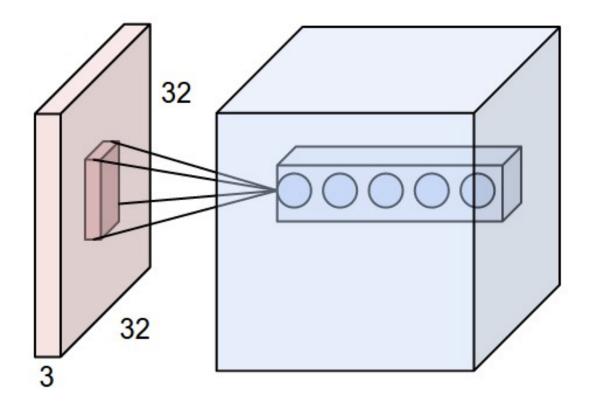
- When using images as inputs, **fully-connected networks** (FCN) would have too many weights:
 - Slow.
 - Overfitting.

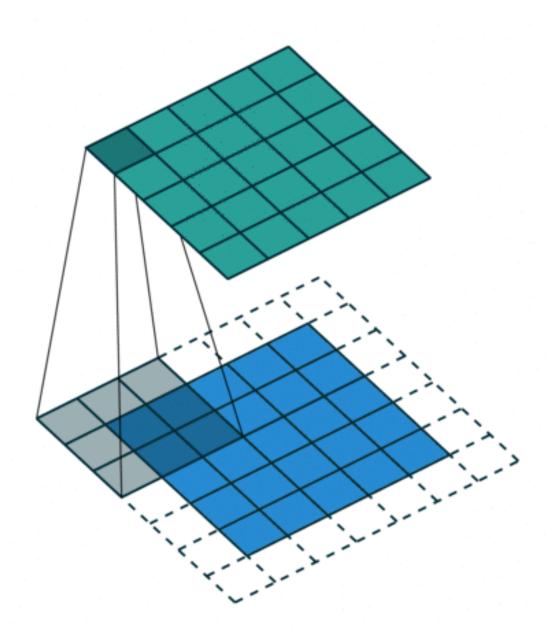


- Convolutional layers reduce the number of weights by reusing weights at different locations.
 - Principle of a convolution.
 - Fast and efficient.



Convolutional layers

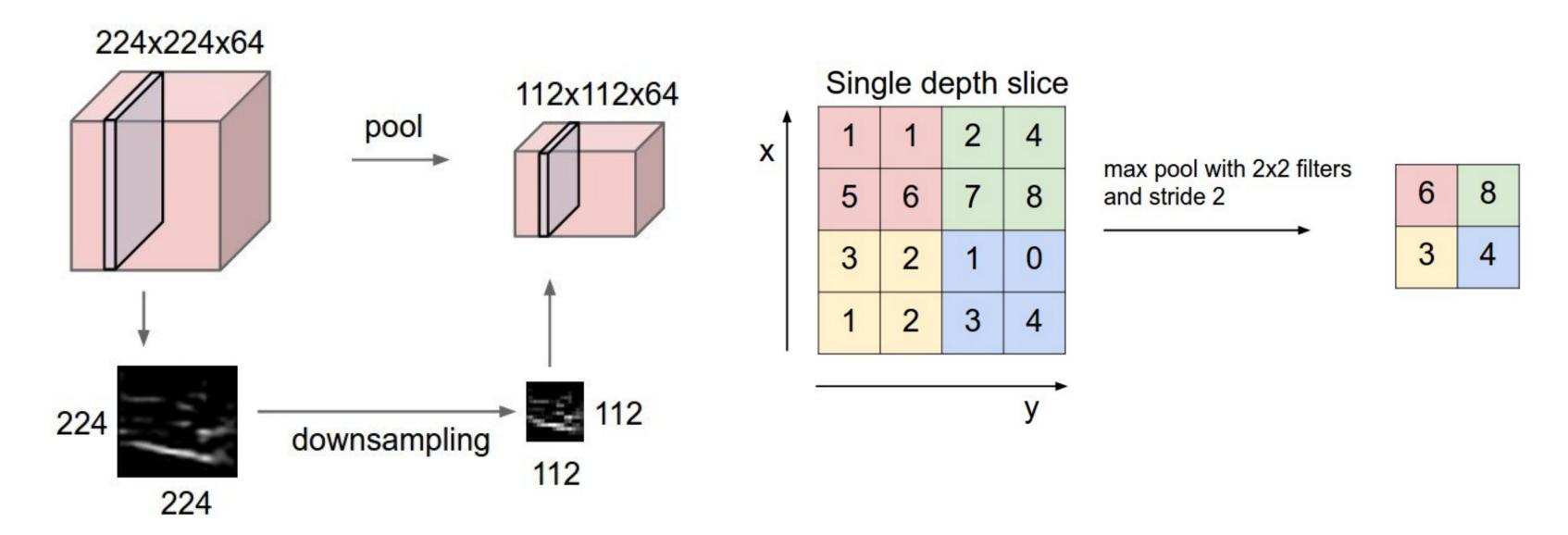




- A convolutional layer extracts features of its inputs.
- d filters are defined with very small sizes (3x3, 5x5...).
- Each filter is convoluted over the input image (or the previous layer) to create a **feature map**.
- The set of d feature maps becomes a new 3D structure: a **tensor**.
- If the input image is 32x32x3, the resulting tensor will be 32x32xd.
- The convolutional layer has only very few parameters: each feature map has 3x3 values in the filter and a bias, i.e. 10 parameters.
- The convolution operation is differentiable: backprop will work.

Source: https://github.com/vdumoulin/conv_arithmetic

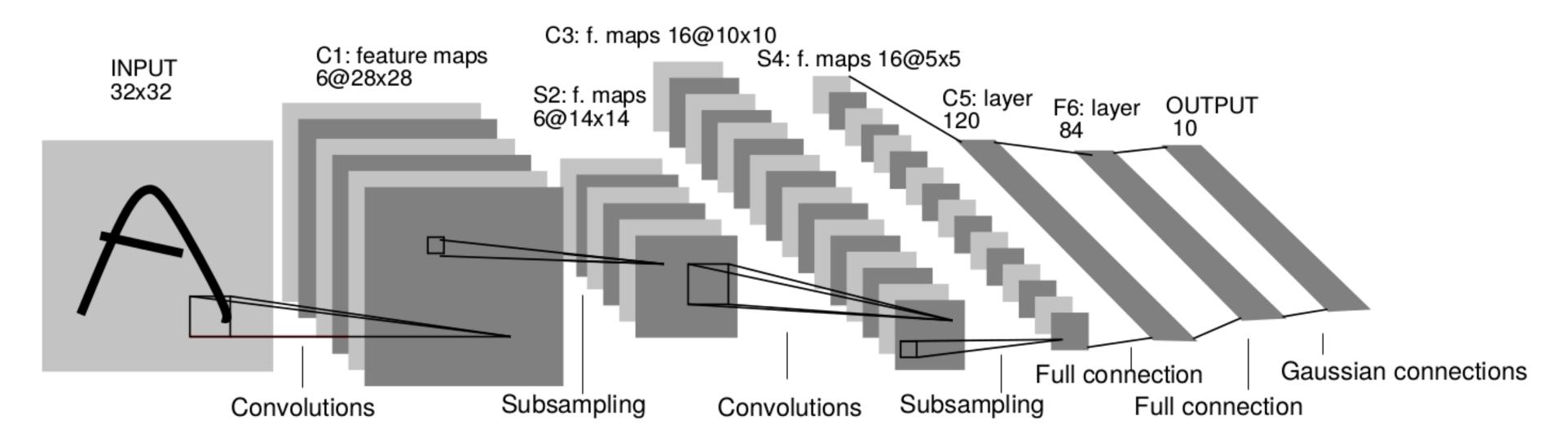
Max-pooling



Source: http://cs231n.github.io/convolutional-networks/

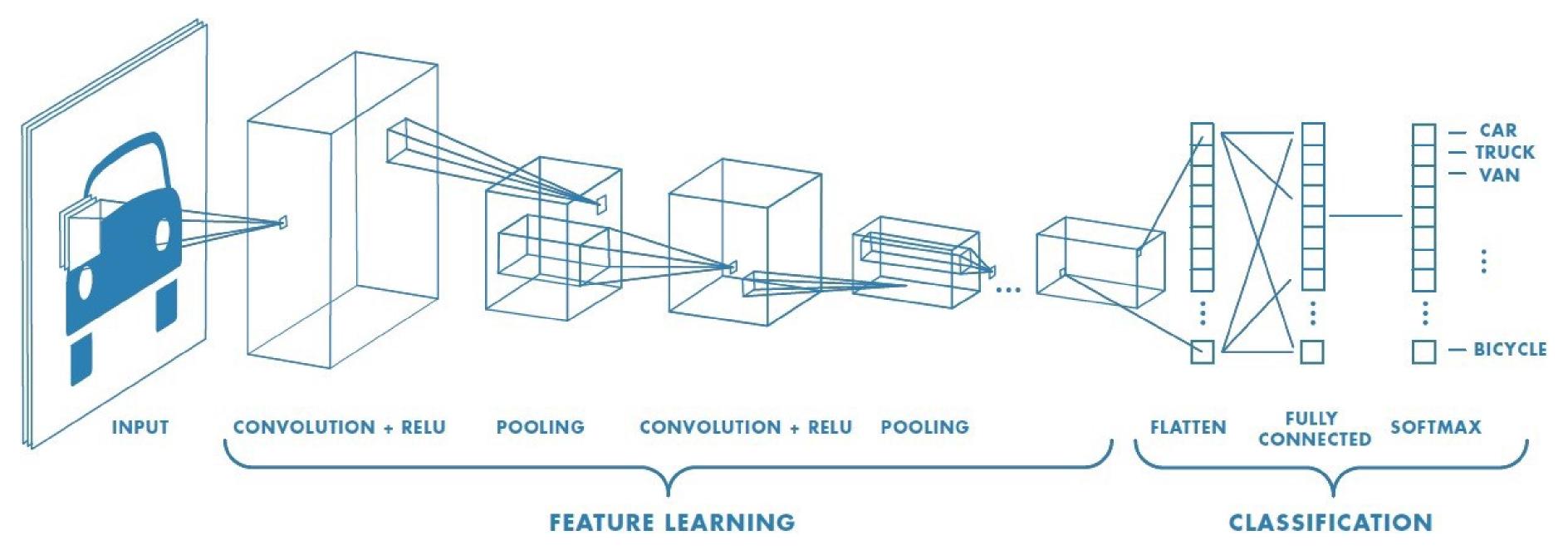
- The number of elements in a convolutional layer is still too high. We need to reduce the spatial dimension of a convolutional layer by **downsampling** it.
- For each feature, a **max-pooling** layer takes the maximum value of a feature for each subregion of the image (mostly 2x2).
- Pooling allows translation invariance: the same input pattern will be detected whatever its position in the input image.
- Max-pooling is also differentiable.

Convolutional neural networks



- A convolutional neural network (CNN) is a cascade of convolution and pooling operations, extracting layer by layer increasingly complex features.
- The spatial dimensions decrease after each pooling operation, but the number of extracted features increases after each convolution.
- One usually stops when the spatial dimensions are around 7x7.
- The last layers are fully connected. Can be used for regression and classification depending on the output layer and the loss function.
- Training a CNN uses backpropagation all along: the convolution and pooling operations are differentiable.

Convolutional neural networks



Source: https://towardsdatascience.com/a-comprehensive-guide-to-convolutional-neural-networks-the-eli5-way-3bd2b1164a53

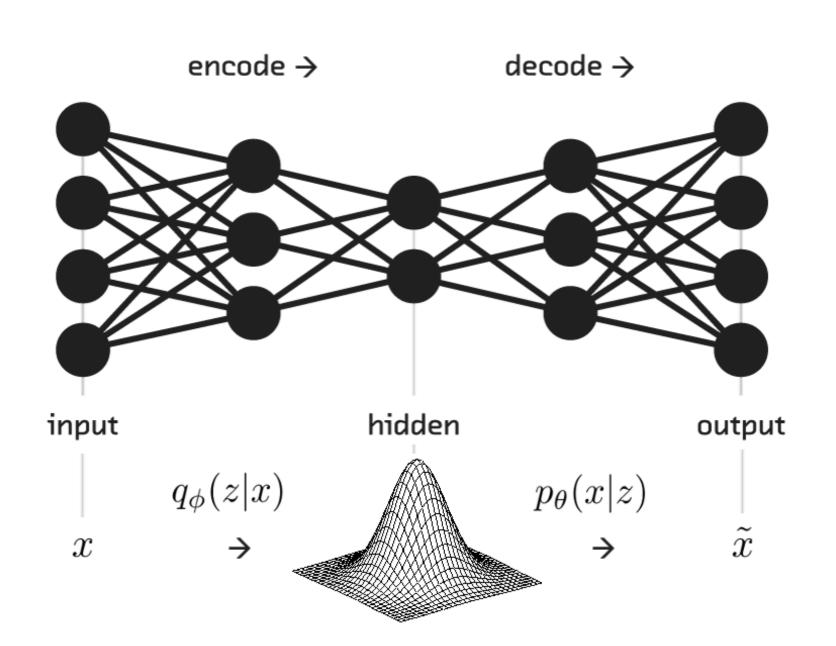
• The only thing we need to know is that CNNs are non-linear function approximators that work well with images.

$$\mathbf{y} = F_{ heta}(\mathbf{x})$$

- The conv layers extract complex features from the images through learning.
- The last FC layers allow to approximate values (regression) or probability distributions (classification).

3 - Autoencoders

Autoencoders



- The problem with FCN and CNN is that they extract features in supervised learning tasks.
 - Need for a lot of annotated data (image, label).
- Autoencoders allows unsupervised learning:
 - They only need inputs (images).
- Their task is to **reconstruct** the input:

$$\mathbf{y} = \mathbf{\tilde{x}} pprox \mathbf{x}$$

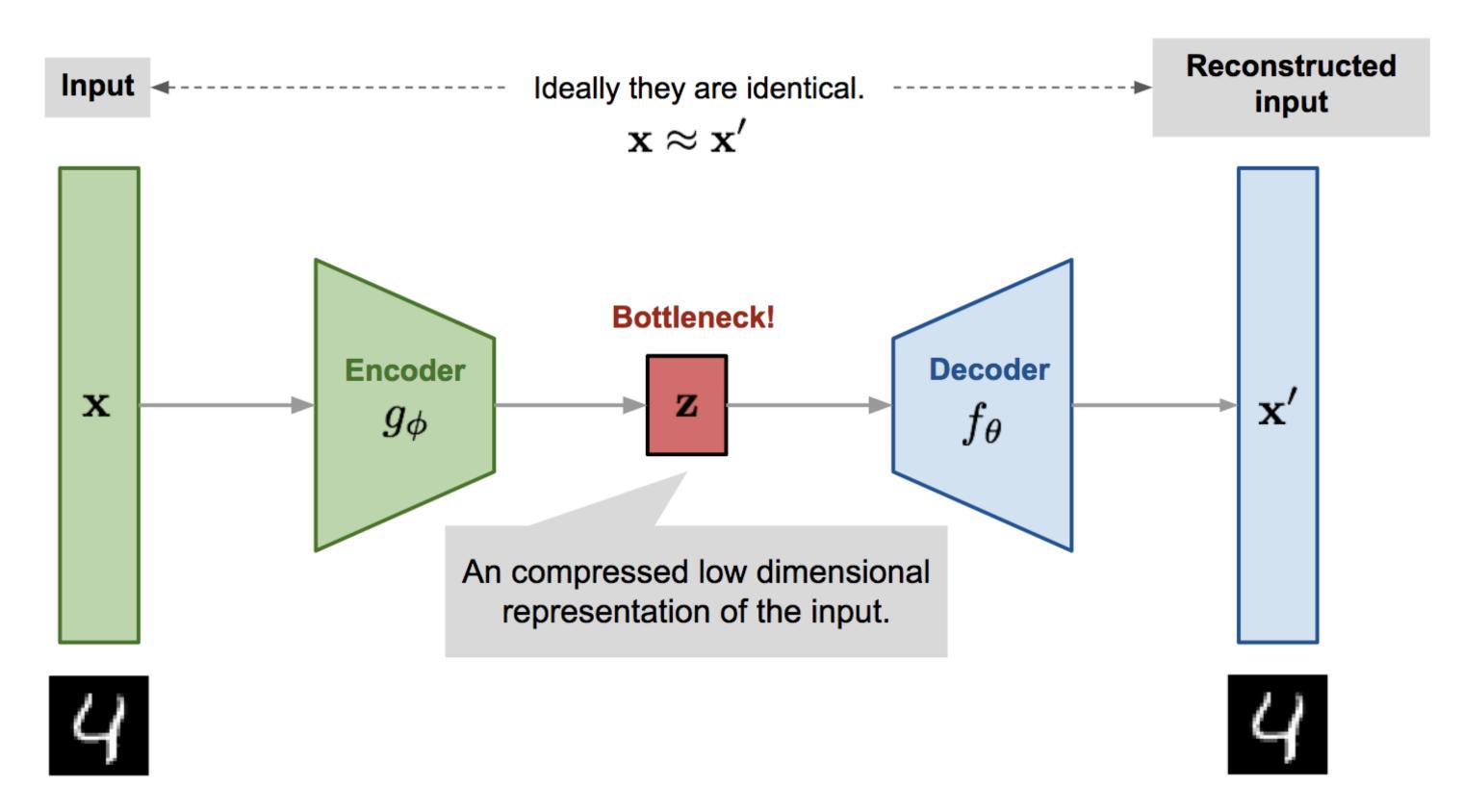
• The reconstruction loss is simply the mse between the input and its reconstruction.

$$\mathcal{L}_{ ext{autoencoder}}(heta) = \mathbb{E}_{\mathbf{x} \in \mathcal{D}}[||\mathbf{ ilde{x}} - \mathbf{x}||^2]$$

Apart from the loss function, they are trained as regular NNs.

Autoencoders

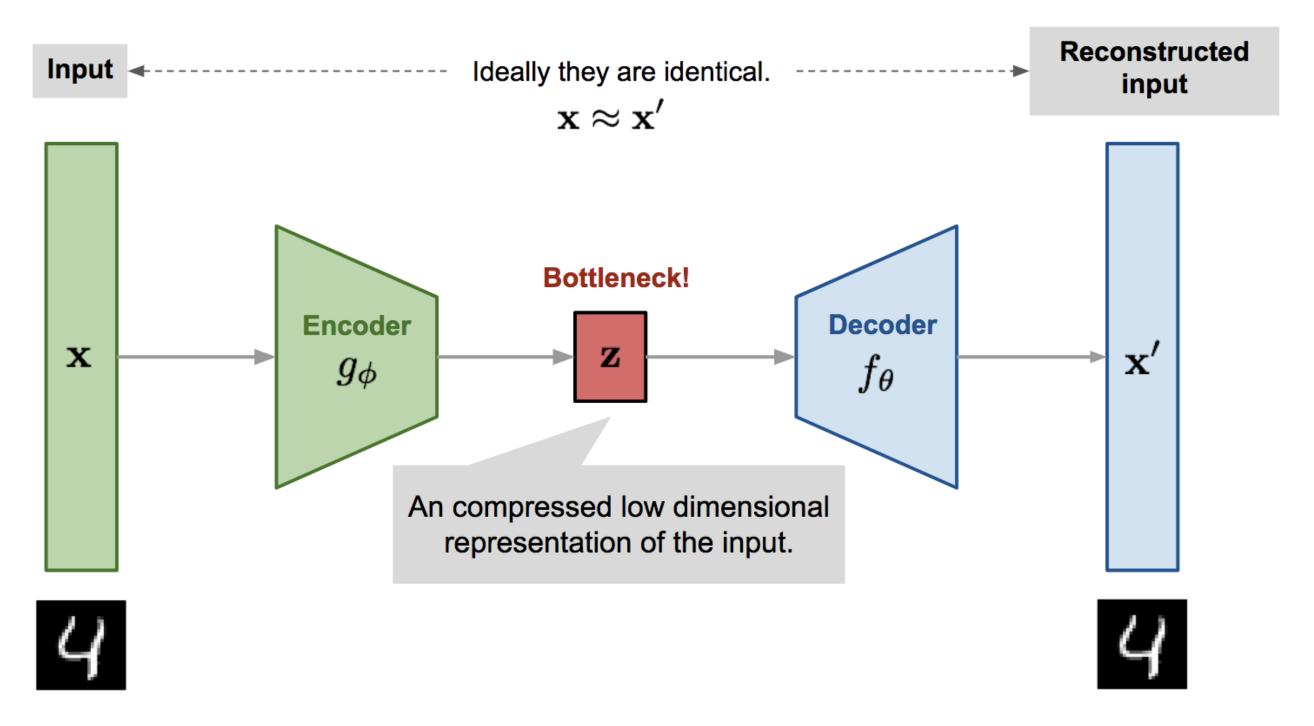
- Autoencoders consists of:
 - the **encoder**: from the input **x** to the **latent space z**.
 - the **decoder**: from the latent space z to the reconstructed input \tilde{x} .



Source: https://lilianweng.github.io/lil-log/2018/08/12/from-autoencoder-to-beta-vae.html

Autoencoders

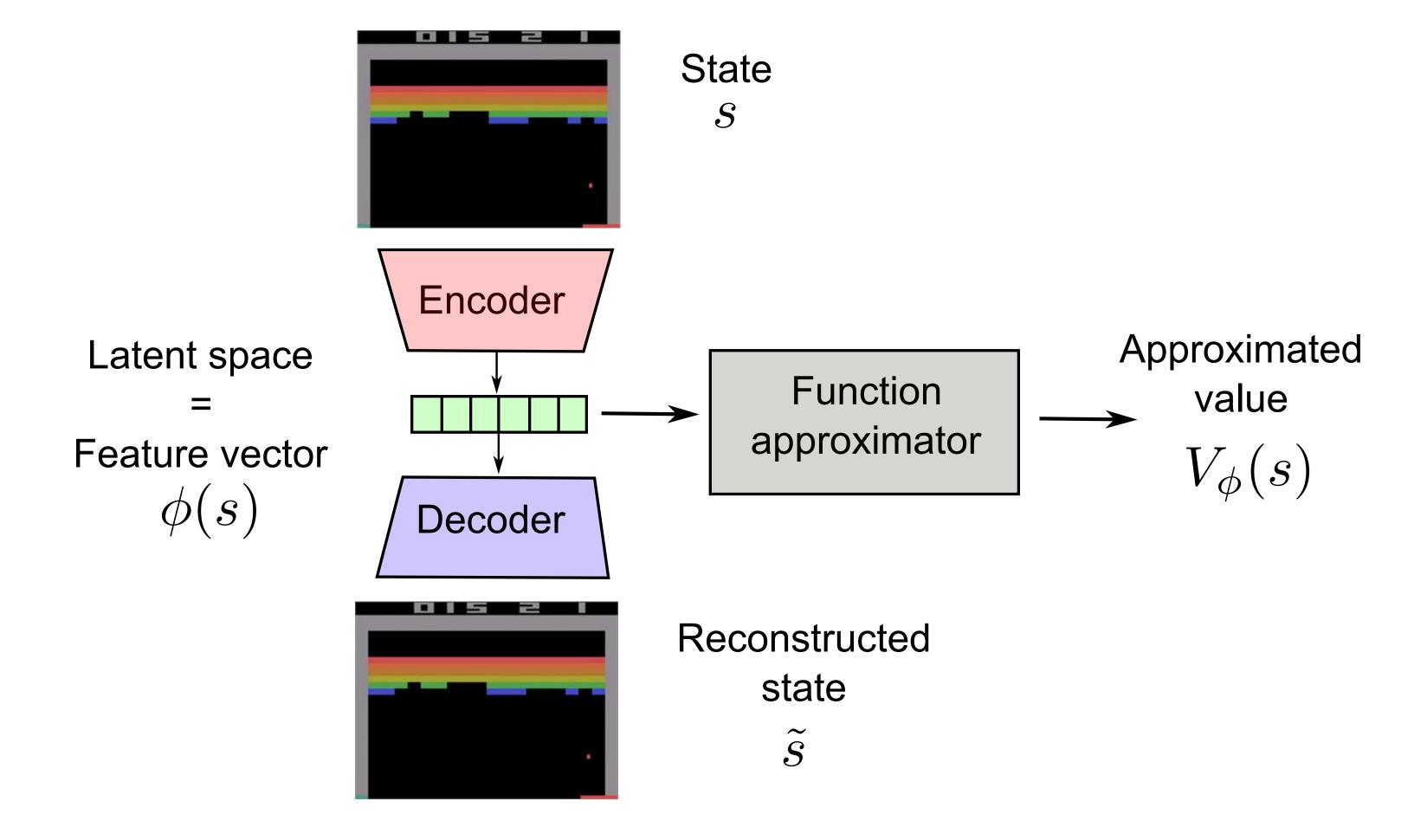
- The latent space z is a compressed representation (bottleneck) of the inputs x.
- It has to learn to compress efficiently the inputs without losing too much information, in order to reconstruct the inputs.
 - Dimensionality reduction.
 - Unsupervised feature extraction.



Source: https://lilianweng.github.io/lil-log/2018/08/12/from-autoencoder-to-beta-vae.html

Autoencoders in deep RL

- In deep RL, we can construct the feature vector with an autoencoder.
- The autoencoder can be trained offline with a random agent or online with the current policy (auxiliary loss).



ullet FCN, CNN and AE are **feedforward neural networks**: they transform an input ${f x}$ into an output ${f y}$:

$$\mathbf{y} = F_{ heta}(\mathbf{x})$$

• If you present a sequence of inputs $\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_t$ to a feedforward network, the outputs will be independent from each other:

$$\mathbf{y}_0 = F_{ heta}(\mathbf{x}_0)$$

$$\mathbf{y}_1 = F_{ heta}(\mathbf{x}_1)$$

• • •

$$\mathbf{y}_t = F_{ heta}(\mathbf{x}_t)$$

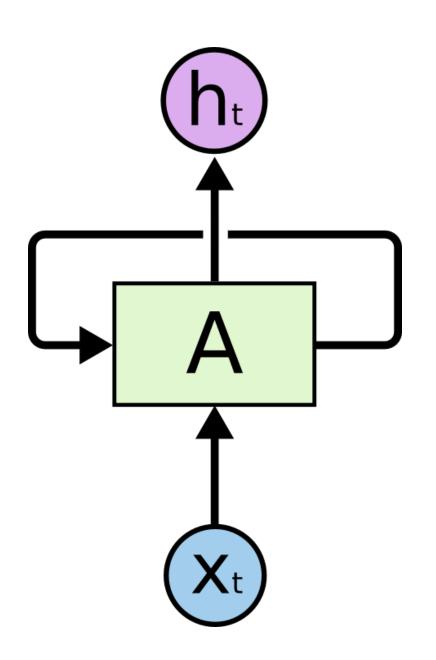
• The output \mathbf{y}_t does **not** depend on the history of inputs $\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_{t-1}$.

- This not always what you want.
- ullet If your inputs are frames of a video, the correct response at time t might also depend on previous frames.



Source: https://srirangatarun.wordpress.com/2018/07/09/video-frame-prediction-with-keras/

- The task of the NN could be to explain what happens at each frame.
- As we saw, a single frame is often not enough to predict the future (Markov property).

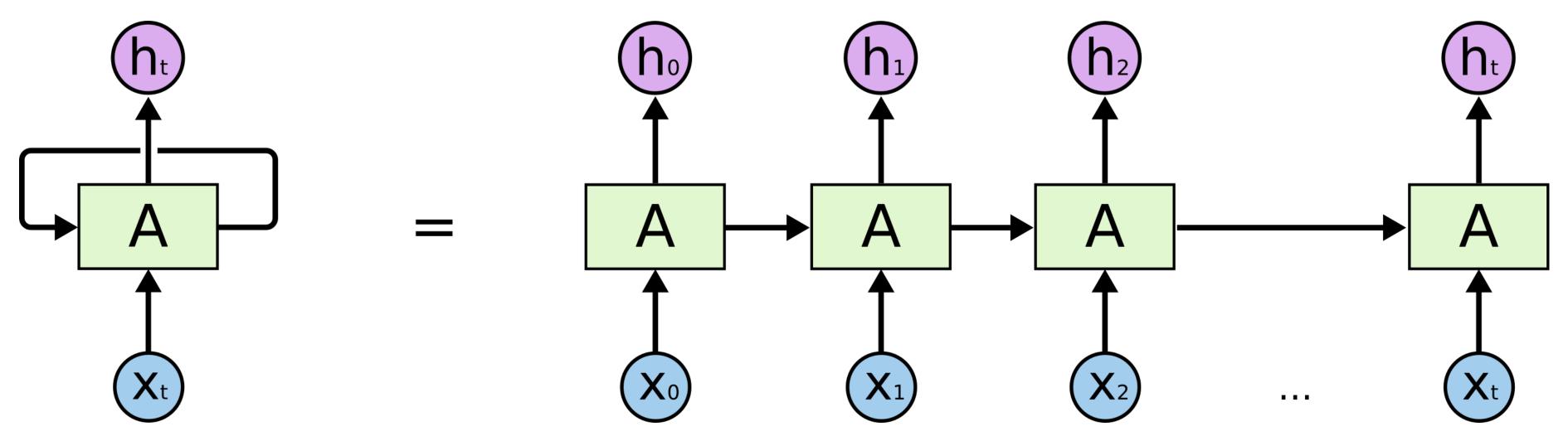


- A **recurrent neural network** (RNN) uses it previous output as an additional input (*context*).
- ullet All vectors have a time index t denoting the time at which this vector was computed.
- ullet The input vector at time t is \mathbf{x}_t , the output vector is \mathbf{h}_t :

$$\mathbf{h}_t = f(W_x imes \mathbf{x}_t + W_h imes \mathbf{h}_{t-1} + \mathbf{b})$$

Source: C. Olah

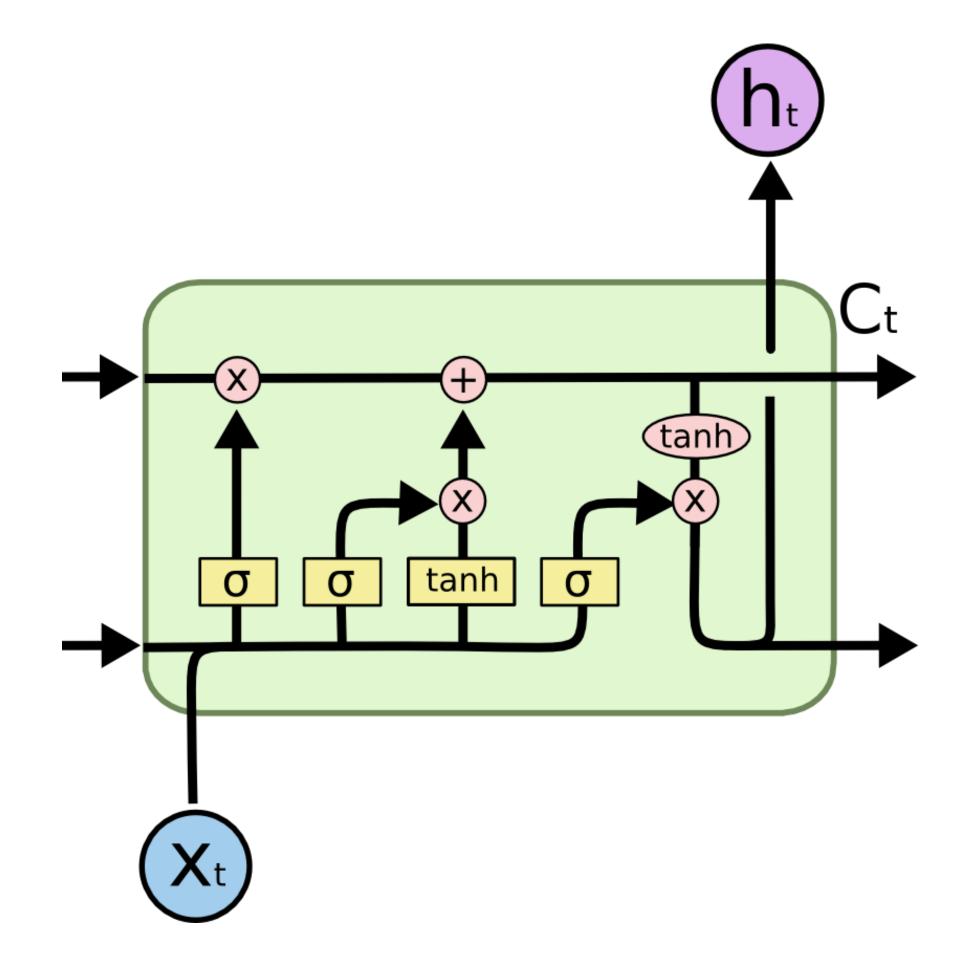
- The input \mathbf{x}_t and previous output \mathbf{h}_{t-1} are multiplied by **learnable weights**:
 - ullet W_x is the input weight matrix.
 - W_h is the recurrent weight matrix.



Source: C. Olah

- This is equivalent to a deep neural network taking the whole history $\mathbf{x}_0, \mathbf{x}_1, \dots, \mathbf{x}_t$ as inputs, but reusing weights between two time steps.
- The weights are trainable using backpropagation through time (BPTT).
- A RNN can learn the **temporal dependencies** between inputs.

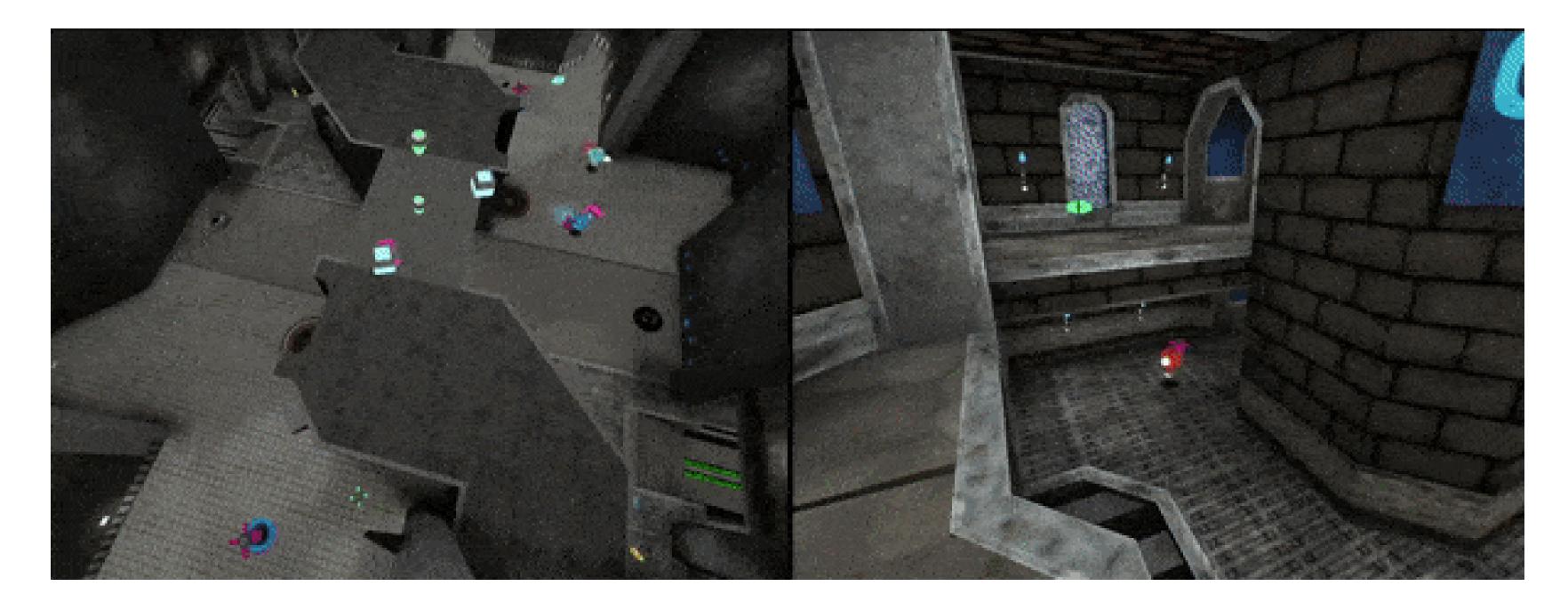
LSTM cell



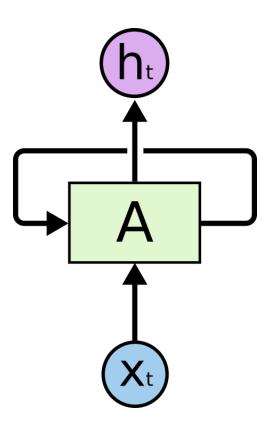
Source: C. Olah

- A popular variant of RNN is LSTM (long short-term memory).
- In addition to the input \mathbf{x}_t and output \mathbf{h}_t , it also has a **state** (or **memory** or **context**) \mathbf{C}_t which is maintained over time.
- It also contains three multiplicative gates:
 - The input gate controls which inputs should enter the memory.
 - The forget gate controls which memory should be forgotten.
 - The output gate controls which part of the memory should be used to produce the output.

RNN in RL



Source: https://deepmind.com/blog/article/capture-the-flag-science



- An obvious use case of RNNs in deep RL is for POMDP (partially observable MDP).
- If the individual states s_t do not have the Markov property, the output of a LSTM does:
 - The output of the RNN is a representation of the complete history s_0, s_1, \ldots, s_t .
- We can apply RL on the output of a RNN and solve POMDPs for free!