OptiMUS-0.3: Using LLMs to model and solve optimization problems at scale

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Stanford CS/MS&E 331

Automating the modeling bottleneck

Integer programming powers decision-making in operations

• E.g., power system scheduling, medical resource allocation, ...

Expertise barrier [Gurobi '23]:

- 81% of Gurobi users hold advanced degrees
- 49% have formal training in operations research

Small firms, municipalities, NGOs lack modeling expertise

• Leads to missed opportunities in efficiency

Goal: automate modeling to democratize optimization

Challenges

Long problem descriptions

Real specs can span dozens of pages → more modeling errors

Large problem data

• Industrial problems involve massive data tables

Hallucination

- LLMs invent constraints or API calls
- Hard to detect: code may run but model logic is wrong

Poor model quality

- Solve time depends on formulation structure
- LLMs rarely exploit modeling tricks used by experts

Dataset: NLP4LP

355 problems: 289 easy LPs, 65 hard LP/MILPs

• Easy: short text, scalar params

• Hard: long, multi-dimensional

Each instance includes text, LaTeX, code, and solution

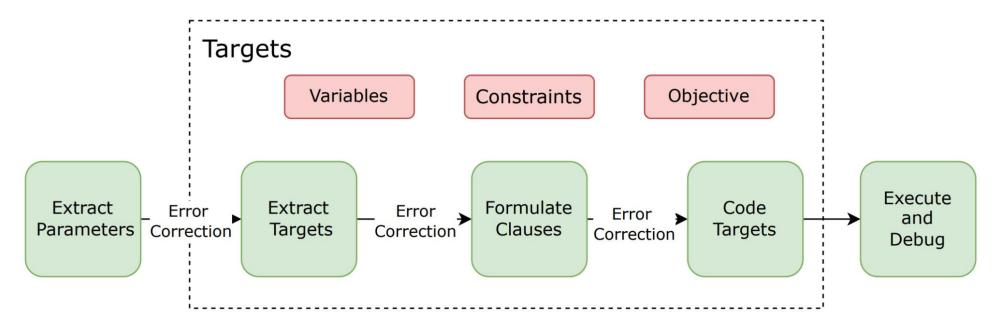
Guarded release to prevent leakage

Components of an integer program

```
maximize c \cdot z
subject to Az \leq b
Some variables must be integral
```

- Parameters: c, A, b
- Clauses: Objective, constraints
- Variables: z

OptiMUS pipeline



- LLMs at every stage
- Human + solver feedback:
 - Guide iterative LLM corrections and debugging for reliability

Description **Parameters** Clauses Formulation Coding Data Testing Have Feedback?

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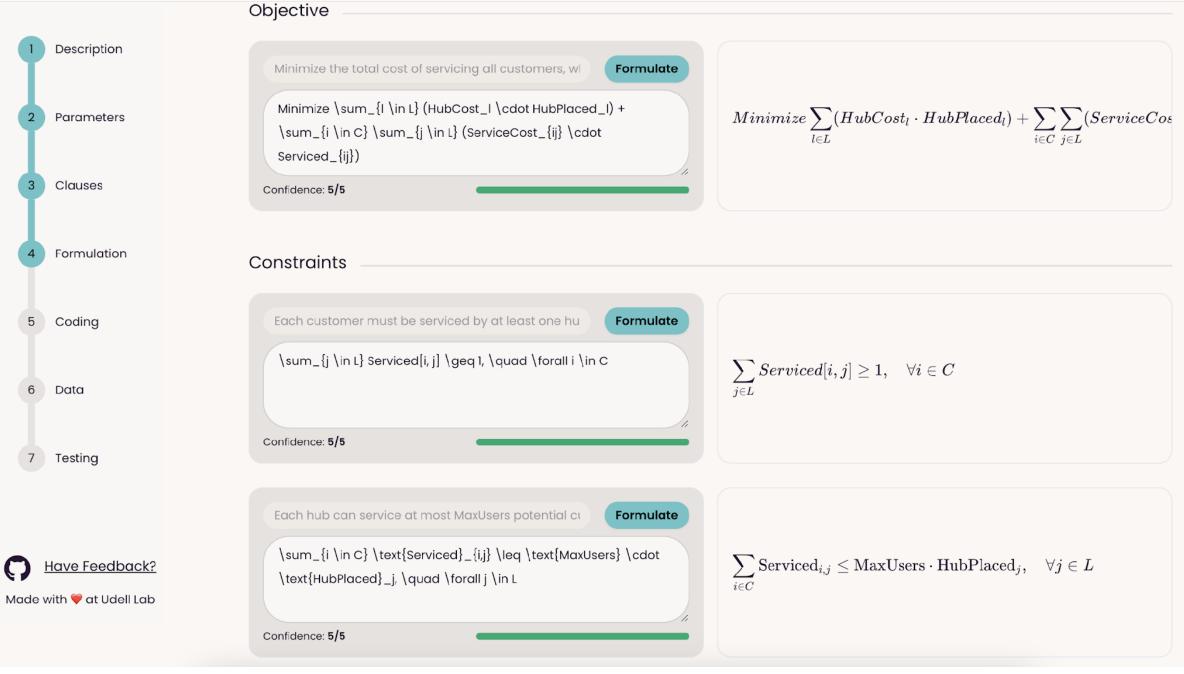
Problem Description

We are trying to figure out where to place a bike rental hub (a place where users park their cars and have bicycles available for rental). We have a set of potential hub locations L, and a set of customers we want to service C. Each customer i has cost COST(i, j) to be serviced by placing a hub at location j. Each hub I costs HUB_COST(I) to build, and each hub can service at most MAX_USERS potential customers. Our goal is to minimize the cost of servicing all the customers. Every customer should be serviced.

gurobipy

Random

Analyze



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Objective Description 1 model.setObjective(gp.quicksum(HubCost[l] * HubPlaced[l] for l in L) + gp.quicksum(ServiceCost[i, j] * Serviced[i, j] for $Minimize \sum_{l \in L} (HubCost_l \cdot HubPlaced_l) + \sum_{i \in C} \sum_{j \in L} (ServiceC)$ i in C for j in L), qp.GRB.MINIMIZE) **Parameters Generate Code** Confidence: 5/5 Clauses Constraints Formulation 1 → for i in C: model.addConstr(gp.quicksum(Serviced[i, j] for j in L) >= 1 $\sum Serviced[i,j] \geq 1, \quad orall i \in C$, name=f"customer_serviced_{i}") Coding **Generate Code** Confidence: 5/5 Data 1 → for j in range(len(L)): model.addConstr(gp.quicksum(Serviced[i, j] for i in range Testing $\sum ext{Serviced}_{i,j} \leq ext{MaxUsers} \cdot ext{HubPlaced}_j, \quad orall j \in L$ (len(C))) <= MaxUsers * HubPlaced[j], name</pre> =f"hub_service_capacity_{j}") **Generate Code** Confidence: 5/5 Have Feedback? 1 → for i in range(len(C)): Made with ϕ at Udell Lab 2 for j in range(len(L)): madal addonatedocameianeti el . Hubblanateil

```
Description
Parameters
Clauses
Formulation
Coding
Data
Testing
```

Have Feedback? Made with at Udell Lab

Full Code

```
2 import json
    import numpy as np
 5 import gurobipy as gp
7 with open("tmpData/sPXhp1SzuK5M8ELe2ddp/data.json", "r") as f:
        data = json.load(f)
10
11 ServiceCost = data["Cost"]
12 L = list(range(data["L"]))
13 MaxUsers = data["MaxUsers"]
14 C = list(range(data["C"]))
15 HubCost = data["HubCost"]
17 # Define model
18 model = gp.Model('model')
20
21 # ===== Define variables ======
22 HubPlaced = model.addVars(len(L), name='HubPlaced', vtype=gp.GRB.BINARY)
23 Serviced = model.addVars(len(C), len(L), name='Serviced', vtype=gp.GRB.BINARY)
25 # ===== Define constraints =====
27 for i in C:
```

Results

```
...
Run Successful!
Status: Optimal (2)
Objective Value: 24.0000
Runtime: 0.0122
Iteration Count: 11
Variables:
HubPlaced[0]: 0.0000
HubPlaced[1]: 1.0000
HubPlaced[2]: 1.0000
HubPlaced[3]: 0.0000
HubPlaced[4]: 1.0000
Serviced[0,0]: 0.0000
Serviced[0,1]: 0.0000
Serviced[0,2]: 1.0000
Serviced[0,3]: 0.0000
```

Synthesize Full Code from Clause Codes

Run Code

Fix Code

Error correction

- Goal: Mitigate hallucinations
 - Typical errors: wrong parameters, redundant constraints, invalid code
- Two correction layers:
 - Reflective prompts: LLM self-checks and revises outputs
 - Confidence-based feedback: uncertain results flagged for user review
- Reflective prompting process:
 - Analyzed errors at every modeling stage
 - Designed targeted reflective prompts for each error type
- Substantially lowers modeling error rates

Are units the same for both sides of this constraint?

$$(p_a+x_a)\cdot d_a\cdot (1+e_a\cdot rac{x_a}{p_a})\leq m_a, orall a\in A$$
?

... Left-hand side (LHS):

- (p_a+x_a) represents the new price for article a, which is in euros (ullet).
- d_a represents the sales forecast (demand) for article a for the next twelve months at the current price, which is in units of the article.
- $(1+e_a\cdot rac{x_a}{p_a})$ is a unitless factor ...

Therefore, the unit of the left-hand side is: euros (€) × units of the article

Right-hand side (RHS):

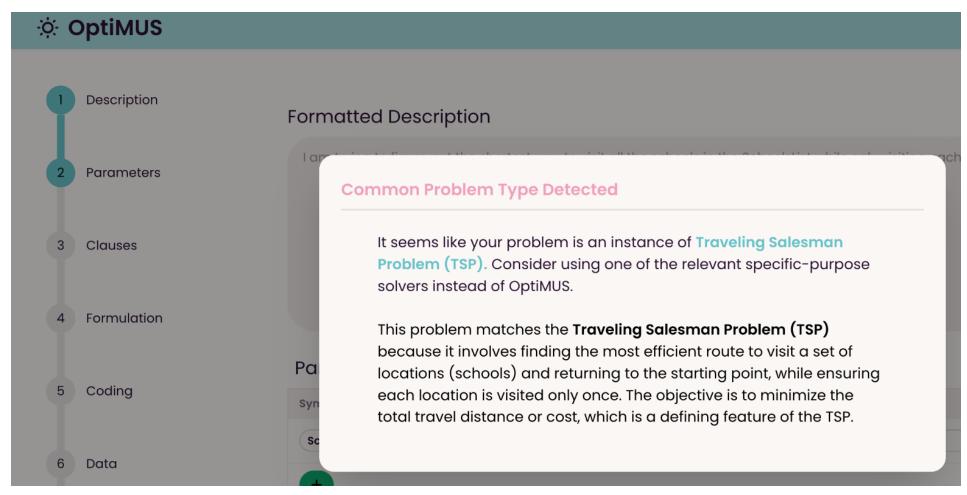
- m_a represents the maximum production volume for article a, which is in units of the article (e.g., number of shirts, pants, etc.).

The unit of the right-hand side is: units of the article

... this inconsistency suggests an error in the formulation of Constraint 5. To correct this, we should ... here is the corrected constraint:

$$d_a \cdot (1 + e_a \cdot rac{x_a}{p_a}) \leq m_a, orall a \in A$$

Identifying special problems



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Structure detection agent

- Goal: Identify and exploit special structures
 - Enhances solver performance and simplifies formulations
- Common structures:
 - Special Ordered Sets (SOS)
 - Indicator and semi-continuous variables
 - Piecewise-linear constraints

Method:

- Iterates through known structures
- LLM decides whether structure applies, then reformulates

	LLM	NL4OPT	NLP4LP	IndustryOR
Methods based on direct prompting				
Standard	GPT-4o	47.3%	33.2%	28.0%
Standard	o1	> 95%	68.8%	44.0%
Reflexion	GPT-4o	53.0%	42.6%	_
Methods based on fine-tuning LLMs				
LLMOPT	Qwen1.5-14B	93.0%*	83.8%*	46.0%*
ORLM	Deepseek-Math	86.5%*	$72.9\%^{*}$	38.0%*
Methods based on agentic frameworks				
CoE	GPT-4o	64.2%	49.2%	_
OptiMUS-0.2	GPT-4o	78.8%	68.0%	_
OptiMUS-0.3	GPT-4o	86.6%	73.7%	37.0%
OptiMUS-0.3	o1	_	80.6%	46.0%

Takeaways:

- Decomposition frameworks out-perform LLMs alone
 - Especially with cheaper models
- Fine-tuning adds a performance increase
 - But OptiMUS is competitive without fine-tuning