Contents

[Introduction 2](#_Toc480983836)

[Data 2](#_Toc480983837)

[Associated Variables 2](#_Toc480983838)

[Exploratory Analysis 3](#_Toc480983839)

[Project Objective 8](#_Toc480983840)

[Model Development 8](#_Toc480983841)

[Model Interpretation 12](#_Toc480983842)

[Relevant Prediction 13](#_Toc480983843)

[Conclusion & Suggestion 13](#_Toc480983844)

Introduction

This project aims to investigate the relationship between the overall academic performance of high school students and their institutional setting. In this study, we analyze data from 372 high schools in New York City. The data consisted of the average SAT scores of 2014-2015 school’s cohorts, along with various school and cohort’s attributes, such as the school’s borough and ethnicity proportion. Our intention is to identify variables that potentially affect the overall academic outcomes, and to quantify the extent that such variables have.

Data

|  |  |  |
| --- | --- | --- |
| Data | Source | Description |
| score.csv | https://www.kaggle.com/nycopendata/high-schools | Average SAT scores(Math, Reading, Writing), along with various attributes of 435 schools in NYC. The data pertained to 2014-2015 cohorts |
| demographics.csv | http://schools.nyc.gov/NR/rdonlyres/46093164-D8AA-40DD-A400-8F80CEBC8DD5/0/DemographicSnapshot201112to201516Public\_FINAL.xlsx | Contains information about the gender proportion of each school |
| survey\_2014.csv | http://schools.nyc.gov/documents/misc/2014%20Public%20Data%20File%20SUPPRESSED.xlsx | 2014 survey result collected from parents and teachers |

Associated Variables

In this analysis, we combine data from the mentioned 3 files. We narrow down the associated features from the original sources to just 26 variables. We use R-script(mungdata.R) to perform the data munging and collect the processed result in processed\_score.csv. Noted that the total number of observation that we analyze is reduced to 372 instances because of the missing SAT score in some of the data in score.csv. The explanation of each variable in processed\_score.csv is shown in the following table.

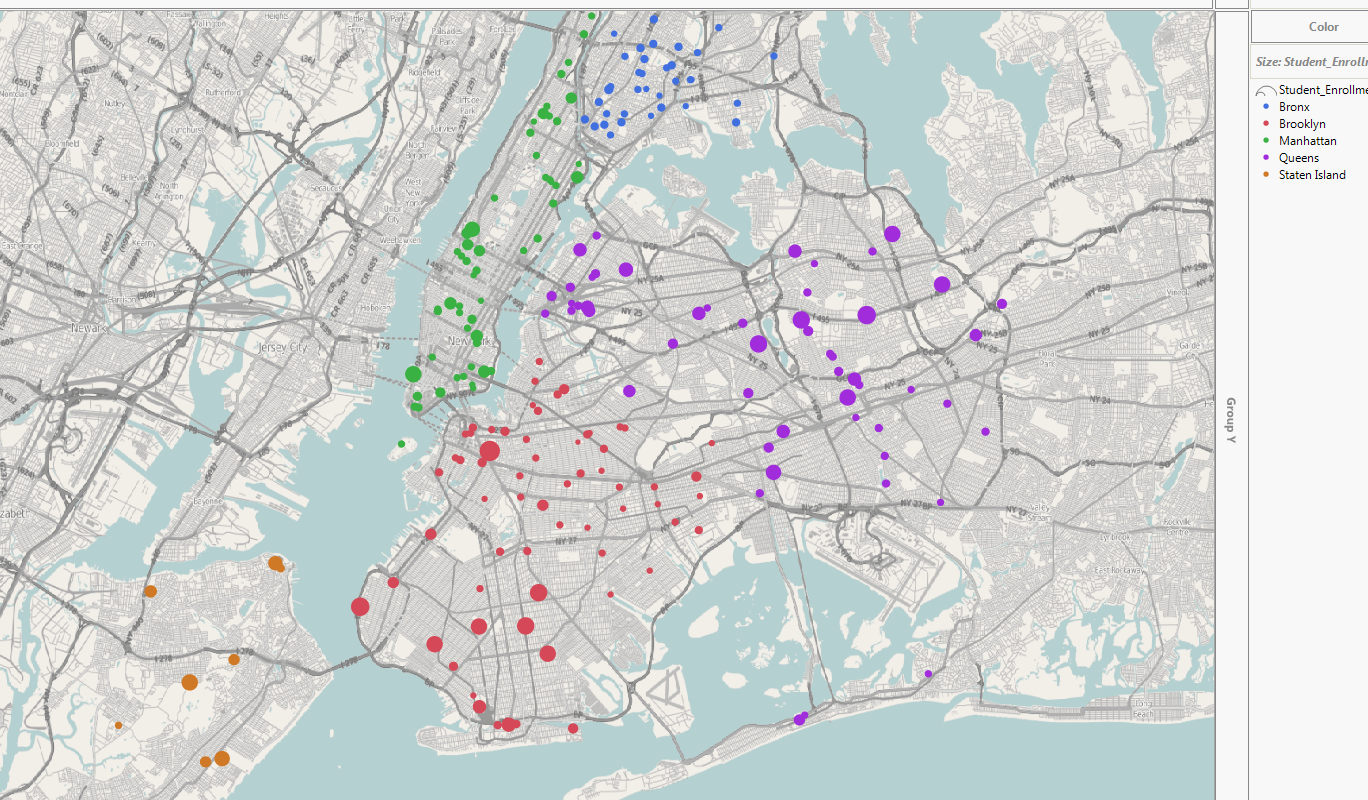
|  |  |  |
| --- | --- | --- |
| Variable Name | Description | Type |
| DBN | School’s unique identifier | Character |
| Borough | School’s Borough. Comprised of 5 area: Staten Island, Queens, Manhattan, Brooklyn, Bronx | Character |
| City | City where the school is located | Character |
| Latitude | School’s Latitude | Numeric |
| Longitude | School’s Longitude | Numeric |
| Start\_Time | School’s Opening hour | Numeric(e.g.: convert from 8:15 AM to 8.15) |
| End\_Time | School’s Ending hour | Numeric(e.g.: convert from 4:00 PM to 16.00) |
| Student\_Enrollment | Number of school’s enrollment | Numeric |
| Percent\_White | %White students in 2014-2015 cohort | Numeric |
| Percent\_Black | %Black students in 2014-2015 cohort | Numeric |
| Percent\_Hispanic | %Hispanic students in 2014-2015 cohort | Numeric |
| Persent\_Asian | %Asian students in 2014-2015 cohort | Numeric |
| \*Average\_SAT\_Math | Average SAT Math score of 2014-2015 cohort | Numeric |
| \*\*Average\_SAT\_Reading | Average SAT Reading score of 2014-2015 cohort | Numeric |
| \*\*Averate\_SAT\_Writing | Average SAT Writing score of 2014-2015 cohort | Numeric |
| Female\_Percent | %Female students in 2014-2015 cohort | Numeric |
| Male\_Percent | %Male students in 2014-2015 cohort | Numeric |
| Disabilities\_Percent | %Disability students in 2014-2015 cohort | Numeric |
| EngLearner\_Percent | %English learner students in 2014-2015 cohort | Numeric |
| Poverty\_Percent | %Poverty students in 2014-2015 cohort | Numeric |
| Parent\_Response\_Rate | Parent response rate on 2014 school’s survey | Numeric |
| Teacher\_Response\_Rate | Teacher response rate on 2014 school’s survey | Numeric |
| Instructional\_Core\_Satisfaction | %Response regarding instructional satisfaction | Numeric |
| Systems\_for\_Improvement\_Satisfaction | %Response regarding system satisfaction | Numeric |
| School\_Culture\_Satisfaction | %Response regarding culture satisfaction | Numeric |
| Class\_Hours | School’s operating duration | Numeric(difference in hour: end\_time – open\_time) |

\* - Dependent variable

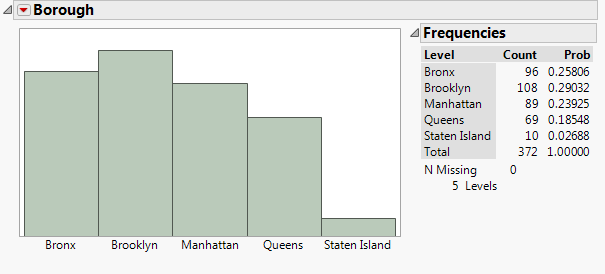
\*\* - Not included in the analysis

Exploratory Analysis

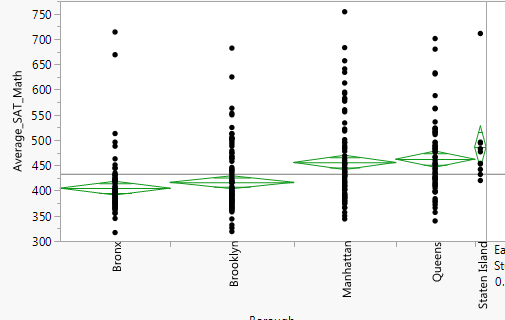
In this analysis, because of a limited time frame, we will quantify the academic performance solely based on the SAT-Math score outcome. The objective is to develop a model to predict the Average\_SAT\_Math using all other independent variables.

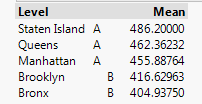


We indicate the location of each school in the above graph. The circle’s size corresponds to the size of enrollment. The school’s distribution in each borough can be summarized as follows:

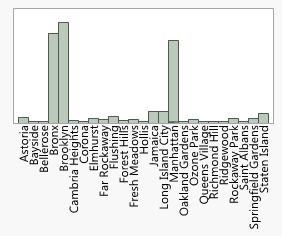


We investigate the effect of spatial information (Borough) on SAT Math score by performing ANOVA. We find that this variable maybe helpful in predicting the SAT score.





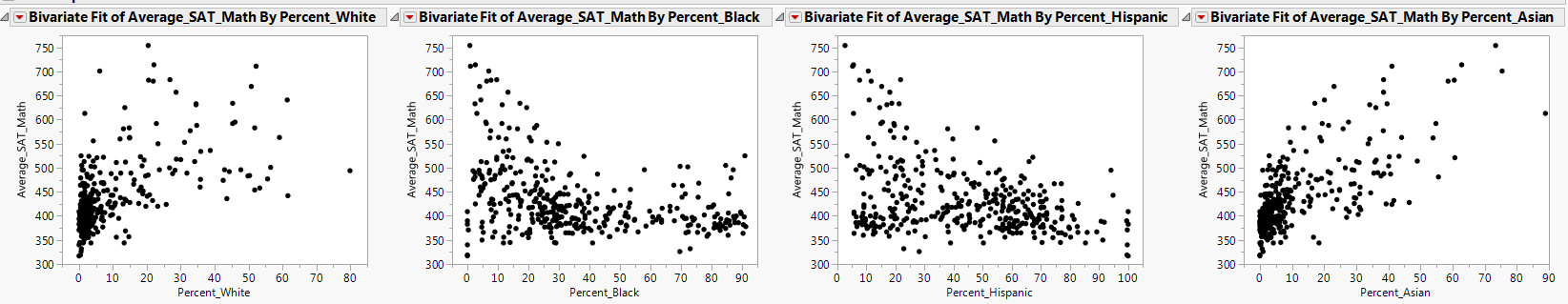
We also investigate the distribution of schools in each City but find that this variable is too fined-grained and decide to drop it as fear of running into overfitting.



The statistics of other variables are shown in the following table.

|  |  |
| --- | --- |
| Variable | Statistics |
| Start\_Time |  |
| End\_Time |  |
| Student\_Enrollment |  |
| Percent\_White |  |
| Percent\_Black |  |
| Percent\_Hispanic |  |
| Persent\_Asian |  |
| Female\_Percent |  |
| Male\_Percent |  |
| Disabilities\_Percent |  |
| EngLearner\_Percent |  |
| Poverty\_Percent |  |
| Parent\_Response\_Rate |  |
| Teacher\_Response\_Rate |  |
| Instructional\_Core\_Satisfaction |  |
| Systems\_for\_Improvement\_Satisfaction |  |
| School\_Culture\_Satisfaction |  |
| Class\_Hours |  |

For preliminary analysis, the scatter plot between ethnicity proportion and SAT-Math score shows some predictive power and indicates that these variables should be included in the model.



Project Objective

Uncover the relationship between the academic setting and cohort’s academic outcomes(as measured by the average SAT-Math scores). Linear Regression is chosen as our base model to fit the data on because of its simplicity and interpretability.

Model Development

The initial model building consisted of all independent variables (exclude DBN, City, Latitudes, Longitudes, and Female\_Percent (as this variable is reflected in Male\_Percent)). We obtain the following model:

|  |  |  |
| --- | --- | --- |
| Effect Summary | Parameter Estimates | Residual Plot |
|  |  |  |

Although the base model shows a strong predictive power (RSquare = 0.87 and RMSE = 26), it has many undesirable properties; the model contains many variables that are not statistically significant, some independent variables are highly correlated (as shown by VIF), and the Residual Plot shows Heteroscedasticity problem (verified by Park-Test). To attenuate theses effects, we perform a series of model development, which can be summarized as follows:

1. Manually create a dummy variable based on Borough. As opposed to the one generated by JMP, this will allow us to remove an individual borough that we found not significant. Bronx is treated at the base level since it has the lowest Average SAT-Math score means.
2. Re-fit the model. Iteratively remove variables with high VIF and P-Value that exceeds 0.01 significant threshold.

|  |  |  |
| --- | --- | --- |
| Effect Summary | Parameter Estimates | Residual Plot |
|  |  |  |

1. As Heteroscedasticity is still presented, we apply Log transformation to Average SAT-Math score and re-fit the model. Drop any unnecessary variable as stated in 2)

|  |  |  |
| --- | --- | --- |
| Effect Summary | Parameter Estimates | Residual Plot |
|  |  |  |

1. We try to eliminate Heteroscedasticity by plotting every independent variable against Log(Avg\_SAT\_Math) and transform them appropriately if we think that leads to a more linear relationship.

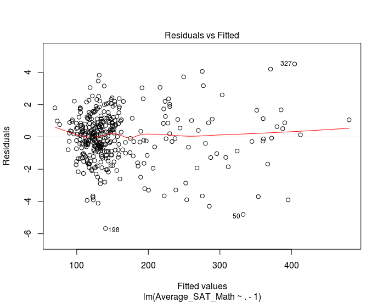
|  |  |  |
| --- | --- | --- |
| Variable | Plot of variable vs Log(Avg\_SAT\_Math) and transformation fit | Transformation Taken |
| \*Percent\_White |  | Log(Percent\_White + 0.1) |
| \*Percent\_Black |  | Log(Percent\_Black + 0.1) |
| \*Percent\_Hispanic |  | Log(Percent\_Hispanic + 0.1) |
| \*Percent\_Asian |  | Log(Percent\_Asian + 0.1) |
| \*EngLearner\_Percent |  | Log(EngLearner\_Percent) |

\* Add 0.1 to the original value before applying the Log transformation because some instances have 0 value

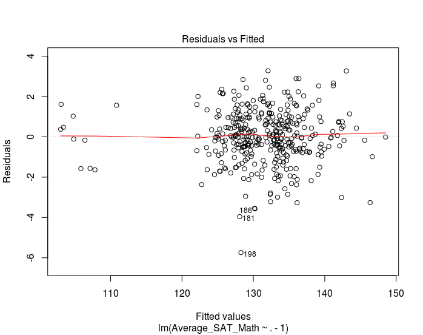
1. Re-fit the model using the transformed variables. Drop any unnecessary variable as stated in 2)

|  |  |  |
| --- | --- | --- |
| Effect Summary | Parameter Estimates | Residual Plot |
|  |  |  |

1. We have lessened the effect of Heteroscedasticity but the issue is still presented. We turn to Weighted Least Squares Regression approach by assuming the assumption of non-constant error variance. We switch to using R to conduct the analysis at this point (as performing the analysis in JMP can be quite tedious). The analysis code can be found in analysis.R . We use the transformed data collected from step 4). As the observations come from aggregated result, we firstly try to weight the error variance by the enrollment size (that is, multiply every variable by sqrt(Student\_Enrollment) ) and fit the regression model with no intercept. The residual plot indicates that Heteroscedasticity is still presented.



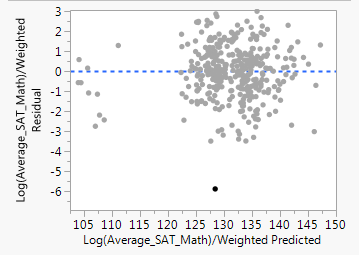
1. Now, we try another approach where error variance is weighted by model’s residuals; firstly, fit the regression model using transformed variables in step 4) and then use the mean square residual of each borough as a weight for WLS. The residual plot indicate that Heteroscedasticity issue is now fixed.



1. We import the transformed data back to JMP(weighted\_score.csv) and drop any unnecessary variable as stated in 2). We obtain the following model:

|  |  |  |
| --- | --- | --- |
| Effect Summary | Parameter Estimates | Residual Plot |
|  |  |  |

1. We drop the data point that poses too much influence on the model. Its Cook’s Distance is 0.244, far exceeds the recommended threshold Cook’s Distance (4/372 = 0.01).



1. We refit the model using the remaining 371 observations:

|  |  |  |
| --- | --- | --- |
| Effect Summary | Parameter Estimates | Residual Plot |
|  |  |  |

As the highest Cook’s Distance of data used to fit this model is 0.09 and not too severe, no further data are dropped.

1. We then perform Park-Test to verify for Heteroscedasticity. The P-Value for Y\_hat when regressed on r^2 is 0.55 and when regressed on log(r^2) is 0.90. This indicates that the Heteroscedasticity is now fixed.

The model in step 8) is our selected model. The model equation is

|  |
| --- |
|  |

Where Weighted is the means of Residual Square per group and has the following values:

|  |  |
| --- | --- |
| Group | Weighted |
| Bronx | 0.0463926118015564 |
| Brooklyn | 0.0447919246176774 |
| Manhattan | 0.0446127098917998 |
| Queens | 0.0484199559569425 |
| Staten Island | 0.0584236025734739 |

The equation can be simplified to

|  |
| --- |
|  |

Model Interpretation

The F-Statistics and P-Value of the model’s coefficients are all less than 0.01 significant threshold, thus, indicate that they are all statistically significant. We also use the obtained model to predict the value of Log(Average\_SAT\_Math), using the original 372 instances, and transform the value back to the original space, Average\_SAT\_Math, to assess the model’s performance. The model’s performance is: R-Squared = 0.84 and RMSE = 28.25.

The model’s interpretation is as follows:

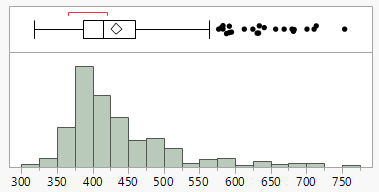
* For every 100 persons increase in student enrollment, we expect a 0.39% increase in Average\_SAT\_Math score
* For a 1% increase in the ratio of Black students, we expect a 0.02% decrease in Average\_SAT\_Math score
* For a 1% increase in the ratio of Asian students, we expect a 0.03% increase in Average\_SAT\_Math score
* As the percentage of Disability students increased by 1, we expect a 0.1% decrease in Average\_SAT\_Math score
* For a 1% increase in the ratio of English learner students, we expect a 0.04% decrease in Average\_SAT\_Math score
* As the percentage of Poverty students increased by 1, we expect a 0.1% decrease in Average\_SAT\_Math score
* As the percentage of responders who satisfied with the system improvement increased by 1, we expect a 0.6% decrease in Average\_SAT\_Math score
* As the percentage of responders who satisfied with the school culture increased by 1, we expect a 0.7% increase in Average\_SAT\_Math score
* On average, the Average\_SAT\_Math score of schools in Queens borough is 3% lower than other schools

Model Observation:

* We presume that larger class size may deteriorate academic performance. The model instead tells us that this is not the case. Other variables, such as student-to-teacher ratio, should be included to make more accurate prediction.
* Increase in the ratio of Black students deteriorates academic performance, vice versa for Asian students. White and Hispanic students have no effect.
* It is understandable that the ratios of disability students, English learner students, and poverty students are negatively correlated with the academic performance.
* The satisfaction of system improvement is negatively correlated with the Average\_SAT\_Math score. This seems counter-intuitive and required further investigation.
* The means Average\_SAT\_Math of schools in Queens is the second highest among all 5 boroughs. Yet, the model suggests that the score of schools in this area is around 3% lower than other schools.

Relevant Prediction

We demonstrate the model prediction by using data from the school “New Explorations into Science, Technology and Math High School”(DBN: 01M539). The predicted Average\_SAT\_Math of the school is 646.8 while the actual score is 657. From the histogram plot of Average\_SAT\_Math, the score that the students obtained is quite on a high side. The prediction is fairly closed and agrees with the model’s interpretation since the school comprised of a high percentage of Asian students (much higher than the average), low percentage of Black students, nearly none English learners, etc.



Conclusion & Suggestion

With R-Squared = 0.84 and RMSE = 28.25, we are content with the model’s performance. However, highly accurate model is not our main goal here as we opt for simpler and interpretable model. For highest predictive performance reason, readers should also consider cross-validation technique to prevent overfitting, as well as other non-linear modellings.

We also quantify the effect of each variable based on just one aspect of academic outcome, the Average\_SAT\_Math score. It is also interesting to investigate Average\_SAT\_Reading and Average\_SAT\_Writing scores as well. It may turn out that each variable has a different impact on a different section of SAT score.