

FAT Exam

About Subject

- Understand the concepts via solving problems
- No question will be asked as it is taught, your originality will be tested – (i.e.) Do not expect a question "Write LCS"
- Apply your ideas
- No memorization

About Question Paper

- Read a question fully – Do not start thinking / understand terms used in the question inbetween
- You need to put more time on understanding and thinking rather than writing
- 10 questions will be given
- All carry equal marks but may not be of same complexity
- Some questions may easy to solve and some may require more time

Good Scoring

- Preparation and Knowledge in subject – 50%
- Time management and Presentation – 50%
- Pre–requisite: Good health and sleep before attending exams
- Eat well, sleep well
- Talk less, discuss more before exam and *do not discuss after exam*
- Don't worry about anything which is not in your control

Basic Preparation

- Go through problems in the handout mentioned from page 3 to 7
- Have a thorough understanding of the problem
- Better work out (write on a paper) and learn
- Pen and paper will help you a lot always to have a good understanding

Better Preparation

- Learn algorithms of problems dealt in the class
- Proofs may be skipped for exams but they are very important to understand
- Take slides and go through

Day of Examination

- Enter into exam hall earlier
- Fill first page of your answer sheet carefully
- Question paper will be distributed 5 to 10 minutes ahead
- Read the question paper thoroughly
- Don't panic if it takes time
- You can read and understand the question paper till 9 : 15 am

Day of Examination

- Have a rough estimate of time required to answer each question
- Arrange the question so that first you answer whichever is easy for you
- Basically shortest job first algorithm
- Never start a question without fully understanding

Components to be Written

- Write the basic logic / technique that you are going to use
- Write the algorithm with minimal English words
- Do an illustration
- Refine algorithm if required
- Do time and space complexity analysis of the steps of the algorithm
- Express time complexity in Big-Oh notation
- Everything can be done with pen. No beautification is required

Points to remember

- If you spend more time on a question then leave some space and move on to next question
- You can come back if time permits
- Never leave a question unanswered
- Put question number with clarity
- Do not write any theory
- Do only what is asked in the question

Example Problem 1

- Given two sequences of numbers S1 and S2 of equal size, design an algorithm to find the maximum sum of a^b where a is a number in S1 and b is the number in S2. Numbers a and b can be used in the computation only once
- $\max (\sum a^b)$ where $a \in S1$ and $b \in S2$
- For example if $S1 = \{12, 4, 45\}$ and $S2 = \{4, 2, 3\}$ maximum value possible is 4102369

Example Problem 1

- This is a easy problem
- Question setter will not expect the student to answer more than 15 minutes to answer this question
- For few questions answer can be a single page also
- You will given marks as long as it is complete and correct

Basic Idea / Technique Followed

- Arranging number in descending order and taking power of corresponding elements
- Greedy

Algorithm

Step 1: Read the number of elements in sets S1 and S2, let it be n

Step 2: Read elements of S1 and S2

Step 3: Sort the elements in descending order

Sep 4: Let $\text{sum} = 0$

Sep 5: For $i = 1$ to n

$$\text{sum} += S1[i] \wedge S2[i]$$

Step 6: print sum

Illustration

$S1 = \{12, 4, 45\}$ and $S2 = \{4, 2, 3\}$

$\text{sum} = 0$

Sort in descending order

$S1 = \{45, 12, 4\}$, $S2 = \{4, 3, 2\}$

$\text{sum} += 45^4 = 4100625$

$\text{sum} += 12^3 = 4102353$

$\text{sum} += 4^2 = 4102369$

print 4102369

Complexity Analysis

Step 3: Sort the elements in descending order

Best possible – Merge sort – $O(n \log n)$

Sep 4: Let $\text{sum} = 0$ – $O(1)$

Sep 5: For $i = 1$ to n – $O(n)$

$\text{sum} += S1[i] \wedge S2[i]$

Step 6: print sum – $O(1)$

Time Complexity – $O(n \log n)$

Space Complexity – No extra space other than input – $O(1)$

Example 2 – Partition problem

- Determine whether a given set can be partitioned into two subsets such that the sum of elements in both subsets is the same
- $a = \{1, 5, 11, 5\}$ – True
- $a = \{1, 5, 3\}$ – False

Example 2 – Partition problem

- This is a difficult question which may need more time to analyze different cases and figure out an algorithm
- Question setter will expect the student to take 20 to 30 minutes to answer this question

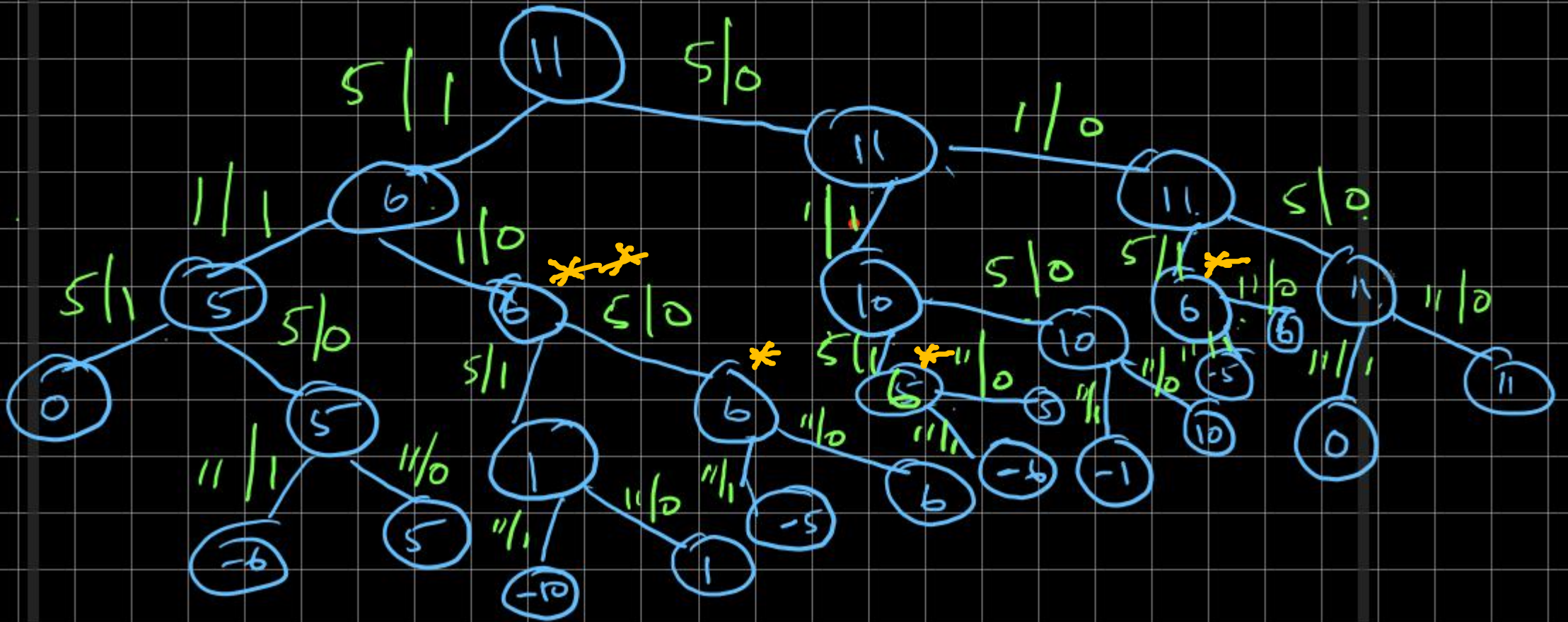
Basic Idea

- Include / Not include a number in a set
- Dynamic programming – Problem has optimal substructure
- Optimal solution can be constructed from optimal solutions of its subproblems
- $\{1, 5\}$ – sum 6 can be formed from this
- $\{1, 5, 11\}$ – still sum 6 can be formed by picking a subset with elements 1 and 5 only
- Overlapping subproblem – draw state space tree and see

Basic Idea

$$S = \{5, 1, 5, 11\}, \text{ Sum} = 22$$

Form a subset with S_{donor}



Recursive Solution

- In the previous image, 6 with only one star are same because they have still the same subset remaining
- 6 with two stars are not same as others with one star as the subset remaining is different

Recursive Solution

- 1) Calculate sum of the array. If sum is odd, there can not be two subsets with equal sum, so return false.
- 2) If sum of array elements is even, calculate $\text{sum}/2$ and find a subset of array with sum equal to $\text{sum}/2$.

Recursive Solution

We start from the last element of the set and branch out for including the n^{th} element and not including it

$\text{subsetSum}(\text{arr}, n, \text{sum}/2) = \text{subsetSum}(\text{arr}, n-1, \text{sum}/2)$ or
 $\text{subsetSum}(\text{arr}, n-1, \text{sum}/2 - \text{arr}[n])$

Bottom up DP

- Form a two dimensional table – Store boolean values
- Rows representing desired sum from 1 to sum
- Columns representing subsets of given set with elements one by one included that is j th column of table contains j elements from given set

Bottom up DP

- $\text{table}[i, j] = \text{true}$ if subset represented by column j can form sum i
- False otherwise
- Fill all cells in partition table from 1×1 to $\text{sum} \times n$, where n is the number of elements in given set

Table Construction in Bottom up DP

Condition 1 – Applied always

- Copy previous column value (i.e.) $\text{table}[i,j] = \text{table}[i][j-1]$ based on optimal substructure
- If a sum can be formed from a set $S1$ then it can be formed from its superset
- that is $\{1,5\}$ can form sum 6 then from its superset $\{1, 5, 5\}$ we can form sum 6

Table Construction in Bottom up DP

- Condition 2 – Apply only if sum is greater than or equal to element in the given array which is getting entry added in the subset
- entry in the current cell = entry in the previous column of current row or entry in the previous column of row corresponding to sum without the element that is added into the subset
- $\text{sum} \geq \text{arr}[j-1]$ then
- $\text{table}[i][j]$ or $\text{table}[i-\text{arr}[j-1]][j-1]$

Initialization of Table

	{}	{5}	{5,1}	{5,1,5}	{5,1,5,11}
0	True	True	True	True	True
1	False				
2	False				
3	False				
4	False				
5	False				
6	False				
7	False				
8	False				
9	False				
10	False				
11	False				

	{}	{5}	{5,1}	{5,1,5}	{5,1,5,1}
0	True	True	True	True	True
1	False	False	False		
2	False				
3	False				
4	False				
5	False				
6	False				
7	False				
8	False				
9	False				
10	False				
11	False				

- `table[1][2]` is false as per condition 1
- Since $1 \geq 1$ the new element in the subset apply condition 2
- `table[1][2] = false` or `table[1-1][0]`
- `table[1][2] = false` or `true = true`

Filling of Table

	{}	{5}	{5,1}	{5,1,5}	{5,1,5,11}
0	True	True	True	True	True
1	False	False	True	True	True
2	False	False	False	False	False
3	False	False	False	False	False
4	False	False	False	False	False
5	False	True	True	True	True
6	False	False	True	True	True
7	False	False	False	False	False
8	False	False	False	False	False
9	False	False	False	False	False
10	False	False	False	True	True
11	False	False	False	True	True

Time and Space Complexity

- Time complexity – $O(\text{Sum} * n)$ where n is the number of elements in the set

Wish you all the best

