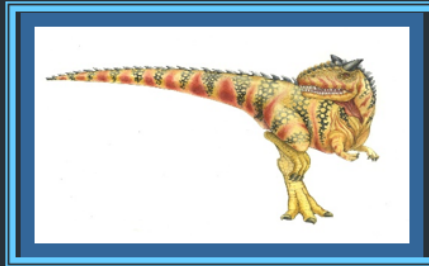


## Module 3: L2: Resource allocation and management , RAG, Deadlock



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# Outline

- ✂ Resource allocation and management
- ✂ RAG
- ✂ Deadlock
- ✂ Deadlock Characterization
- ✂ Methods for Handling Deadlocks
- ✂ Deadlock Prevention
- ✂ Deadlock Avoidance
- ✂ Deadlock Detection
- ✂ Recovery from Deadlock

# Objectives

- To develop a description of deadlocks, which prevent sets of concurrent processes from completing their tasks
- To present a number of different methods for preventing or avoiding deadlocks in a computer system.

# Resource Allocation

Resource Allocation may fall under

- Single-tasking Resource Allocation
- Multitasking Resource Allocation
- Real resources Allocation
- Virtual resources Allocation

- Meet resource needs of each program
- Prevent programs from interfering with one another
- Efficiently use hardware and other resources
- Keep detailed records of available resources; know which resources can satisfy which requests
- Schedule resources based on specific allocation policies
- Update records to reflect resource commitment and release by programs and users

# Real and Virtual Resources



- Real resources
  - Physical devices and associated system software
- Virtual resources
  - Resources that are apparent to a process or user
  - Meet or exceed real resources by
    - Rapidly shifting resources unused by one program to other programs that need them
    - Substituting one type of resource for another

# System Model

- System consists of resources
- Resource types  $R_1, R_2, \dots, R_m$   
*CPU cycles, memory space, I/O devices*
- Each resource type  $R_i$  has  $W_i$  instances.
- Each process utilizes a resource as follows:
  - **request**
  - **use**
  - **release**

# Resource-Allocation Graph

A set of vertices  $V$  and a set of edges  $E$ .

- $V$  is partitioned into two types:
  - $P = \{P_1, P_2, \dots, P_n\}$ , the set consisting of all the processes in the system
  - $R = \{R_1, R_2, \dots, R_m\}$ , the set consisting of all resource types in the system
- **request edge** – directed edge  $P_i \rightarrow R_j$
- **assignment edge** – directed edge  $R_j \rightarrow P_i$

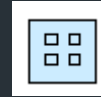


# Resource-Allocation Graph (Cont.)

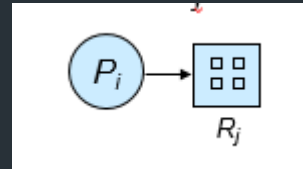
- Process



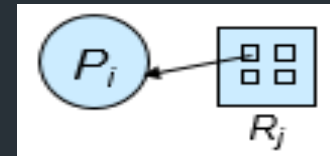
Resource Type with 4 instances



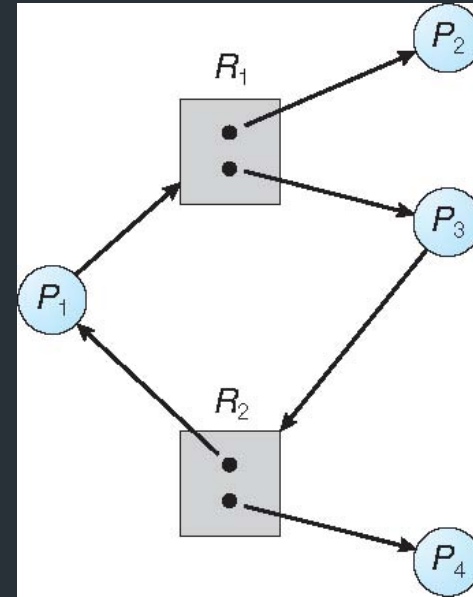
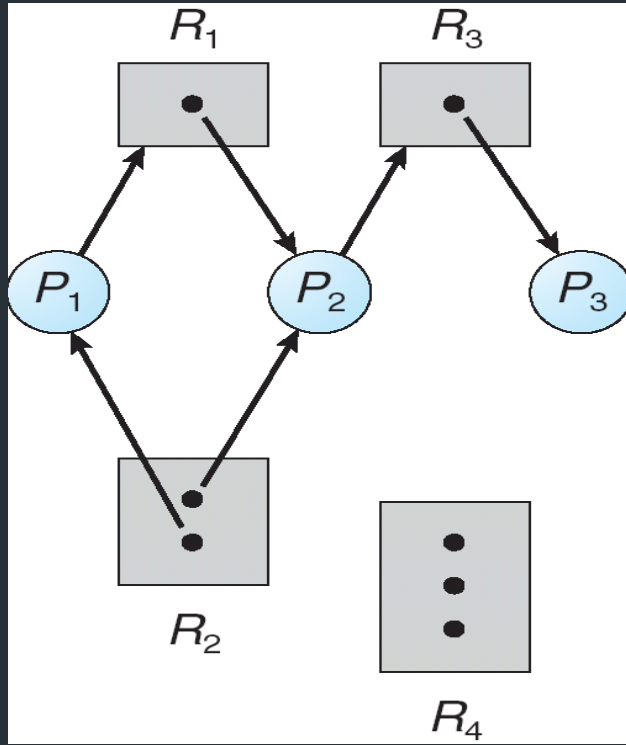
- $P_i$  requests instance of  $R_j$



- $P_i$  is holding an instance of  $R_j$



# Example of a Resource Allocation Graph



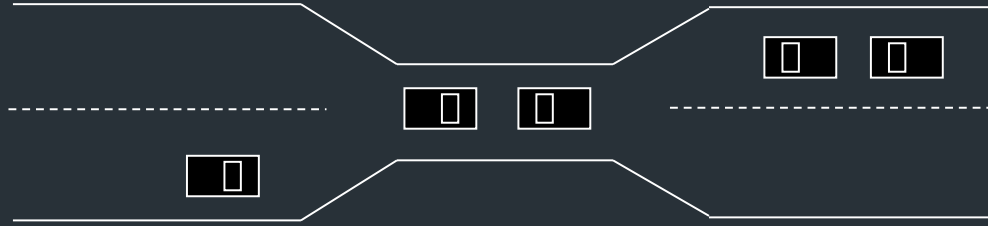
Example of Graph With A Cycle

# The Deadlock Problem

- A set of blocked processes each holding a resource and waiting to acquire a resource held by another process in the set.
- Example
  - System has 2 disk drives.
  - $P_1$  and  $P_2$  each hold one disk drive and each needs another one.
- Example
  - semaphores  $A$  and  $B$ , initialized to 1

$P_0$	$P_1$
wait (A);	wait(B)
wait (B);	wait(A)

# Bridge Crossing Example



- Traffic only in one direction.
- Each section of a bridge can be viewed as a resource.
- If a deadlock occurs, it can be resolved if one car backs up (preempt resources and rollback).
- Several cars may have to be backed up if a deadlock occurs.
- Starvation is possible.

# Deadlock Characterization

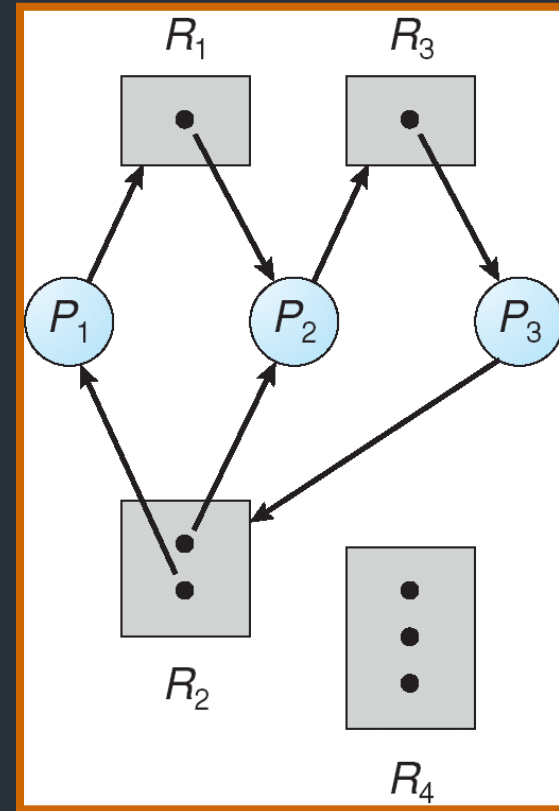
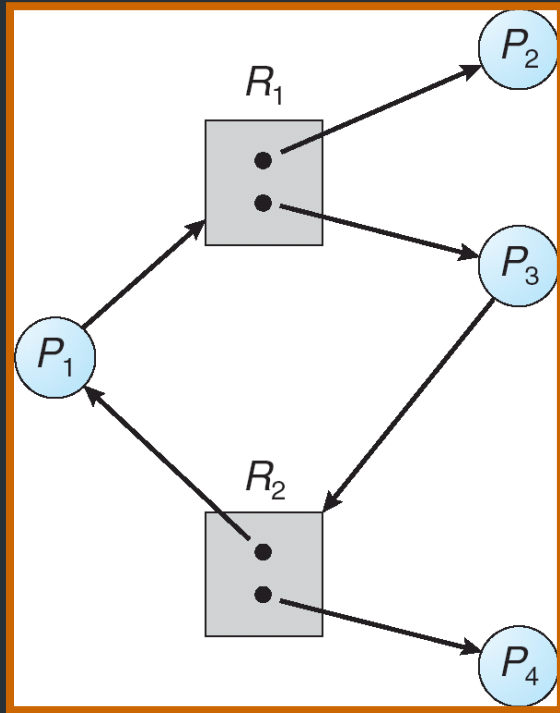
Deadlock can arise if four conditions hold simultaneously.

- **Mutual exclusion:** only one process at a time can use a resource.
- **Hold and wait:** a process holding at least one resource is waiting to acquire additional resources held by other processes.
- **No preemption:** a resource can be released only voluntarily by the process holding it, after that process has completed its task.
- **Circular wait:** there exists a set  $\{P_0, P_1, \dots, P_n\}$  of waiting processes such that  $P_0$  is waiting for a resource that is held by  $P_1$ ,  $P_1$  is waiting for a resource that is held by  $P_2$ , ...,  $P_{n-1}$  is waiting for a resource that is held by  $P_n$ , and  $P_n$  is waiting for a resource that is held by  $P_0$ .

# Basic Facts

- If graph contains no cycles  $\Rightarrow$  no deadlock.
- If graph contains a cycle  $\Rightarrow$ 
  - if only one instance per resource type, then deadlock.
  - if several instances per resource type, possibility of deadlock.

## Graph With A Cycle But No Deadlock



## Resource Allocation Graph With A Deadlock

# Methods for Handling Deadlocks

- Ensure that the system will *never* enter a deadlock state.
- Allow the system to enter a deadlock state and then recover.
- Ignore the problem and pretend that deadlocks never occur in the system; used by most operating systems, including UNIX.



# Deadlock Prevention

Restrain the ways request can be made.

- **Mutual Exclusion** – not required for sharable resources; must hold for non-sharable resources.
- **Hold and Wait** – must guarantee that whenever a process requests a resource, it does not hold any other resources.
  - Require process to request and be allocated all its resources before it begins execution, or allow process to request resources only when the process has none.
  - Low resource utilization; starvation possible.

# Deadlock Prevention (Cont.)

- **No Preemption** –

- If a process that is holding some resources requests another resource that cannot be immediately allocated to it, then all resources currently being held are released.
- Preempted resources are added to the list of resources for which the process is waiting.
- Process will be restarted only when it can regain its old resources, as well as the new ones that it is requesting.

- **Circular Wait** – impose a total ordering of all resource types, and require that each process requests resources in an increasing order of enumeration.

# Deadlock Avoidance

Requires that the system has some additional *a priori* information available.

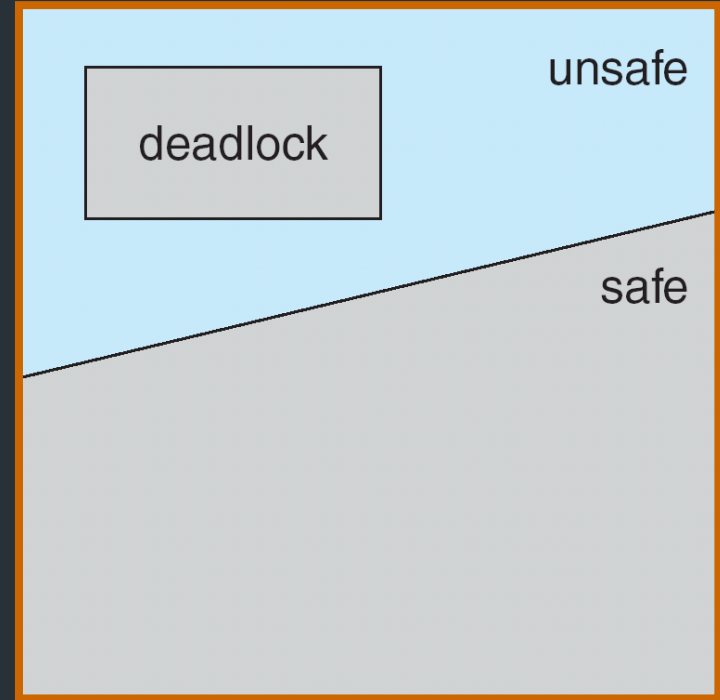
- Simplest and most useful model requires that each process declare the *maximum number* of resources of each type that it may need.
- The deadlock-avoidance algorithm dynamically examines the resource-allocation state to ensure that there can never be a circular-wait condition.
- Resource-allocation *state* is defined by the number of available and allocated resources, and the maximum demands of the processes.

# Safe State

- When a process requests an available resource, system must decide if immediate allocation leaves the system in a safe state.
- System is in **safe state** if there exists a sequence  $\langle P_1, P_2, \dots, P_n \rangle$  of ALL the processes in the system such that for each  $P_i$ , the resources that  $P_i$  can still request can be satisfied by currently available resources + resources held by all the  $P_j$ , with  $j < i$ .
- That is:
  - If  $P_i$  resource needs are not immediately available, then  $P_i$  can wait until all  $P_j$  have finished.
  - When  $P_j$  is finished,  $P_i$  can obtain needed resources, execute, return allocated resources, and terminate.
  - When  $P_i$  terminates,  $P_{i+1}$  can obtain its needed resources, and so on.

# Basic Facts

- If a system is in safe state  $\Rightarrow$  no deadlocks.
- If a system is in unsafe state  $\Rightarrow$  possibility of deadlock.
- Avoidance  $\Rightarrow$  ensure that a system will never enter an unsafe state.



Safe, Unsafe , Deadlock  
State

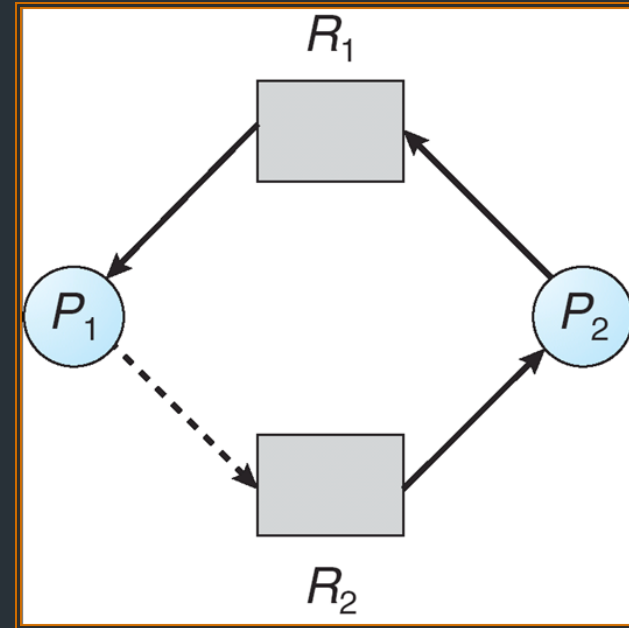
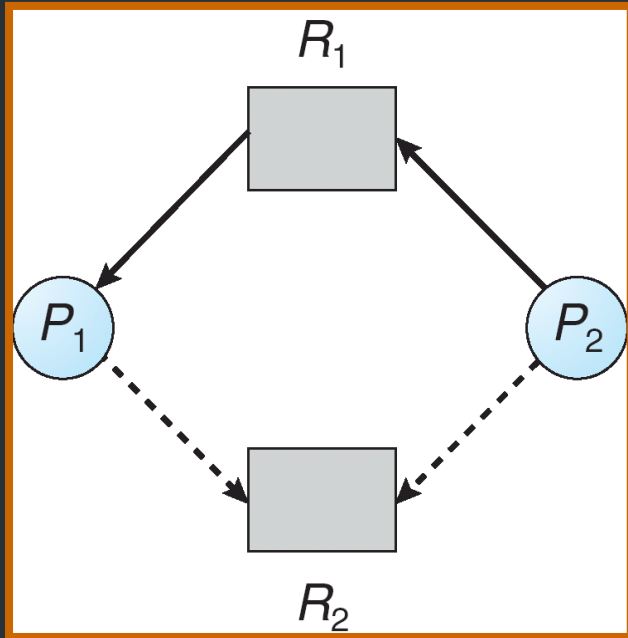
# Avoidance algorithms

- Single instance of a resource type. Use a resource-allocation graph
- Multiple instances of a resource type. Use the banker's algorithm

# Resource-Allocation Graph Scheme

- *Claim edge*  $P_i \rightarrow R_j$  indicated that process  $P_j$  may request resource  $R_j$ ; represented by a dashed line.
- Claim edge converts to request edge when a process requests a resource.
- Request edge converted to an assignment edge when the resource is allocated to the process.
- When a resource is released by a process, assignment edge reconverts to a claim edge.
- Resources must be claimed *a priori* in the system.

# Resource-Allocation Graph



Unsafe State In Resource-Allocation Graph



# Resource-Allocation Graph Algorithm



- Suppose that process  $P_i$  requests a resource  $R_j$
- The request can be granted only if converting the request edge to an assignment edge does not result in the formation of a cycle in the resource allocation graph

# Banker's Algorithm

- Multiple instances.
- Each process must a priori claim maximum use.
- When a process requests a resource it may have to wait.
- When a process gets all its resources it must return them in a finite amount of time.

# Data Structures for the Banker's Algorithm

Let  $n$  = number of processes, and  $m$  = number of resources types.

- **Available:** Vector of length  $m$ . If available  $[j] = k$ , there are  $k$  instances of resource type  $R_j$  available.
- **Max:**  $n \times m$  matrix. If  $Max[i,j] = k$ , then process  $P_i$  may request at most  $k$  instances of resource type  $R_j$ .
- **Allocation:**  $n \times m$  matrix. If  $Allocation[i,j] = k$  then  $P_i$  is currently allocated  $k$  instances of  $R_j$ .
- **Need:**  $n \times m$  matrix. If  $Need[i,j] = k$ , then  $P_i$  may need  $k$  more instances of  $R_j$  to complete its task.

$$Need[i,j] = Max[i,j] - Allocation[i,j].$$

# Resource-Request Algorithm for Process $P_i$

*Request* = request vector for process  $P_i$ . If  $Request_i[j] = k$  then process  $P_i$  wants  $k$  instances of resource type  $R_j$ .

1. If  $Request_i \leq Need_i$ , go to step 2. Otherwise, raise error condition, since process has exceeded its maximum claim.
2. If  $Request_i \leq Available$ , go to step 3. Otherwise  $P_i$  must wait, since resources are not available.
3. Pretend to allocate requested resources to  $P_i$  by modifying the state as follows:

$$Available = Available - Request_i;$$

$$Allocation_i = Allocation_i + Request_i;$$

$$Need_i = Need_i - Request_i;$$

- If *safe*  $\Rightarrow$  the resources are allocated to  $P_i$ .
- If *unsafe*  $\Rightarrow P_i$  must wait, and the old resource-allocation state is restored

# Safety Algorithm (Banker's Algorithm )



1. Let **Work** and **Finish** be vectors of length  $m$  and  $n$ , respectively. Initialize:  
 $Work = Available$   
 $Finish[i] = false$  for  $i = 0, 1, \dots, n-1$ .
2. Find and  $i$  such that both:
  - (a)  $Finish[i] = false$
  - (b)  $Need_i \leq Work$If no such  $i$  exists, go to step 4.
3.  $Work = Work + Allocation_i$   
 $Finish[i] = true$   
go to step 2.
4. If  $Finish[i] == true$  for all  $i$ , then the system is in a safe state.

## Banker's Algorithm Example Solutions

### Exercise 1

Assume that there are 5 processes,  $P_0$  through  $P_4$ , and 4 types of resources. At  $T_0$  we have the following system state:

Max Instances of Resource Type A = 3 (2 allocated + 1 Available)

Max Instances of Resource Type B = 17 (12 allocated + 5 Available)

Max Instances of Resource Type C = 16 (14 allocated + 2 Available)

Max Instances of Resource Type D = 12 (12 allocated + 0 Available)

#### Given Matrices

	<u>Allocation Matrix</u> (No of the allocated resources By a process)				<u>Max Matrix</u> Max resources that may be used by a process				<u>Available Matrix</u> Not Allocated Resources			
	A	B	C	D	A	B	C	D	A	B	C	D
<b>P<sub>0</sub></b>	0	1	1	0	0	2	1	0	1	5	2	0
<b>P<sub>1</sub></b>	1	2	3	1	1	6	5	2				
<b>P<sub>2</sub></b>	1	3	6	5	2	3	6	6				
<b>P<sub>3</sub></b>	0	6	3	2	0	6	5	2				
<b>P<sub>4</sub></b>	0	0	1	4	0	6	5	6				
<b>Total</b>	2	12	14	12								

$$\text{Need}(i) = \text{Max}(i) - \text{Allocated}(i)$$

$$(i=0) \quad (0,2,1,0) - (0,1,1,0) = (0,1,0,0)$$

$$(i=1) \quad (1,6,5,2) - (1,2,3,1) = (0,4,2,1)$$

$$(i=2) \quad (2,3,6,6) - (1,3,6,5) = (1,0,0,1)$$

$$(i=3) \quad (0,6,5,2) - (0,6,3,2) = (0,0,2,0)$$

$$(i=4) \quad (0,6,5,6) - (0,0,1,4) = (0,6,4,2)$$

Ex. Process P1 has max of (1,6,5,2) and allocated by (1,2,3,1)

$$\text{Need}(p1) = \text{max}(p1) - \text{allocated}(p1) = (1,6,5,2) - (1,2,3,1) = (0,4,2,1)$$

**Need Matrix = Max Matrix  
- Allocation Matrix**

	A	B	C	D
P <sub>0</sub>	0	1	0	0
P <sub>1</sub>	0	4	2	1
P <sub>2</sub>	1	0	0	1
P <sub>3</sub>	0	0	2	0
P <sub>4</sub>	0	6	4	2

**2. Use the safety algorithm to test if the system is in a safe state or not?**

**a. We will first define work and finish:**

**Initially work = available = ( 1, 5, 2, 0)**

**Finish = False for all processes**

Finish matrix	
P <sub>0</sub>	False
P <sub>1</sub>	False
P <sub>2</sub>	False
P <sub>3</sub>	False
P <sub>4</sub>	False

Work vector			
1	5	2	0

**b. Check the needs of each process [ needs(pi) <= Max(pi)], if this condition is true:**

- Execute the process , Change Finish[i] =True
- Release the allocated Resources by this process
- Change The Work Variable = Allocated (pi) + Work

**need<sub>0</sub> (0,1,0,0) <= work(1,5,2,0)**

P0 will be  
executed because  
need(P0) <= Work  
P0 will be True

Finish matrix	
<b>P<sub>0</sub> - 1</b>	<b>True</b>
P <sub>1</sub>	False
P <sub>2</sub>	False
P <sub>3</sub>	False
P <sub>4</sub>	False

P0 will release the allocated  
resources(0,1,1,0)  
Work = Work  
(1,5,2,0)+Allocated(P0)  
(0,1,1,0) = 1,6,3,0

Work vector			
<b>1</b>	<b>6</b>	<b>3</b>	<b>0</b>

**Need<sub>1</sub> (0,4,2,1) <= work(1,6,3,0) Condition Is False P1 will Not be executed**

**Need<sub>2</sub> (1,0,0,1) <= work(1,6,3,0) Condition Is False P2 will Not be executed**

**Need<sub>3</sub> (0,0,2,0) <= work(1,6,3,0) P3 will be executed**

P3 will be  
executed because  
need(P3) <= Work  
P3 will be True

Finish matrix	
<b>P<sub>0</sub> - 1</b>	<b>True</b>
<b>P<sub>1</sub></b>	False
P <sub>2</sub>	False
<b>P<sub>3</sub> -2</b>	<b>True</b>
P <sub>4</sub>	False

P3 will release the allocated  
resources (0,6,3,2)  
Work = Work  
(1,6,3,0)+Allocated(P3)  
( 0,6,3,2) = 1,12,6,2

Work vector			
<b>1</b>	<b>12</b>	<b>6</b>	<b>2</b>



**Need<sub>4</sub> (0,6,4,2) <= work(1,12,6,2) P4 will be executed**

P4 will be  
executed because  
need(P4) <= Work  
P4 will be True

Finish matrix	
P <sub>0</sub> - 1	True
P <sub>1</sub>	False
P <sub>2</sub>	False
P <sub>3</sub> -2	True
P <sub>4</sub> -3	True

P4 will release the allocated  
resources (0,0,1,4)  
Work = Work  
(1,12,6,2) + Allocated(P4)  
(0,0,1,4) = 1,12,7,6

Work vector			
1	12	7	6

**Need<sub>1</sub> (0,4,2,1) <= work(1,12,7,6) P1 will be executed**

P1 will be  
executed because  
need(P1) <= Work  
P1 will be True

Finish matrix	
P <sub>0</sub> - 1	True
P <sub>1</sub> -4	True
P <sub>2</sub>	False
P <sub>3</sub> -2	True
P <sub>4</sub> -3	True

P1 will release the allocated  
resources (1,2,3,1)  
Work = Work  
(1,12,7,6) + Allocated(P1)  
(1,2,3,1) = 2,14,10,7

Work vector			
2	14	10	7

**Need<sub>2</sub> (1,0,0,1) <= work(2,14,10,7) P2 will be executed**

P2 will be  
executed because  
need(P2) <= Work  
P2 will be True

Finish matrix	
P <sub>0</sub> - 1	True
P <sub>1</sub> -4	True
P <sub>2</sub> -5	True
P <sub>3</sub> -2	True
P <sub>4</sub> -3	True

P2 will release the allocated  
resources (1,3,6,5)  
Work = Work  
(2,14,10,7) + Allocated(P2)  
(1,3,6,5) = 3,17,16,12

Work vector			
3	17	16	12

The system is in a safe state and the processes will be executed in the following order:

P0,P3,P4,P1,P2

# Example of Banker's Algorithm

- 5 processes  $P_0$  through  $P_4$ ;

3 resource types:

$A$  (10 instances),  $B$  (5 instances), and  $C$  (7 instances).

- Snapshot at time  $T_0$ :

	<u>Allocation</u>			<u>Max Available</u>			<u>Need</u>			
	$A$	$B$	$C$	$A$	$B$	$C$	$A$	$B$	$C$	
$P_0$	0	1	0	7	5	3	3	3	2	
$P_1$	2	0	0	3	2	2				
$P_2$	3	0	2	9	0	2				
$P_3$	2	1	1	2	2	2				
$P_4$	0	0	2	4	3	3				
							$P_0$	7	4	3
							$P_1$	1	2	2
							$P_2$	6	0	0
							$P_3$	0	1	1
							$P_4$	4	3	1

Need is defined to be Max – Allocation

## Example (Cont.)

- The content of the matrix *Need* is defined to be *Max – Allocation*.

*Need*

*A B C*

$P_0$  7 4 3

$P_1$  1 2 2

$P_2$  6 0 0

$P_3$  0 1 1

$P_4$  4 3 1

- The system is in a safe state since the sequence  $\langle P_1, P_3, P_4, P_2, P_0 \rangle$  satisfies safety criteria.

# Example: $P_1$ Request (1,0,2)

- Check that Request  $\leq$  Available (that is,  $(1,0,2) \leq (3,3,2) \Rightarrow$  true.

	<u>Allocation</u>	<u>Max</u>	<u>Available</u>
	<i>A B C</i>	<i>A B C</i>	<i>A B C</i>
$P_0$	0 1 0	7 5 3	3 3 2
$P_1$	2 0 0	3 2 2	
$P_2$	3 0 2	9 0 2	
$P_3$	2 1 1	2 2 2	
$P_4$	0 0 2	4 3 3	



	<u>Allocation</u>	<u>Need</u>	<u>Available</u>
	<i>A B C</i>	<i>A B C</i>	<i>A B C</i>
	0 1 0	7 4 3	2 3 0
$P_1$	3 0 2	0 2 0	
$P_2$	3 0 1	6 0 0	
$P_3$	2 1 1	0 1 1	
$P_4$	0 0 2	4 3 1	

- Executing safety algorithm shows that sequence  $\langle P_1, P_3, P_4, P_0, P_2 \rangle$  satisfies safety requirement.
- Can request for (3,3,0) by  $P_4$  be granted?
- Can request for (0,2,0) by  $P_0$  be granted?

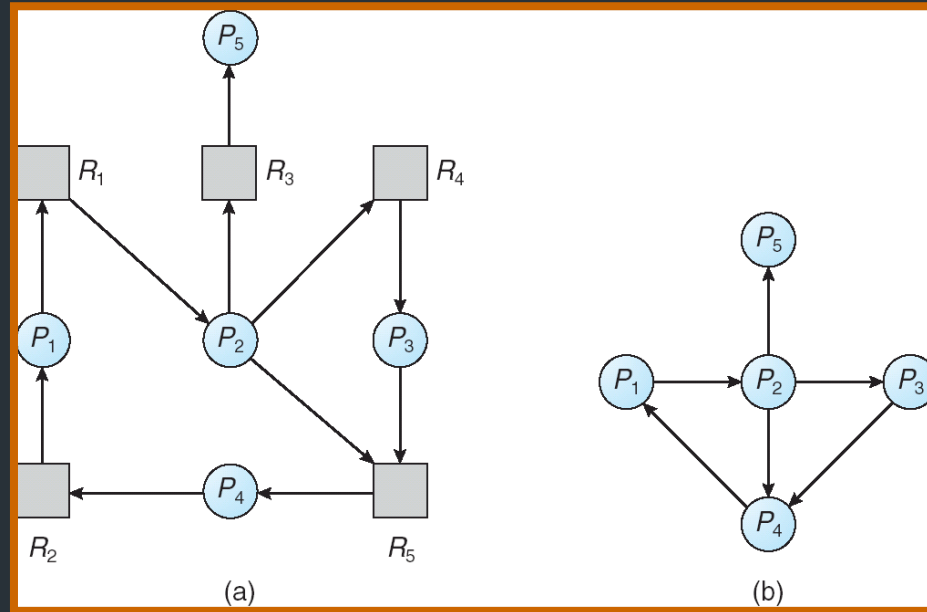
# Deadlock Detection

- Allow system to enter deadlock state
- Detection algorithm
- Recovery scheme

# Single Instance of Each Resource Type

- Maintain *wait-for* graph
  - Nodes are processes.
  - $P_i \rightarrow P_j$  if  $P_i$  is waiting for  $P_j$ .
- Periodically invoke an algorithm that searches for a cycle in the graph. If there is a cycle, there exists a deadlock.
- An algorithm to detect a cycle in a graph requires an order of  $n^2$  operations, where  $n$  is the number of vertices in the graph.

# Resource-Allocation Graph and Wait-for Graph



Resource-Allocation Graph

Corresponding wait-for graph

## Several Instances of a Resource Type

# Detection Algorithm

1. Let *Work* and *Finish* be vectors of length  $m$  and  $n$ , respectively Initialize:
  - (a) *Work* = *Available*
  - (b) For  $i = 1, 2, \dots, n$ , if  $Allocation_i \neq 0$ , then  
 $Finish[i] = false$ ; otherwise,  $Finish[i] = true$ .
2. Find an index  $i$  such that both:
  - (a)  $Finish[i] == false$
  - (b)  $Request_i \leq Work$If no such  $i$  exists, go to step 4.
3.  $Work = Work + Allocation_i$   
 $Finish[i] = true$   
go to step 2.
4. If  $Finish[i] == false$ , for some  $i$ ,  $1 \leq i \leq n$ , then the system is in deadlock state.  
Moreover, if  $Finish[i] == false$ , then  $P_i$  is deadlocked.

Algorithm requires an order of  $O(m \times n^2)$  operations to detect whether the system is in deadlocked state.



# Example of Detection Algorithm

- Five processes  $P_0$  through  $P_4$ ; three resource types A (7 instances), B (2 instances), and C (6 instances).
- Snapshot at time  $T_0$ :

	<u>Allocation</u>	<u>Request</u>	<u>Available</u>
	A B C	A B C	A B C
$P_0$	0 1 0	0 0 0	0 0 0
$P_1$	2 0 0	2 0 2	
$P_2$	3 0 3	0 0 0	
$P_3$	2 1 1	1 0 0	
$P_4$	0 0 2	0 0 2	

- Sequence  $\langle P_0, P_2, P_3, P_1, P_4 \rangle$  will result in  $Finish[i] = \text{true}$  for all  $i$ .

## Example (Cont.)

- $P_2$  requests an additional instance of type  $C$ .

	<u>Request</u>		
	$A$	$B$	$C$
$P_0$	0	0	0
$P_1$	2	0	1
$P_2$	0	0	1
$P_3$	1	0	0
$P_4$	0	0	2

- State of system?

# Detection-Algorithm Usage

- When, and how often, to invoke depends on:
  - How often a deadlock is likely to occur?
  - How many processes will need to be rolled back?
    - one for each disjoint cycle
- If detection algorithm is invoked arbitrarily, there may be many cycles in the resource graph and so we would not be able to tell which of the many deadlocked processes “caused” the deadlock.

# Recovery from Deadlock: Process Termination

- Abort all deadlocked processes.
- Abort one process at a time until the deadlock cycle is eliminated.
- In which order should we choose to abort?
  - Priority of the process.
  - How long process has computed, and how much longer to completion.
  - Resources the process has used.
  - Resources process needs to complete.
  - How many processes will need to be terminated.
  - Is process interactive or batch?

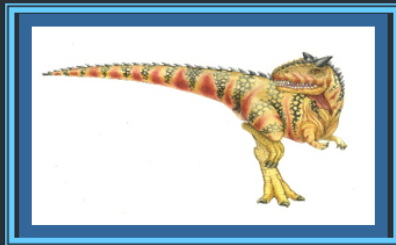
# Recovery from Deadlock: Resource Preemption

- Selecting a victim – minimize cost.
- Rollback – return to some safe state, restart process for that state.
- Starvation – same process may always be picked as victim, include number of rollback in cost factor.

# References

- Silberschatz, Gagne, Galvin: Operating System Concepts, 9<sup>th</sup> Edition

Thank you



**Exercise 2:**

If the system is in a safe state, can the following requests be granted, why or why not? Please also run the safety algorithm on each request as necessary.

- a. P1 requests (2,1,1,0)

We cannot grant this request, because we do not have enough available instances of resource A.

- b. P1 requests (0,2,1,0)

There are enough available instances of the requested resources, so first let's pretend to accommodate the request and see the system looks like:

	Allocation				Max				Available				Need Matrix				
	A	B	C	D	A	B	C	D	A	B	C	D		A	B	C	D
P <sub>0</sub>	0	1	1	0	0	2	1	0	1	3	1	0	P <sub>0</sub>	0	1	0	0
P <sub>1</sub>	1	4	4	1	1	6	5	2					P <sub>1</sub>	0	2	1	1
P <sub>2</sub>	1	3	6	5	2	3	6	6					P <sub>2</sub>	1	0	0	1
P <sub>3</sub>	0	6	3	2	0	6	5	2					P <sub>3</sub>	0	0	2	0
P <sub>4</sub>	0	0	1	4	0	6	5	6					P <sub>4</sub>	0	6	4	2

Now we need to run the safety algorithm:

Initially

Work vector	Finish matrix	
1	P <sub>0</sub>	False
3	P <sub>1</sub>	False
1	P <sub>2</sub>	False
0	P <sub>3</sub>	False
	P <sub>4</sub>	False

Let's first look at P<sub>0</sub>. Need<sub>0</sub> (0,1,0,0) is less than work, so we change the work vector and finish matrix as follows:

Work vector	Finish matrix	
1	P <sub>0</sub>	True
4	P <sub>1</sub>	False
2	P <sub>2</sub>	False
0	P <sub>3</sub>	False
	P <sub>4</sub>	False



Need<sub>1</sub> (0,2,1,1) is not less than work, so we need to move on to P<sub>2</sub>.

Need<sub>2</sub> (1,0,0,1) is not less than work, so we need to move on to P<sub>3</sub>.

Need<sub>3</sub> (0,0,2,0) is less than or equal to work.  
Let's update work and finish:

Work vector	Finish matrix	
1	P <sub>0</sub>	True
10	P <sub>1</sub>	False
5	P <sub>2</sub>	False
2	P <sub>3</sub>	True
	P <sub>4</sub>	False

Let's take a look at Need<sub>4</sub> (0,6,4,2). This is less than work, so we can update work and finish:

Work vector	Finish matrix	
1	P <sub>0</sub>	True
10	P <sub>1</sub>	False
6	P <sub>2</sub>	False
6	P <sub>3</sub>	True
	P <sub>4</sub>	True

We can now go back to P<sub>1</sub>. Need<sub>1</sub> (0,2,1,1) is less than work, so work and finish can be updated:

Work vector	Finish matrix	
1	P <sub>0</sub>	True
14	P <sub>1</sub>	True
10	P <sub>2</sub>	False
7	P <sub>3</sub>	True
	P <sub>4</sub>	True

Finally, Need<sub>2</sub> (1,0,0,1) is less than work, so we can also accommodate this. Thus, the system is in a safe state when the processes are run in the following order:

P<sub>0</sub>, P<sub>3</sub>, P<sub>4</sub>, P<sub>1</sub>, P<sub>2</sub>. We therefore can grant the resource request.