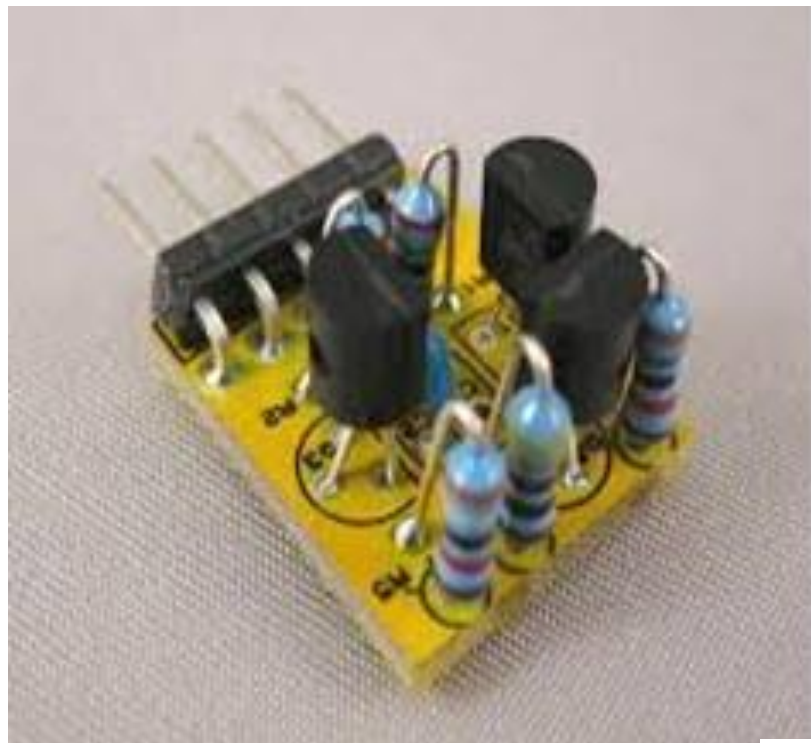


Module 3

MOSFET Active Biasing and Differential Amplifiers

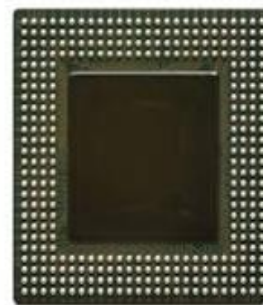
**Introduction to Current Mirror – Basic, Wilson and Cascode
Current Mirror, MOSFET Basic Differential Pair, Large Signal and
Small Signal Analysis of Differential Amplifier, Differential
Amplifier with active load.**



PQFP



DIP



FCBGA

Integrated circuits are made up of several components such as R, C, L, diodes and transistors. They are built on a small single block or chip of a semiconductor known as an integrated circuit (IC). All of them work together to perform a particular task. The IC is easily breakable, so to be attached to a circuit board, it is often housed in a plastic package with metal pins

The conventional method of making circuits was to select components like R, C, L, diode and semiconductors. There are so many factors stopping to build off big circuits like:

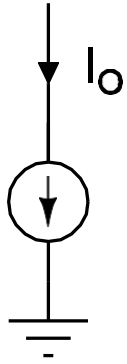
1. Bulky in size.
2. Not entirely shockproof
3. Reliability
4. More power consumption
5. Less durability

Current Mirror

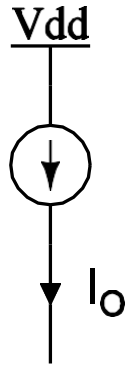
- **Current mirror method is a simple way to replicate well defined DC current sources in several independent circuit branches and is very popularly used in analog circuit design.**
- **Current source is also widely used as active load to improve amplifier gain.**
- **Current mirror is also a basic building block in current domain signal processing circuits.**

The current mirror is an **analog circuit** that senses the reference current and generates the **copy or number of copies of the reference current**, with the same characteristics. The replicated current is as stable as the reference current source. **The replicated current could be the same as the reference current ($I_{\text{copy}} = I_{\text{REF}}$)**, or it could be either multiple or fraction of the reference current. ($I_{\text{copy}} = N \cdot I_{\text{ref}}$ or $I_{\text{copy}} = (1/N) \cdot I_{\text{REF}}$).

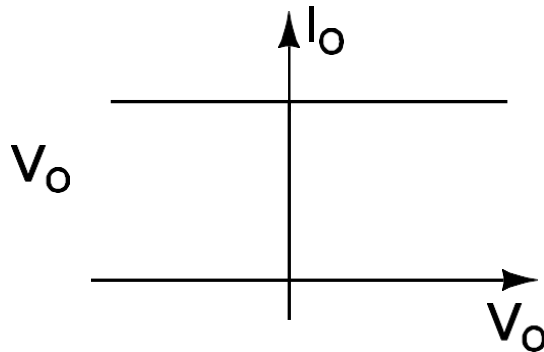
Types of Current Source



current sink

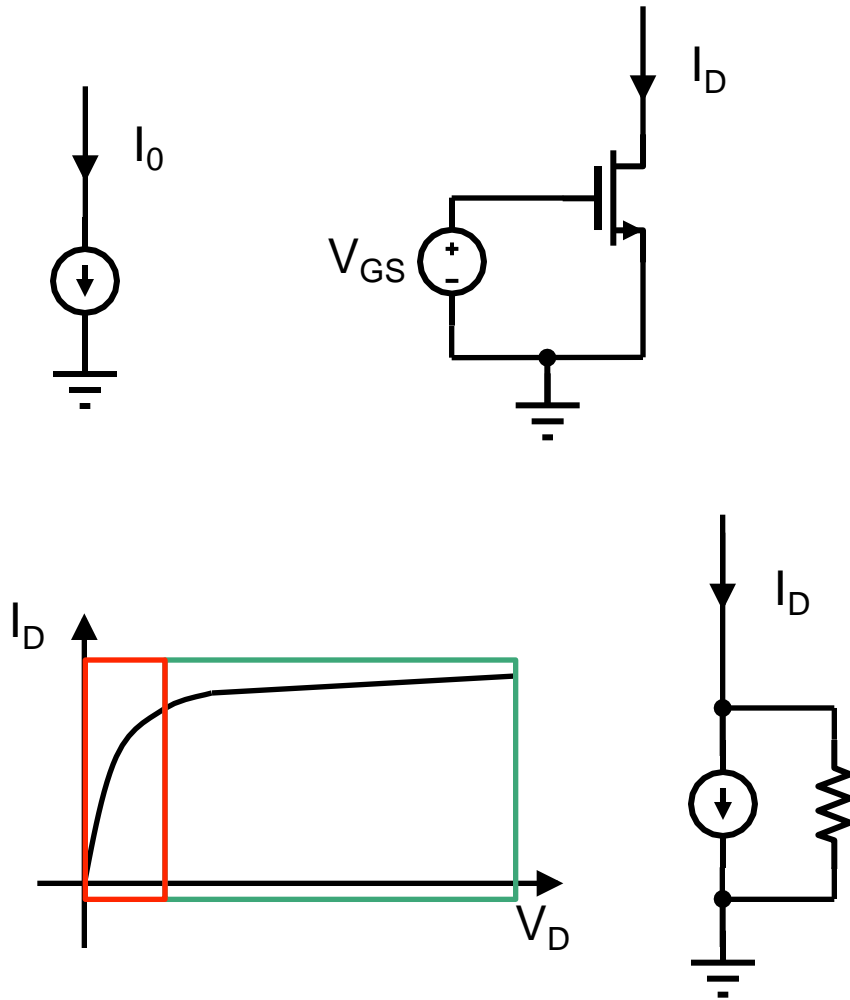


current source

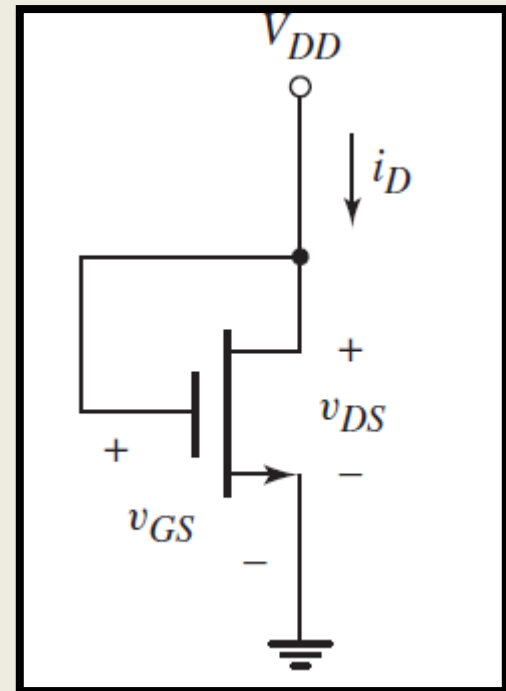
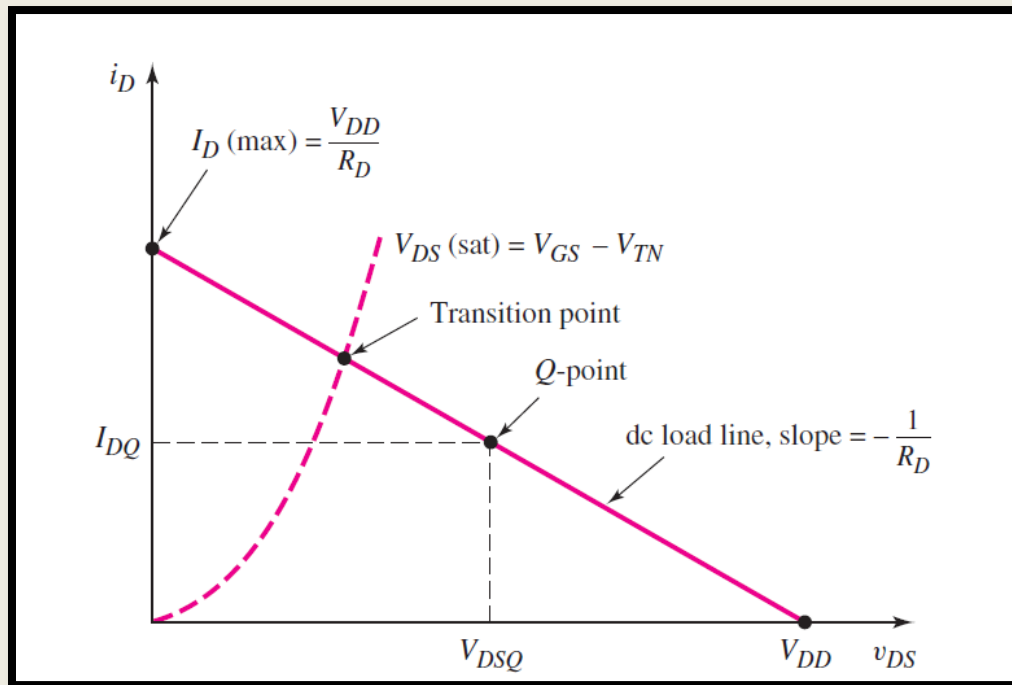


- Current source provides current to external circuit.
- Current sink receives current from the external circuit.
- we refer both current source and sink as current source.
- I-V plot of an ideal current source is shown.
- Current is not a function of the voltage across the current source.

Realization of Current Source



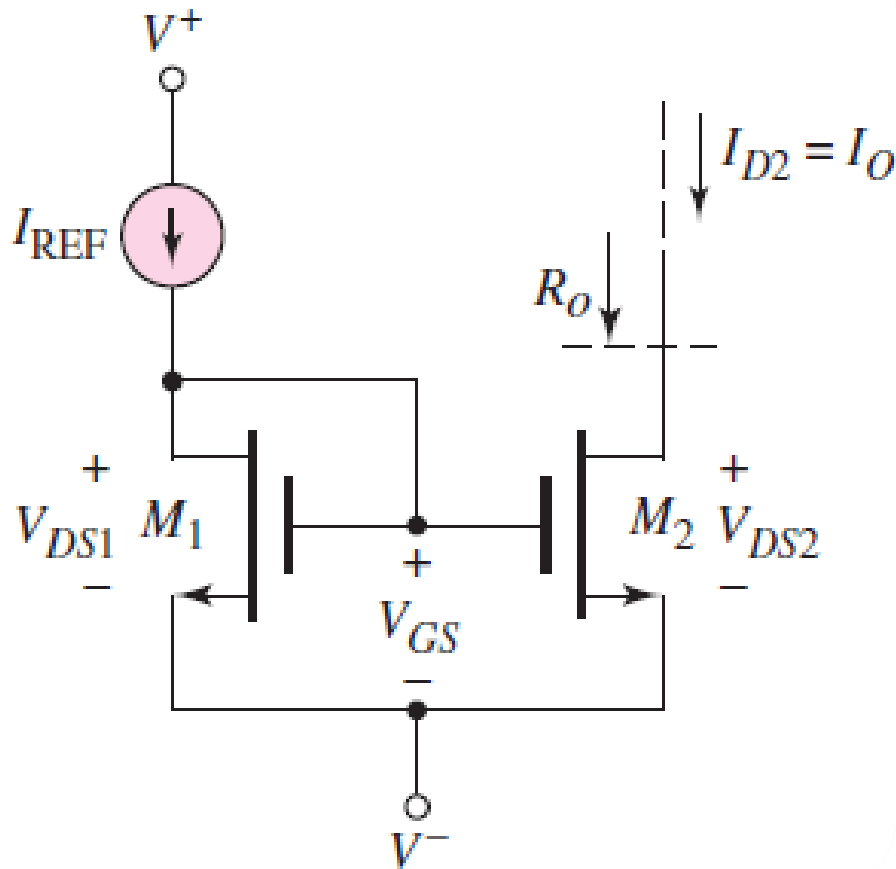
- Realization of current source by MOSFET in saturation region by providing certain V_{GS} .
- I_D is a function of V_{GS} .
- Due to the channel length modulation effect of the MOSFET, the output resistance of the current is finite.
- There is a minimum output voltage for the MOSFET current source, V_{DSsat} to keep the transistor in saturation region.



$$v_{DS} = v_{GS} > v_{DS}(\text{sat}) = v_{GS} - V_{TN}$$

$$i_D = K_n(v_{GS} - V_{TN})^2 = K_n(v_{DS} - V_{TN})^2$$

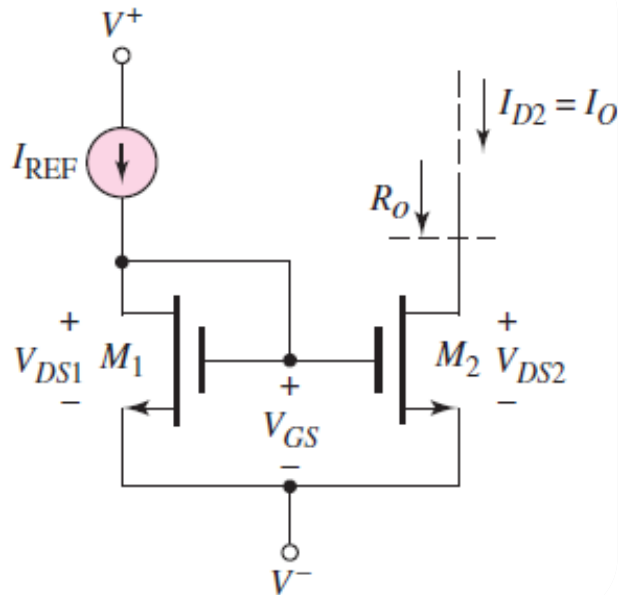
Current Mirror Basic



The drain and source terminals of the enhancement-mode transistor M_1 are connected, which means that M_1 is always **biased in the saturation region**.

Assuming Channel Length Modulation $\lambda = 0$ The drain current of M_1 is given by

Current Mirror Basic



Solving for V_{GS} yields

$$V_{GS} = V_{TN1} + \sqrt{\frac{I_{REF}}{K_{n1}}}$$

$$\begin{aligned} I_{REF} &= I_{D1} \\ &= \frac{1}{2} K'_n \left(\frac{W_1}{L_1} \right) (V_{GS} - V_{TN1})^2 \end{aligned}$$

$$I_{REF} = K_{n1} (V_{GS} - V_{TN1})^2$$

$$\frac{I_{REF}}{K'_n} = (V_{GS} - V_{TN1})^2$$

(1)

Wkt:

$$I_{REF} = I_{D1}$$

$$I_{REF} = \frac{V_{DD} - V_{GS}}{R}$$

**The MOSFET M2 has the same V_{GS} as M1;
We assume that its operating in saturation we have**

$$I_O = I_{D2} = \frac{1}{2} K'_{n2} \left(\frac{W_2}{L_2} \right) (V_{GS} - V_{TN})^2 = K_{n2} (V_{GS} - V_{TN2})^2$$

2

Wkt

Solving for V_{GS} yields

$$V_{GS} = V_{TN1} + \sqrt{\frac{I_{REF}}{K_{n1}}}$$

Substituting Equation we have

$$I_O = K_{n2} \left[\sqrt{\frac{I_{REF}}{K_{n1}}} + V_{TN1} - V_{TN2} \right]^2$$

Taking the ratio of equations 1 and 2 we get

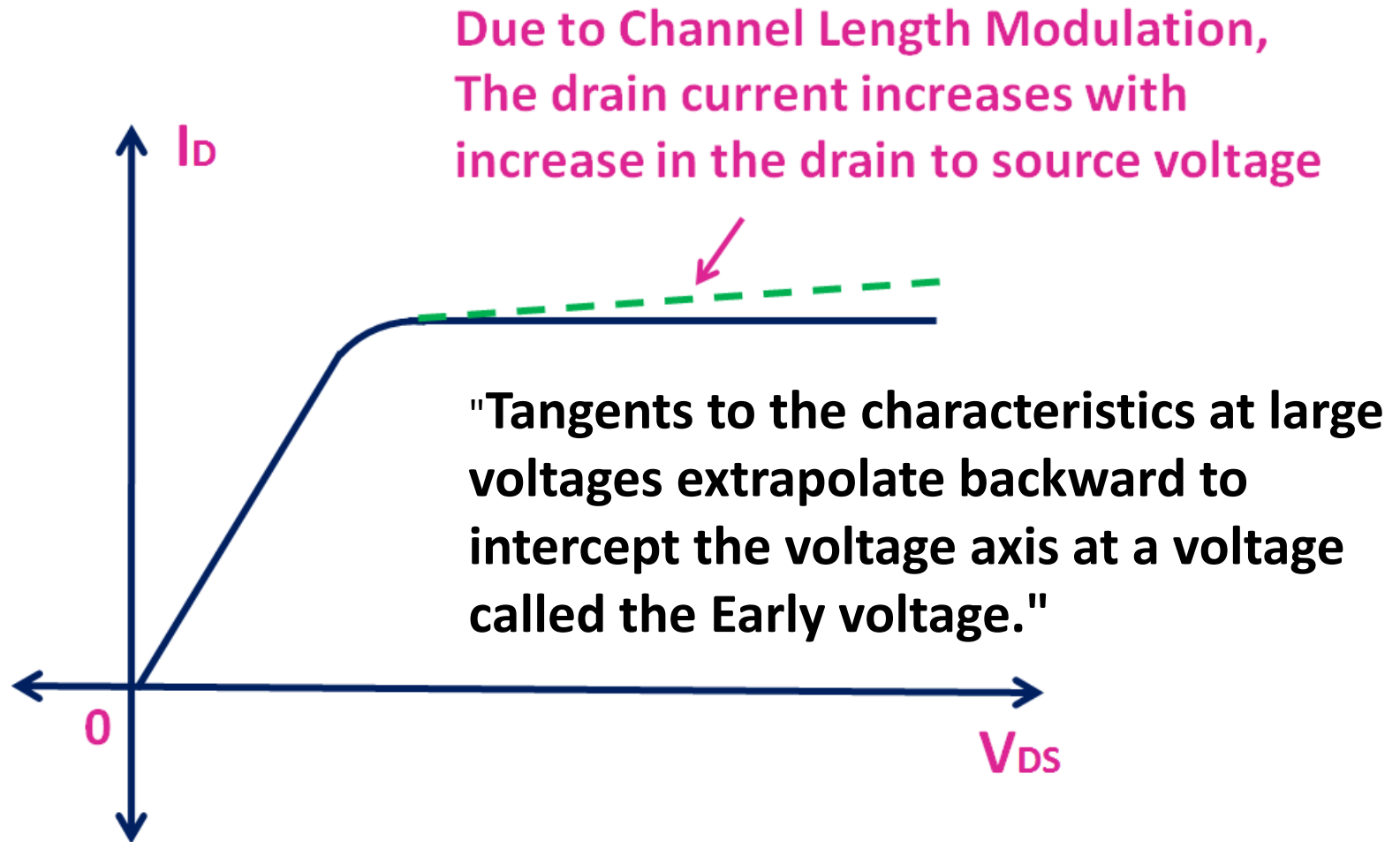
$$\frac{I_O}{I_{REF}} = \frac{I_{D2}}{I_{D1}} = \frac{\left(\frac{W_2}{L_2} \right)}{\left(\frac{W_1}{L_1} \right)}$$

If M1 and M2 are identical transistors, then $V_{TN1} = V_{TN2}$ and $K_{n1} = K_{n2}$

Since there is **NO GATE CURRENT** in **MOSFETS**, the induced load current is identical to the reference current, **provided the two transistors are matched.**

$$I_O = I_{REF}$$

Channel Length Modulation



we can write the load and reference currents as follows:

$$I_O = K_{n2}(V_{GS} - V_{TN2})^2(1 + \lambda_2 V_{DS2})$$

and

$$I_{REF} = K_{n1}(V_{GS} - V_{TN1})^2(1 + \lambda_1 V_{DS1})$$

Since transistors in the current mirror are processed on the same integrated circuit, all physical parameters, such as V_{TN} , μ_n , C_{ox} , and λ , are essentially identical for both devices. Therefore, taking the ratio of I_O to I_{REF} , we have

$$\frac{I_O}{I_{REF}} = \frac{(W/L)_2}{(W/L)_1} \cdot \frac{(1 + \lambda V_{DS2})}{(1 + \lambda V_{DS1})}$$

$$V_{DS2} + \Delta V_{DS2} = I_O + \Delta I_O$$

that $V_{DS1} = V_{GS1} = \text{constant}$ for a given reference current.

Normally, $\lambda V_{DS1} = \lambda V_{GS1} < 1$, and if $(W/L)_2 = (W/L)_1$,

then the change in bias current with respect to a change in V_{DS2} is

Initial analysis we have neglected CLM

However it has significant effect on the operation of the current source circuit

1. V_O increases above this value, I_O also increases according to the incremental output resistance r_{o2} of M2

Its given by

$$\frac{I_O}{I_{ref}} = \frac{1}{1} \frac{(1 + \lambda V_{DS2})}{1}$$

$$I_O = I_{ref} (1 + \lambda V_{DS2})$$

$$\frac{1}{R_o} = \frac{dI_O}{dV_{DS2}} = \frac{1}{r_o} = \lambda I_{Ref}$$

Where

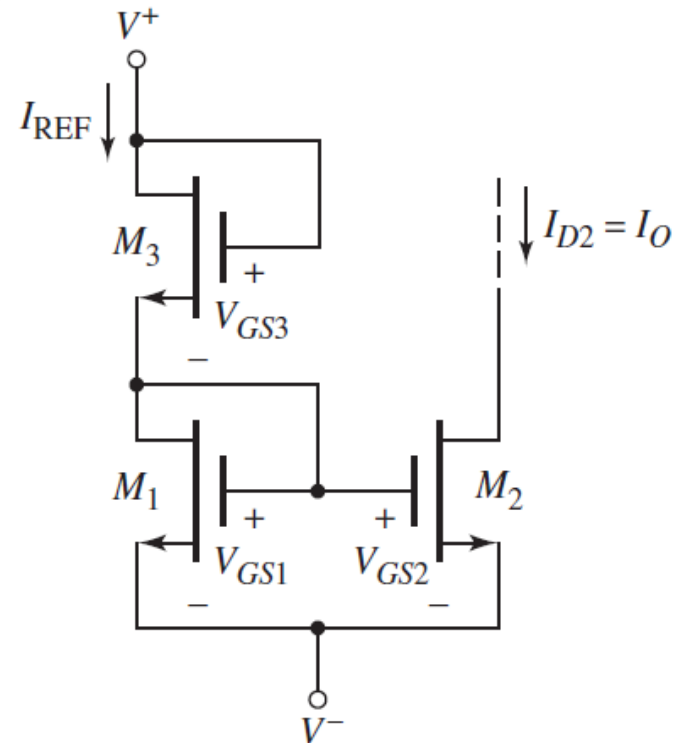
$$r_o = \frac{1}{\lambda I_{Ref}}$$

$$\lambda = \frac{1}{V_A}$$

Replacing R by MOSFET

The reference current in bipolar current-source circuits is generally established by the bias voltages and a resistor.

Since MOSFETs can be configured to act like a resistor, the reference current in MOSFET current mirrors is usually established by using additional transistors.



MOSFET current source

MOSFET current source

V^-

Transistors $M1$ and $M3$ are in series; assuming $\lambda = 0$,
ALSO $I_{D1}=I_{D3}$

$$K_{n1}(V_{GS1} - V_{TN1})^2 = K_{n3}(V_{GS3} - V_{TN3})^2$$

From the circuit, we see that

$$V_{GS1} + V_{GS3} = V^+ - V^-$$

Therefore,

$$V_{GS1} = \frac{\sqrt{\frac{(W/L)_3}{(W/L)_1}}}{1 + \sqrt{\frac{(W/L)_3}{(W/L)_1}}} \cdot (V^+ - V^-) + \frac{\left(1 - \sqrt{\frac{(W/L)_3}{(W/L)_1}}\right)}{\left(1 + \sqrt{\frac{(W/L)_3}{(W/L)_1}}\right)} \cdot V_{TN} = V_{GS2}$$

$$k_{n1}[V_{GS1}-V_{TN1}]^2=K_{n3}[V_{Gs3}-V_{TN3}]^2$$

$$\left[\frac{W}{L}\right]_1[V_{GS1}-V_{TN1}]^2=\left[\frac{W}{L}\right]_3[V_{Gs3}-V_{TN3}]^2$$

$$[V_{GS1}-V_{TN1}]^2=\frac{\left[\frac{W}{L}\right]_3[V_{Gs3}-V_{TN3}]^2}{\left[\frac{W}{L}\right]_1}$$

$$V_{GS1}-V_{TN1}=\sqrt{\frac{\left[\frac{W}{L}\right]_3[V_{Gs3}-V_{TN3}]^2}{\left[\frac{W}{L}\right]_1}}$$

$$V_{GS1}-V_{TN1}=\sqrt{\frac{\left[\frac{W}{L}\right]_3}{\left[\frac{W}{L}\right]_1}}[V_{Gs3}-V_{TN3}]$$

$$X=\sqrt{\frac{\left[\frac{W}{L}\right]_3}{\left[\frac{W}{L}\right]_1}}$$

$$V_{GS1} - V_{TN1} = \sqrt{X} (V_{Gs3}) - \sqrt{X} (V_{TN3})$$

$$V_{GS1} = \sqrt{X} (V_{Gs3}) - \sqrt{X} (V_{TN3}) + V_{TN1}$$

$$V_{GS1} = \sqrt{X} (V_{Gs3}) + [1 - \sqrt{X}] (V_{TN})$$

KVL:

$$V_{Gs1} + V_{Gs3} = V^+ - V^-$$

$$V_{Gs3} = V^+ - V^- - V_{Gs1}$$

$$V_{GS1} = \sqrt{X} (V^+ - V^- - V_{Gs1}) + [1 - \sqrt{X}] (V_{TN})$$

$$V_{GS1} + \sqrt{X} (V_{Gs1}) = \sqrt{X} (V^+ - V^-) + [1 - \sqrt{X}] (V_{TN})$$

$$V_{GS1} (1 + \sqrt{X}) = \sqrt{X} (V^+ - V^-) + [1 - \sqrt{X}] (V_{TN})$$

$$V_{GS1} = \frac{\sqrt{X}}{(1 + \sqrt{X})} (V^+ - V^-) + \frac{[1 - \sqrt{X}]}{(1 + \sqrt{X})} (V_{TN}) = V_{GS2}$$

Therefore,

$$V_{GS1} = \frac{\sqrt{\frac{(W/L)_3}{(W/L)_1}}}{1 + \sqrt{\frac{(W/L)_3}{(W/L)_1}}} \cdot (V^+ - V^-) + \frac{\left(1 - \sqrt{\frac{(W/L)_3}{(W/L)_1}}\right)}{\left(1 + \sqrt{\frac{(W/L)_3}{(W/L)_1}}\right)} \cdot V_{TN} = V_{GS2}$$

Finally, the load current, for $\lambda = 0$, is given by

$$I_O = \frac{k'_n}{2} \cdot \left(\frac{W}{L} \right)_2 (V_{GS2} - V_{TN})^2$$

Cascode Current Mirror

1. In order to suppress the effect of λ , we can force

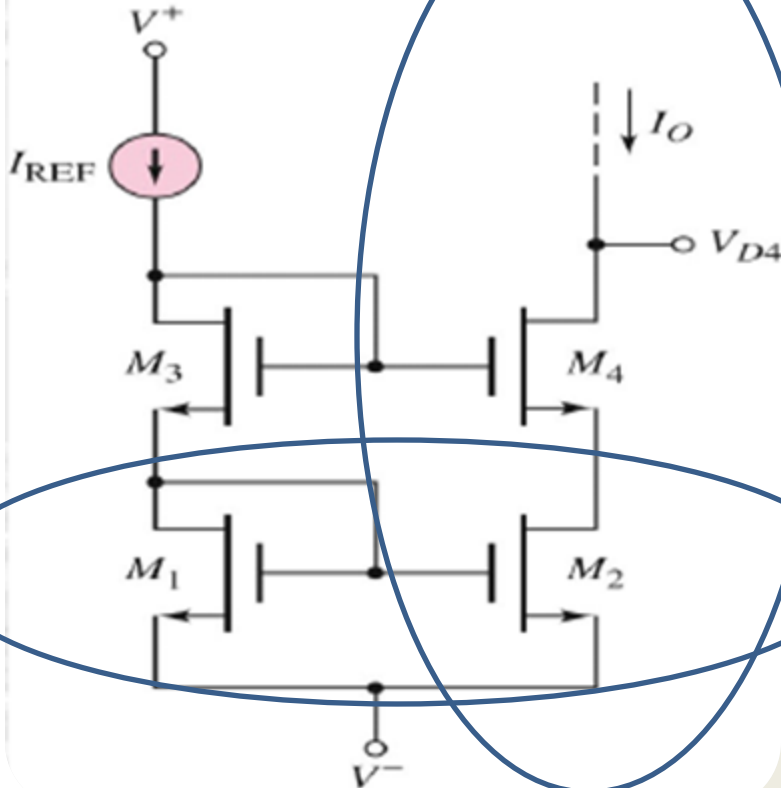
$$V_{DS1} = V_{DS2}$$

2. Its ensured by introducing cascode in the output stage

3. In MOSFET current-source circuits, the output resistance is a **measure of the stability with respect to changes in the output voltage**. This output resistance can be increased by modifying the circuit

Cascode Current Mirror

Cascode Stage



Current Mirror

The reference current is established by including another MOSFET in the reference branch of the circuit as was done in the basic two-transistor current mirror. Assuming all transistors are identical, then $I_O = I_{REF}$.

Gate voltages of M1 and M3 are constant, hence M2 and M4 also constant

Assume :

Generation of V_B

$$V_{GS4} = V_{G4} - V_{S4} = V_B - V_Y$$

$$V_{DS2} = V_X, V_{DS1} = V_Y; \text{ For } V_{DS2} = V_{DS1}; V_Y = V_X$$

$$V_B = V_{GS4} + V_Y = V_{GS4} + V_X = V_{GS4} + V_{GS1} \quad (\text{WKT: } V_{DS1} = V_{GS1})$$

$$V_{DS1} \neq V_{DS2}$$

$$V_B = V_{GS4} + V_X$$

$$+V_B - V_{GS4} - V_Y = 0$$

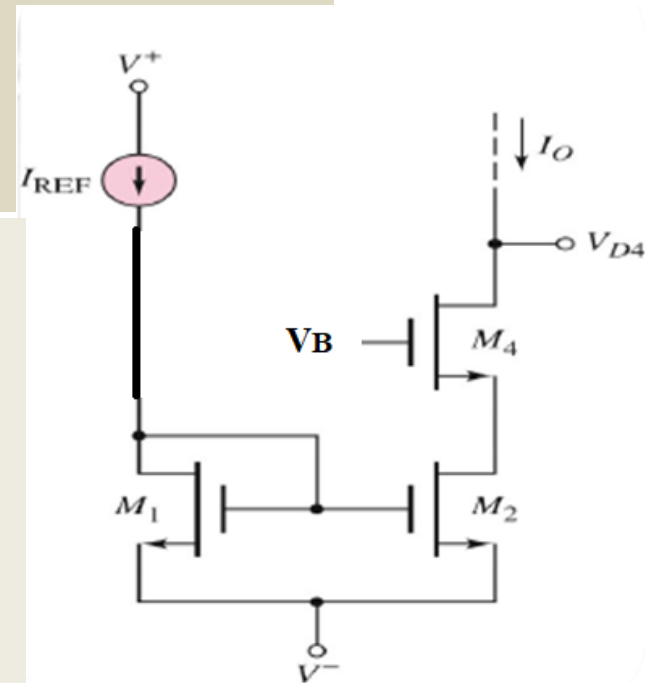
$$V_{GS4} + V_X - V_{GS4} - V_Y = 0$$

$$V_X = V_Y$$

M1 is diode connected hence its in saturation

$V_{GS1} = V_{GS2}$, same current I_{D1} flow through M2 (Saturation)

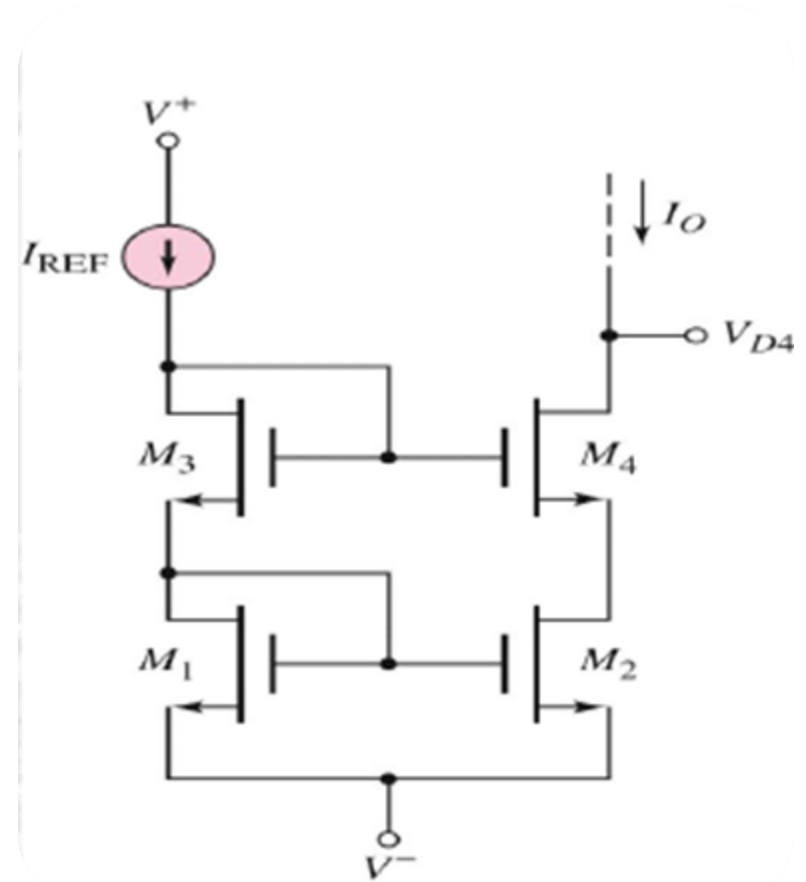
V_B (Bias Voltage) = Saturation

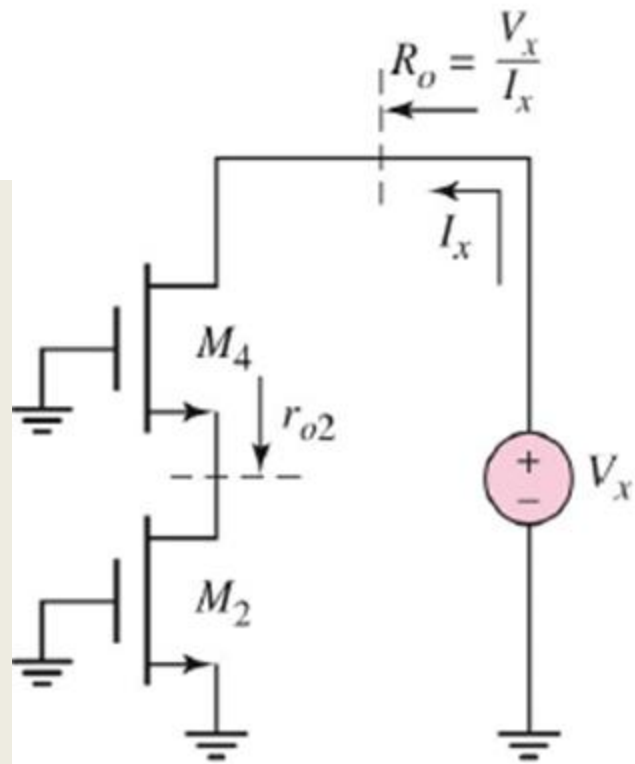


Output Impedance

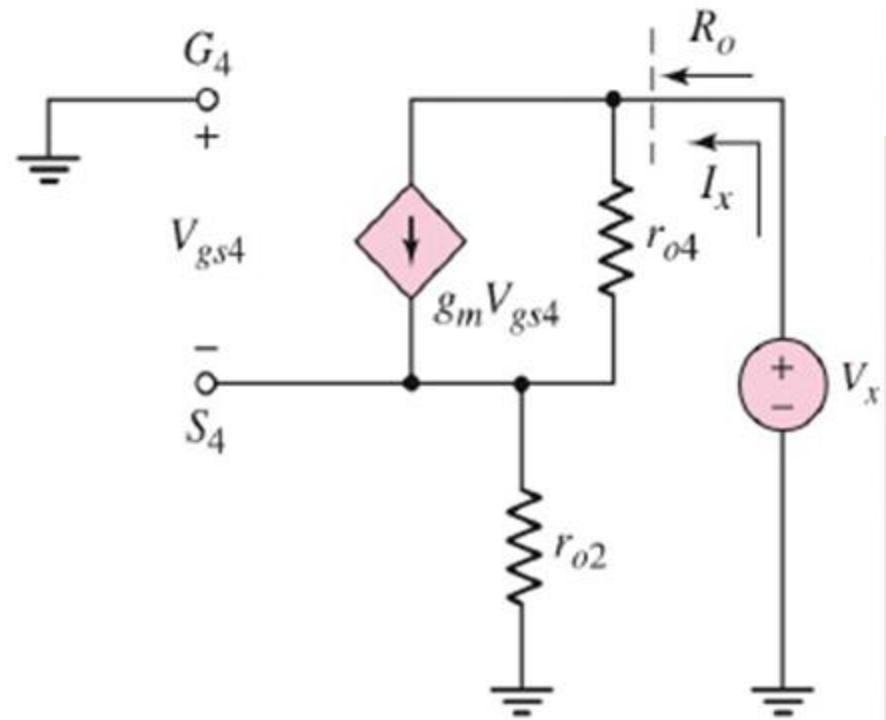
Draw the small signal equivalent

A diode connected MOSFET being fed by a constant current Behave as constant DC potential





(a)



(b)

For determining R_o

$$I_x = g_m V_{gs4} + \frac{V_x - (-V_{gs4})}{r_{o4}}$$

$$V_{gs4} = -I_x r_{o2}$$

$$I_x + \frac{r_{o2}}{r_{o4}} I_x + g_m r_{o2} I_x = \frac{V_x}{r_{o4}}$$

$$R_O = \frac{V_x}{I_x} = r_{o4} + r_{o2} (1 + g_m r_{o4})$$

Normally

$$g_m r_{o4} \gg 1 \Rightarrow g_m r_{o4} r_{o2} \gg r_{o4}$$

$$R_o \cong g_m r_{o4} r_{o2}$$

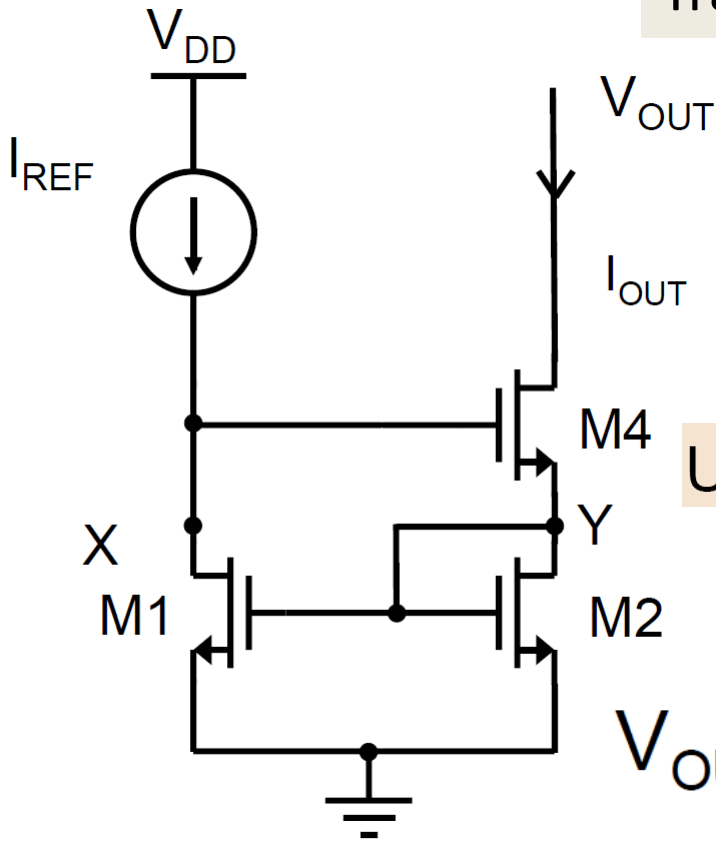
Output resistance of this cascode configuration much larger than basic two transistor Logic

dIO is proportional to $1/R_o$

The load current in the cascode circuit is more stable against variations of the output voltage

Wilson Current Mirror

Transistor M1 and M2 have the same overdrive



$$\frac{I_{OUT}}{I_{IN}} = \frac{\left(\frac{W}{L}\right)_2 (1 + \lambda V_Y)}{\left(\frac{W}{L}\right)_1 (1 + \lambda V_X)}$$

Use feedback to stabilize the output current

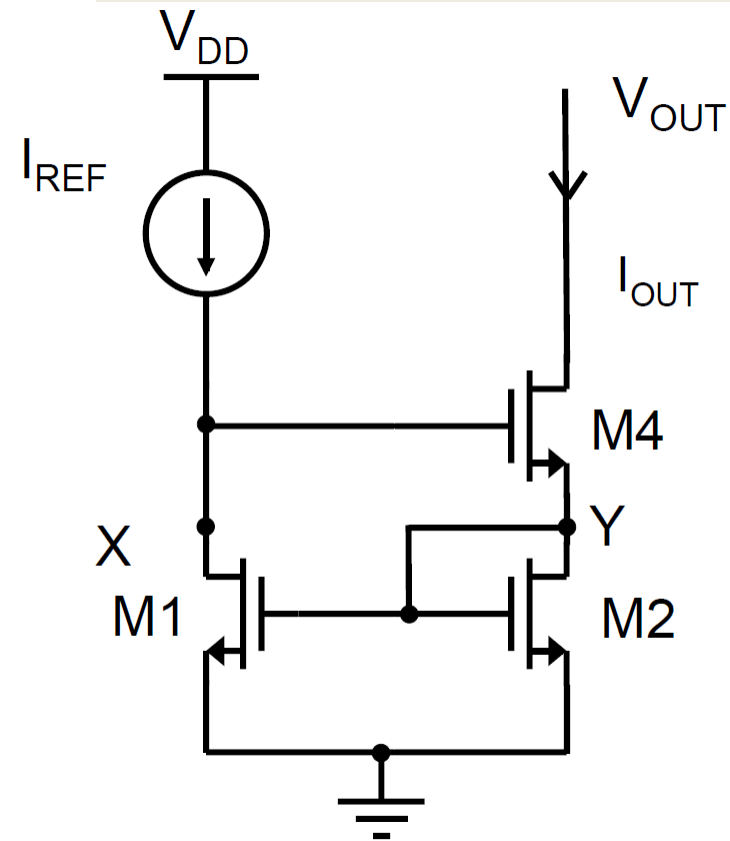
$$V_{OUT} \uparrow \Rightarrow I_{OUT} \uparrow \Rightarrow V_Y \uparrow \Rightarrow V_X \downarrow \Rightarrow I_{OUT} \downarrow$$

- MOSFET IC Biasing
- Current source circuit

Circuit Source: Donald Neamen

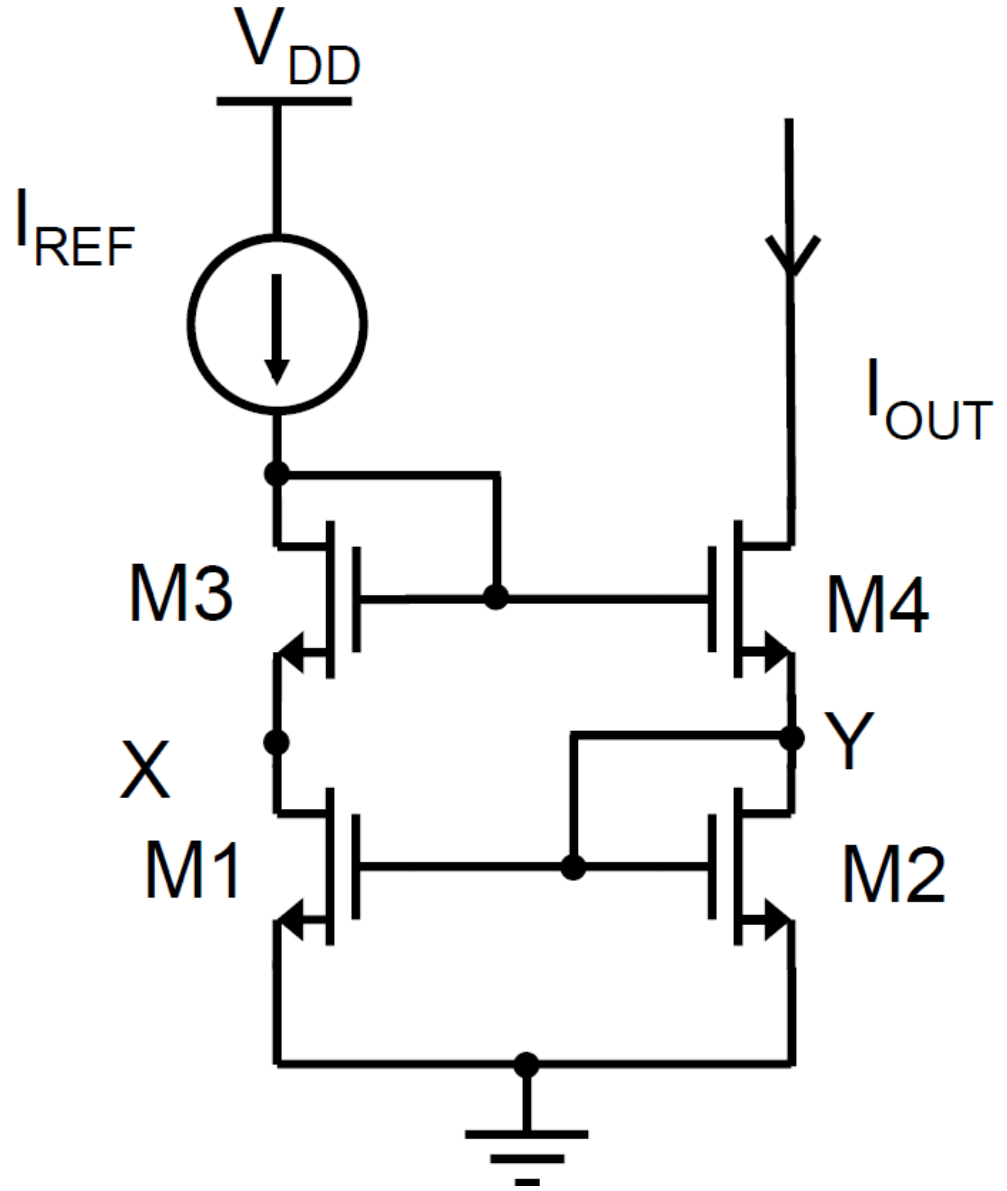
$$I_{ref} = \frac{1}{2} \mu_n C_{ox} \left[\frac{W}{L} \right]_1 (V_{GS} - V_{TN})^2 (1 + \lambda V_{DS1})$$

$$I_{out} = \frac{1}{2} \mu_n C_{ox} \left[\frac{W}{L} \right]_1 (V_{GS} - V_{TN})^2 (1 + \lambda V_{DS})$$



$$V_{OUT} \uparrow \Rightarrow I_{OUT} \uparrow \Rightarrow V_Y \uparrow \Rightarrow V_X \downarrow \Rightarrow I_{OUT} \downarrow$$

Modified Wilson current source



Two additional multi-MOSFET current sources are shown in Figure (a) The circuit is the **Wilson current source**.

Note:

V_{DS} values of $M1$ and $M2$ are not equal. Since λ is not zero the ratio $\frac{I_o}{I_{REF}}$ is slightly different from the aspect ratios.

This problem is solved in the **modified Wilson current source**, shown in Figure b, which includes transistor $M4$. For a constant reference current, the **drain-to-source voltages of $M1$, $M2$, and $M4$ are held constant**. The primary advantage of these circuits is the increase in output resistance, which further stabilizes the load current