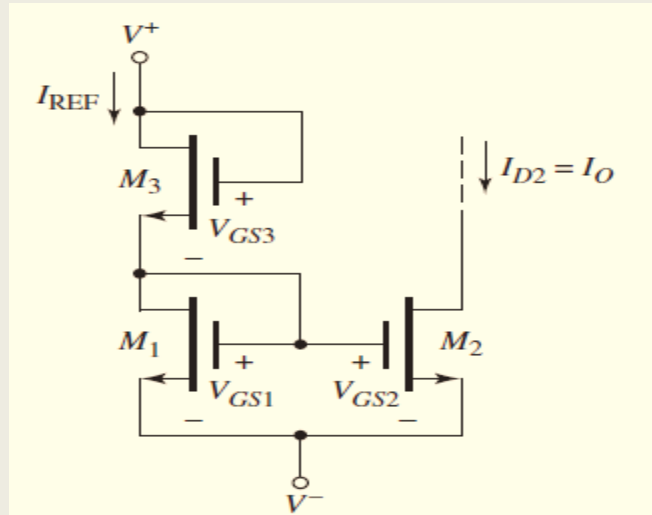


# Numerical

Design a MOSFET current source circuit to meet a set of specifications.



The bias voltages are  $V^+ = 2.5 \text{ V}$  and  $V^- = 0$ . Transistors are available with parameters  $k'_n = 100 \mu\text{A/V}^2$ ,  $V_{TN} = 0.4 \text{ V}$ , and  $\lambda = 0$ . Design the circuit such that  $I_{REF} = 100 \mu\text{A}$ ,  $I_O = 60 \mu\text{A}$ , and  $V_{DS2(sat)} = 0.4 \text{ V}$ .

We have  $V_{DS2}(\text{sat}) = 0.4 = V_{GS2} - 0.4$ , so that  $V_{GS2} = V_{GS1} = 0.8 \text{ V}$   
Then for transistor  $M_2$ ,

$$\left(\frac{W}{L}\right)_2 = \frac{I_0}{\left(\frac{k'_n}{2}\right)(V_{GS2} - V_{TN})^2} = \frac{60}{\left(\frac{100}{2}\right)(0.8 - 0.4)^2} = 7.5$$

For transistor  $M_1$ ,

$$\left(\frac{W}{L}\right)_1 = \frac{I_{\text{REF}}}{\left(\frac{k'_n}{2}\right)(V_{GS1} - V_{TN})^2} = \frac{100}{\left(\frac{100}{2}\right)(0.8 - 0.4)^2} = 12.5$$

WKT

From the circuit, we see that

$$V_{GS1} + V_{GS3} = V^+ - V^-$$

The value of  $V_{GS3}$  is found as

$$V_{GS3} = (V^+ - V^-) - V_{GS1} = 2.5 - 0.8 = 1.7 \text{ V}$$

Then for transistor  $M_3$  we find

$$\left(\frac{W}{L}\right)_3 = \frac{I_{\text{REF}}}{\left(\frac{k'_n}{2}\right)(V_{GS3} - V_{TN})^2} = \frac{100}{\left(\frac{100}{2}\right)(1.7 - 0.4)^2} = 1.18$$

# Problem Statement

Consider the MOSFET current-source circuit in Figure with  $V^+ = +2.5$  V and  $R = 15$  k $\Omega$ . The transistor parameters are  $V_{TN} = 0.5$  V,  $k'_n = 80$   $\mu$ A/V<sup>2</sup>,  $W/L = 6$ , and  $\lambda = 0$ . Determine  $I_{REF}$ ,  $I_O$ , and  $V_{DS2}(\text{sat})$ .

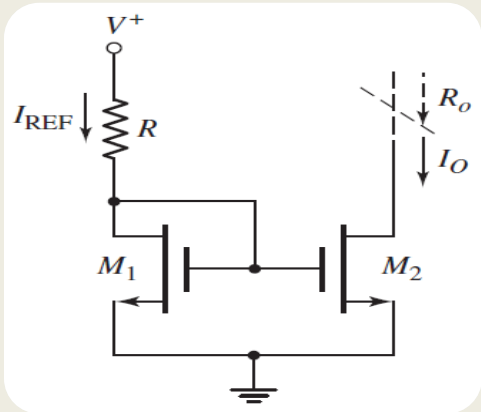
$$I_{REF} = \frac{2.5 - V_{GS}}{15} = \left( \frac{0.08}{2} \right) (6) (V_{GS} - 0.5)^2$$

$$2.5 - V_{GS} = 3.6 (V_{GS}^2 - V_{GS} + 0.25)$$

$$3.6 V_{GS}^2 - 2.6 V_{GS} - 1.6 = 0$$

$$V_{GS} = \frac{2.6 \pm \sqrt{6.76 + 23.04}}{2(3.6)}$$

$$V_{GS} = 1.12 \text{ V} (1.1193)$$



$$I_{REF} = \frac{2.5 - 1.1193}{15} \Rightarrow I_{REF} = 92.0 \mu\text{A} \quad (92.05)$$

$$I_o = 92.0 \mu\text{A}$$

$$V_{DS2}(\text{sat}) = V_{GS} - V_{TN} = 1.1193 - 0.5$$

$$V_{DS2}(\text{sat}) = 0.619 \text{ V}$$

## MOSFET Current source circuit

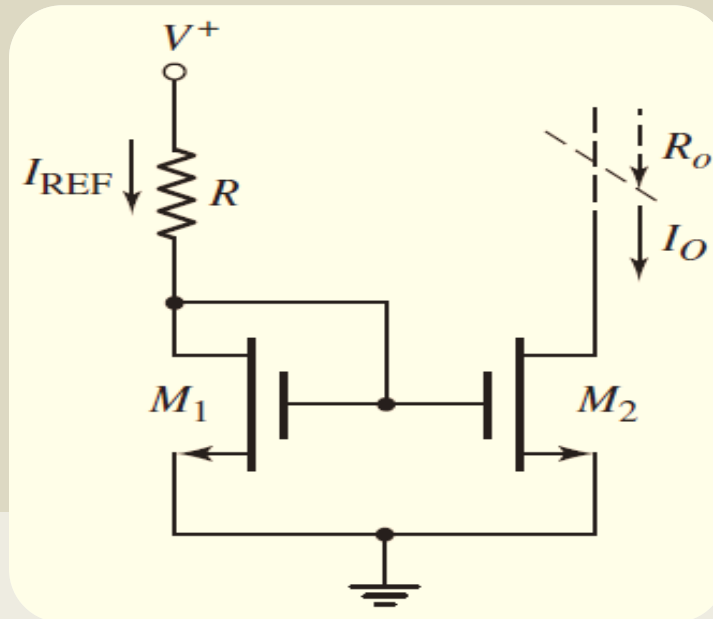
$$V^+ = 2V$$

Parameters are  $V_{TN} = 0.5V$ ,  $K_n = 80\mu A/V^2$ ,  $V_{DS2}(sat) = 0.25V$  and  $\lambda = 0.015V^{-1}$

(a) Design the circuit such that  $I_{REF} = 50\mu A$  and normal bias current  $I_0 = 100\mu A$

(b) Find the output resistance ( $R_o$ )

(c) Determine the percentage change in  $I_0$  for a change in drain to source voltage  $\Delta V_{DS2} = 1V$



1

$$I_{REF} = 50 = \left(\frac{80}{2}\right) \left(\frac{W}{L}\right)_1 (V_{GS} - 0.5)^2$$

$$I_{REF} = 0.050 = \frac{2.0 - V_{GS}}{R}$$

Design such that  $V_{DS2}(\text{sat}) = 0.25 = V_{GS} - 0.5$   
 $V_{GS} = 0.75 \text{ V}$

$$0.050 = \frac{2 - 0.75}{R} \Rightarrow \underline{R = 25 \text{ K}}$$

$$50 = \left(\frac{80}{2}\right) \left(\frac{W}{L}\right)_1 (0.75 - 0.5)^2 \Rightarrow \underline{\left(\frac{W}{L}\right)_1 = 20}$$

$$\frac{\left(\frac{W}{L}\right)_1}{\left(\frac{W}{L}\right)_2} = \frac{I_{REF}}{I_O} \Rightarrow \frac{20}{\left(\frac{W}{L}\right)_2} = \frac{50}{100} \Rightarrow \underline{\left(\frac{W}{L}\right)_2 = 40}$$

2

$$R_o = \frac{1}{\lambda I_o} = \frac{1}{(0.015)(0.1)} \Rightarrow R_o = 667 \text{ K}$$

$$\Delta I_o = \frac{\Delta V}{R_o} = \frac{1}{666} \Rightarrow 1.5 \text{ } \mu\text{A}$$

3

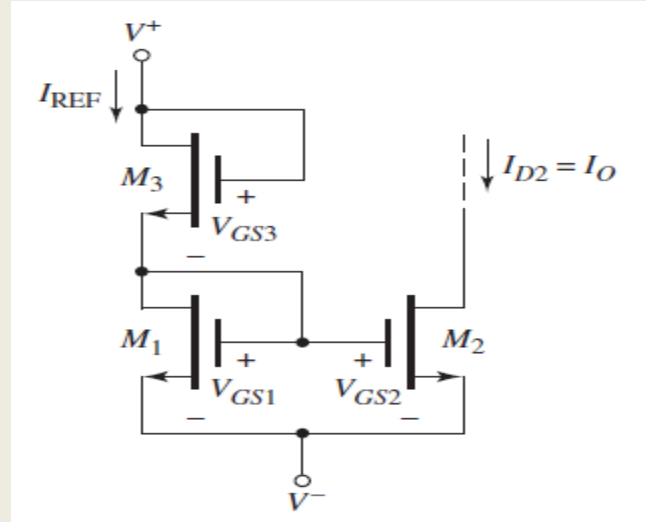
$$\Delta I_o = \frac{\Delta V}{R_o} = \frac{1}{666} \Rightarrow 1.5 \text{ } \mu\text{A}$$

$$\frac{\Delta I_o}{I_o} \times 100\% = \left( \frac{1.5}{100} \right) \times 100\% \Rightarrow \underline{1.5\%}$$



A:1

Design a MOSFET current source circuit to meet a set of specifications.

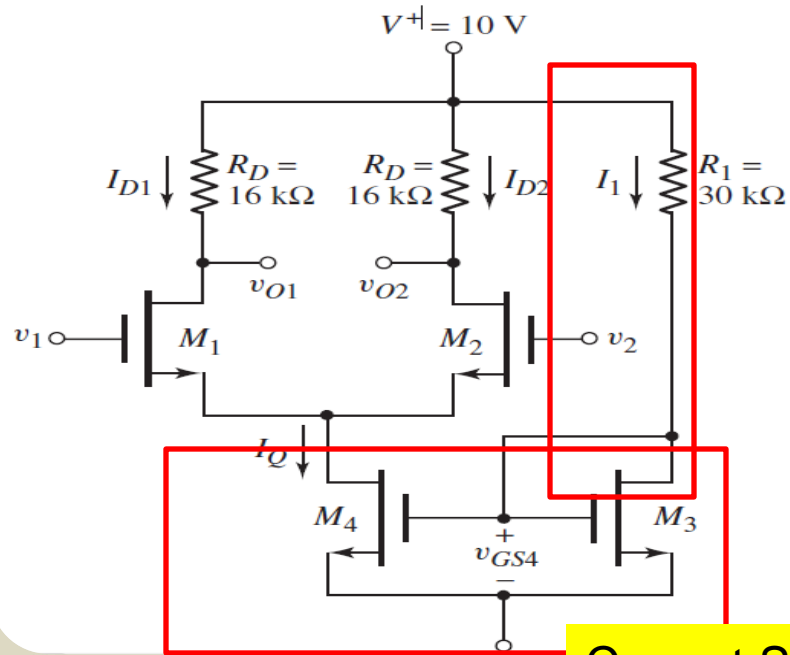


The bias voltages are  $V^+ = 5\text{ V}$  and  $V^- = 0$ . Transistors are available with parameters  $k'_n = 20\text{ }\mu\text{A/V}^2$ ,  $V_{TN} = 1\text{ V}$ , and  $\lambda = 0$ . Design the circuit such that  $I_{REF} = 0.25\text{ mA}$ ,  $I_O = 0.1\text{ mA}$ , and  $V_{DS2(sat)} = 0.85\text{ V}$

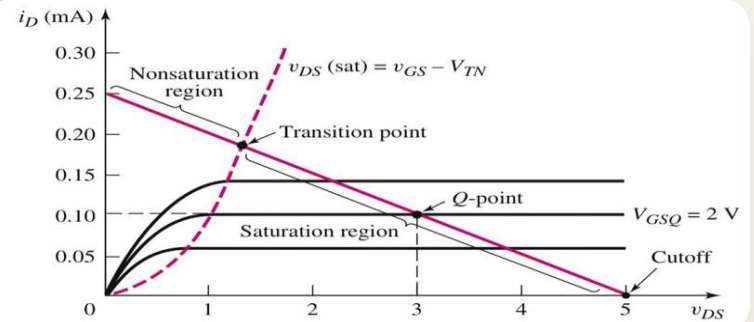
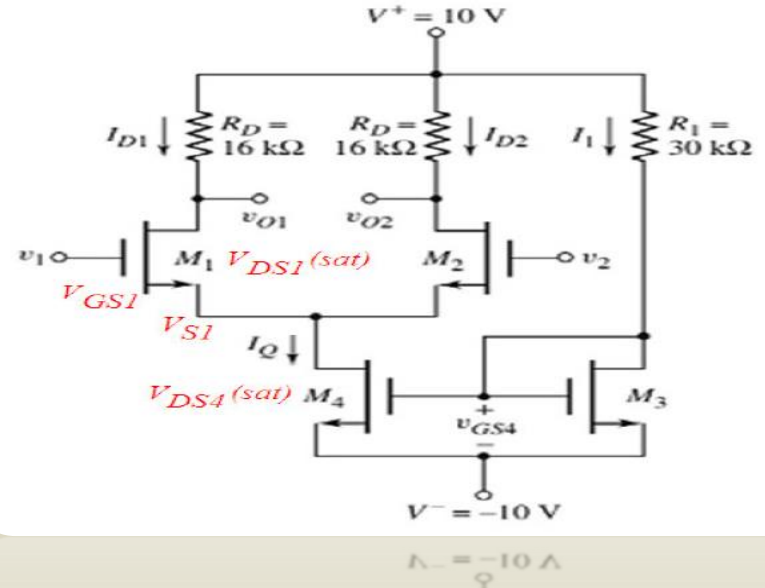
# Calculate the dc characteristics of a MOSFET diffamp

*Consider the diff – amp shown in Figure 11.20. The transistor parameters are  $K_{n1} = K_{n2} = 0.1 \text{ mA/V}^2$ ,  $K_{n3} = K_{n4} = 0.3 \text{ mA/V}^2$ , and for all transistors  $\lambda = 0$  and  $V_{TN} = 1 \text{ V}$*

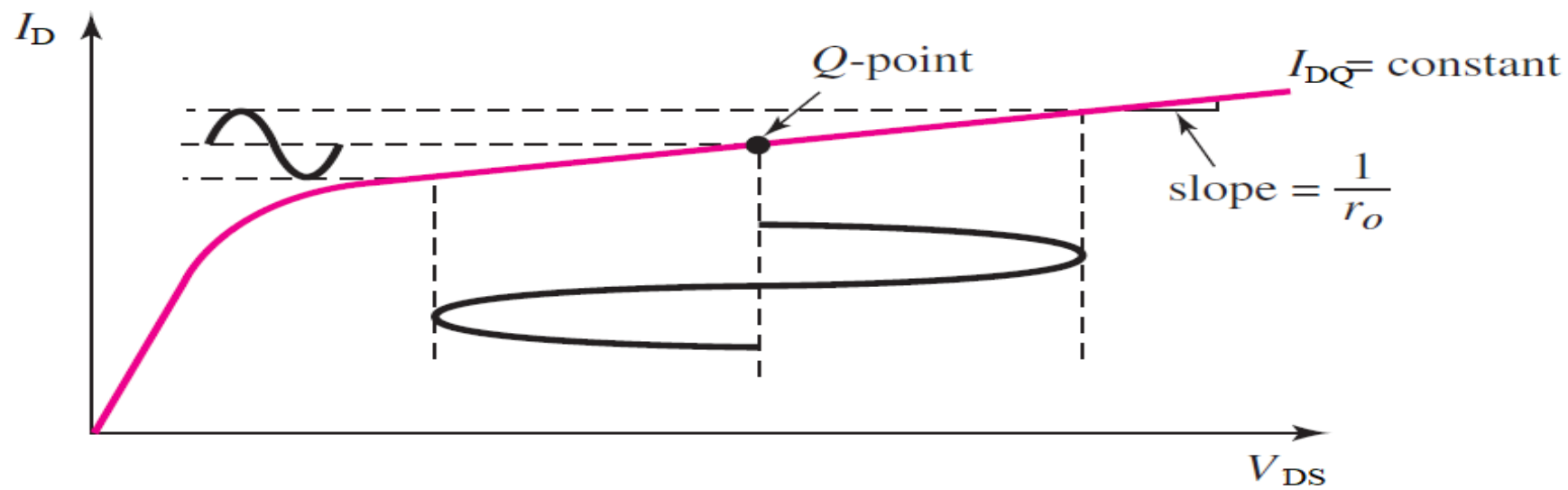
*Determine the maximum range of common – mode input voltage, i.e. find  $v_{CM (max)}$  and  $v_{CM (min)}$*



Current Source



Circuit Source: Donald A. Neamen



The reference current can be determined from:

$$I_1 = \frac{V^+ - V^- - V_{GS4}}{R_1} = \frac{20 - V_{GS4}}{R_1} \quad \text{Eq.1}$$

$$I_1 = K_{n3} (V_{GS4} - V_{TN})^2 \quad \text{Eq.2}$$

Comparing equation 1 and 2

$$\frac{20 - V_{GS4}}{30} = (0.3)(V_{GS4} - 1)^2$$

$$20 - V_{GS4} = 9(V_{GS4} + 1 - 2V_{GS4})$$

$$20 - V_{GS4} = 9V_{GS4}^2 + 9 - 18V_{GS4}$$

$$9V_{GS4}^2 - 17V_{GS4} - 11 = 0$$

$$V_{GS4} = 2.40 \text{ V}$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Substitute  $V_{GS4} = 2.40 \text{ V}$  from Eq.1

$$I_1 = \frac{20 - 2.40}{30} = 0.587 \text{ A}$$

Since M3 and M4 are identical, we also find

$$I_Q = 0.587 \text{ mA}$$

The quiescent drain currents in M1 and M2 are

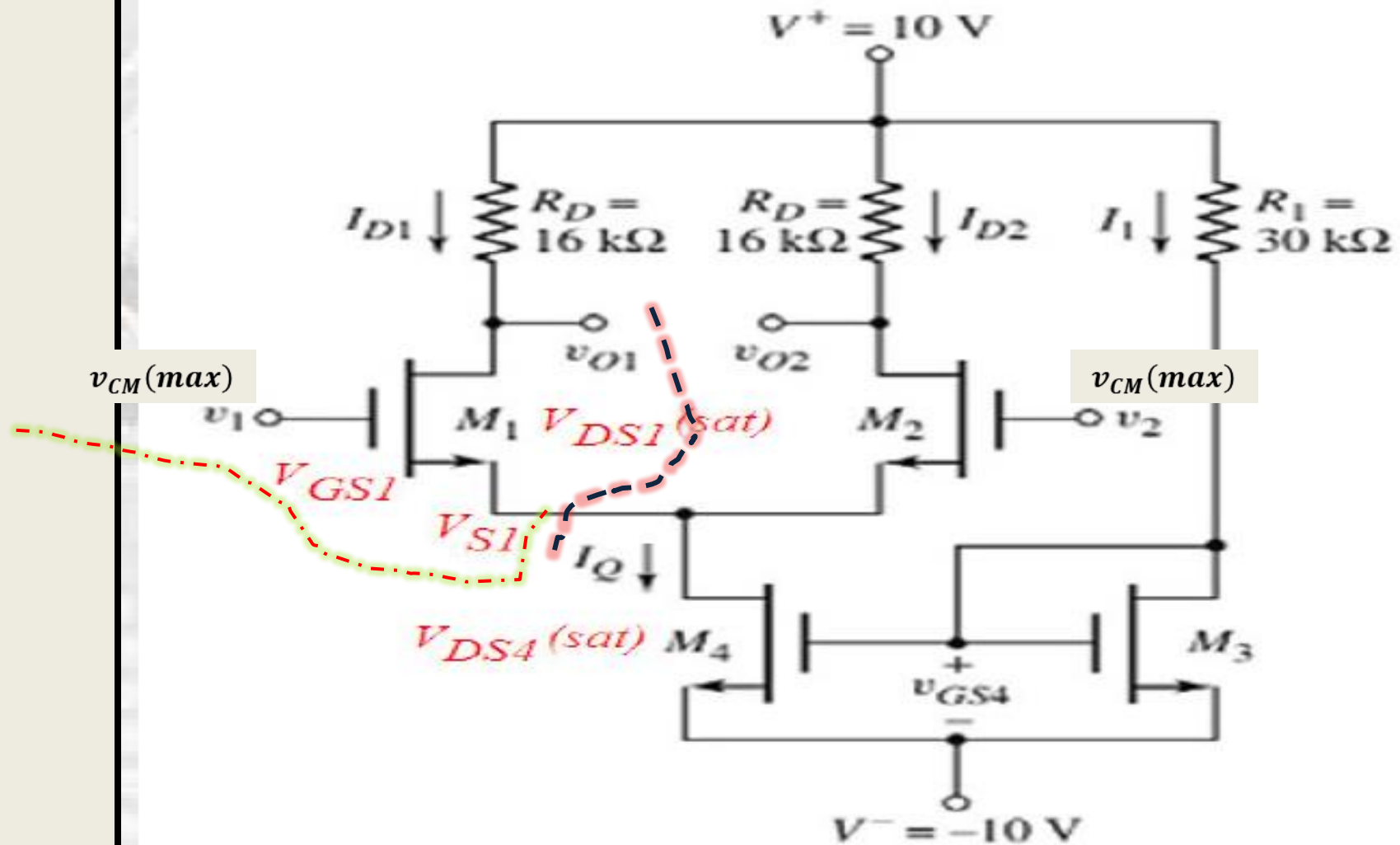
$$I_{D1} = I_{D2} = I_Q/2$$

The gate-to-source voltages are then

$$V_{GS1} = V_{GS2} = \sqrt{\frac{I_{D1}}{K_{n1}}} + V_{TN} = \sqrt{\frac{0.293}{0.1}} + 1 = 2.71\text{V}$$

The quiescent values of  $v_{O1}$  and  $v_{O2}$  are

$$v_{O1} = v_{O2} = 10 - I_D R_D = 10 - (0.293)(16) = 5.31\text{V}$$



Circuit Source: Donald A. Neamen

The maximum common-mode input voltage when  $M_1$  and  $M_2$  reach the trans

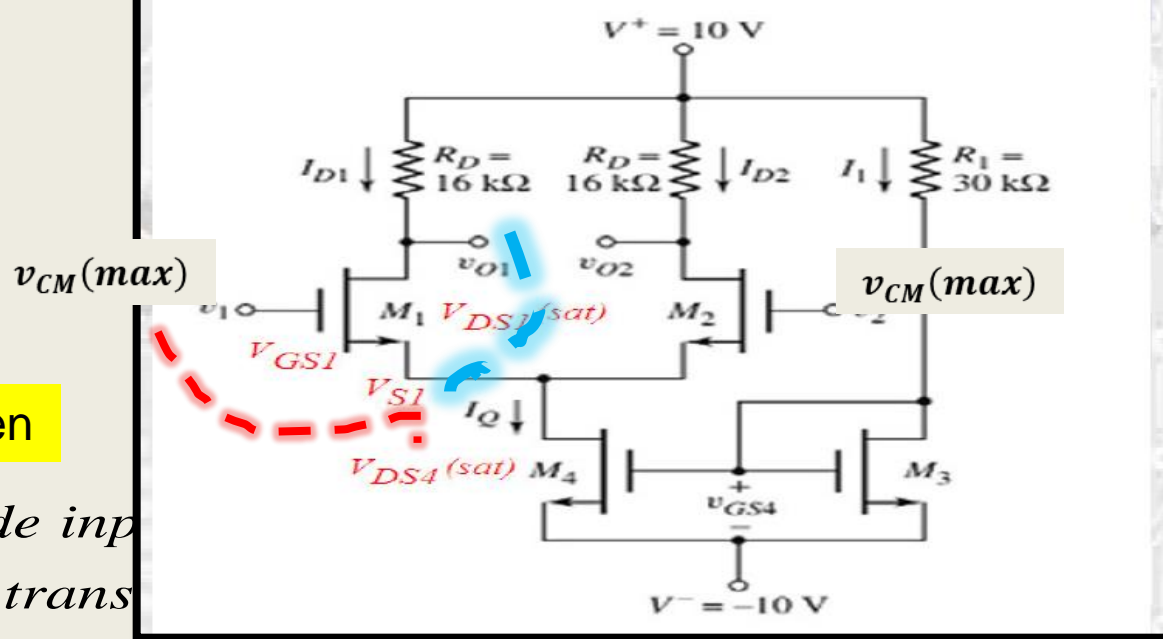
$$V_{DS1} = V_{DS2} = V_{DS1(sat)} = V_{GS1} - V_{TN}$$

$$V_{DS1} = 2.71 - 1 = 1.71 \text{ V}$$

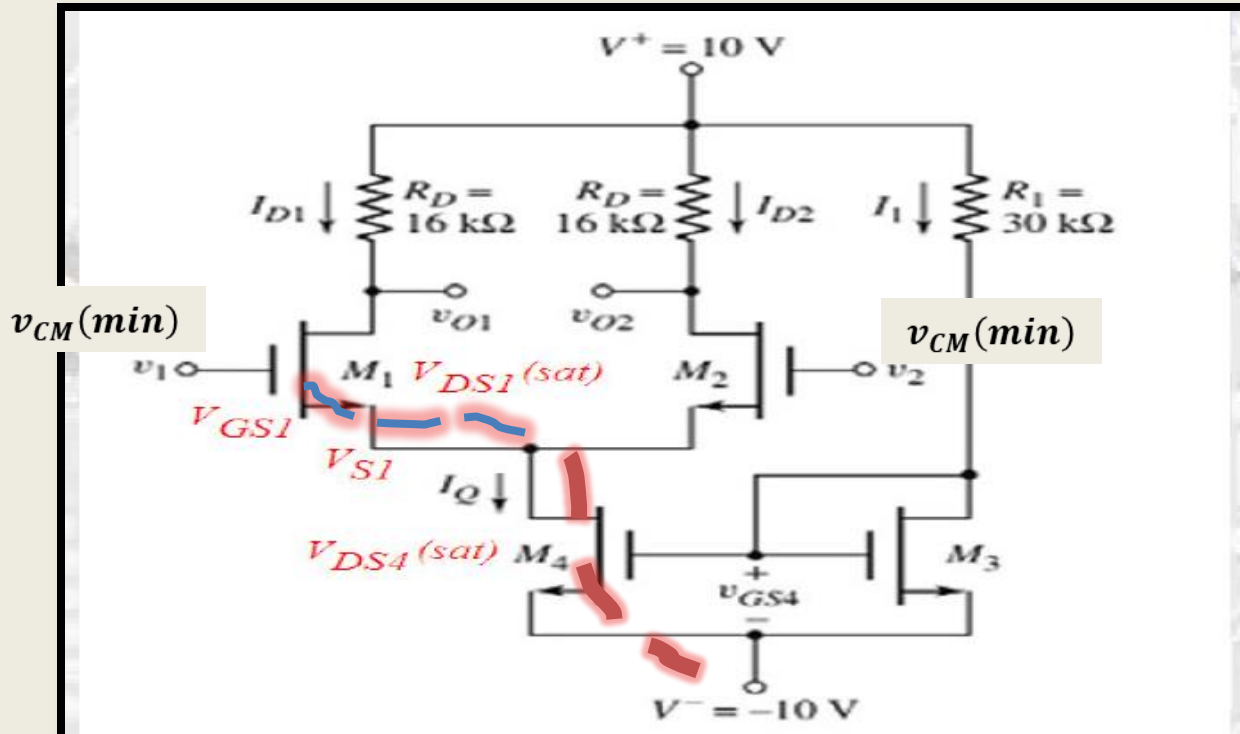
$$v_{CM(max)} = V_{S1(max)} + V_{GS1}$$

Therefore,

$$\begin{aligned} v_{CM(max)} &= v_{O1} - V_{DS1(sat)} + V_{GS1} \\ &= 5.31 - 1.71 + 2.71 = 6.31 \text{ V} \end{aligned}$$







The minimum common – mode input voltage is the value when  $M_4$  reaches the transition point,

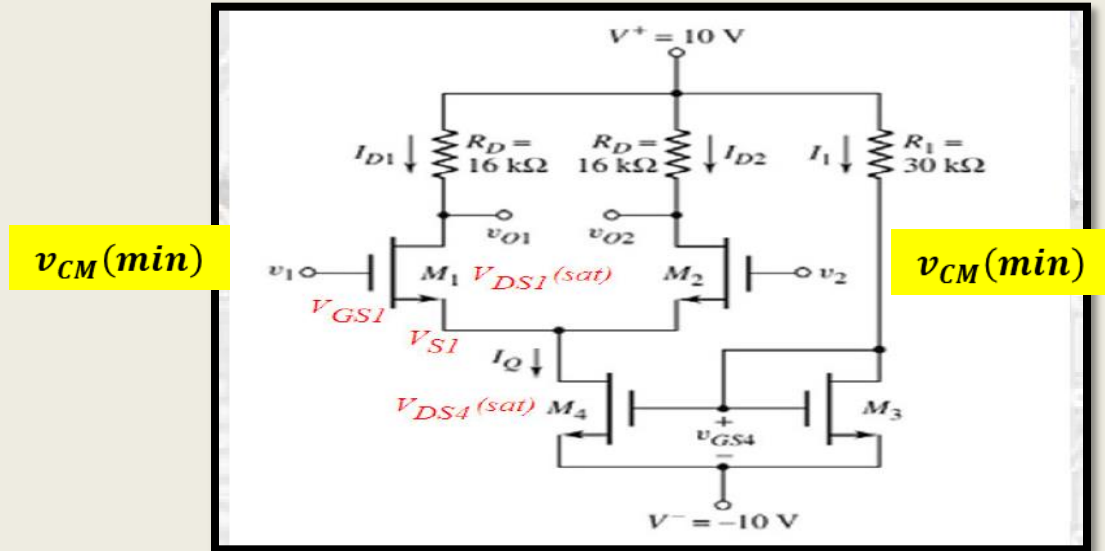
$$V_{DS4} = V_{DS4}(\text{sat}) = V_{GS4} - V_{TN} = 2.4 - 1 = 1.4\text{ V}$$

*Therefore,*

$$V_{CM \text{ (min)}} = V_S + V_{GS1}$$

$$V_{CM (min)} = V^{--} + V_{DS4 (sat)} + V_{GS1} = (-10) + 1.4 + 2.71 = -5.89 \text{ V}$$

For this circuit the maximum range for the common-mode input voltage is  $-5.89 < v_{CM} < 6.31$  V.



# A:2

For the differential amplifier in Figure , the parameters are:  $V_+ = 5\text{ V}$ ,  $V_- = -5\text{ V}$ ,  $R_1 = 80\text{ k}\Omega$ , and  $R_D = 40\text{ k}\Omega$ .

The transistor parameters are  $\lambda = 0$  and  $V_{TN} = 0.8\text{ V}$  for all transistors, and  $K_{n3} = K_{n4} = 100\text{ }\mu\text{A/V}^2$  and  $K_{n1} = K_{n2} = 50\text{ }\mu\text{A/V}^2$ . Determine the range of the common-mode input voltage.

a

