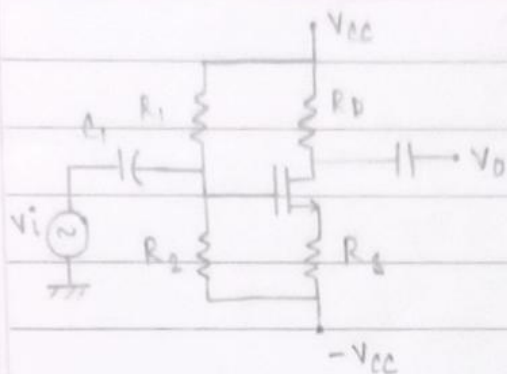


5.



$$V_{CC} = 10V$$

$$R_1 = 100 k\Omega$$

$$R_2 = 50 k\Omega$$

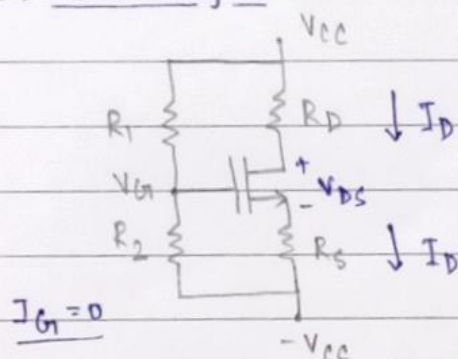
$$R_D = 5 k\Omega$$

$$R_S = 1 k\Omega$$

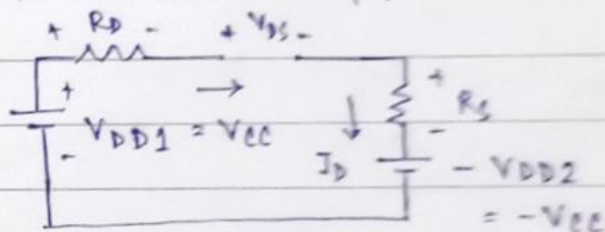
$$V_T = 1V$$

$$k_n = 0.5 \text{ mA/V}^2$$

(a) DC analysis:



KVL at D-S loop,



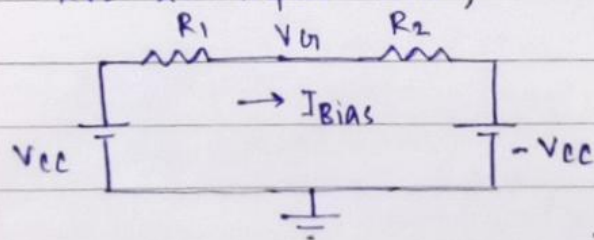
$$-V_{CC} + I_D R_D + V_{DS} + I_D R_S - V_{CC} = 0$$

$$\Rightarrow V_{DS} = 2V_{CC} - I_D (R_D + R_S)$$

$$\text{When } I_D = 0, V_{DS} = 2V_{CC}$$

$$\text{When } V_{DS} = 0, I_D = \frac{2V_{CC}}{R_D + R_S}$$

KVL at input side,



$$-V_{CC} + I_{Bias} (R_1 + R_2) - V_{CC} = 0$$

$$\Rightarrow I_{Bias} = \frac{2V_{CC}}{R_1 + R_2}$$

$$-V_{CC} + I_{Bias} R_1 + I_{Bias} R_2 - V_{CC} = 0$$

$$\text{Now, } I_{Bias} R_2 - V_{CC} = V_G$$

$$\therefore V_G = \left( \frac{2V_{CC}}{R_1 + R_2} \right) R_2 - V_{CC}$$

$$-V_S + I_D R_S - V_{CC} = 0$$

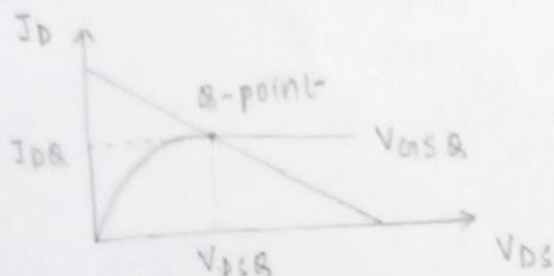
$$\therefore V_S = I_D R_S - V_{CC}$$

$$\begin{aligned}\text{Now, } V_{GS} &= V_G - V_S \\ &= \left( \frac{2V_{CC}}{R_1 + R_2} \right) R_2 - V_{GS} - I_D R_S + V_{CC} \\ &= \left( \frac{2V_{CC}}{R_1 + R_2} \right) R_2 - I_D R_S\end{aligned}$$

$$\therefore I_{DQ} = K (V_{GSQ} - V_T)^2$$

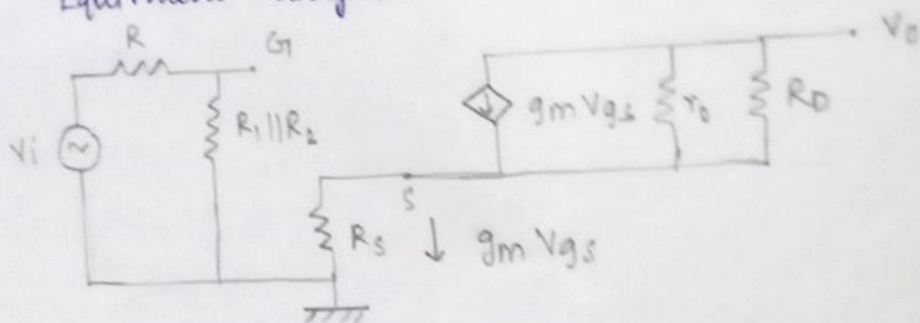
$$V_{DSQ} = 2V_{CC} - I_{DQ} (R_S + R_D)$$

Load line:



(b) Small Signal Analysis:

Equivalent diagram:



$$V_o = -g_m V_{gs} (r_o \parallel R_D)$$

$$V_i = V_{gs} + g_m V_{gs} R_S$$

$$= V_{gs} (1 + g_m R_S)$$

$\therefore$  Small signal voltage gain,

$$A_v = \frac{-g_m (r_o \parallel R_D)}{(1 + g_m R_S)}$$

$$|A_v| = \frac{g_m (r_o \parallel R_D)}{1 + g_m R_S}$$

$$\text{If } r_o = \infty, \text{ then } |A_v| = \frac{g_m R_D}{1 + g_m R_S}$$

(c) For the mentioned values,

$$V_{DS} = 2 \times 10 = 20 \text{ V}$$

$$I_D = \frac{(2 \times 10) \text{ V}}{(5 + 1) \text{ K}\Omega} = 3.33 \text{ mA}$$

$$\text{and, } V_{DSQ} = \left[ \frac{2 \times 10}{(100 + 50) \text{ K}} \right] \times 50 \text{ K} - (3.33 \text{ mA} \times 1 \text{ K}\Omega)$$

$$= 3.33 \text{ V}$$

$$I_{DQ} = 0.5 \text{ mA/V}^2 (3.33 - 1)^2$$

$$= 1.165 \text{ mA}$$

$$V_{DSQ} = 2 \times 10 - [1.165 \text{ mA} \times (1 + 5) \text{ K}]$$

$$= 13.01 \text{ V}$$

$\therefore$  Q-point,

$$V_{GSQ} = 3.33 \text{ V}$$

$$I_{DQ} = 1.165 \text{ mA}$$

$$V_{DSQ} = 13.01 \text{ V}$$

Now, small signal voltage gain,

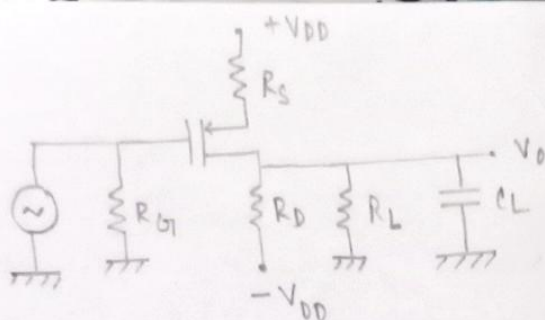
$$A_v = \frac{-g_m R_D}{1 + g_m R_S} \quad [\text{considering } r_o = \infty]$$

$g_m = \frac{I_{DQ}}{V_T}$ $= 3.33 \text{ mA/V}$	$A_v = \frac{-3.33 \text{ mA} \times 5 \text{ K}}{1 + (3.33 \text{ mA} \times 1 \text{ K})}$ $= -3.845$
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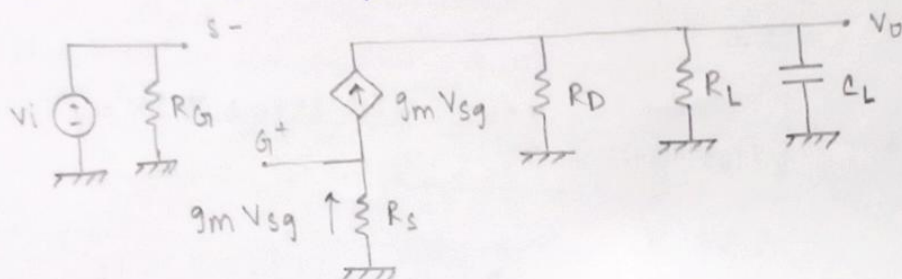
$$\therefore |A_v| = 3.845$$



6.



(a) Small signal Eq. circuit:



To find  $\tau$ , we set  $v_i = 0$ ,  $g_m v_{gs} = 0$   
Eq. resistance seen by  $C_L$  is  $R_D \parallel R_L$ .

$$\tau_p = (R_D \parallel R_L) C_L.$$

To find  $A_{v \max}$ , we open circuit  $C_L$ .

$$v_o = +g_m v_{gs} (R_D \parallel R_L)$$

Applying KVL,

$$v_i = v_{gs} (1 + g_m R_S)$$

$$\therefore |A_v|_{\max} = \frac{v_o}{v_i} = \frac{g_m (R_D \parallel R_L)}{1 + g_m R_S}$$

(b) Given,  $R_D = 10 \text{ k}\Omega$

$R_L = 100 \text{ k}\Omega$

$R_{G1} = 1 \text{ k}\Omega$

$V_{DD} = 20 \text{ V}$

$C_L = 1 \mu\text{F}$

$K_n = 1 \text{ mA/V}^2$

$$v_{GS} = \left( \frac{V_{DD} + V_{DD}}{R_D + R_{G1}} \right) R_{G1} - I_D R_D$$

$$\begin{aligned} \tau_p &= (10 \text{ k} \parallel 100 \text{ k}) \times 1 \mu\text{F} \\ &= \frac{10 \times 100 \times 10^3}{(10 + 100)} \times 1 \times 10^{-6} \\ &= 9.09 \text{ ms.} \end{aligned}$$

8. Given,  $K_n = 0.2 \text{ mA/V}^2$ ,  $V_T = 1 \text{ V}$ ,  $\lambda = 0$ ,  $C_{gd} = 0.02 \text{ pF}$ ,

$$C_{gs} = 0.25 \text{ pF}, I_{DQ} = 0.4 \text{ mA}.$$

$$I_{DQ} = K_n (V_{GS} - V_T)^2$$

$$\Rightarrow V_{GS} = \sqrt{\frac{I_{DQ}}{K_n}} + V_T = 2.41 \text{ V}.$$

$$\text{Now, } g_m = 2K_n (V_{GS} - V_{TN})$$

$$= 2 \times 0.2 \text{ m} (2.41 - 1)$$

$$= 0.4 \times 1.41 \times 10^{-3} \text{ A/V}$$

$$= 0.56 \text{ mA/V}.$$

$$\therefore \text{Unity gain frequency, } f_T = \frac{g_m}{2\pi (C_{gs} + C_{gd})}$$

$$= \frac{0.56 \text{ m}}{2\pi (0.02 \text{ p} + 0.25 \text{ p})}$$

$$= \frac{0.56 \text{ m}}{2\pi (0.27 \text{ p})}$$

$$= 330.09 \text{ MHz}.$$