

Key Friday - C1 slot

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21BLC1500

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19 (a)

$$V_{OT} = \left(1 + \frac{R_f}{R_i}\right) V_{ios} + R_f I_B$$

$$= \left(1 + \frac{10 \text{ k}\Omega}{1 \text{ k}\Omega}\right) (10 \text{ mV}) + (10 \text{ k}\Omega) (300 \text{ nA})$$

$$= 110 \text{ mV} + 3 \text{ mV} = 113 \text{ mV}$$

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(b) R_{comp} is needed:

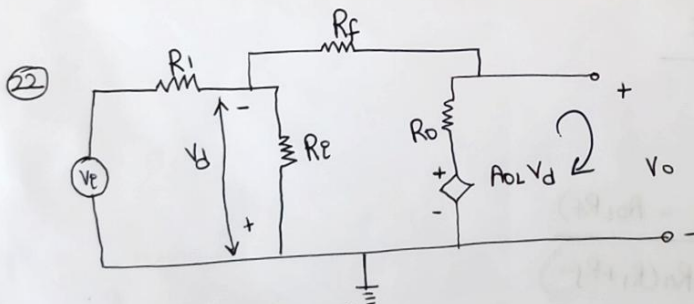
$$R_{comp} = 1 \text{ k}\Omega \parallel 10 \text{ k}\Omega = 990 \Omega$$

(c) R_{comp} in circuit is found so with that we can find

$$V_{OT} = \left(1 + \frac{R_f}{R_i}\right) V_{ios} + R_f I_{os}$$

$$= 110 \text{ mV} + 0.5 \text{ mV}$$

$$= 110.5 \text{ mV}$$



The input impedance R_i of an ~~amp~~ op-amp is usually much greater than R_i , so we may assume

$$V_{eq} = V_i ; R_{eq} = R_i$$

From outer loop:

$$V_o = I R_o + A_{OL} V_d$$

$$V_d + I R_f + V_o = 0$$

Putting V_o value

$$V_o(1 + A_{OL}) = i(R_o - A_{OL}R_f)$$

By KCL:

$$V_i = i(R_1 + R_f) + V_o$$

$$A_{CL} = \frac{V_o}{V_i} = \frac{R_o - A_{OL}R_f}{R_o + R_f + R_1(1 + A_{OL})}$$

$$A_{CL} \approx -\frac{R_f}{R_1}$$

for output resistance R_{of} :

$$i_A = \frac{V_i - 0}{R_1 + R_f}$$

$$i_B = \frac{A_{OL} V_d}{R_o}$$

$$\therefore V_d = -i_A R_f$$

$$\text{So, } i_B = \frac{-A_{OL} i_A R_f}{R_o}$$

$$i_{sc} = i_A + i_B$$

$$\Rightarrow i_{sc} = V_i \frac{(R_o - A_{OL}R_f)}{R_o(R_1 + R_f)}$$

$$\therefore R_{of} = \frac{V_{oc}}{i_{sc}}$$

and $A_{CL} = \frac{V_{oc}}{V_i}$

$$R_{of} = \frac{A_{CL} V_i}{V_i \left[\frac{R_o - A_{OL}R_f}{R_o(R_1 + R_f)} \right]}$$

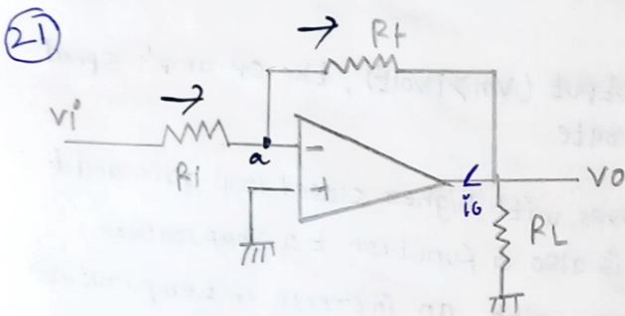
$$R_{of} = \frac{R_0 (R_1 + R_f)}{R_0 + R_f + R_1(1 + A_{OL})}$$

also can be written as

$$R_{of} = \frac{R_0(R_1 + R_f)}{R_0 + R_1 + R_f} \cdot \frac{1 + \frac{R_1 A_{OL}}{R_0 + R_1 + R_f}}$$

(20) input off set voltage due to temperature rise
 $= 0.15 (50 - 30)$
 $= 4.5 \text{ mV}$

Output voltage change $\Rightarrow V_O = V_{OS} \times A_{CL}$
 $= 4.5 \times 100$
 $= 450 \text{ mV}$



KCL:- at node a

$$\frac{V_i - 0}{R_i} = \frac{0 - V_O}{R_f}$$

$$V_O = -\frac{R_f}{R_i} V_i$$

$$= -\frac{100 \text{ K}}{1 \text{ K}} V_i$$

$$= -100 V_i$$

$$i_L + i_i = i_o$$

$$i_i = \frac{V_i - 0}{R_i}$$

$$= \frac{V_i}{1 \text{ K}}$$

$$i_L = \frac{V_O}{R_L} = \frac{-100 V_i}{R_L} = \frac{-2 V_i}{1 \text{ K}} \quad (R_L = 50 \text{ K})$$

$$= \frac{-2 V_i}{1 \text{ K}}$$

$$\begin{aligned}
 i_o &= i_1 + i_L \\
 &= \frac{V_1}{1K} - \frac{2V_1}{1K} \\
 &= -\frac{V_1}{1K}
 \end{aligned}$$

(23)

Slew rate:- The slew rate is defined as the maximum rate of output voltage caused by a step input voltage and is usually specified in V/ μ s.

- * For large signal output ($V_m > 1\text{ volt}$), the OP-amp's speed is limited by slew rate
- * The slew rate improves with higher closed loop gain and supply voltage. It is also a function of temperature and generally decreases with an increase in temperature

\Rightarrow the rate at which the voltage across the capacitor V_C increases is given by,

$$\frac{dV_C}{dt} = \frac{I}{C}$$

- * OP-amp should have either higher current or a small compensating capacitor. [For 741C capacitor charging current is limited 15 μ A]

$$SR (\text{slew rate}) = \frac{I_{\max}}{C} = \frac{15\mu\text{A}}{30\text{PF}} = 0.5\text{ V}/\mu\text{s}$$

$$\Rightarrow V_s = V_m \sin \omega t$$

$$V_o = V_m \sin \omega t$$

$$\frac{dV_o}{dt} = V_m \omega \cos \omega t$$

The maximum rate of change of the output occurs when

$\cos \omega t = 1$, that is

$$SR = \left. \frac{dV_o}{dt} \right|_{\max} = \omega V_m$$

$$\text{Slew Rate} = 2\pi f V_m \text{ V/s} \quad \text{--- (1)}$$

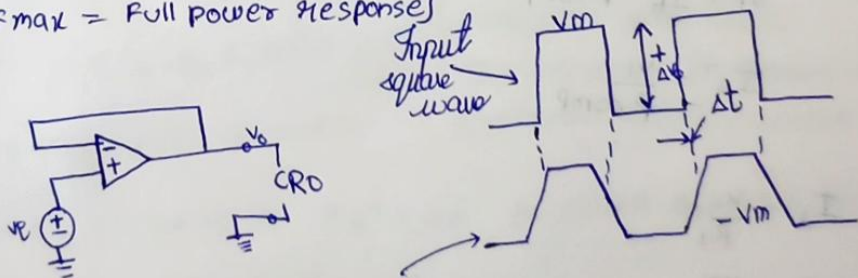
$$= \frac{2\pi f V_m}{10^6} \text{ V/us} \quad \left[\begin{array}{l} f \rightarrow \text{frequency} \\ V_m \rightarrow \text{Peak output amplitude} \end{array} \right]$$

~~* if f_{\max} is~~

* if eq-① is less than slew rate of the op-amp, then output will be undistorted. if frequency or amplitude of input signal is increased to exceed slew rate of op-amp the output will be distorted

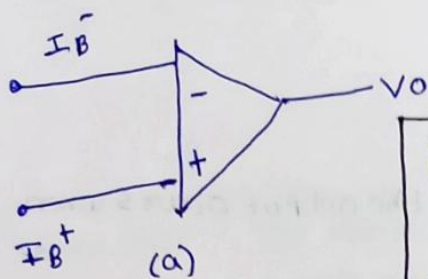
$$f_{\max} (\text{Hz}) = \frac{\text{slew rate}}{6.28 \times V_m} \times 10^6$$

[f_{\max} = Full power response]



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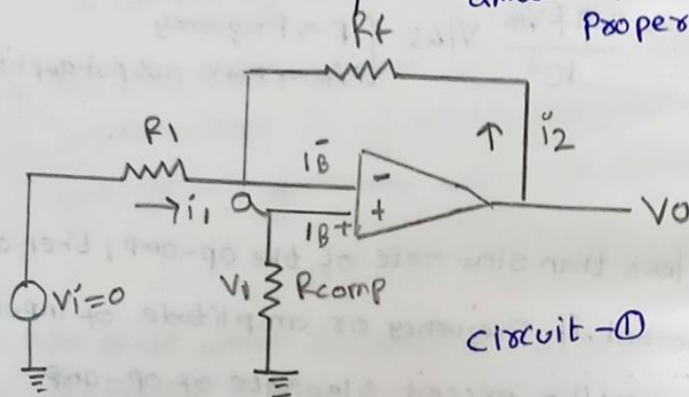
DC Characteristics



$$I_B = I_B^+ + I_B^-$$

input bias current:-
it is a current parameter I_{B1} defined as the average of the currents into the two input terminals with the output at a specified level. it is expressed in units of amperes. all opamps require certain amount of bias current for proper function

① Input Bias Current:-



KVL:-

$$-V_1 + 0 + V_2 - V_O = 0$$

$$V_O = V_2 - V_1$$

$$V_1 = I_{B^+} R_{comp}$$

$$I_{B^+} = \frac{V_1}{R_{comp}}$$

$$I_1 = \frac{V_1}{R_1}$$

$$I_2 = \frac{V_2}{R_f}$$

For Compensation $V_o = 0$, $v_i = 0$ so, $V_2 = V_1$

$$\Rightarrow I_2 = \frac{V_1}{R_f}$$

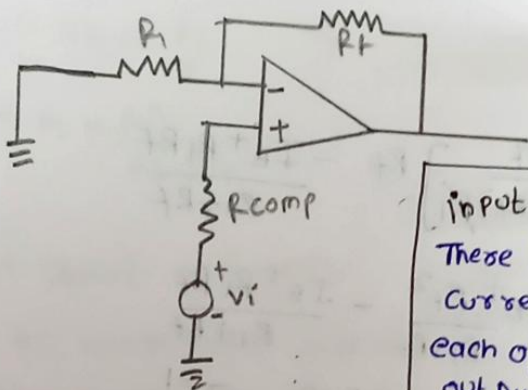
KCL at node a

$$I_B^- = I_2 + I_1 = \frac{V_1}{R_f} + \frac{V_1}{R_i} = V_1 \frac{(R_i + R_f)}{R_i R_f}$$

$$V_1 \frac{(R_i + R_f)}{R_i R_f} = \frac{V_1}{R_{comp}}$$

$$R_{comp} = \frac{R_i R_f}{R_i + R_f} = R_i || R_f$$

The effect of input bias current in a non inverting amplifier can also be compensated by placing a compensated R_{comp} in series with input signal V_i as shown.



$$R_{comp} = R_i || R_f //$$

input offset currents

There is a difference in the input current that flows in or out of each of the input pins even if the output voltage of operational amplifier is 0V.

The difference is known as the input offset current

② input offset current:-

The difference of I_B^+ & I_B^- is called offset current I_{os}

$$I_{os} = I_B^+ - I_B^-$$

$$V_1 = I_B^+ R_{comp}$$

$$I_1 = \frac{V_1}{R_1}$$

KCL at node a:- from circuit - ①

$$I_2 = (I_B^- - I_1) = I_B^- - \left(I_B^+ \frac{R_{comp}}{R_1} \right)$$

$$V_O = I_2 R_f - V_1 = I_2 R_f - I_B^+ R_{comp}$$

$$= \left[I_B^- - I_B^+ \frac{R_{comp}}{R_1} \right] R_f - I_B^+ R_{comp} \text{ --- ①}$$

$$\text{but } R_{comp} = \frac{R_1 R_f}{R_1 + R_f}$$

So, we get

$$V_O = R_f [I_B^- - I_B^+] //$$

⇒ substituting R_{comp}

$$\Rightarrow \left[I_B^- - I_B^+ \frac{\cancel{R_1} R_f}{(R_1 + R_f) \cancel{R_1}} \right] R_f - \frac{I_B^+ R_1 R_f}{R_1 + R_f}$$

$$= I_B^- R_f - I_B^+ \frac{R_f^2}{R_1 + R_f} - \frac{I_B^+ R_1 R_f}{R_1 + R_f}$$

$$= I_B^- R_f - I_B^+ R_f \left[\frac{R_f + R_1}{R_1 + R_f} \right] \rightarrow = 1$$

$$= I_B^- R_f - I_B^+ R_f$$

$$= R_f [I_B^- - I_B^+]$$

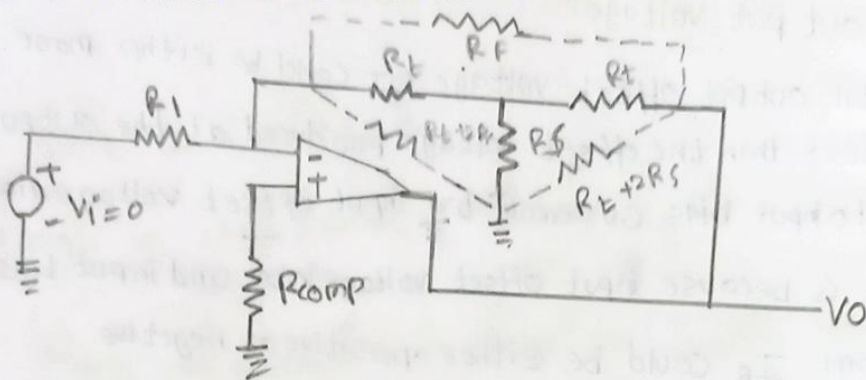
$$V_O = R_f I_{os}$$

∴ We can say that effect of offset current can be minimized by keeping feedback resistance small.

but R_f must be large

So,

T-Feedback is the solution



$$R_f = \frac{R_f^2 + 2R_f R_s}{R_s}$$

To design a T-network, first pick

$$R_f \ll \frac{R_f}{2}$$

$$\text{calculate, } R_s = \frac{R_f^2}{R_f - 2R_f}$$

③ Input offset voltage:-

due to unavoidable imbalances in the op-amp the output voltage is not zero when input voltage is zero, this voltage is called input offset voltage

②

$$V_2 = \left[\frac{R_1}{R_1 + R_f} \right] V_0 \rightarrow \text{from circuit - ①}$$

$$V_0 = \left[\frac{R_1 + R_f}{R_1} \right] V_2 = \left[1 + \frac{R_f}{R_1} \right] V_2$$

$$V_{ios} = |V_1 - V_2| \text{ and } V_1 = 0$$

$$V_{ios} = V_2$$

$$V_o = \left[1 + \frac{R_f}{R_1} \right] V_{ios}$$

④ Total output voltage:-

The total output offset voltage V_{OT} could be either more (or) less than the offset voltage produced at the output due to input bias current or input offset voltage alone.

• This is because input offset voltage V_{ios} and input bias current I_B could be either positive or negative with respect to ground.

\Rightarrow the maximum offset voltage at the output of amplifier without compensating technique used.

$$V_{OT} = \left[1 + \frac{R_f}{R_1} \right] V_{ios} + R_f I_B$$

~~X~~ \neq

with R_{comp}

$$V_{OT} = \left[1 + \frac{R_f}{R_1} \right] V_{ios} + R_f I_{os}$$