

5.6 Circulator

Module:5 Microwave Passive components

Course: BECE305L – Antenna and Microwave Engineering

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Assistant Professor - SENSE

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CHENNAI

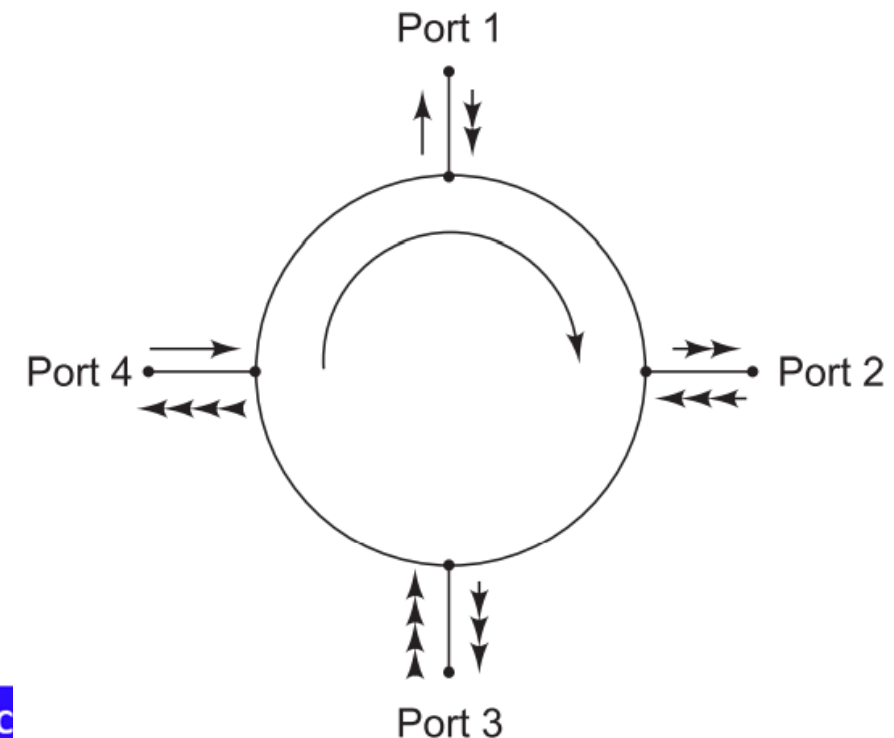
Module:5 Microwave Passive components

6 hours

- Microwave Networks - ABCD, 'S' parameter and its properties. E-Plane Tee, H-Plane Tee, Magic Tee and Multi-hole directional coupler. Principle of Faraday rotation, isolator, circulator and phase shifter.
- Source of the contents: Pozar

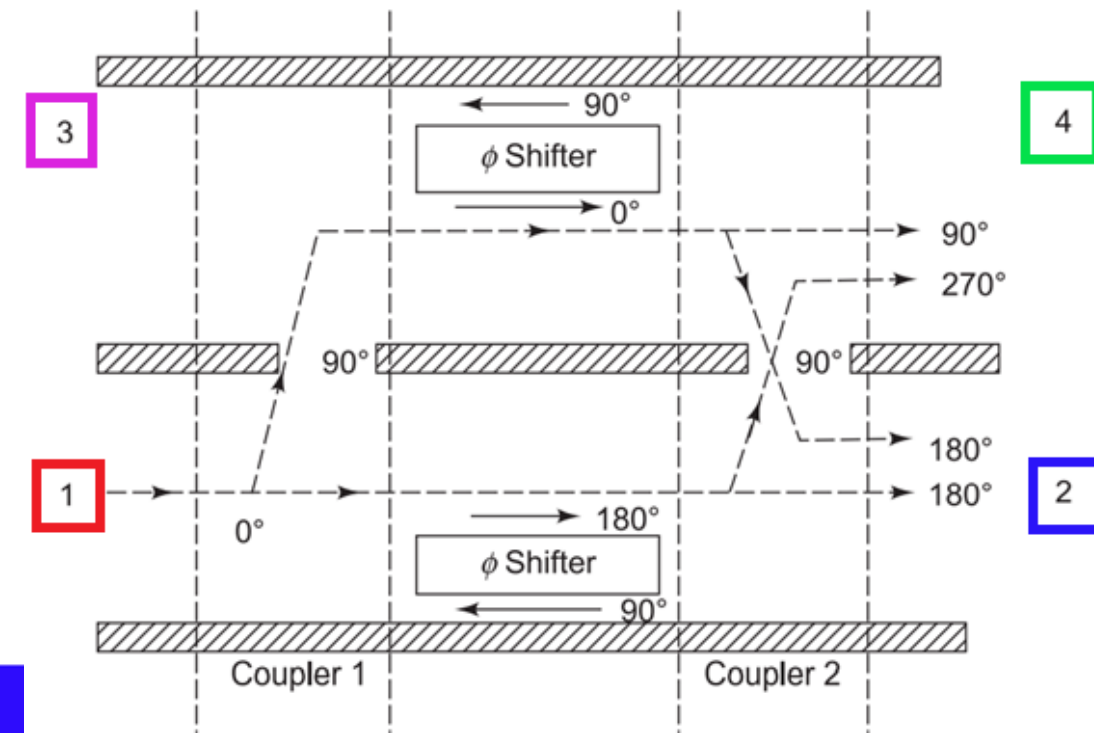
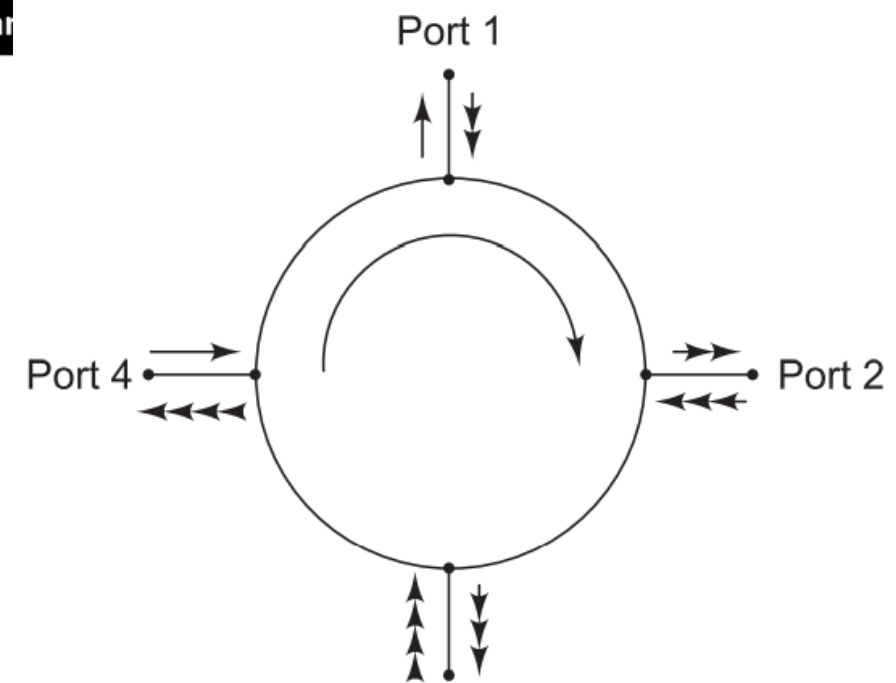
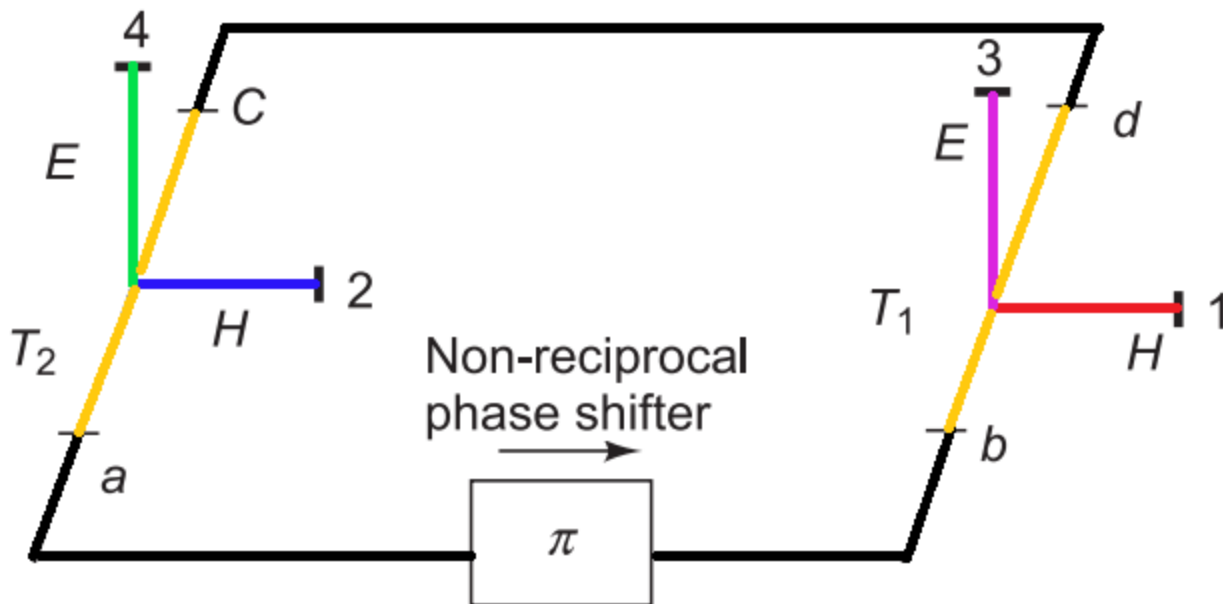
6. Circulators

- Ferromagnetic materials (ferrite: Mg+Mn, Ni+Zn alloys) when placed in dc magnetic field, electromagnetic wave propagation becomes non-reciprocal.
- This property is used for construction of circulators and isolators.
- Circulator: Multiport junction **wave can travel from one port to the next immediate port in one direction only.**
- Commonly used circulators
Three port or
Four port



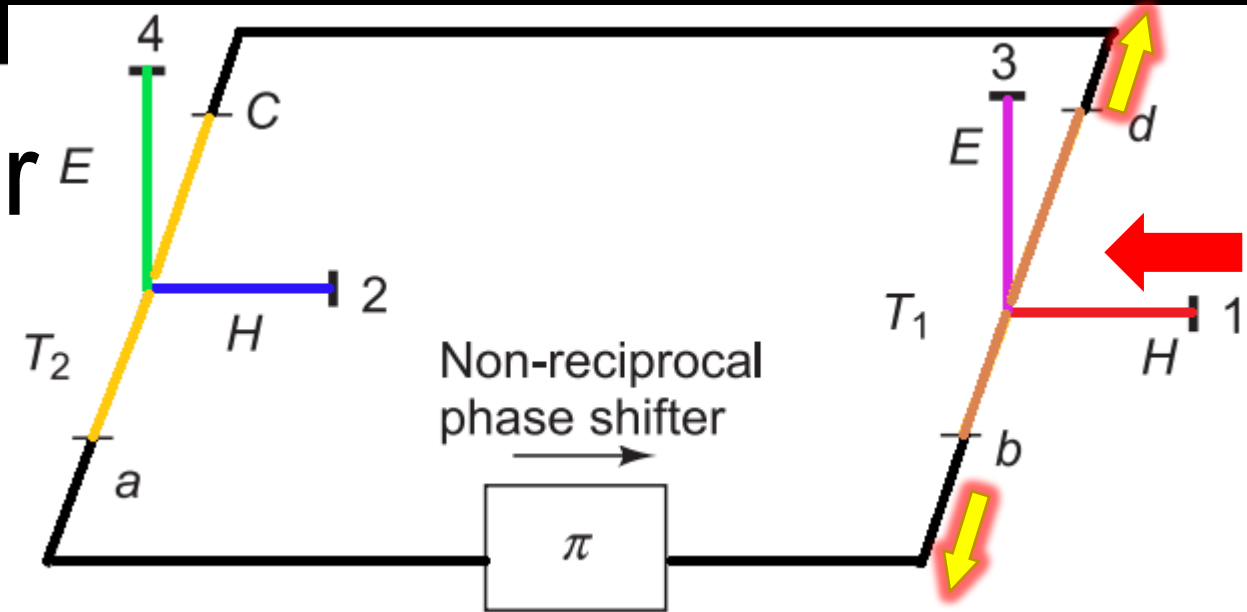
6.1 Four port Circulator

- Four port circulator – can be constructed
 - 1) from two magic Ts and a non reciprocal 180° phase shifter or
 - 2) a combination of two 3dB side hole directional couplers with two non-reciprocal phase shifters



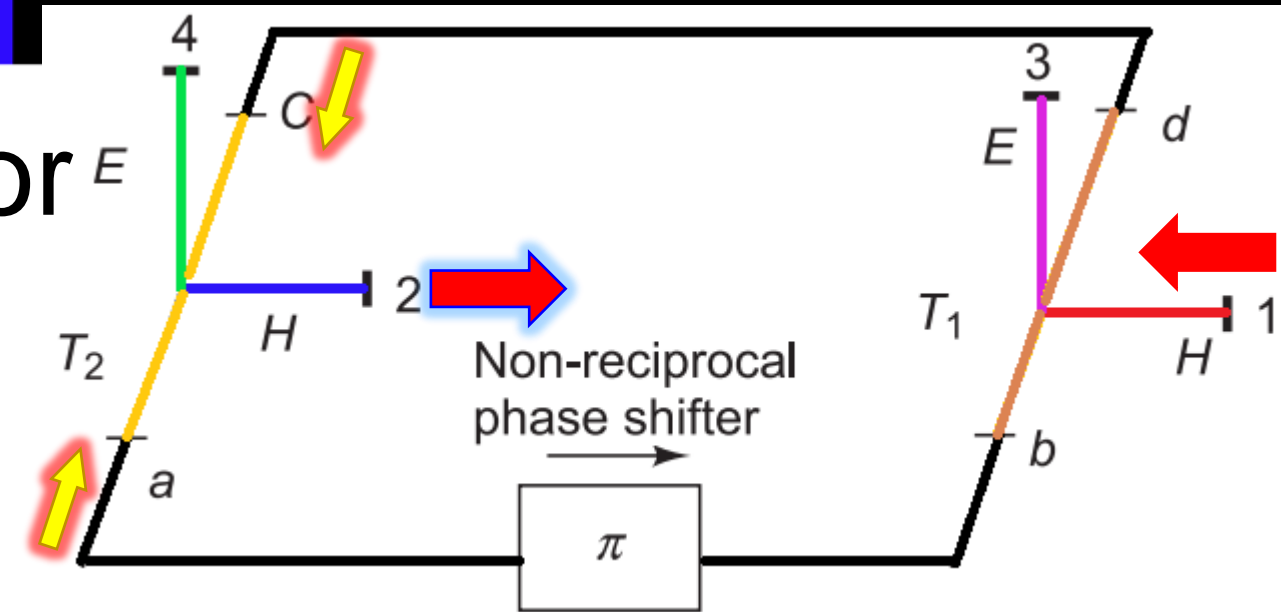
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- **Input signal at port 1** is split into two in phase and equal amplitude waves in collinear **arms b** and **d** of magic tee T_1 .



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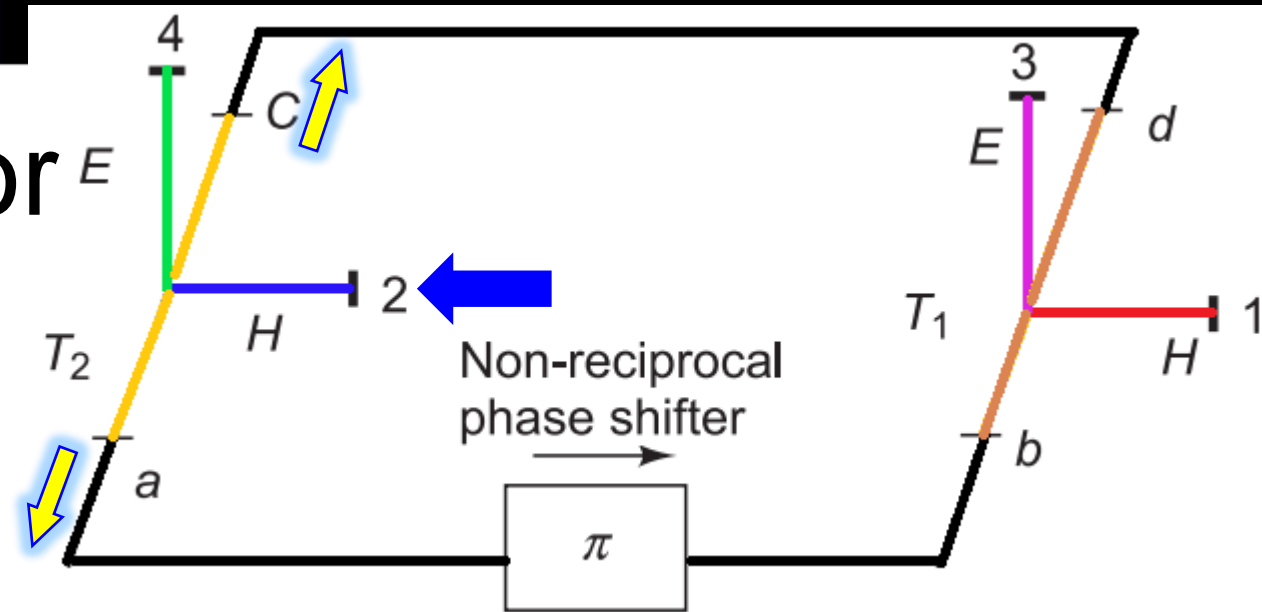
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6.1 Four port Circulator

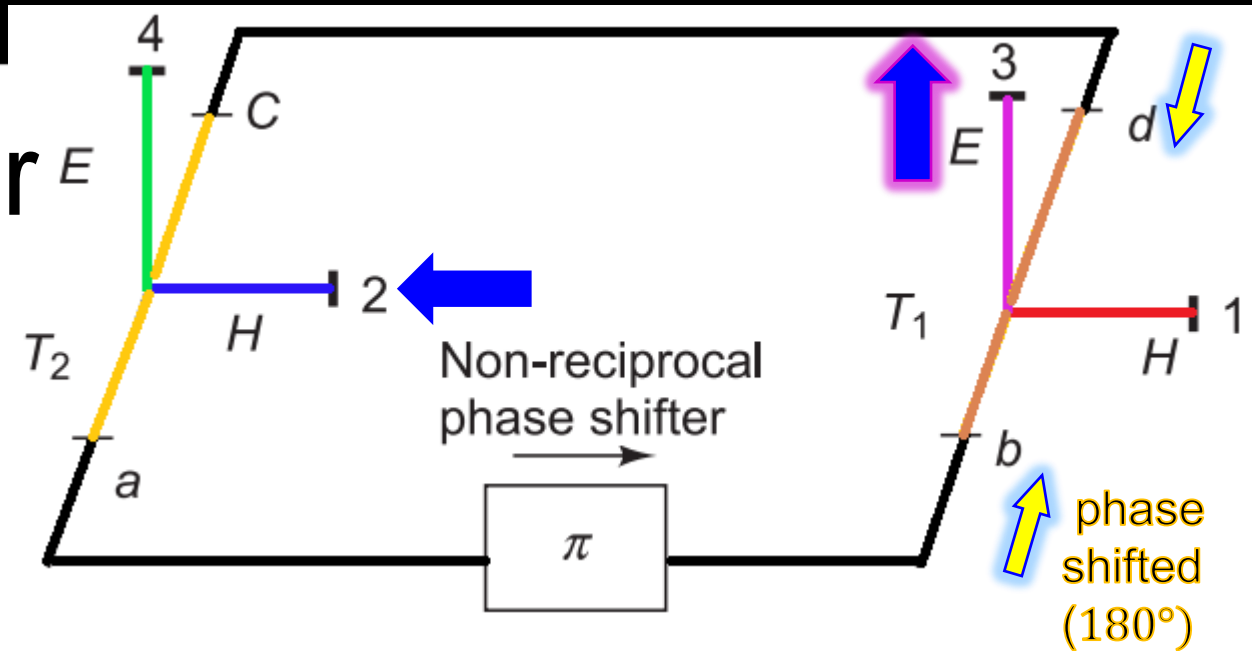
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They enter out of phase at **ports b** and **d** of magic tee **T1**, and appear at **port 3**.



6.1 Four port Circulator

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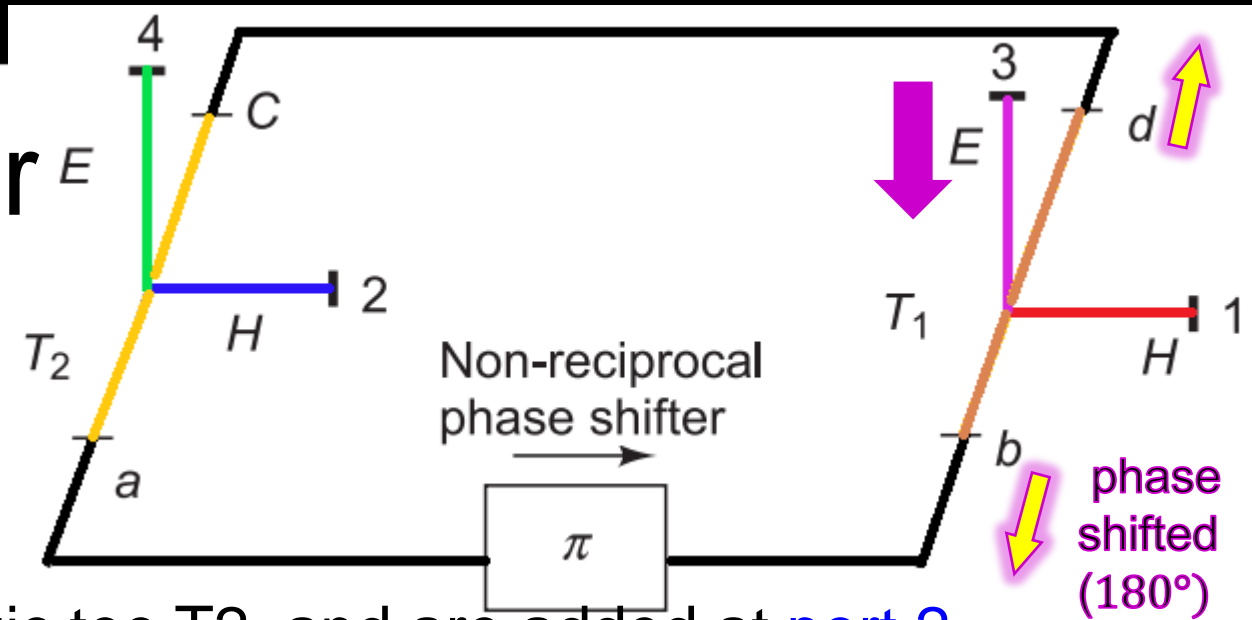
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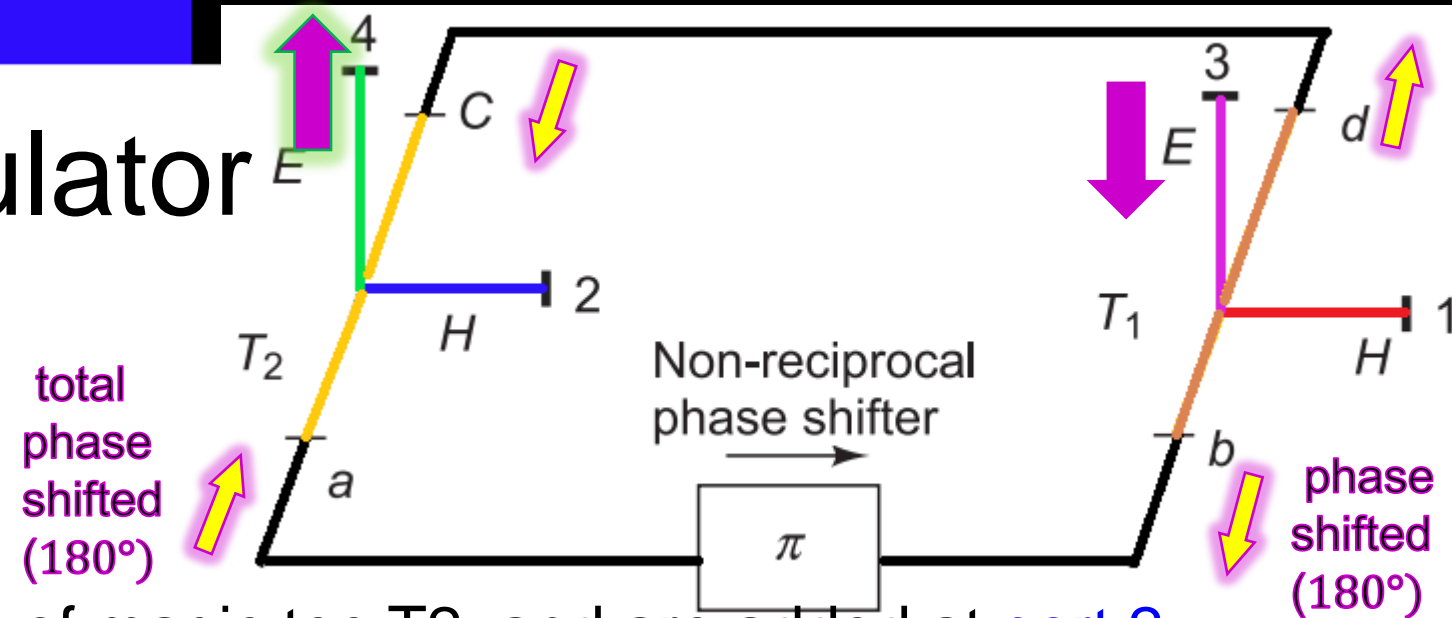
Input signal at port 1 is split into two in phase and equal amplitude waves in collinear **arms b** and **d** of magic tee **T1**.

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• **Input signal at port 3** is split into two out of phase and equal amplitude waves in collinear **arms b** and **d** of magic tee **T1** and appear at **Port 4** of **T2**



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Input signal at port 1 is split into two in phase and equal amplitude waves in collinear **arms b** and **d** of magic tee **T1**.

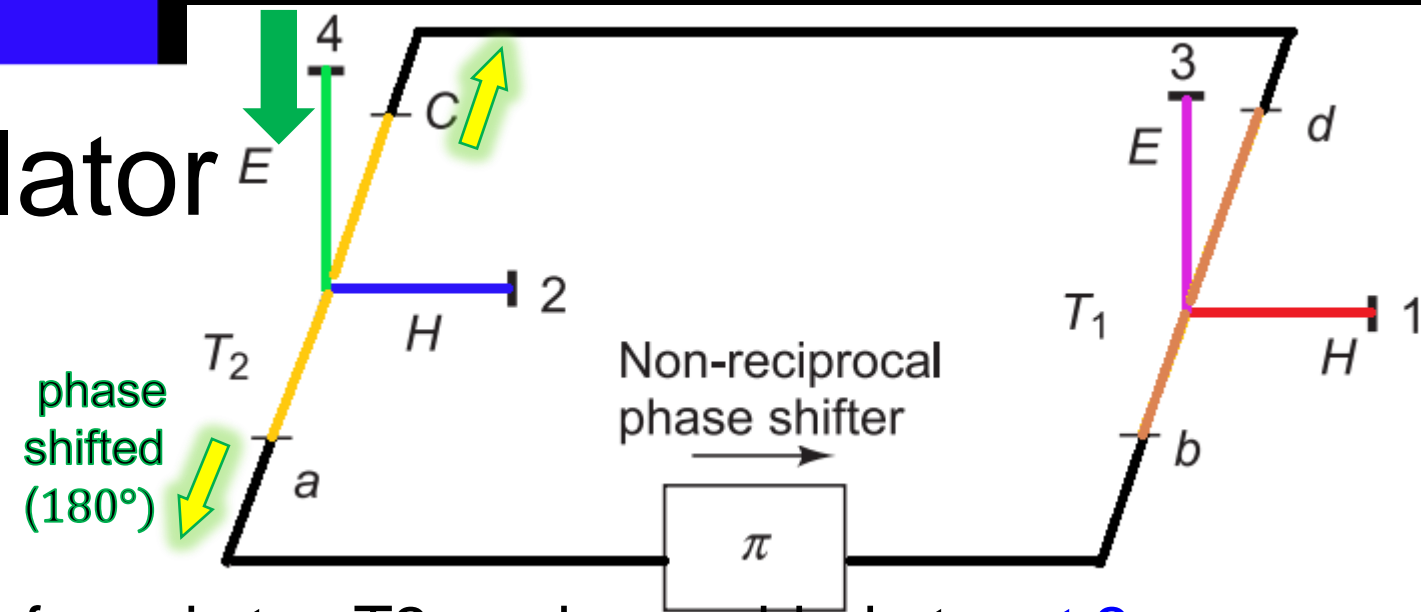
They enter in phase at **ports a** and **c** of magic tee **T2**, and are added at **port 2**.

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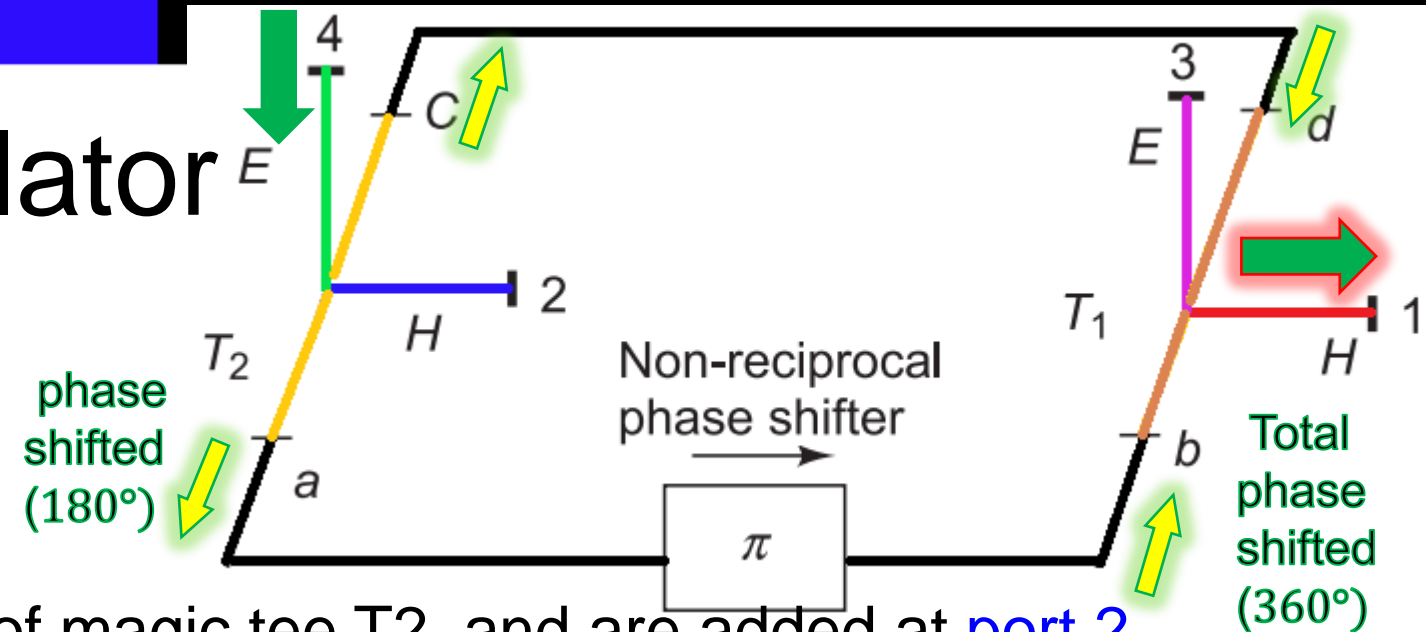
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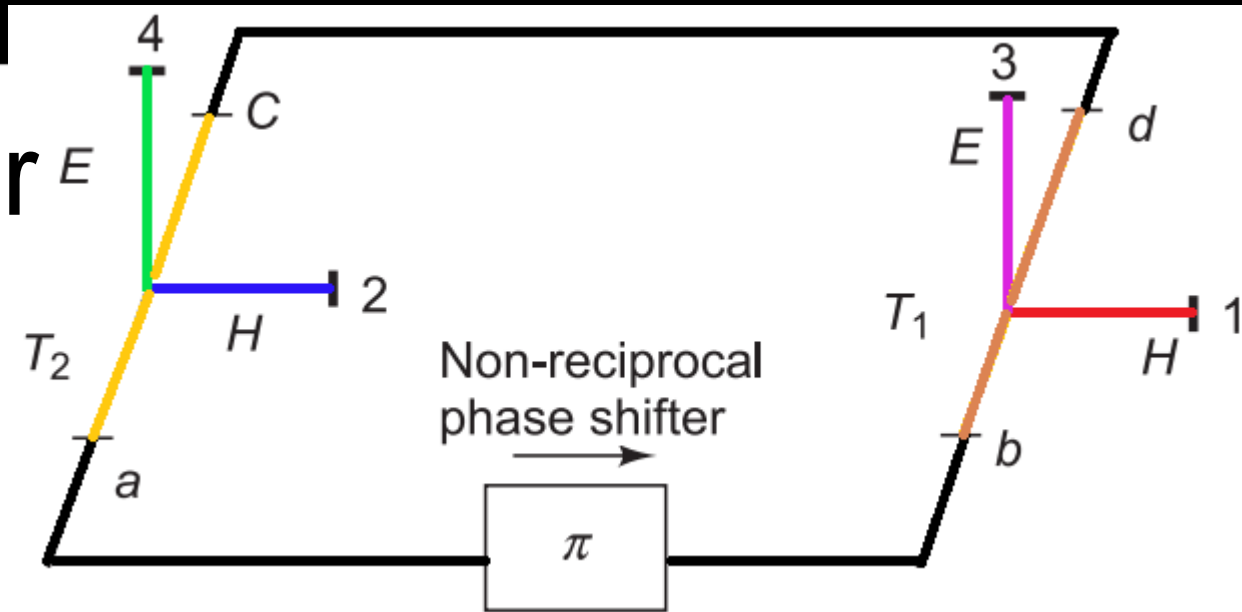
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• **Input signal at port 4** is split into two out of phase and equal amplitude waves in collinear **arms a** and **c** of magic tee **T2** and appear at **Port 1** of **T1**



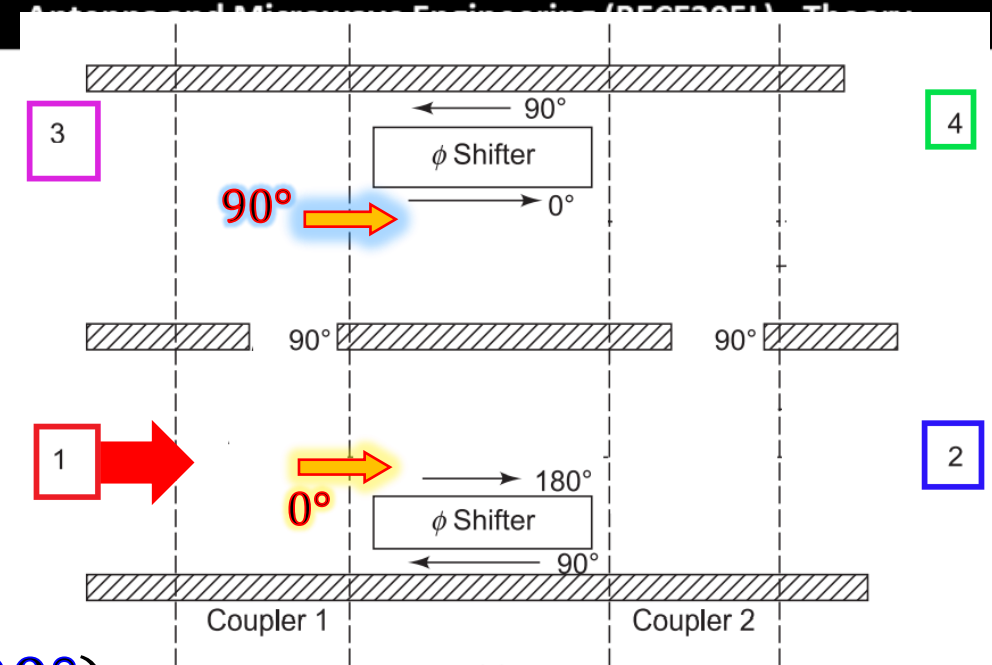
6.1 Four port Circulator



- Configuration 1:
Input signal at port 1 is split into two in phase and equal amplitude waves in collinear arms b and d of magic tee T1. They enter in phase at ports a and c of magic tee T2, and are added at port 2.
- Input signal at port 2 is split into two in phase and equal amplitude waves in collinear arms a and c of magic tee T2. They enter out of phase at ports b and d of magic tee T1, and appear at port 3.
- Input signal at port 3 is split into two out of phase and equal amplitude waves in collinear arms b and d of magic tee T1 and appear at Port 4 of T2
- Input signal at port 4 is split into two out of phase and equal amplitude waves in collinear arms a and c of magic tee T2 and appear at Port 1 of T1
- Port 1 -> port 2; port 2 -> port 3; port 3-> Port 4; Port 4-> Port 1

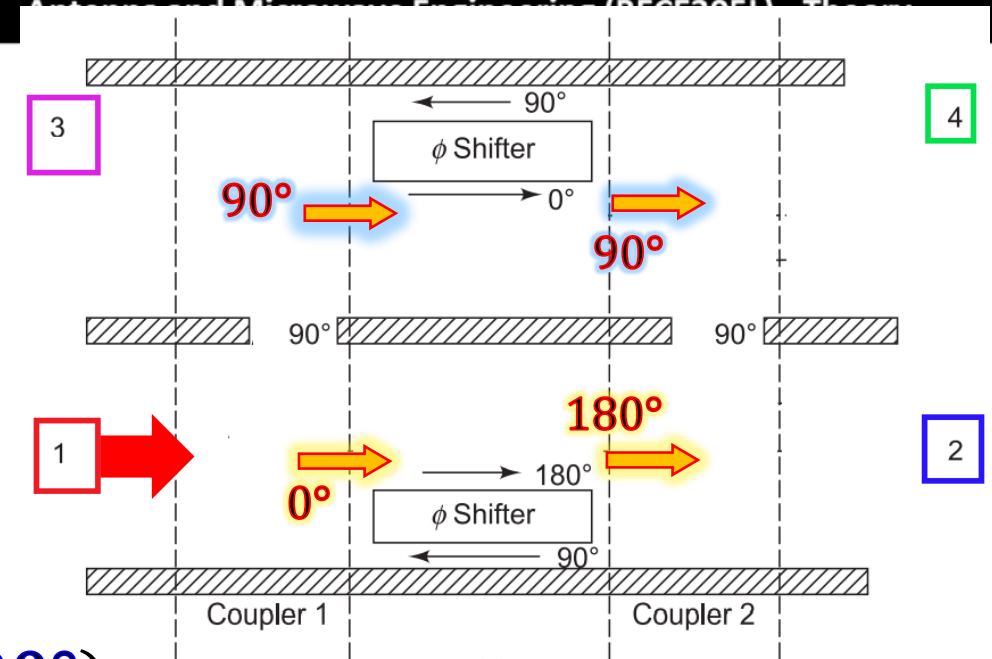
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- Configuration 2:
- Each 3dB coupler introduces 90° phase shift.
- **Input signal in port 1**, splits into two at coupler 1, one with 90° phase shift. (0° , 90°)



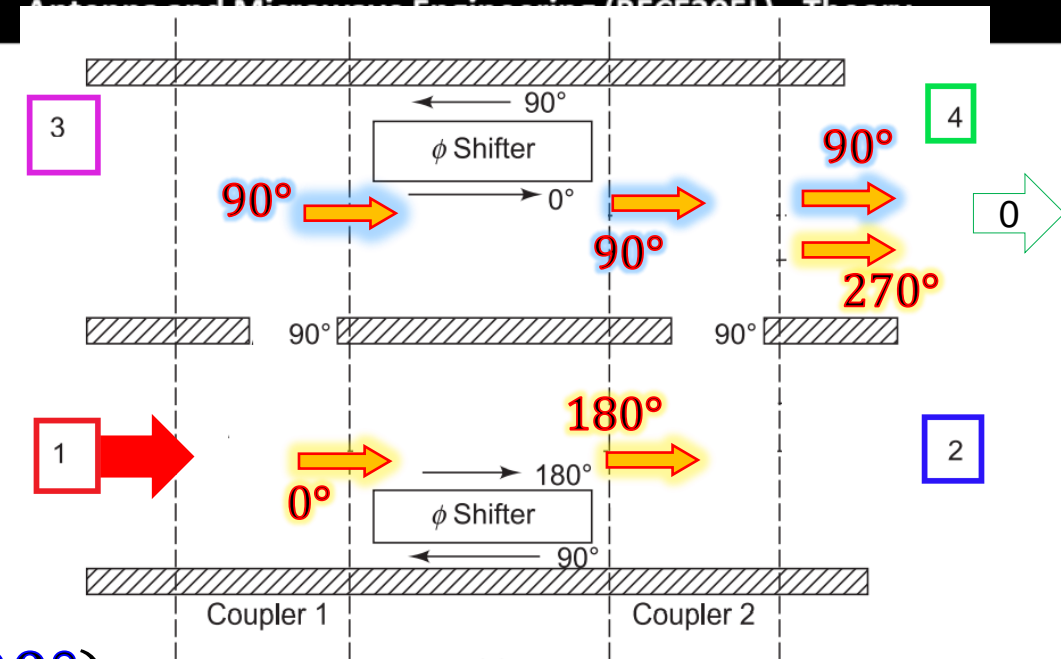
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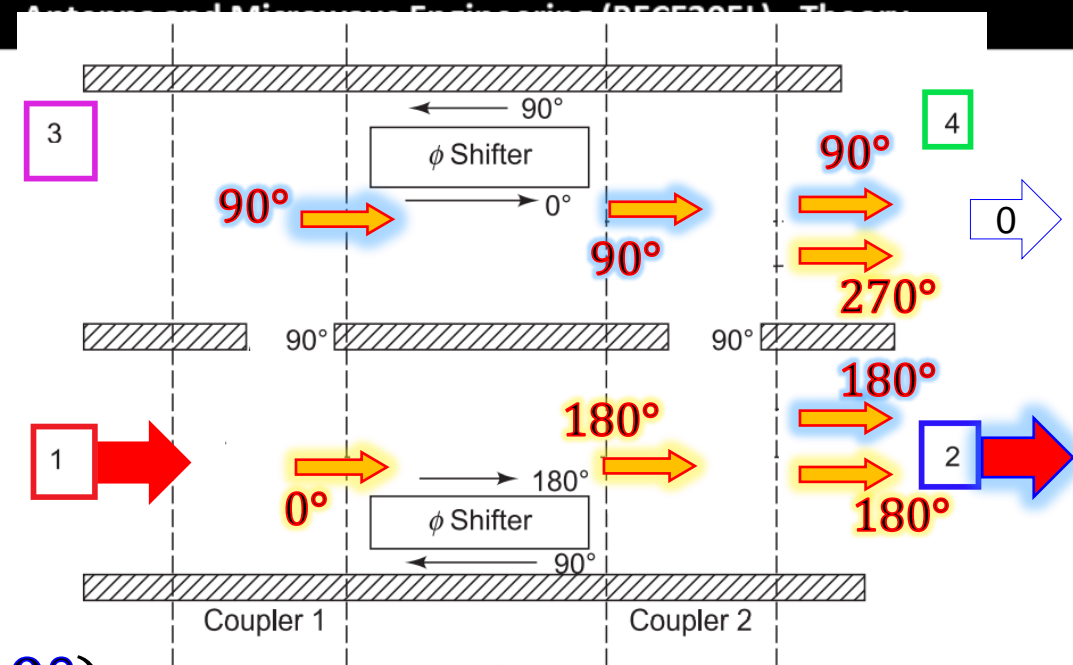
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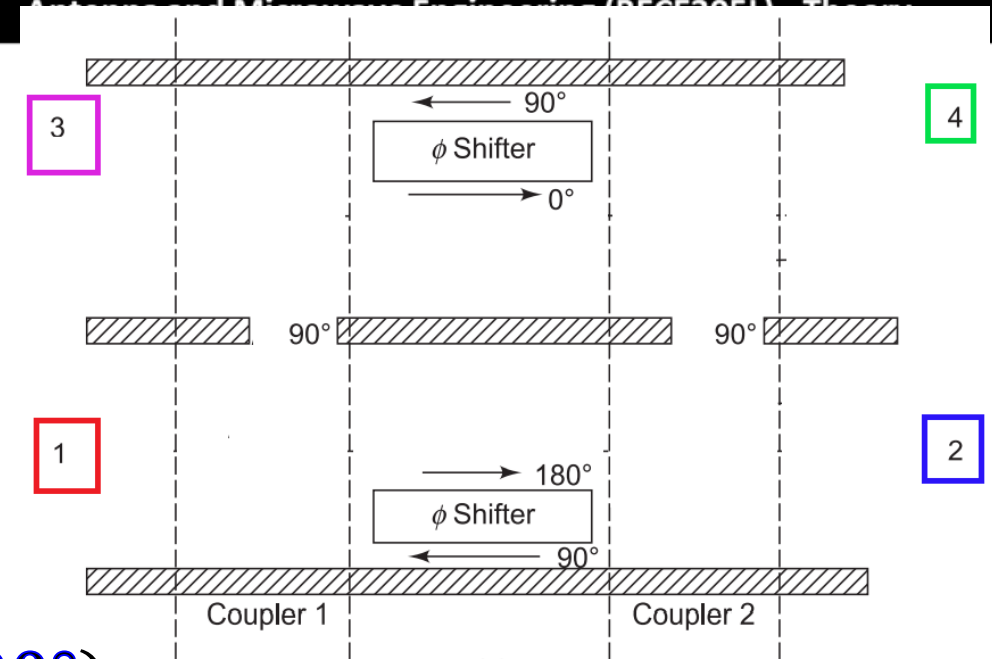
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Summary: **port 1-> port 2**



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Summary: **port 1-> port 2**
- Similarly, **port 2-> port 3;** **port 3-> port 4;** **port 4->port 1**



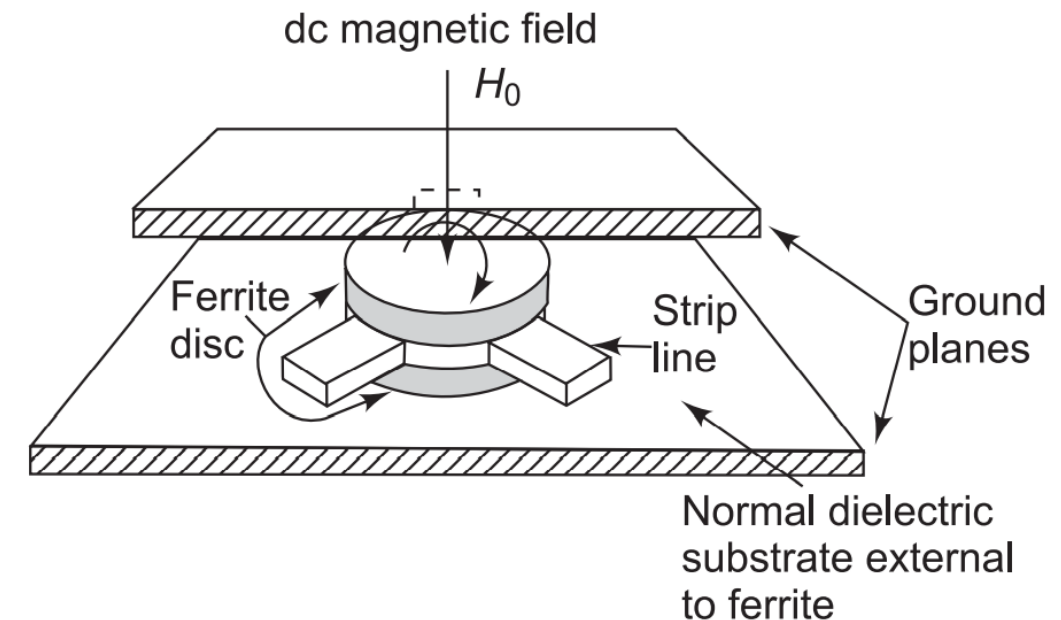
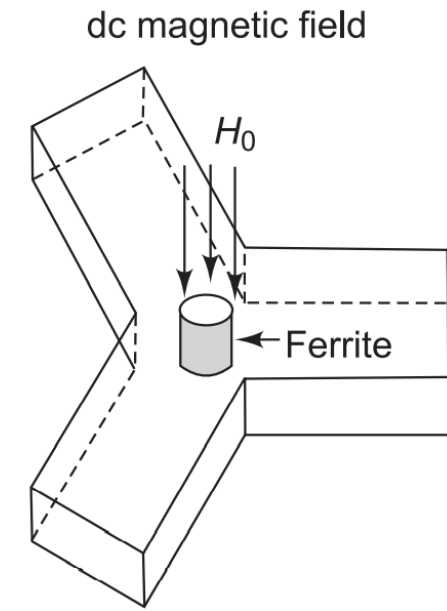
6.1 Four port Circulator

- A perfectly matched, lossless and non-reciprocal four port circulator has the S matrix:

$$[S] = \begin{bmatrix} 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

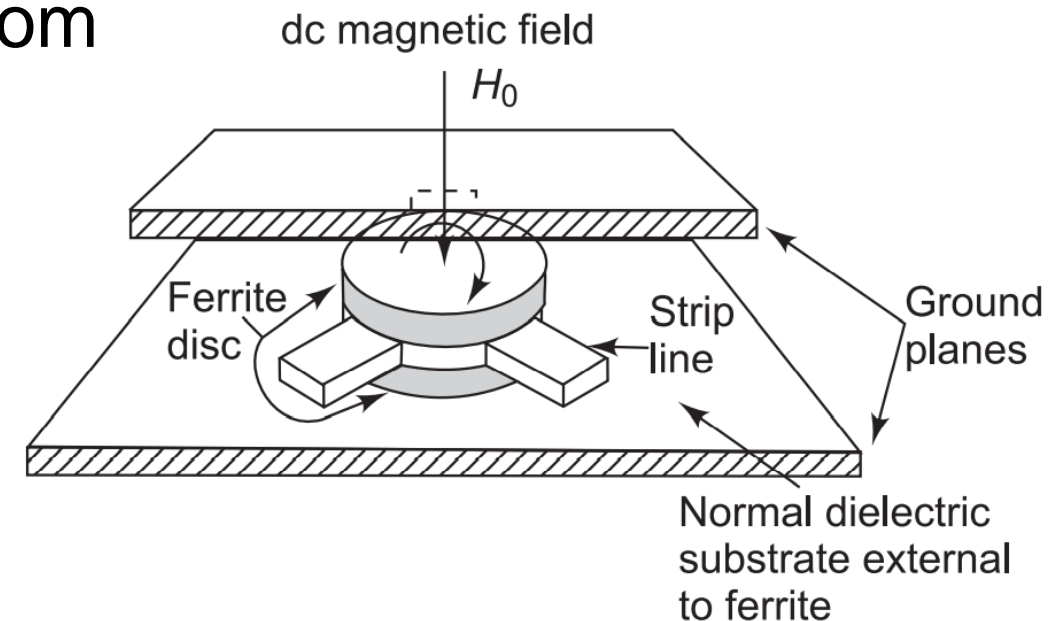
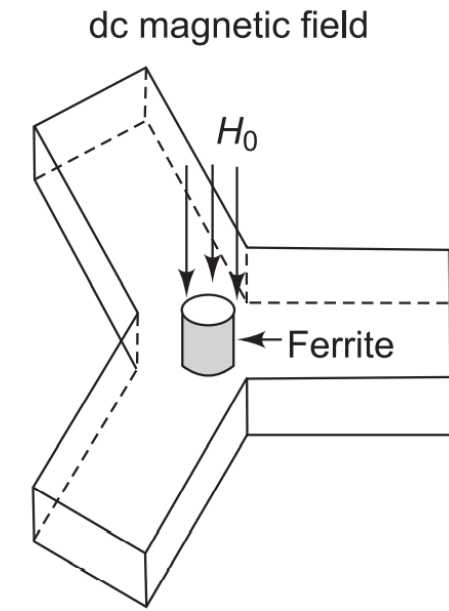
6.2 Three port Circulator

- A three port circulator is formed by a 120° H –plane waveguide or stripline symmetrical Y junction with a ferrite post or disc.



6.2 Three port Circulator

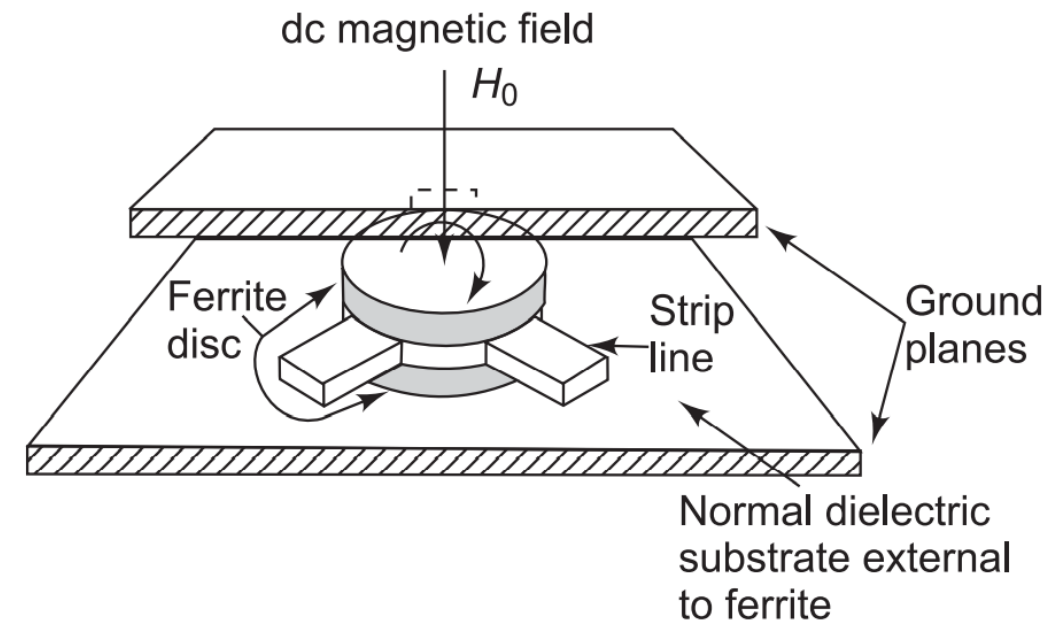
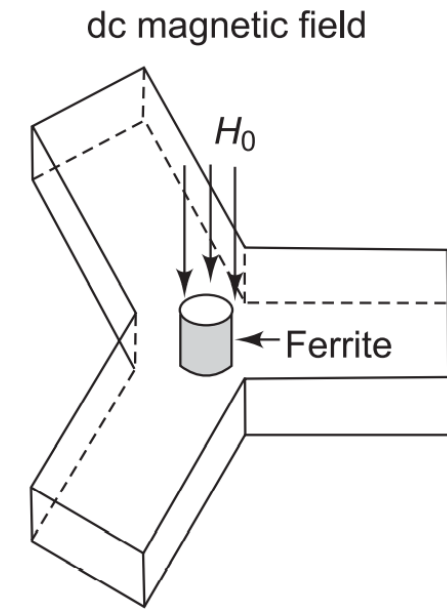
- A three port circulator is formed by a 120° H –plane waveguide or stripline symmetrical Y junction with a ferrite post or disc.
- A steady magnetic field H_0 is applied along the axis of the post/disc.
- Based on the polarization of incident wave and direction of H_0 , microwave signal travels from one port to immediate next one only.



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$$[S] = \begin{bmatrix} 0 & 0 & S_{13} \\ S_{21} & 0 & 0 \\ 0 & S_{32} & 0 \end{bmatrix}$$



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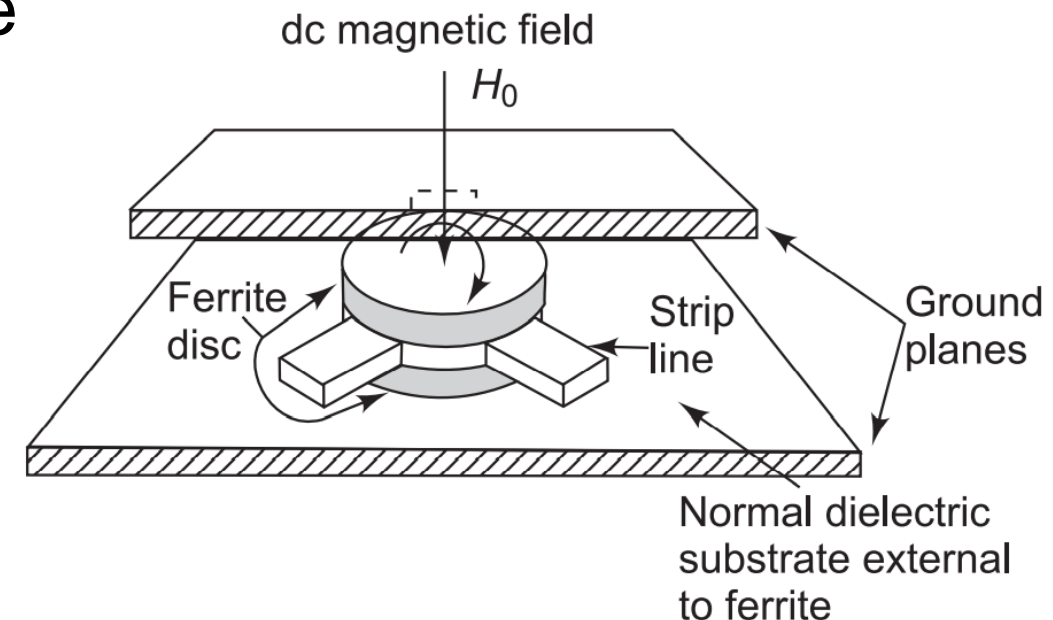
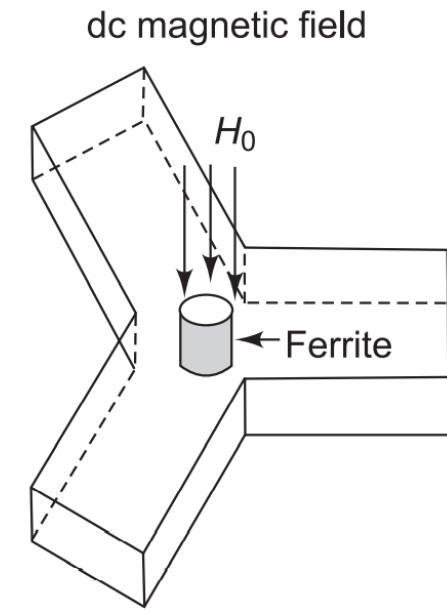
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- By proper choice of terminal planes, phase angles of S_{13} , S_{21} , S_{32} are made zero and

$$S_{13} = S_{21} = S_{32} = 1$$

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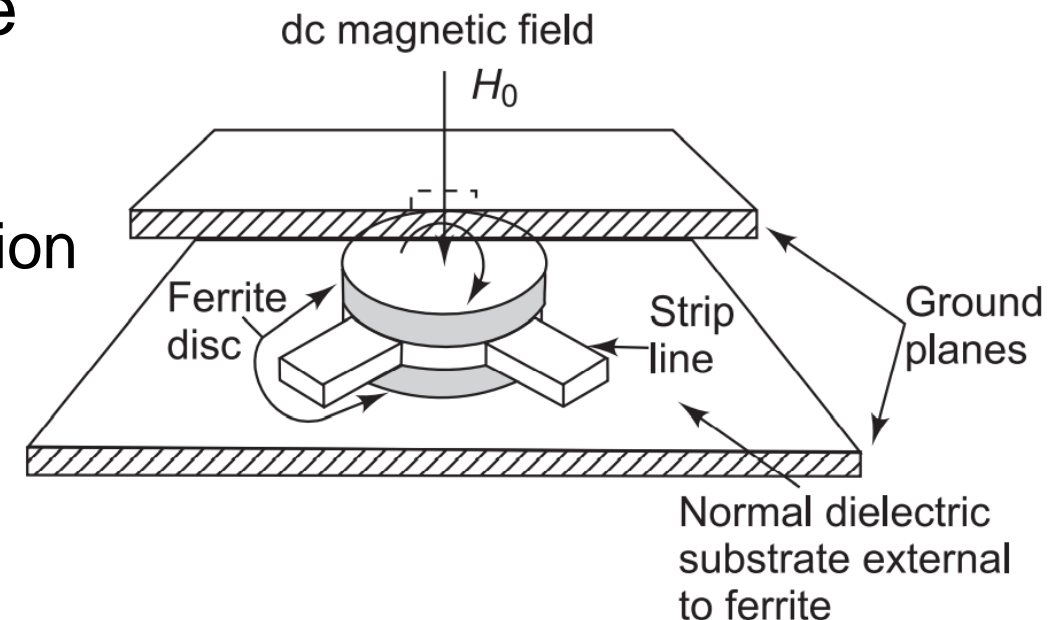
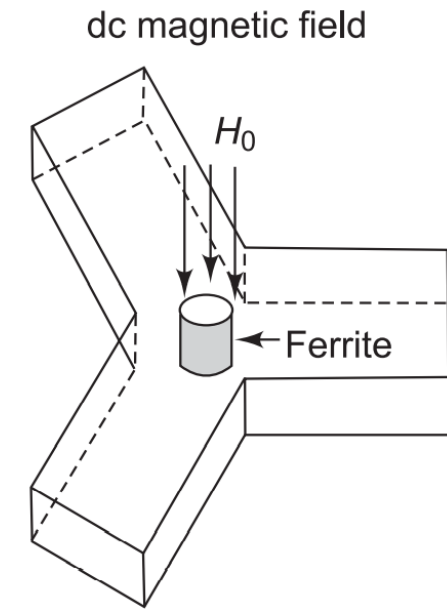
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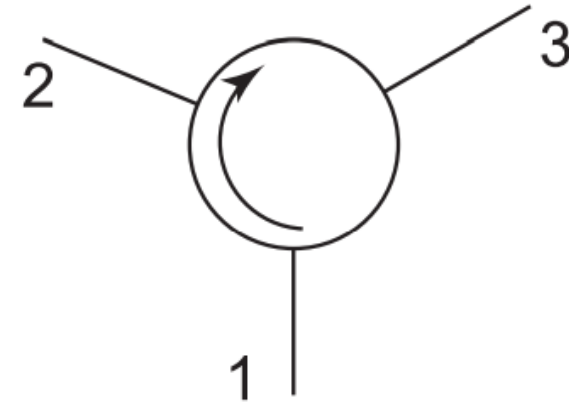
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Practically, finite isolation
 Insertion loss < 1dB
 Isolation \approx 30-40dB
 VSWR < 1.5

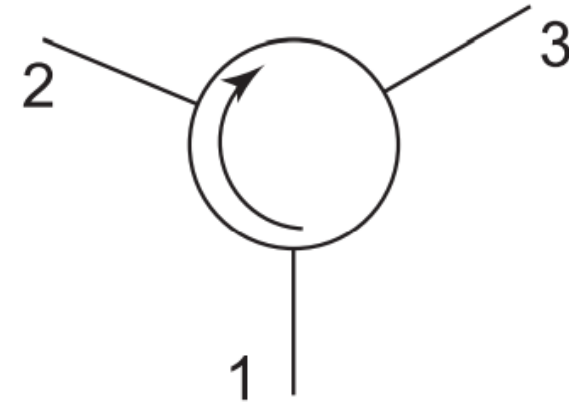


6.3 Problem: A three port circulator has an insertion loss of 1dB, Isolation 30dB and VSWR 1.5. Find the S matrix.



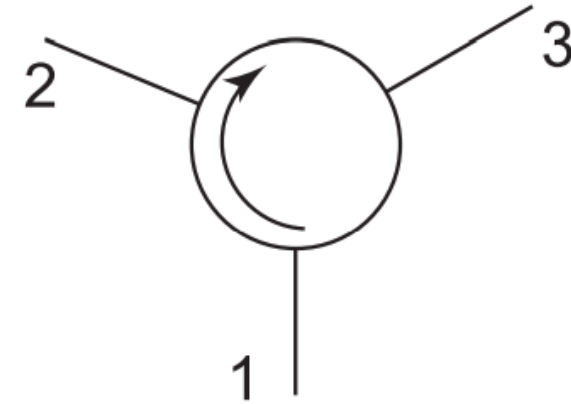
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• $[S] = \begin{bmatrix} S_{11} & S_{12} & S_{13} \\ S_{21} & S_{22} & S_{23} \\ S_{31} & S_{32} & S_{33} \end{bmatrix}$ S matrix of 3 port circulator



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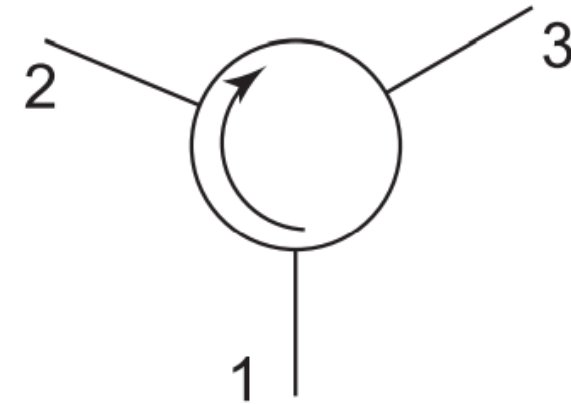
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- Insertion loss=1dB= $-20 \log_{10} |S_{21}|$
 $|S_{21}| = 10^{-1/20} = 0.89$

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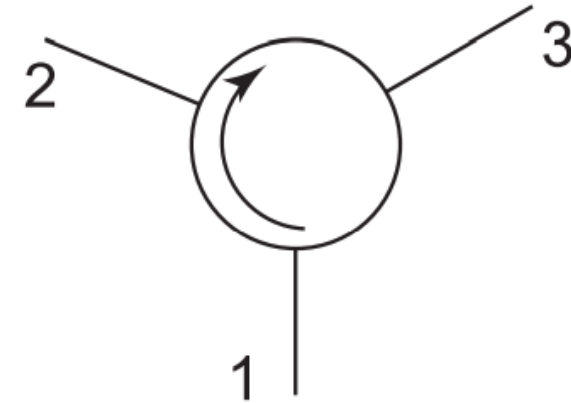


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Same insertion loss between ports (1,2), and (2,3) and (3,1) $|S_{21}| = |S_{32}| = |S_{13}| = 0.89$

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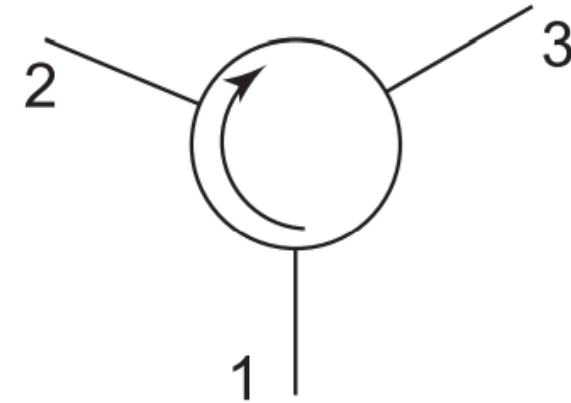
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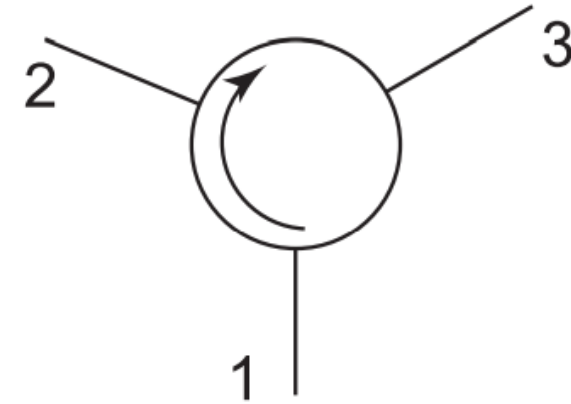
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 $|S_{31}| = 10^{-30/20} = 10^{-1.5} = 0.032 = |S_{23}| = |S_{12}|$

6.3 Problem: A three port circulator has an insertion loss of 1dB, Isolation 30dB and VSWR 1.5. Find the S matrix.

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$$\bullet \text{ Insertion loss} = 1\text{dB} = -20 \log_{10} |S_{21}|$$

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Same insertion loss between ports (1,2), and (2,3) and (3,1) $|S_{21}| = |S_{32}| = |S_{13}| = 0.89$

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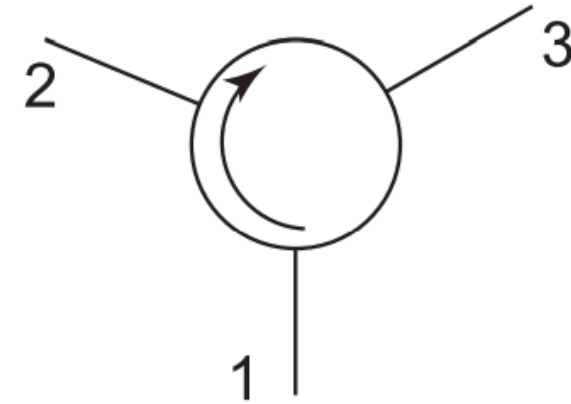
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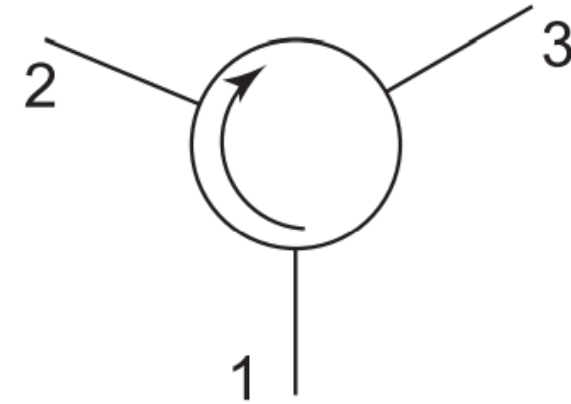
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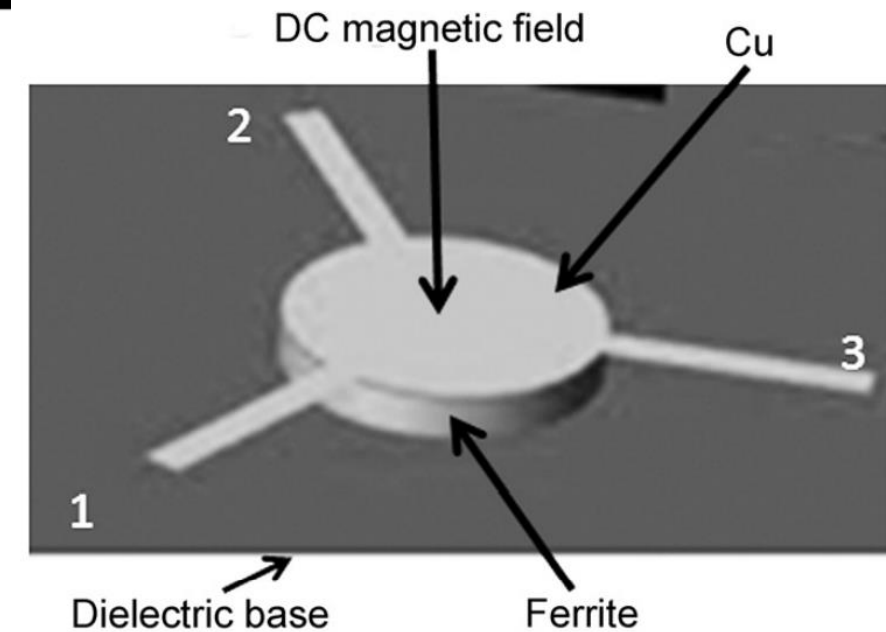
$$\bullet VSWR = 1.5, \text{ reflection coefficient } |\Gamma| = \frac{S-1}{S+1} =$$

$$\frac{1.5-1}{1.5+1} = 0.2 = |S_{11}| = |S_{22}| = |S_{33}|$$

$$[S] = \begin{bmatrix} 0.2 & 0.032 & 0.89 \\ 0.89 & 0.2 & 0.032 \\ 0.032 & 0.89 & 0.2 \end{bmatrix}$$

6.4 Microstrip circulator

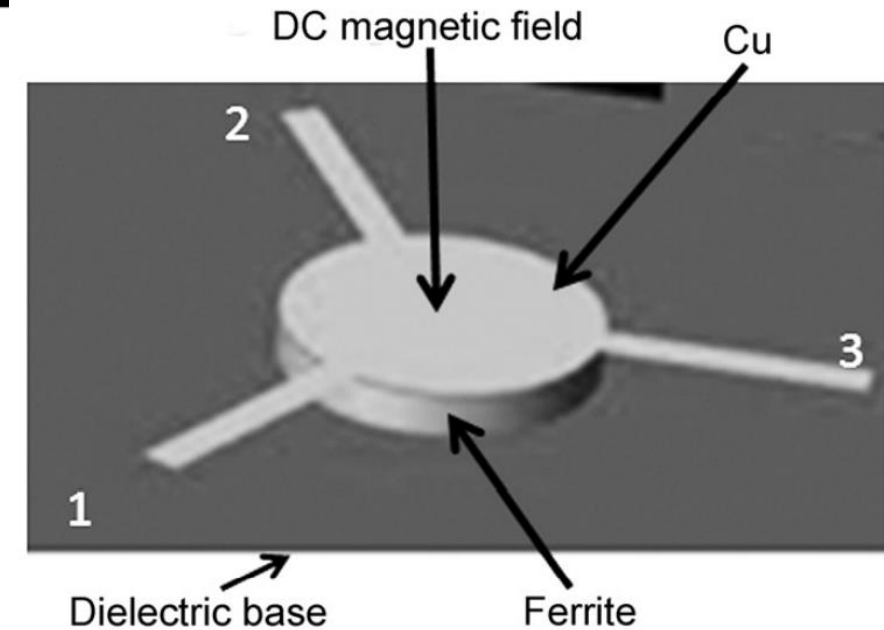
- Remove top ground plane in stripline
- Basic design criteria:
 - Selection of radius R of ferrite disc
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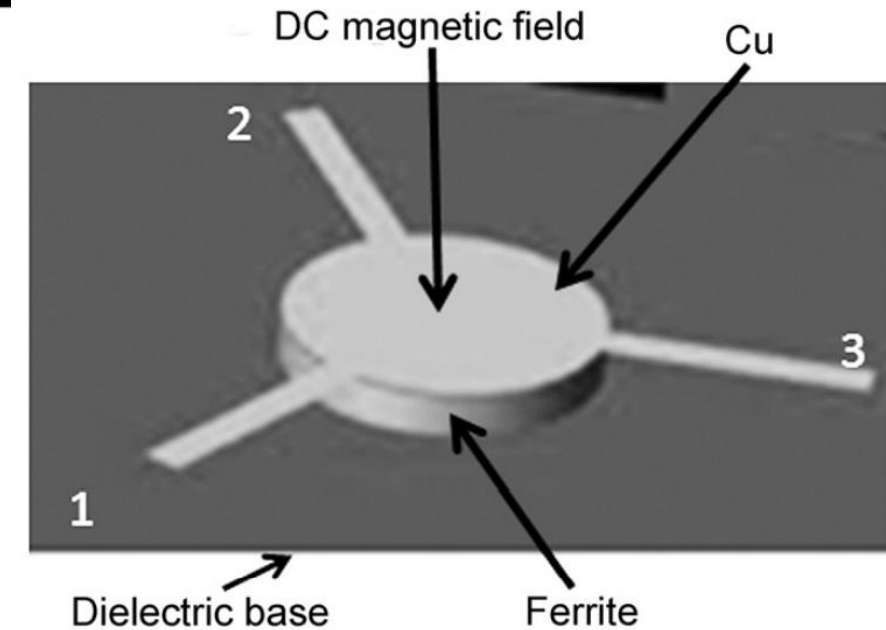
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ϵ_r : Relative permittivity of ferrite



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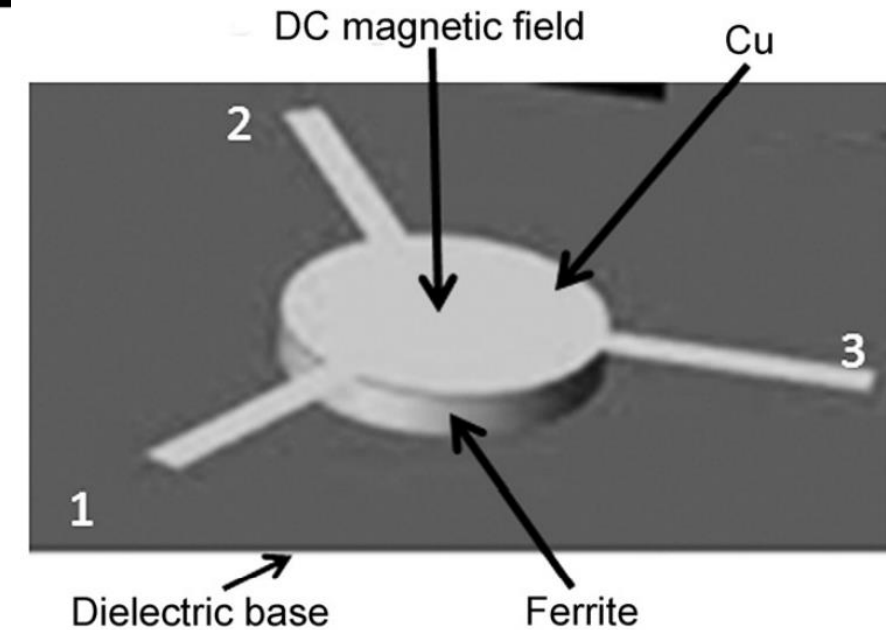
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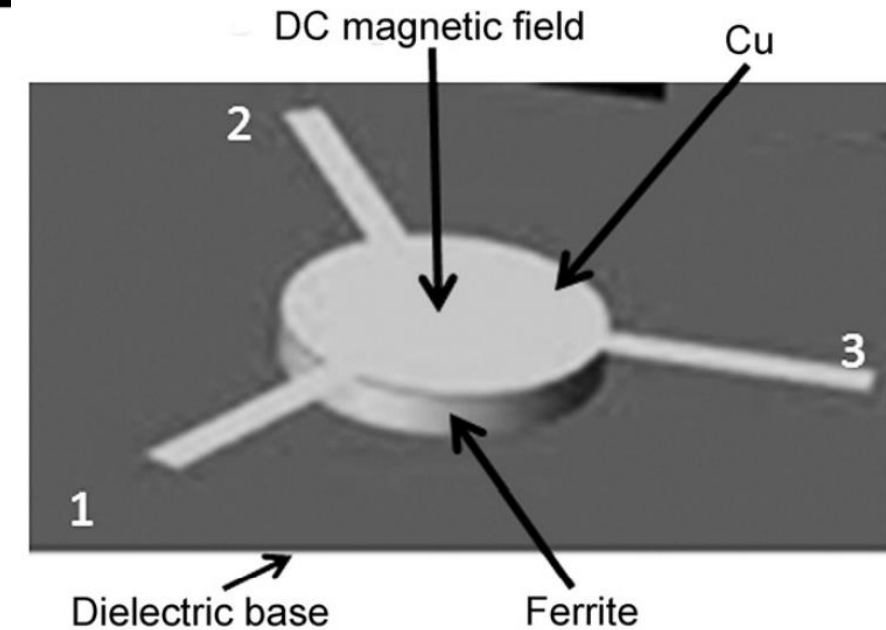
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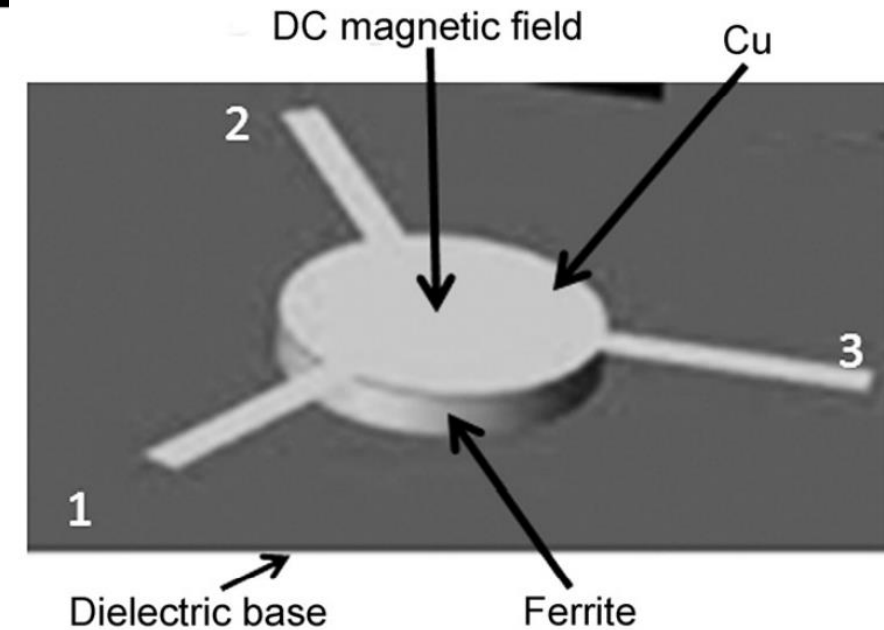
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magnetization = M_s / H_0

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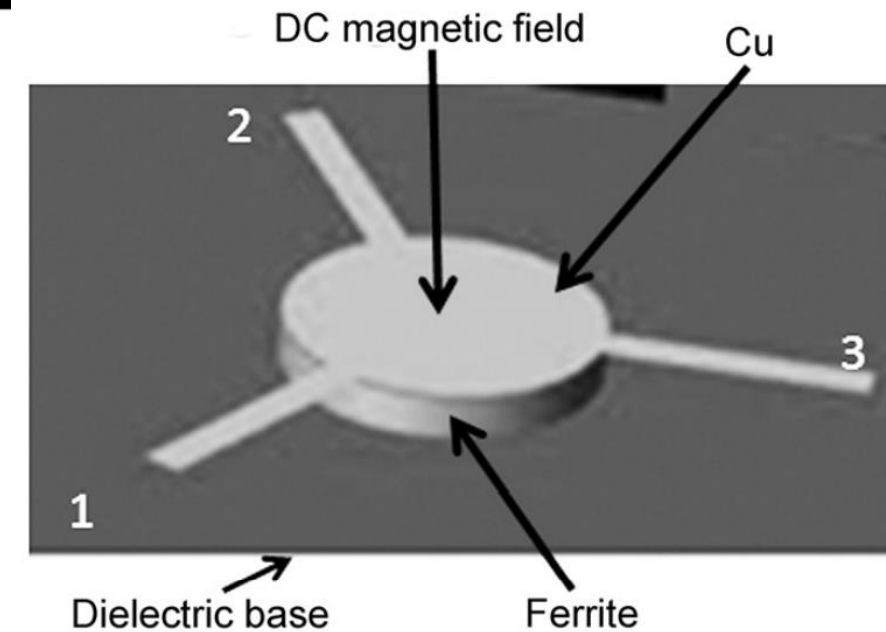
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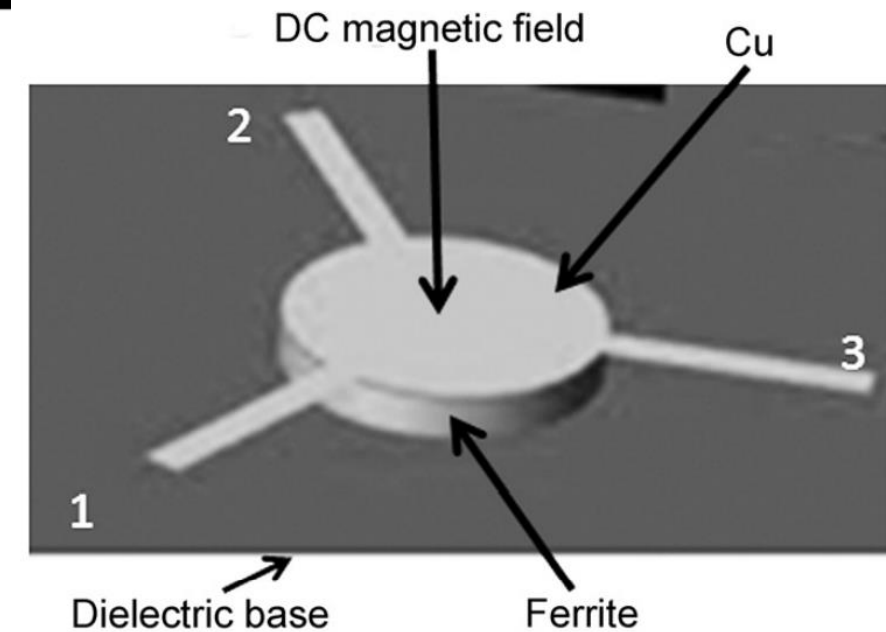
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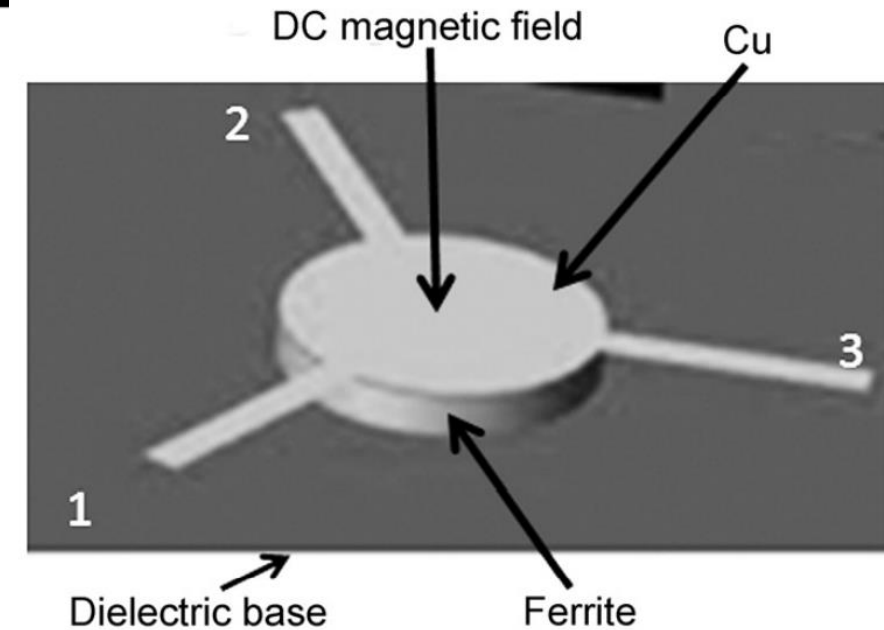
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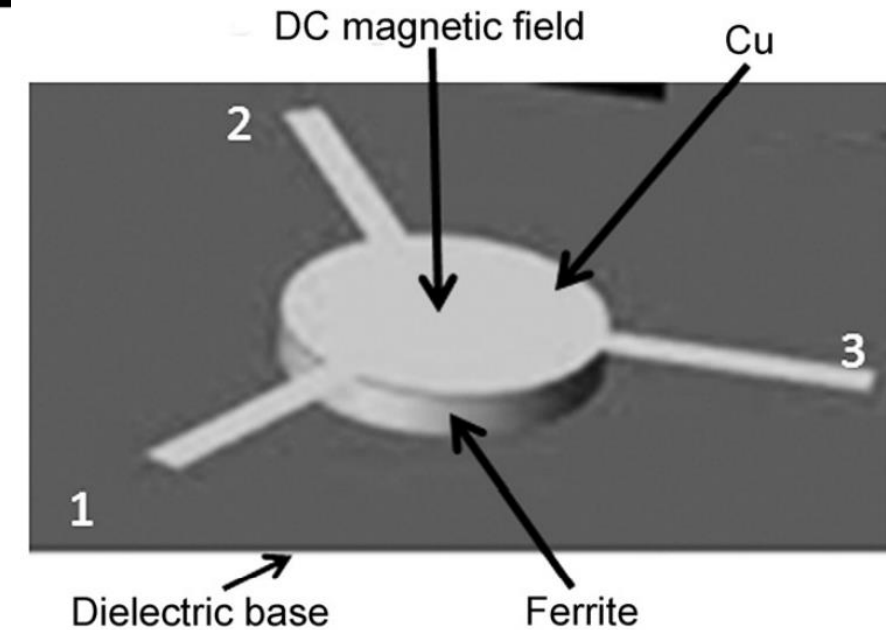
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Low magnetic loss: ferrite $\frac{\gamma^4 \pi M_s}{\omega} = 0.6$



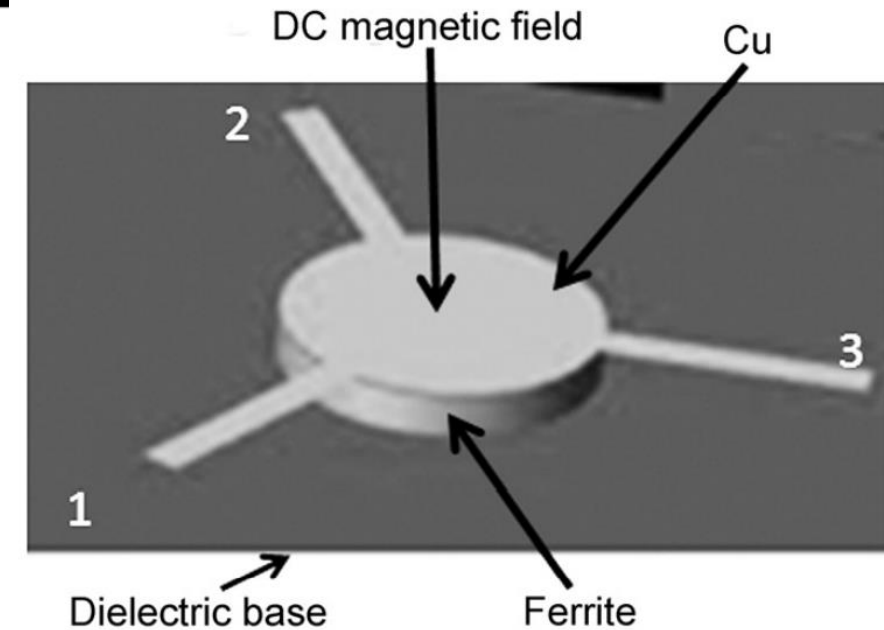
6.4 Microstrip circulator

- Insertion loss between coupled ports:
 - 1) Copper loss of strip and ground plane
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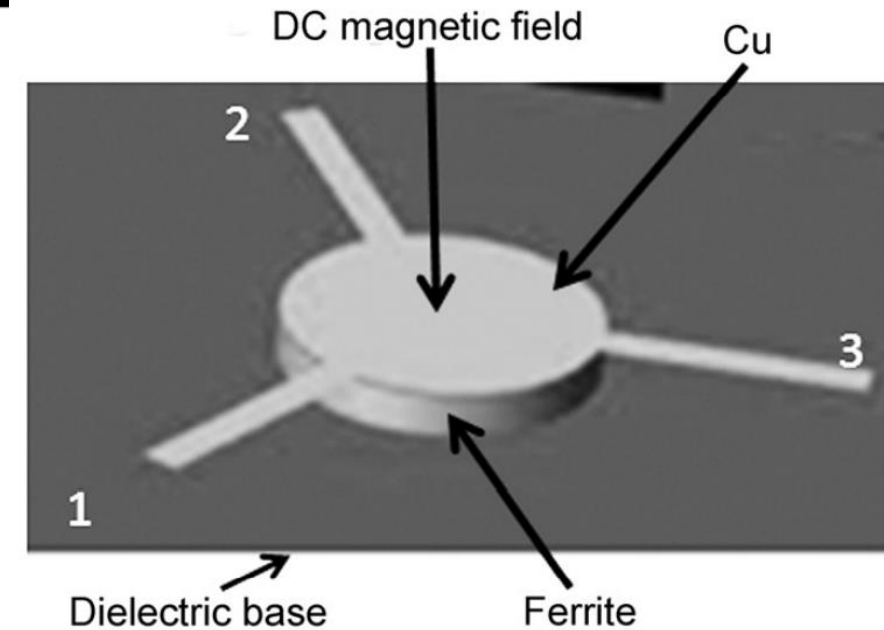
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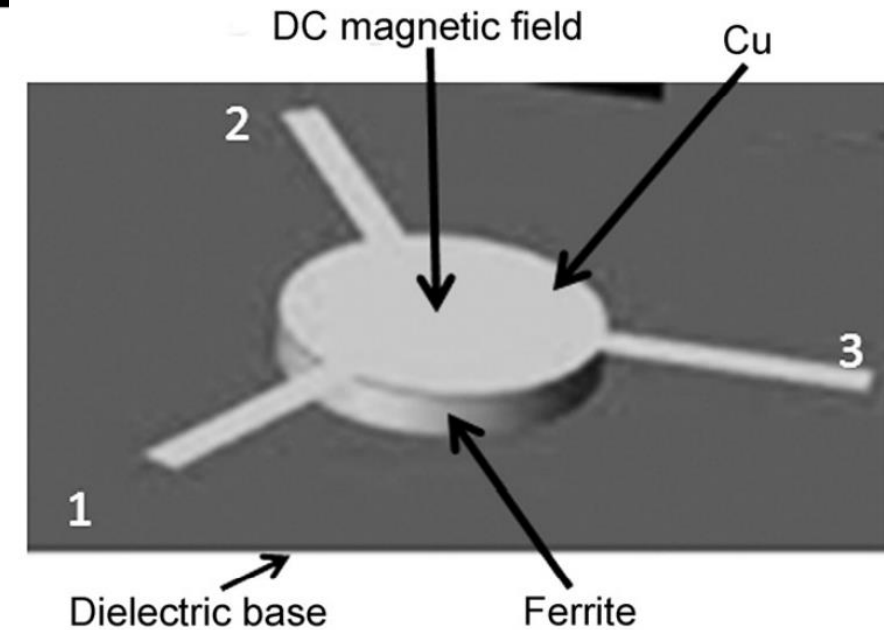
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- **YIG** (Yttrium Iron Garnet) substrate of thickness $h = 0.055''$:
Isolation > 20dB, VSWR < 1.2, Insertion loss IL < 0.8dB, Power handling of 60W over frequency range of 8.5 – 9.9GHz



6.4 Microstrip circulator

- Power handling capability of such device can be increased by
 - 1) Lowering the impedance or increasing intrinsic line width.
 - 2) Increasing substrate thickness h
 - 3) Decreasing $4\pi M_S$ of the material by substituting Al ions in YIG material.

