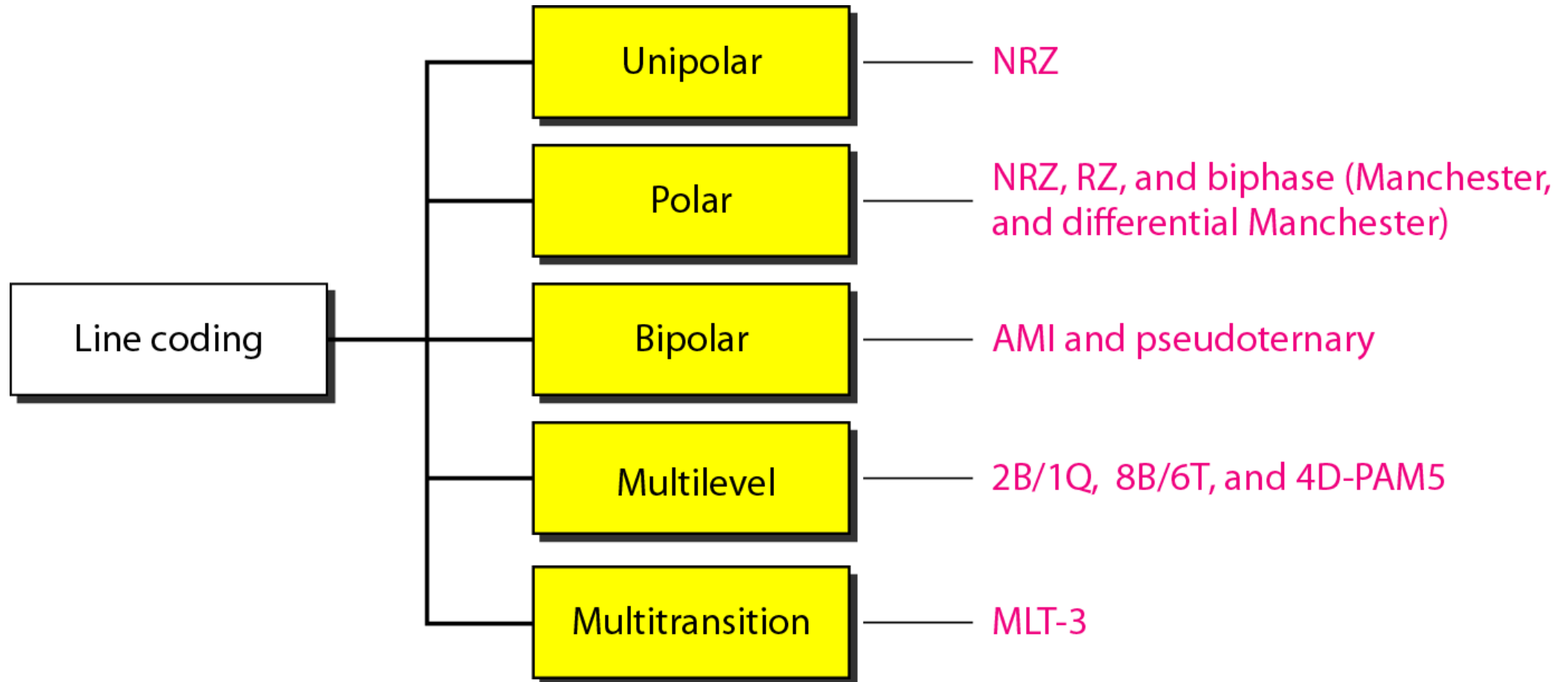
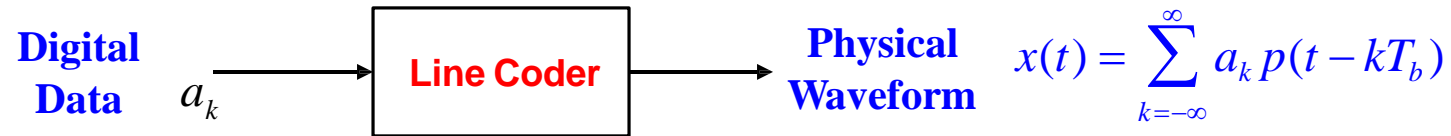


# Line Coding Schemes

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# Line Coding Schemes



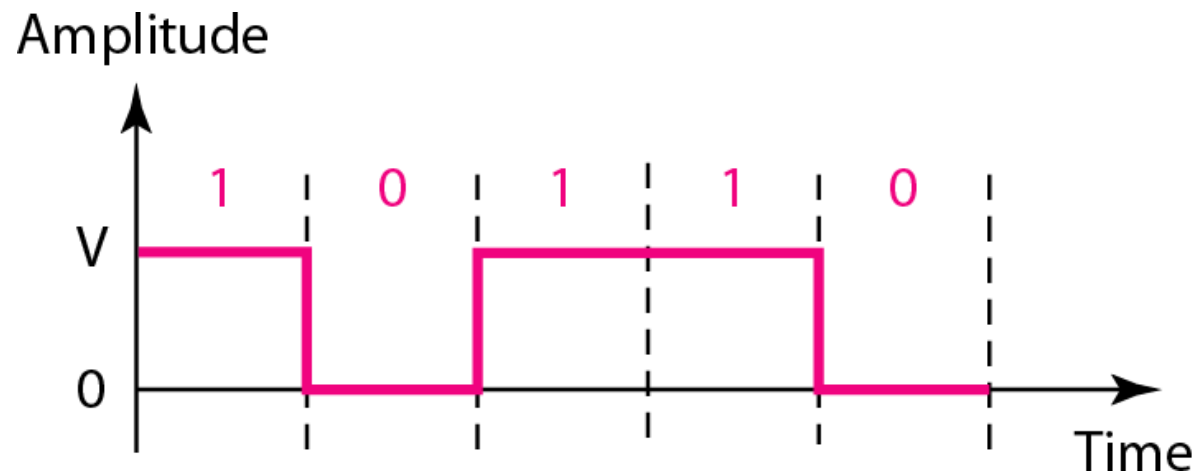
- The input to the line encoder is a sequence of values  $a_k$  that is a function of a data bit or an A/D C output bit.
- The output of the line encoder is a waveform:
  - *Where  $p(t)$  is the Pulse Shape and  $T_b$  is the Bit Period*
  - *$T_b = T_s/n$  for  $n$  bit quantizer (and no parity bits).*
  - *$R_b = 1/T_b = n f_s$  for  $n$  bit quantizer (and no parity bits).*
- The operational details of this function are set by the particular type of **line code** that is being used.

$$x(t) = \sum_{k=-\infty}^{\infty} a_k p(t - kT_b)$$

# Line Coding Schemes

## Unipolar

- Unipolar encoding uses only one voltage level
- All signal levels are on one side of the time axis - either above or below
- **NRZ - Non Return to Zero** scheme is an example of this code. The signal level does not return to zero during a symbol transmission.

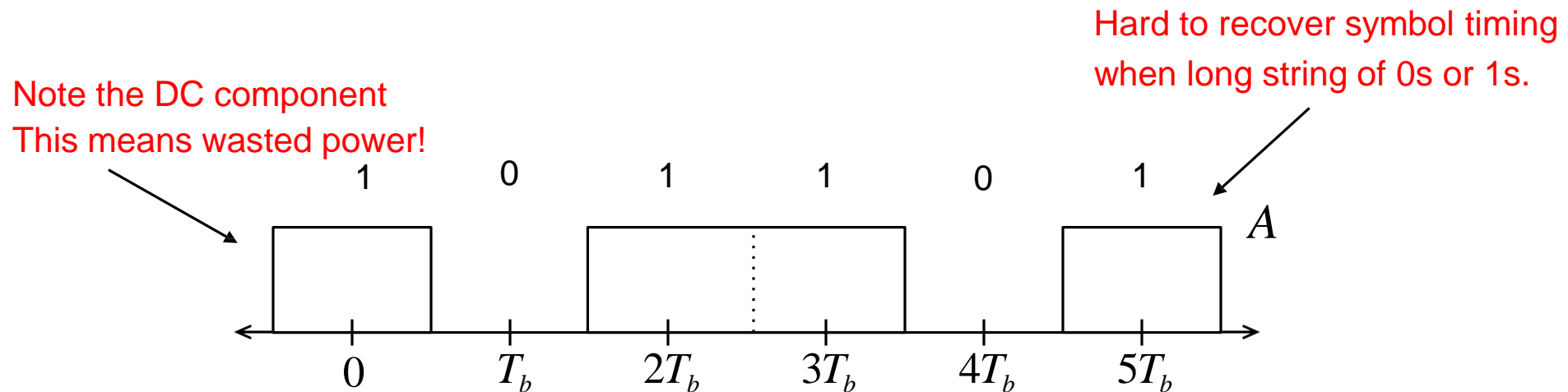


$$\frac{1}{2}V^2 + \frac{1}{2}(0)^2 = \frac{1}{2}V^2$$

Normalized power

# Line Coding Schemes

- Scheme is prone to baseline wandering and D C components.
- It has no synchronization or any error detection.
- It is simple but costly in power consumption.



# Line Coding Schemes

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- The unipolar nonreturn-to-zero line code is defined by the unipolar mapping:

$$a_k = \begin{cases} +A & \text{when } X_k = 1 \\ 0 & \text{when } X_k = 0 \end{cases}$$

- where  $X_k$  is the  $k^{\text{th}}$  data bit.
- In addition, the pulse shape for unipolar NRZ is:

$$p(t) = \Pi\left(\frac{t}{T_b}\right) \quad \text{NRZ pulse shape}$$

- Where  $T_b$  is the bit period.

# Line Coding Schemes

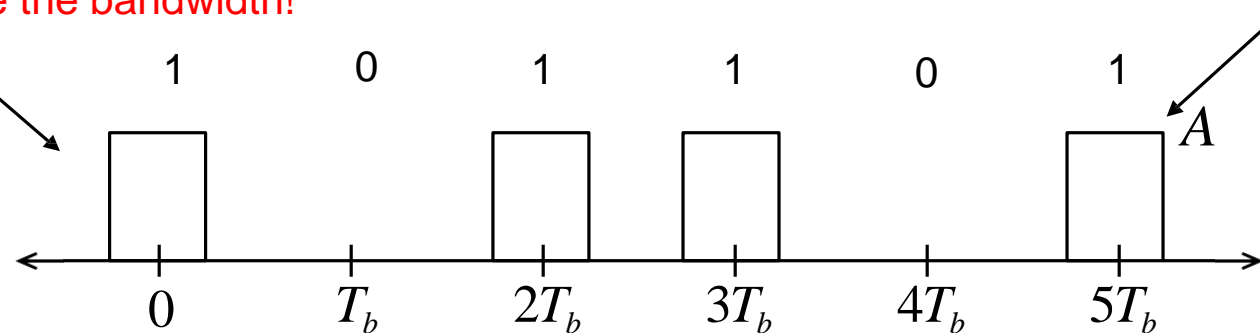
- The **unipolar return-to-zero line code** has the same symbol mapping but a different pulse shape than unipolar NRZ:

$$a_k = \begin{cases} +A & \text{when } X_k = 1 \\ 0 & \text{when } X_k = 0 \end{cases}$$

$$p(t) = \Pi\left(\frac{t}{T_b/2}\right) \quad \text{RZ pulse shape}$$

Pulse of half the duration of NRZ  
requires twice the bandwidth!

Long strings of 1's no longer a problem.  
However strings of 0's still problem.



# Line Coding Schemes

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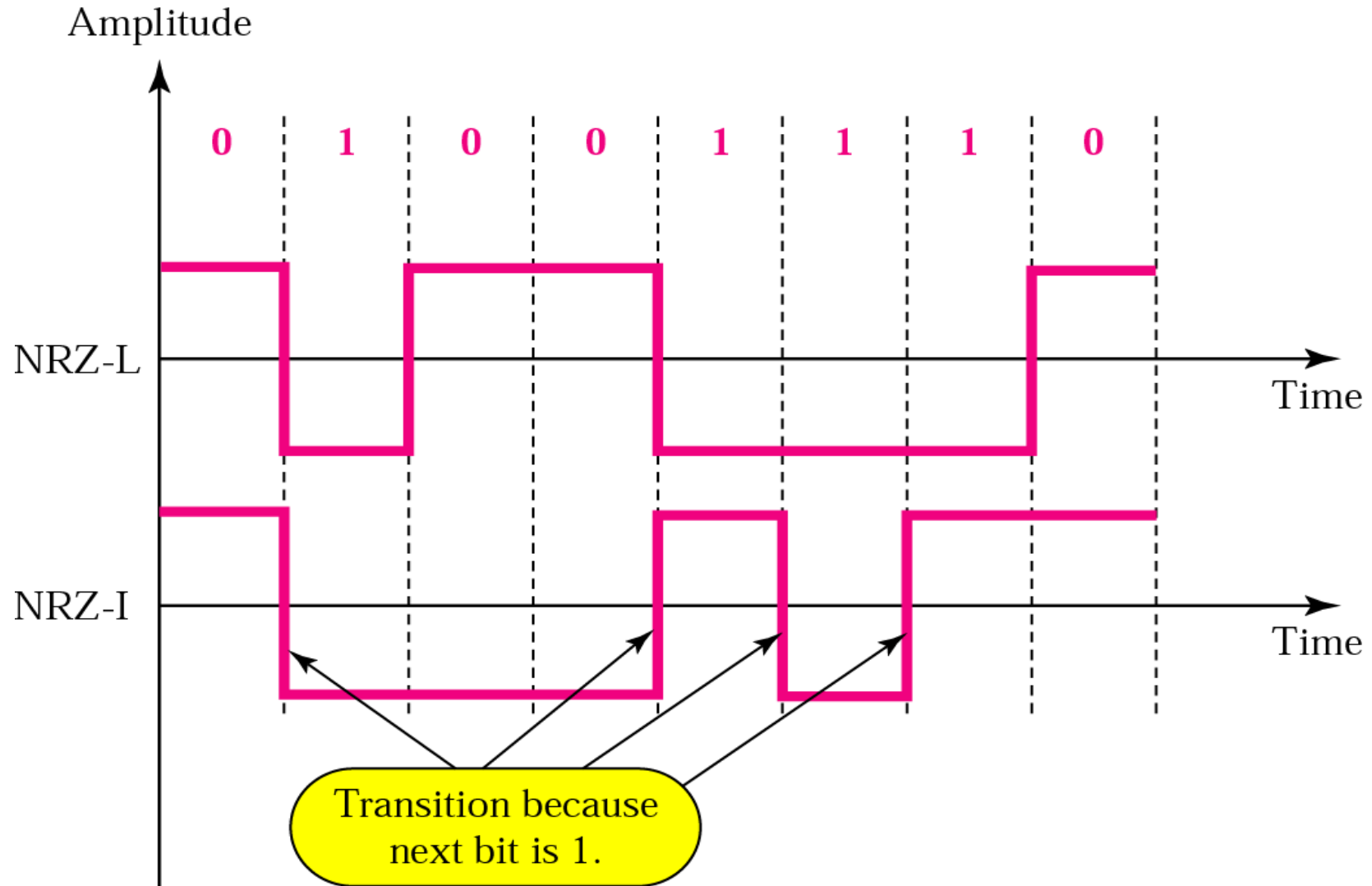
## Polar codes

- Polar encoding uses two voltage levels (positive and negative).

## Variations of Polar Encodings

- In Nonreturn to Zero-level (NRZ-L) the level of the signal is dependent upon the **state of the bit**.
- In Nonreturn to Zero-Invert (NRZ-I) the signal is **inverted if a bit '1'** is encountered.

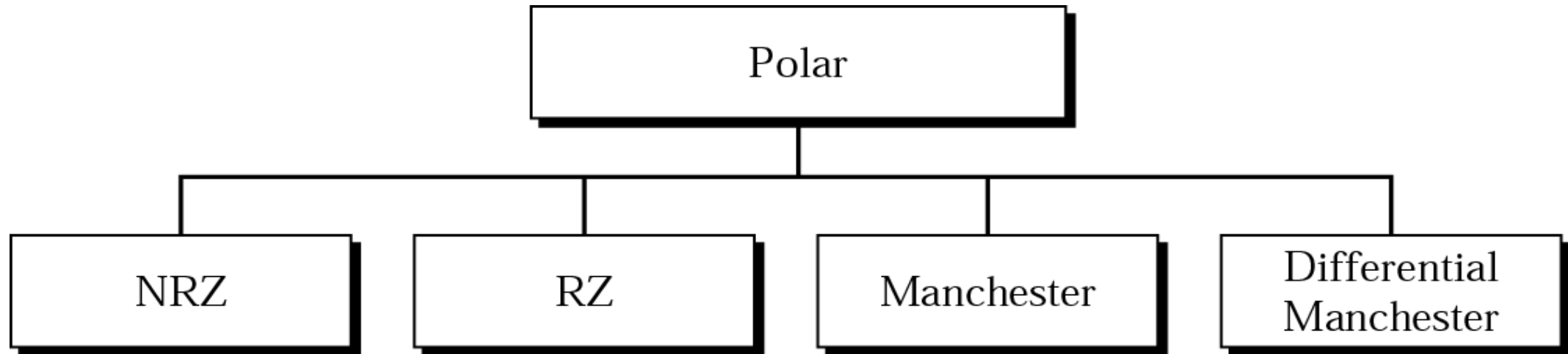
# Line Coding Schemes





# Line Coding Schemes

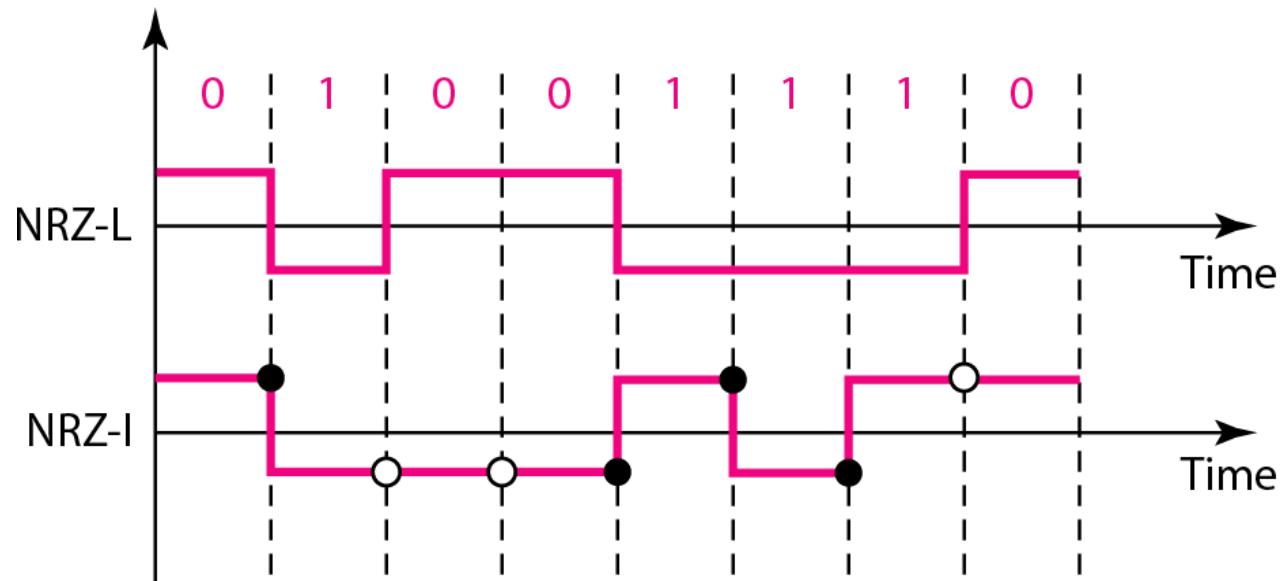
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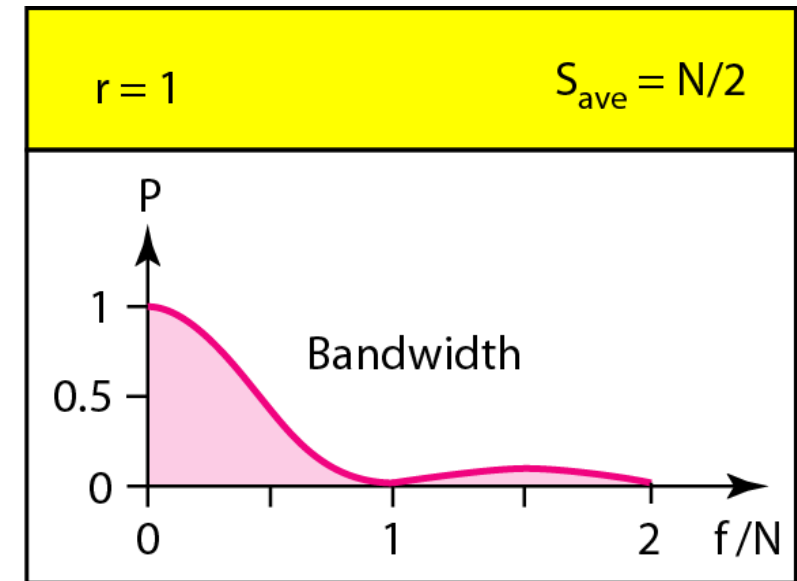
# Line Coding Schemes

## Polar - NRZ

- The voltages are on both sides of the time axis.
- Polar NRZ scheme can be implemented with two voltages. E.g. +V for 0 and -V for 1.



○ No inversion: Next bit is 0      ● Inversion: Next bit is 1



# Line Coding Schemes

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**In NRZ-L the level of the voltage  
determines the value of the bit.  
In NRZ-I the inversion  
or the lack of inversion  
determines the value of the bit.**

# Line Coding Schemes

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**NRZ-L and NRZ-I both have an average signal rate of  $N/2$  Bd.**

**NRZ-L and NRZ-I both have a baseline wandering, it is worse for NRZ-L. Both have no self synchronization & no error detection. Both are relatively simple to implement.**

# Line Coding Schemes

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- *A system is using NRZ-I to transfer 1-Mbps data. What are the average signal rate and minimum bandwidth?*
- **Solution:**

# Line Coding Schemes

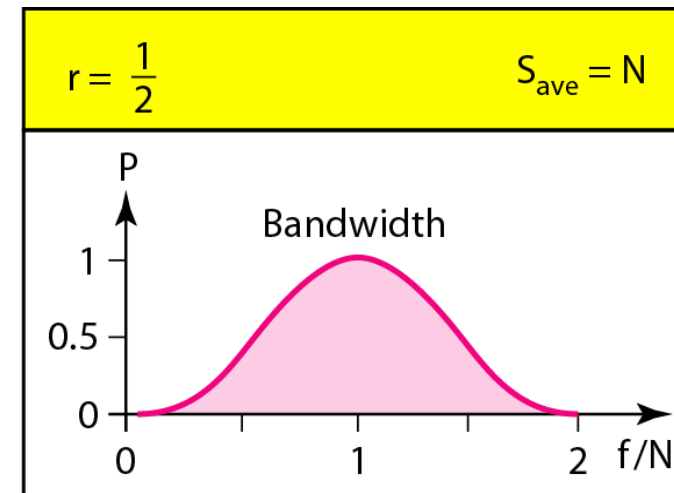
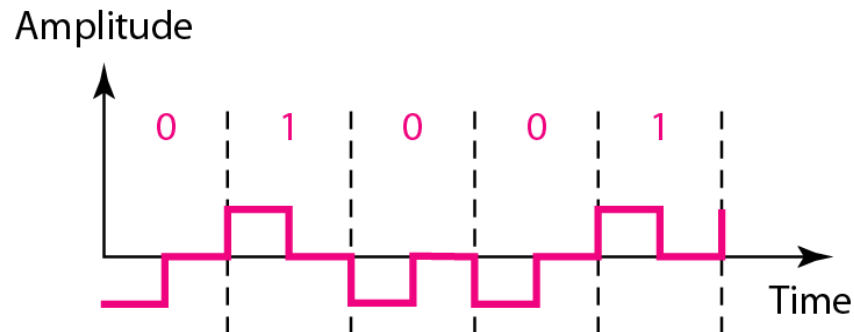
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- *A system is using NRZ-I to transfer 1-Mbps data. What are the average signal rate and minimum bandwidth?*
- **Solution:**
- The average signal rate is  $S = C \times N \times R = 1/2 \times N \times 1 = 500 \text{ kbaud}$ .
- The minimum bandwidth for this average baud rate is  $B_{\min} = S = 500 \text{ kHz}$ .
- Note  $c = 1/2$  for the avg case as worst case is 1 and best case is 0

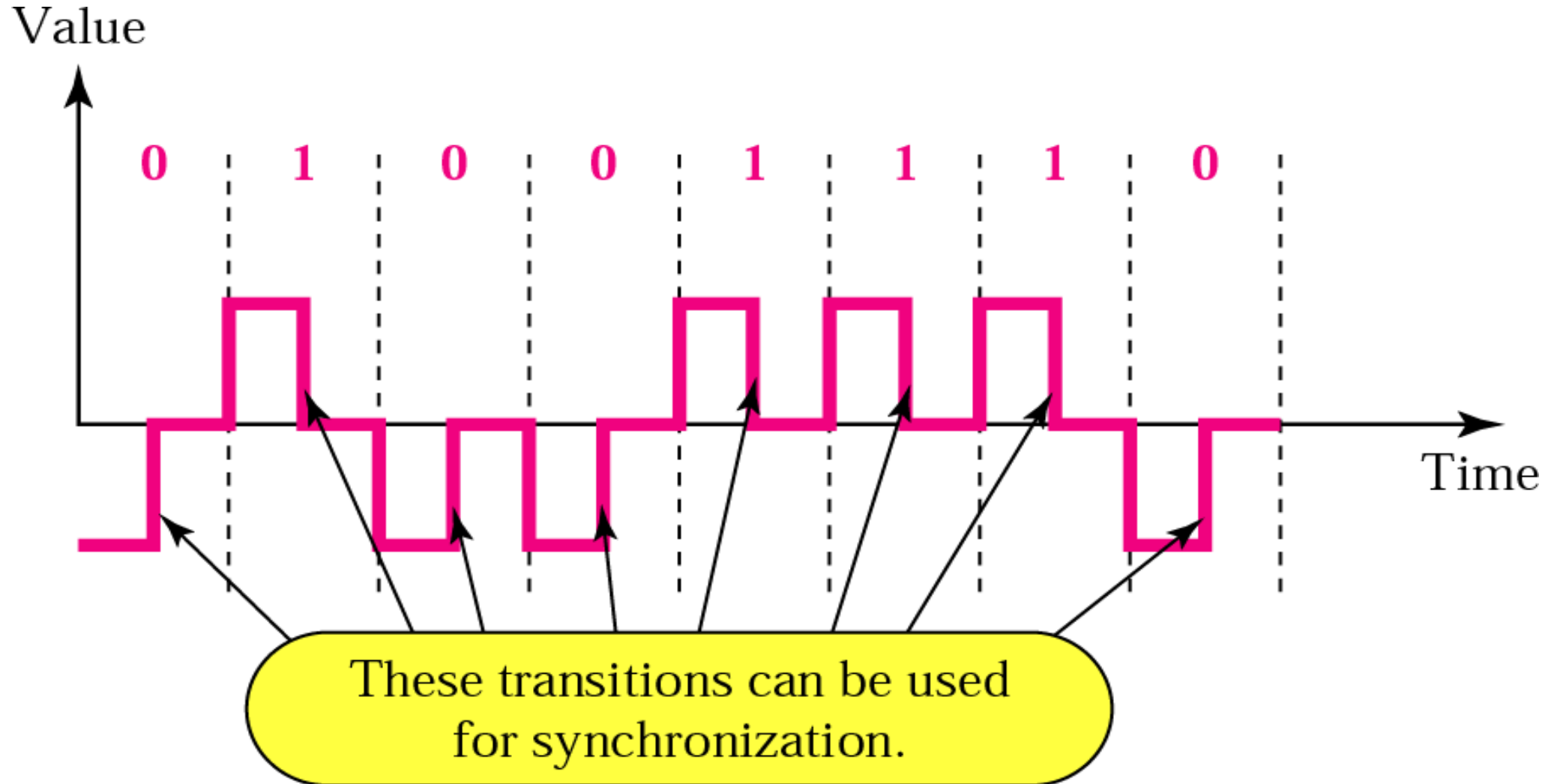
# Line Coding Schemes

## Polar – RZ

- The Return to Zero (RZ) scheme uses three voltage values. **+, 0, -.**
- Each symbol has a transition in the middle.
- Either from high to zero or from low to zero.
- This scheme has more signal transitions (two per symbol) and therefore requires a wider bandwidth.



# Line Coding Schemes





# Line Coding Schemes

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- No DC components or baseline wandering.
- Self synchronization - transition indicates symbol value.
- More complex as it uses three voltage level. It has no error detection capability.

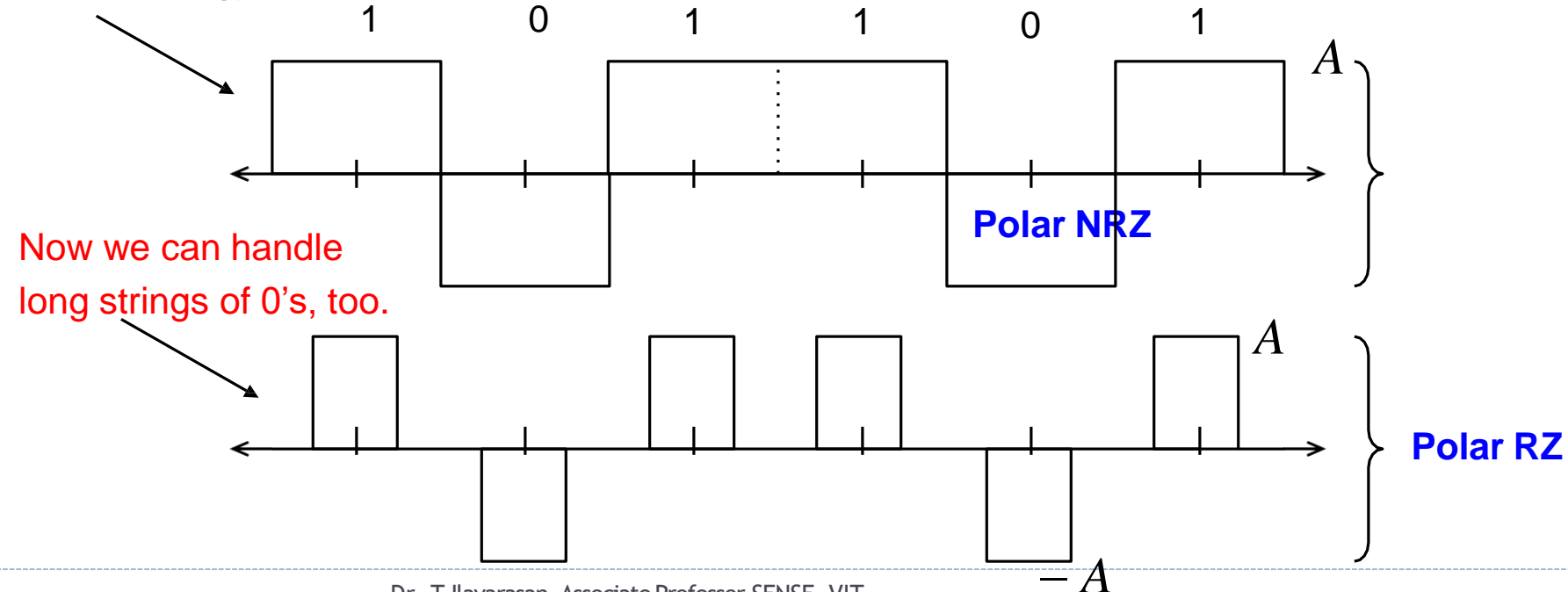
# Line Coding Schemes

- Polar line codes use the antipodal mapping:
- Polar NRZ uses NRZ pulse shape.
- Polar RZ uses RZ pulse shape.

$$a_k = \begin{cases} +A & \text{when } X_k = 1 \\ -A & \text{when } X_k = 0 \end{cases}$$

$$x(t) = \sum_{k=-\infty}^{\infty} a_k p(t - kT_b)$$

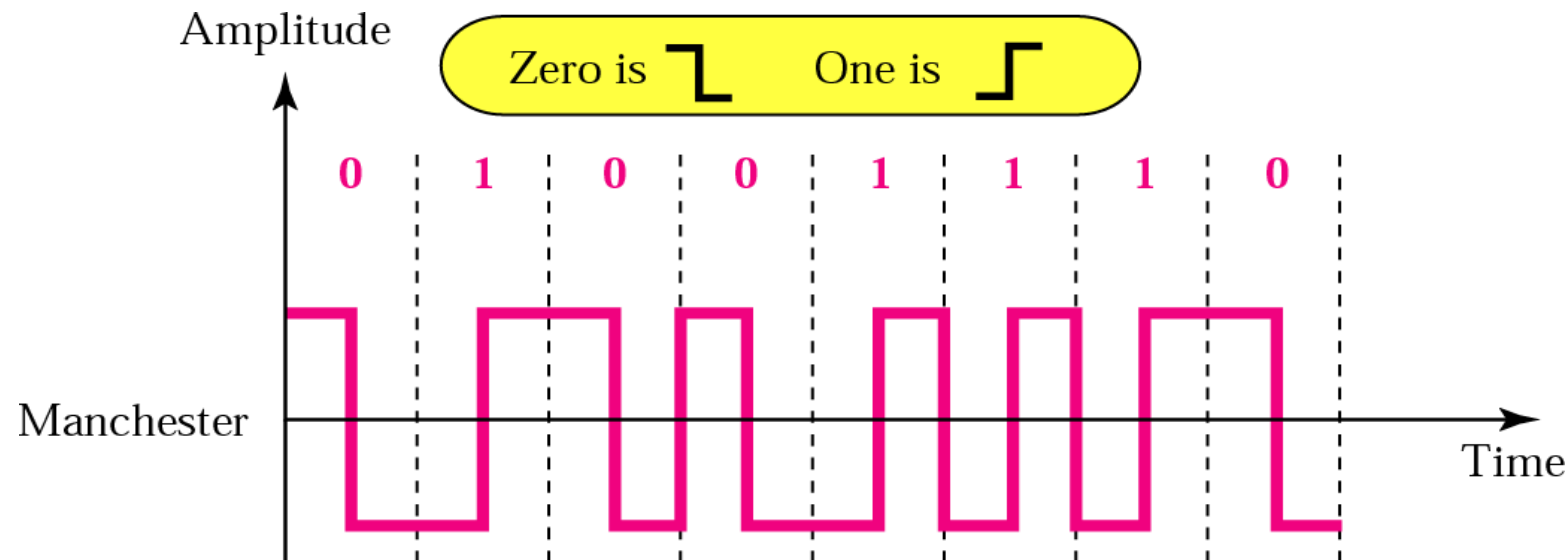
No DC component,  
so more energy efficient.



# Line Coding Schemes

## Polar - Biphasic: Manchester

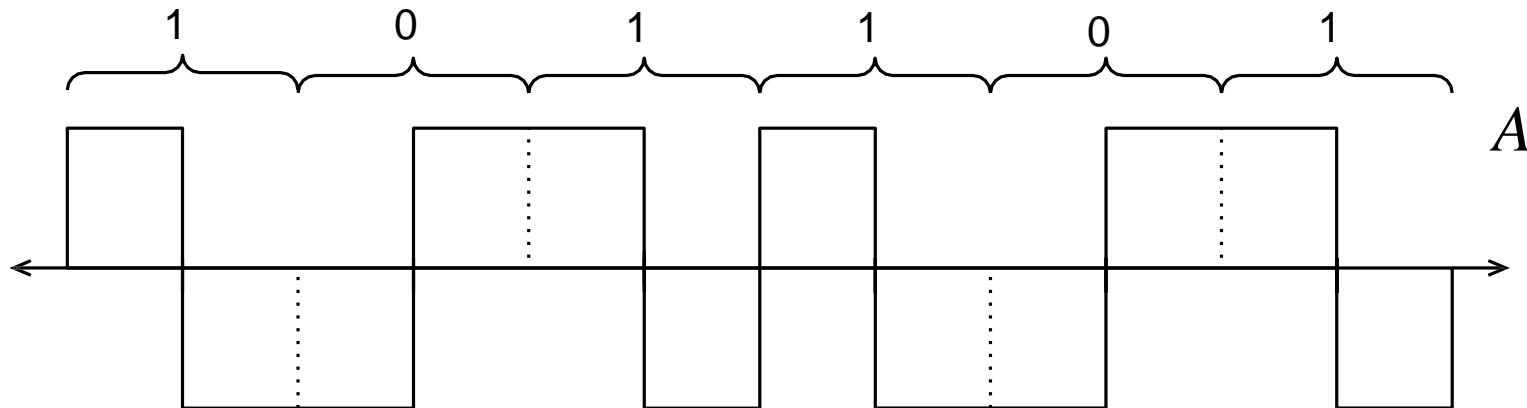
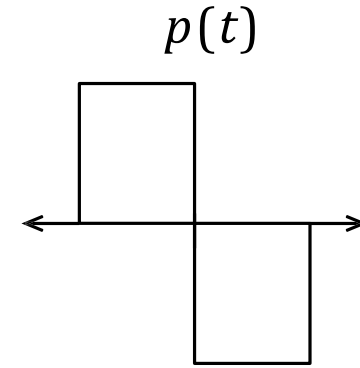
- Manchester coding consists of combining the **NRZ-L** and **RZ** schemes.
- Every symbol has a level transition in the middle: from high to low or low to high.
- The transition at the middle of the bit is used for synchronization and bit representation.



# Line Coding Schemes

- **Manchester line codes** use the antipodal mapping and the following *split-phase* pulse shape:

$$p(t) = \Pi\left(\frac{t + T_b/4}{T_b/2}\right) - \Pi\left(\frac{t - T_b/4}{T_b/2}\right)$$



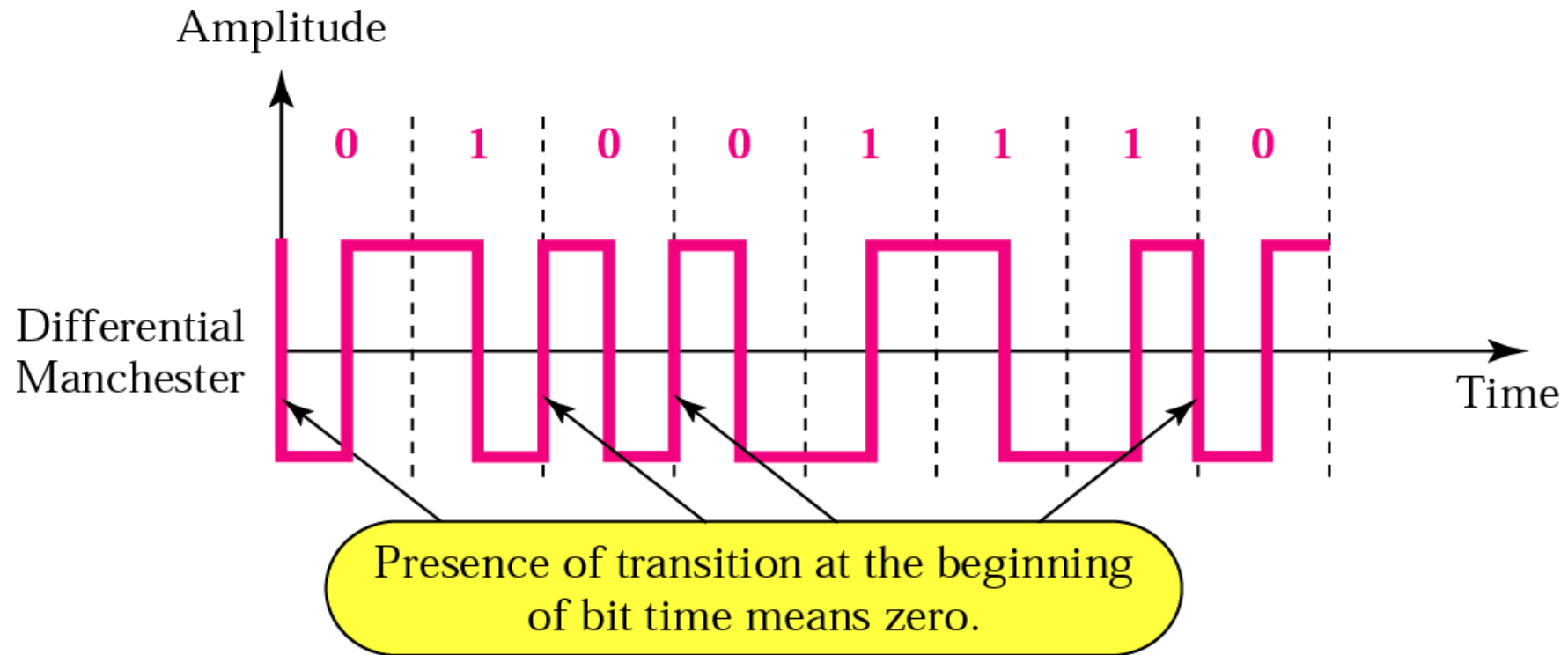
# Line Coding Schemes

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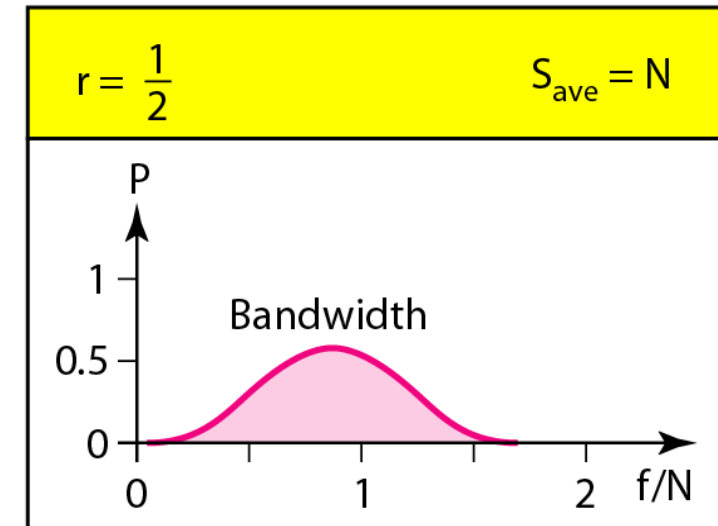
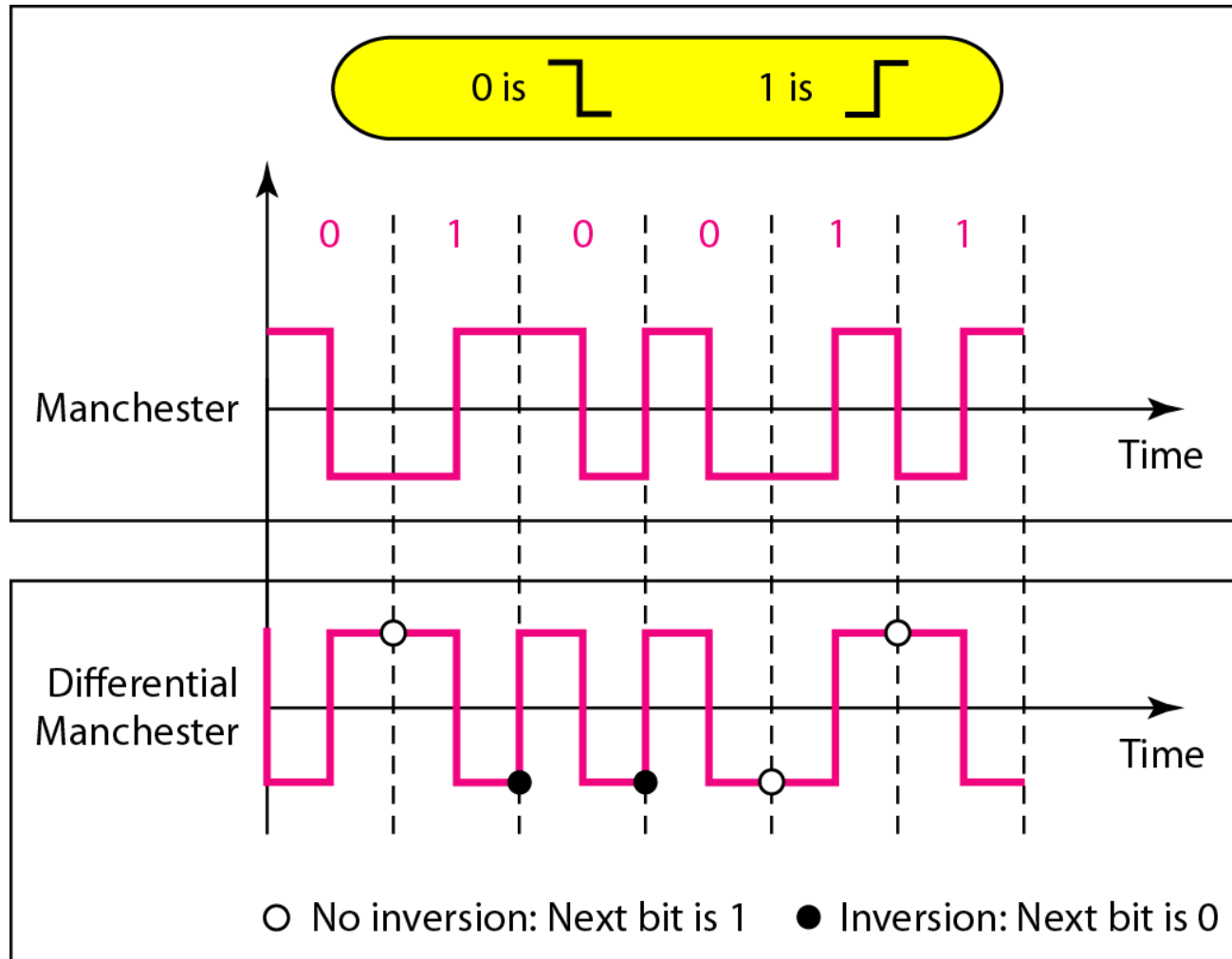
## **Polar - Biphase:Differential Manchester**

- Differential Manchester coding consists of combining the **NRZ-I and RZ** schemes.
- Every symbol has a level transition in the middle.
- But the level at the beginning of the symbol is determined by the symbol value.
- One symbol causes a level change the other does not.
- In differential Manchester encoding, the transition at the middle of the bit is used only for synchronization.
- The bit representation is defined by the inversion or noninversion at the beginning of the bit.

# Line Coding Schemes



# Line Coding Schemes



# Line Coding Schemes

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**In Manchester and differential Manchester encoding, the transition at the middle of the bit is used for synchronization.**



# Line Coding Schemes

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**The minimum bandwidth of Manchester and differential Manchester is 2 times that of NRZ. There is no DC component and no baseline wandering. None of these codes has error detection.**

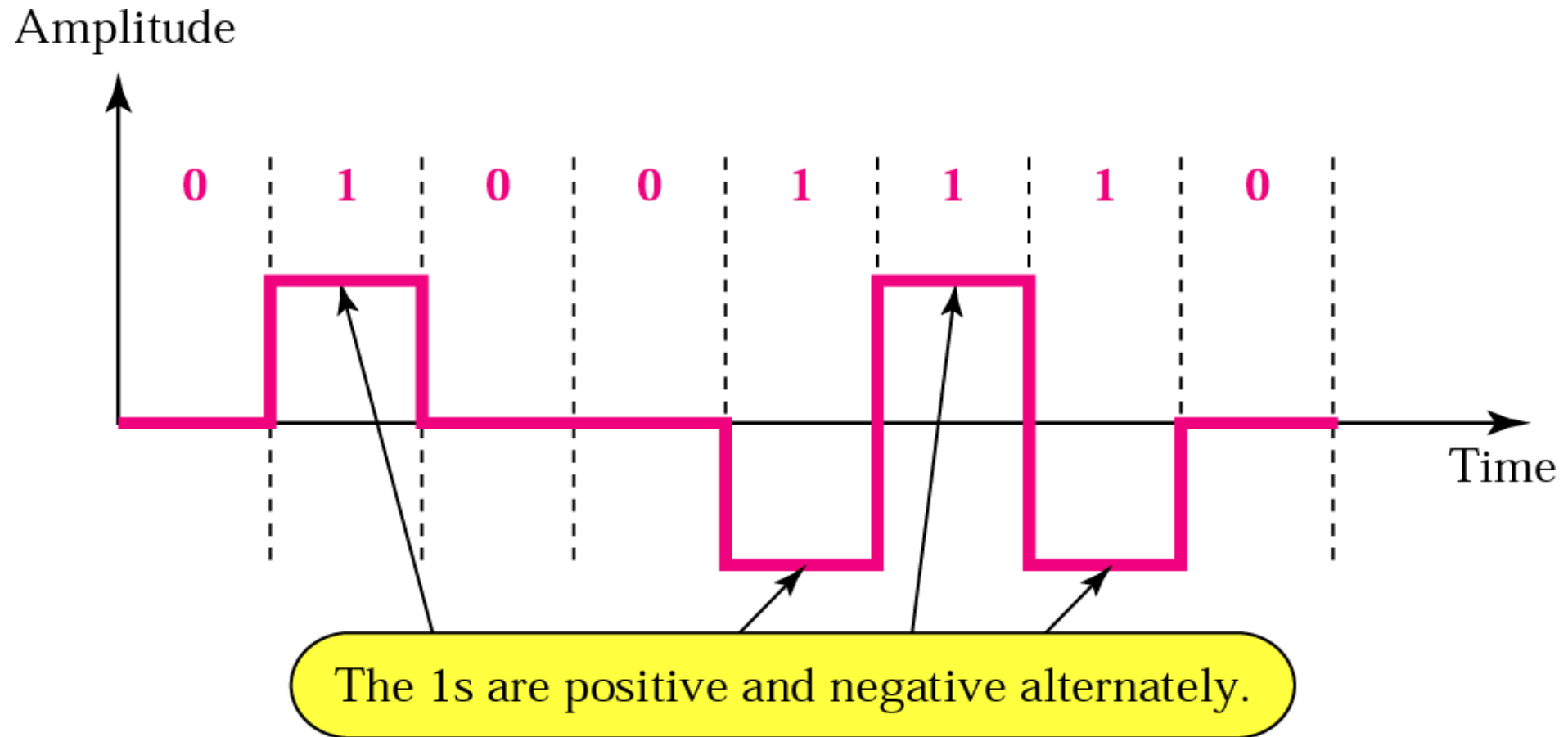
# Line Coding Schemes

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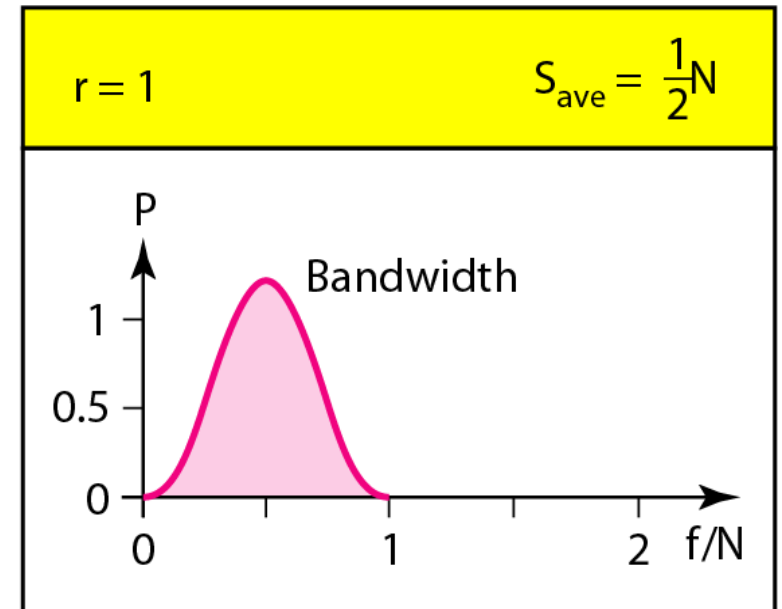
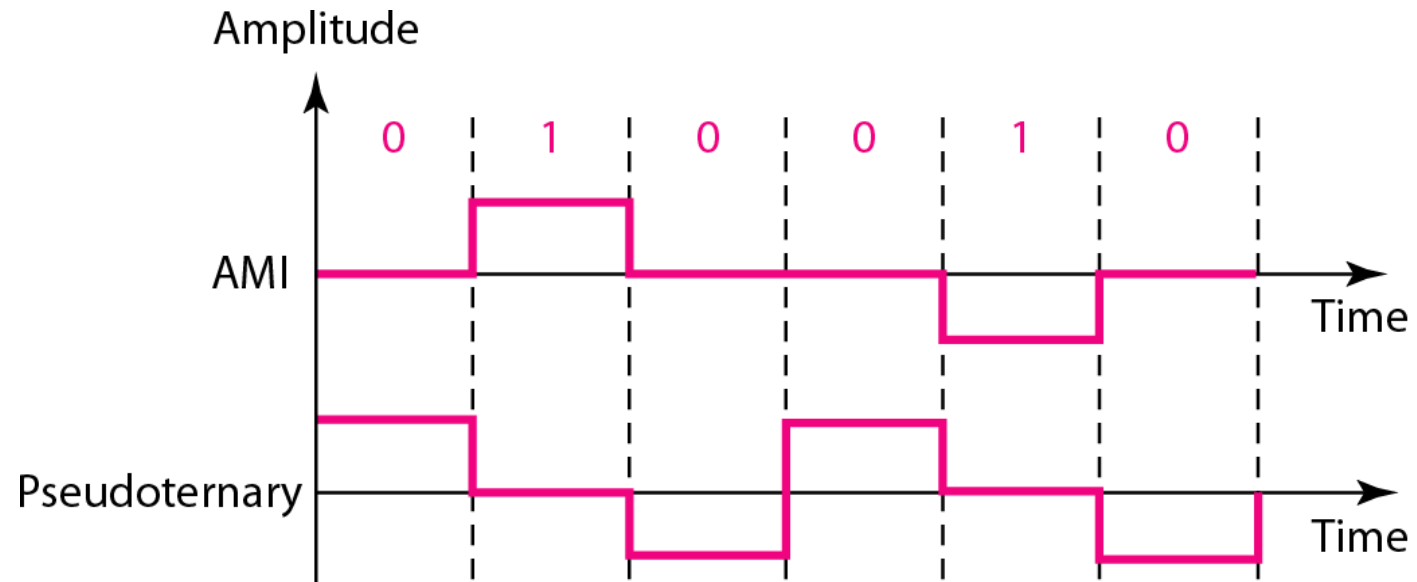
## Bipolar -AMI and Pseudoternary

- Code uses 3 voltage levels: - +, 0, -, to represent the symbols (note not transitions to zero as in RZ).
- Voltage level for one symbol is at “0” and the other alternates between + & -.
- **Bipolar Alternate Mark Inversion (AMI)** - the “0” symbol is represented by zero voltage and the “1” symbol alternates between +V and -V.
- **Pseudoternary** is the reverse of AMI.

# Line Coding Schemes



# Line Coding Schemes



# Line Coding Schemes

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- It is a better alternative to NRZ.
- Has no DC component or baseline wandering.
- Has no self synchronization because long runs of “0”s results in no signal transitions.
- No error detection.

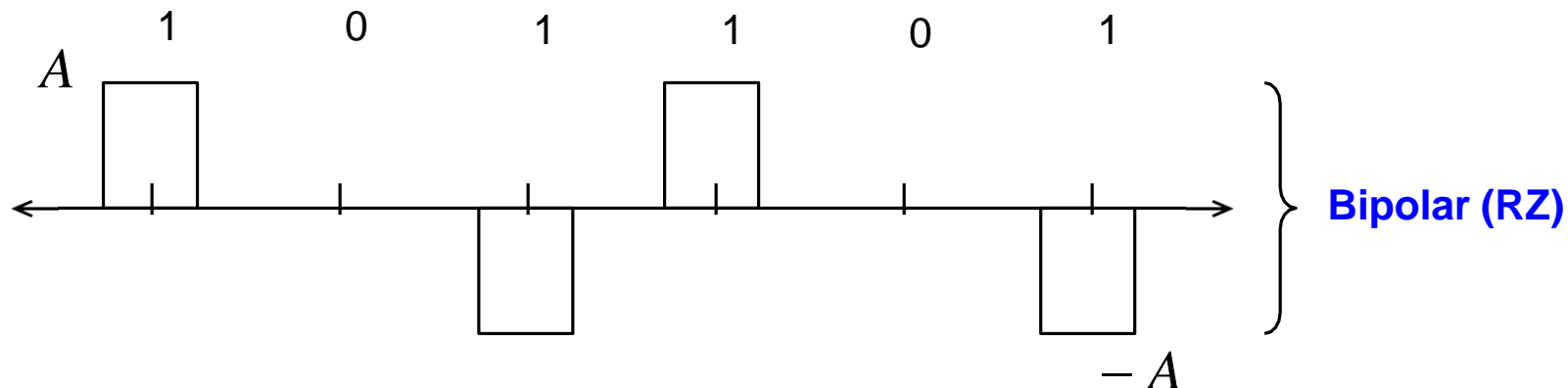
# Line Coding Schemes

- With bipolar line codes a space is mapped to zero and a mark is alternately mapped to -A and +A:

$$a_k = \begin{cases} 0 & \text{when } X_k = 0 \\ -A & \text{when } X_k = 1 \text{ and last mark} \rightarrow +A \\ +A & \text{when } X_k = 1 \text{ and last mark} \rightarrow -A \end{cases}$$

$$x(t) = \sum_{k=-\infty}^{\infty} a_k p(t - kT_b)$$

- Also called pseudoternary signalling and alternate mark inversion (AMI).
- Either RZ or NRZ pulse shape can be used.



# Comparison of Line Codes

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## **Self-synchronization:**

- Manchester codes have built in timing information because they always have a zero crossing in the center of the pulse.
- Polar RZ codes tend to be good because the signal level always goes to zero for the second half of the pulse.
- NRZ signals are not good for self-synchronization.

## **Error probability:**

- Polar codes perform better (are more energy efficient) than Unipolar or Bipolar codes.

## **Channel characteristics:**

- We need to find the PSD of the line codes to answer this .