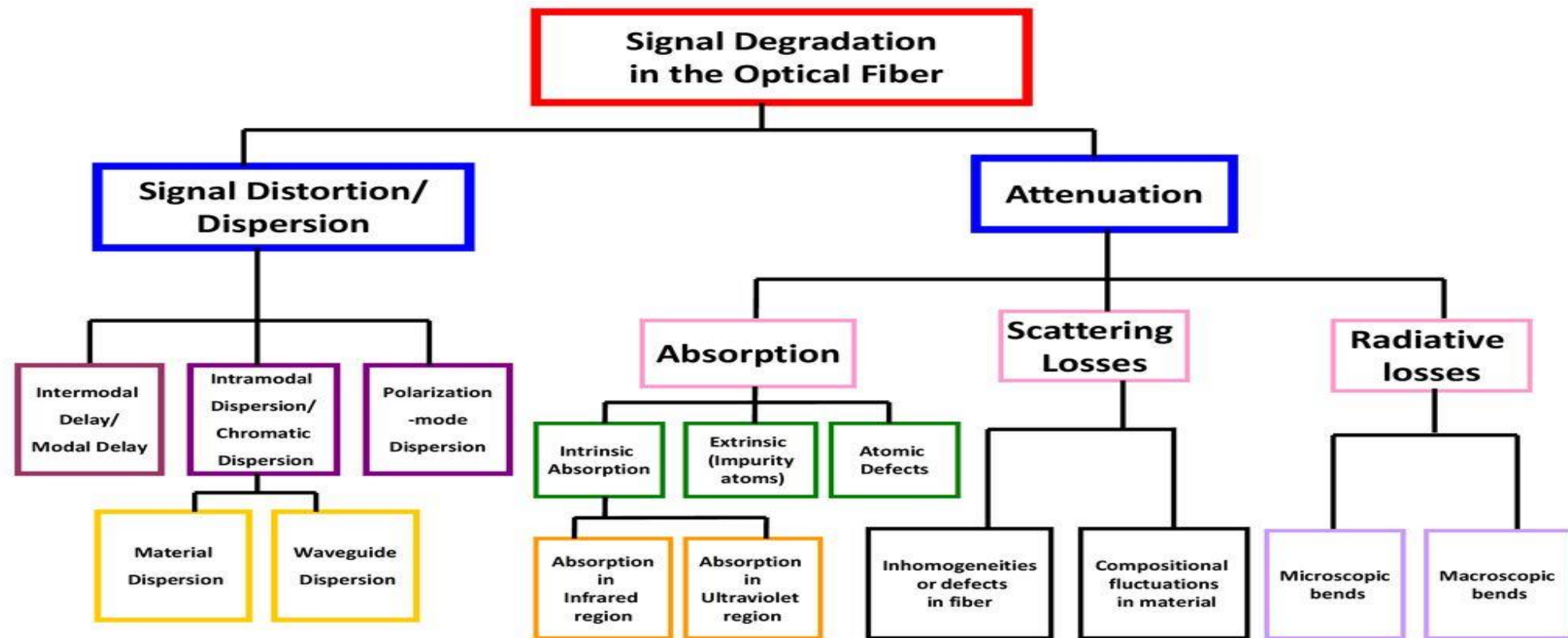


Module - 2

Signal Degradation

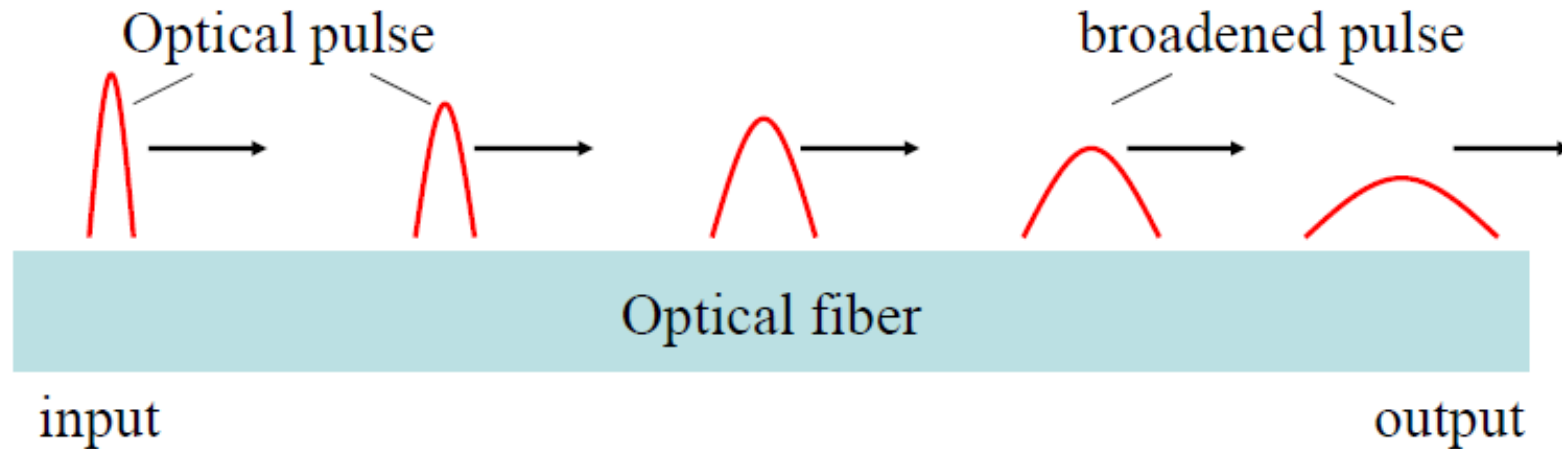


Signal degradation in fiber cable



Fiber Dispersion

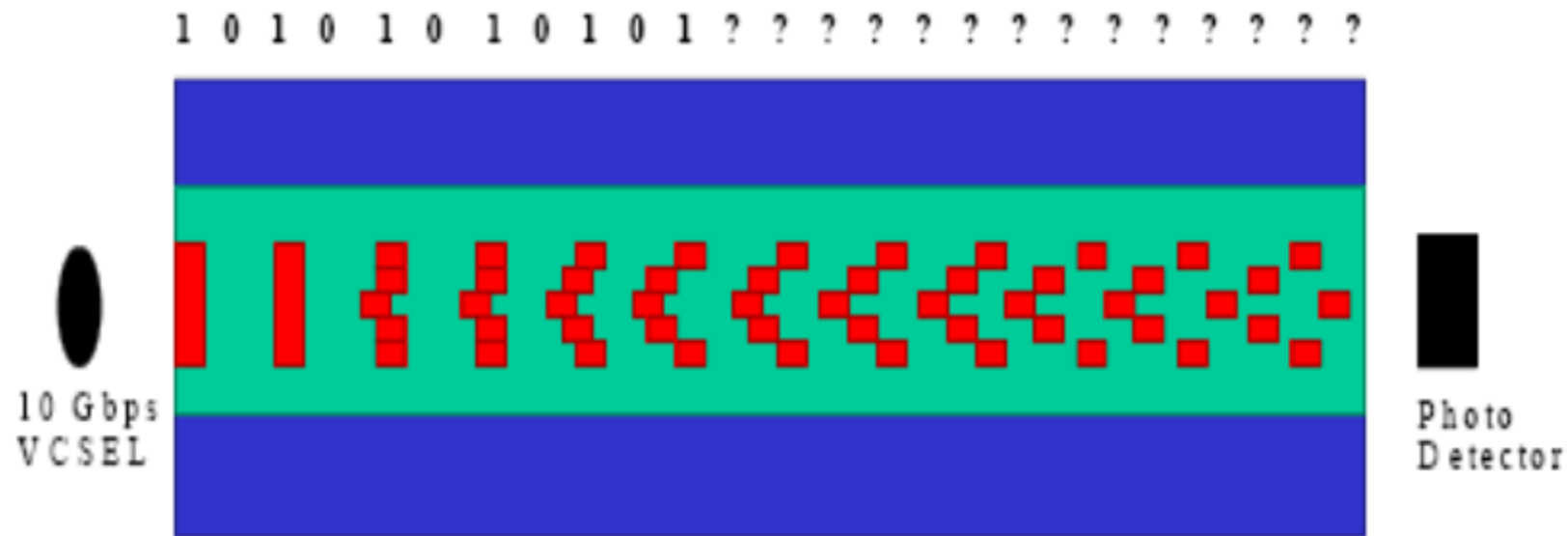
- Fiber dispersion results in **optical pulse broadening** and hence **digital signal degradation**.



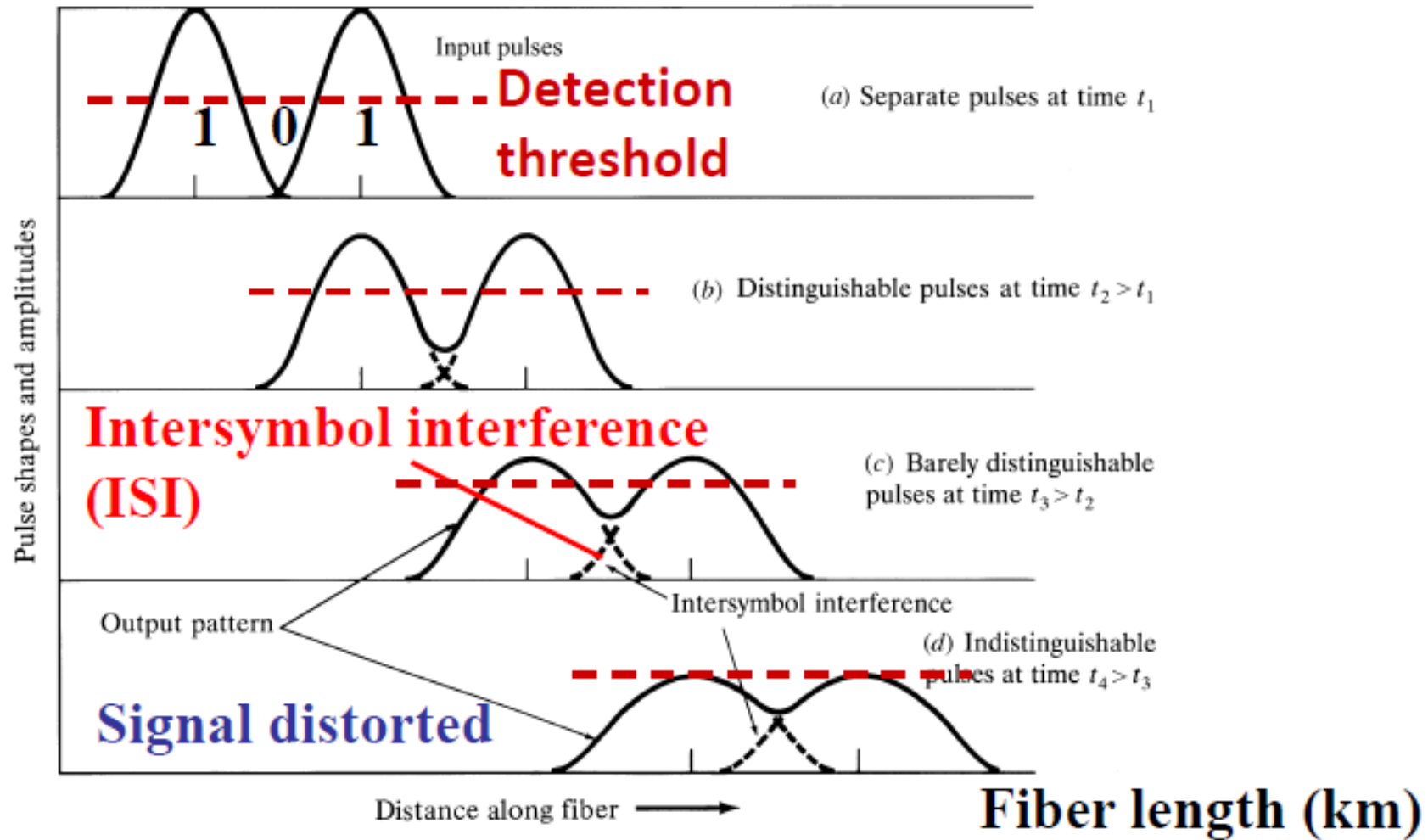
Dispersion mechanisms:

- Modal (or intermodal) dispersion
- Chromatic dispersion (CD)
- Polarization mode dispersion (PMD)

Dispersion in digital systems



Pulse broadening limits fiber bandwidth (data rate)



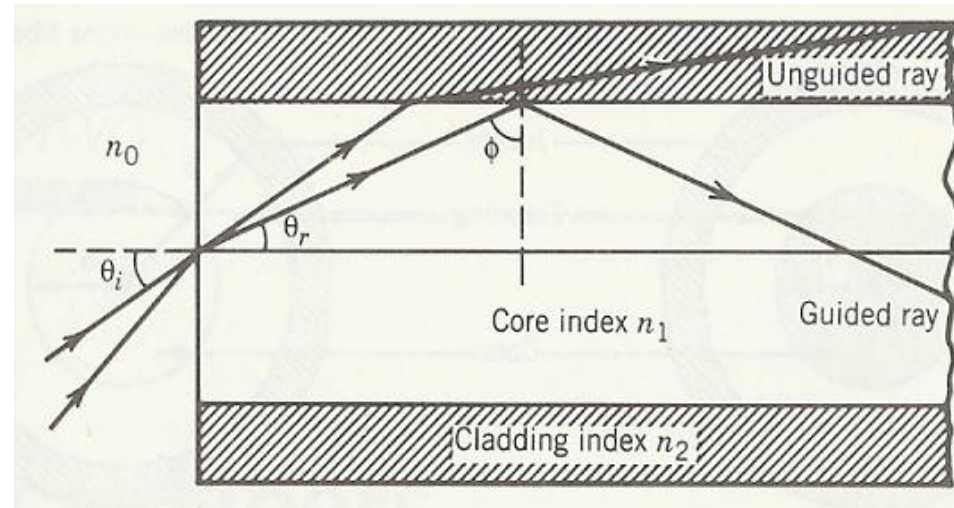
Dispersion types

- Intermodal (modal) Dispersion
- Intramodal Dispersion
- Chromatic Dispersion
 - Material Dispersion
 - Waveguide Dispersion
- Polarization Mode Dispersion

Modal dispersion

- When numerous waveguide modes are propagating, they all travel with different net velocities with respect to the waveguide axis.
- An input waveform distorts during propagation because its energy is distributed among several modes, each traveling at a different speed.
- Parts of the wave arrive at the output before other parts, spreading out the waveform. This is thus known as **multimode (modal) dispersion**.
- Multimode dispersion does not depend on the source linewidth (even a single wavelength can be simultaneously carried by multiple modes in a waveguide).
- **Multimode dispersion would not occur if the waveguide allows only one mode to propagate** - the advantage of single-mode waveguides!

Inter modal dispersion (meridional rays)



Inter modal dispersion (meridional rays)

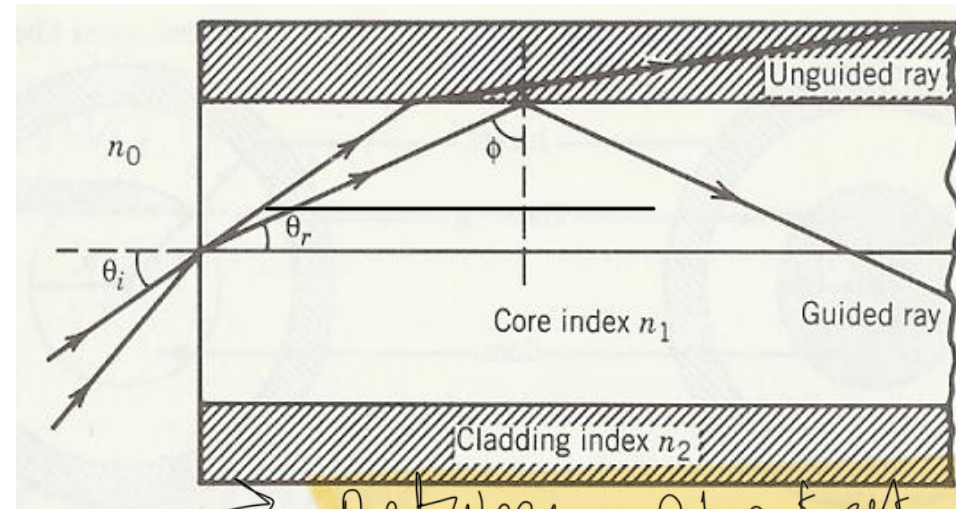
Shortest path $\rightarrow \theta_i = 0$

path length = L

Longest path $\rightarrow \phi = \phi_c$

path length = $L / \sin \phi_c$

Velocity $V \rightarrow c / n_1$



Between shortest and longest

Time delay $\Delta T_{\text{mod}} = \text{Path length difference} / \text{Velocity}$

$$= \left[\left(\frac{L}{\sin \phi_c} \right) - L \right] / \left[c / n_1 \right]$$

$$\boxed{\sin \phi_c = n_2 / n_1} \rightarrow \Delta T_{\text{mod}} = \left(\frac{L}{c} \right) \left(\frac{n_1^2}{n_2} \right) \Delta = \frac{L n_1 \Delta}{c}$$

$$\frac{L}{\sin \phi_c} - L$$

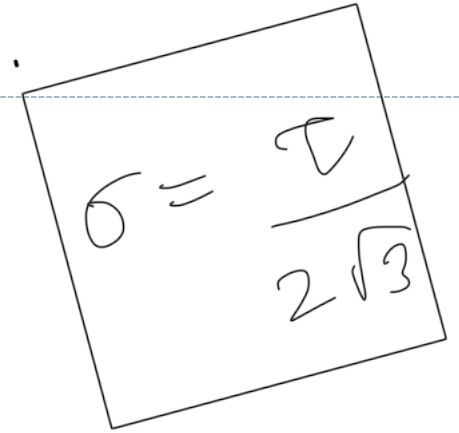
$$\Delta T_{\text{mod}} = \frac{\text{Path length difference}}{\text{velocity}} \quad \frac{L}{c} \Delta n_1$$

$$= \frac{\frac{L}{\sin \phi_c} - L}{c/n_1}$$

$$= \frac{L}{c} \left[\frac{n_1^2}{n_2} \right]$$

RMS pulse broadening

$$\text{RMS pulse width } \sigma = \tau / (2 \sqrt{3})$$


$$\sigma = \frac{\tau}{2\sqrt{3}}$$

RMS pulse spread for a MMSIF:

$$\sigma_s = \Delta T_{\text{mod}} / (2 \sqrt{3}) = L n_1 \Delta / (c 2 \sqrt{3})$$

RMS pulse spread for a MMSIF considering mode coupling:

$$\sigma_{sc} = \frac{\Delta T_{sc}}{L_c} / (2 \sqrt{3}) = (L L_c)^{1/2} n_1 \Delta / (c 2 \sqrt{3})$$

$L_c \rightarrow$ characteristic length of fiber

RMS pulse spread for a MMGIF:

$$\begin{aligned} \Delta T_{gi} &= L n_1 \Delta^2 / 2c && \text{[using ray theory approach]} \\ &= L n_1 \Delta^2 / 8c && \text{[using mode theory approach]} \\ &= L n_1 \Delta^2 / Dc && \text{[where D varies from 2 to 10]} \\ \sigma_{gi} &= \Delta T_{gi} / (2 \sqrt{3}) \\ &= L n_1 \Delta^2 / (20 c \sqrt{3}) = \sigma_s (\Delta / 10) \end{aligned}$$

Attenuation units – Numerical problem

Compare the rms pulse broadening per kilometer for the following three fibers:

- (i). a multimode step index fiber with core index $n_1 = 1.49$ and $\Delta = 1.0\%$,
- (ii). a graded index fiber having an optimum parabolic index profile and the same n_1 and Δ as in (i),
- (iii). the same type of graded index fiber as in (ii) but with $\Delta = 0.5\%$.

Attenuation units – Numerical problem

Compare the rms pulse broadening per kilometer for the following three fibers:

- (i). a multimode step index fiber with core index $n_1 = 1.49$ and $\Delta = 1.0\%$,
- (ii). a graded index fiber having an optimum parabolic index profile and the same n_1 and Δ as in (i),
- (iii). the same type of graded index fiber as in (ii) but with $\Delta = 0.5\%$.

| | | | |
|-------|------------------------|---|--------------|
| (i) | σ_{step} | = | 14.3 ns / km |
| (ii) | σ_{gi} | = | 14.3 ps / km |
| (iii) | σ_{gi} | = | 3.58 ps / km |

Dispersion Characteristics of optical fiber

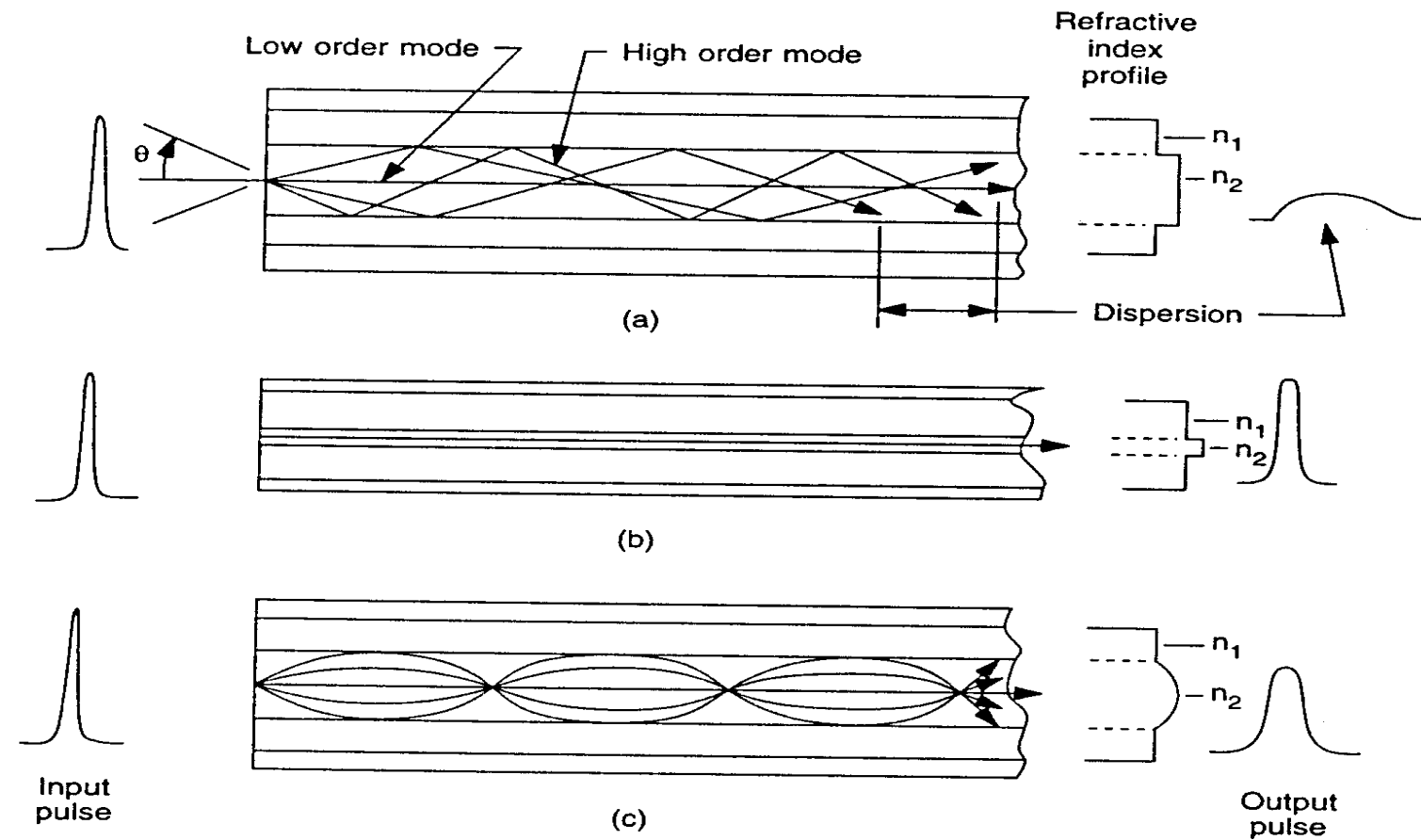


FIG. 2. Characteristics of common optical fibers—(a) multimode step index; (b) single-mode step index; (c) multimode graded index.

Bit-rate distance product

How much will a light pulse spread after traveling along 1 km of a step-index fiber whose $NA = 0.275$ and $n_{core} = 1.487$?

Bit-rate distance product

How does modal dispersion restricts fiber bit rate?

Suppose we transmit at a low bit rate of 10 Mb/s

→ Pulse duration = $1 / 10^7 \text{ s} = 100 \text{ ns}$

Using the above e.g., each pulse will spread up to approx. 100 ns (i.e. approx. pulse duration !) every km

→ The broadened pulses overlap! (Intersymbol interference (ISI))

*Modal dispersion limits the bit rate of a fiber-optic link to $\sim 10 \text{ Mb/s}$.
(a coaxial cable supports this bit rate easily!)

Bit-rate distance product

- We can relate the pulse broadening ΔT to the information-carrying capacity of the fiber measured through the bit rate B .
- Although a precise relation between B and ΔT depends on many details, such as the pulse shape, it is intuitively clear that ΔT should be less than the allocated bit time slot given by $1/B$.
- An order-of-magnitude estimate of the supported bit rate is obtained from the condition $B\Delta T < 1$.
- Bit-rate distance product (limited by modal dispersion)

$$BL < \frac{c}{n_1 \Delta}$$

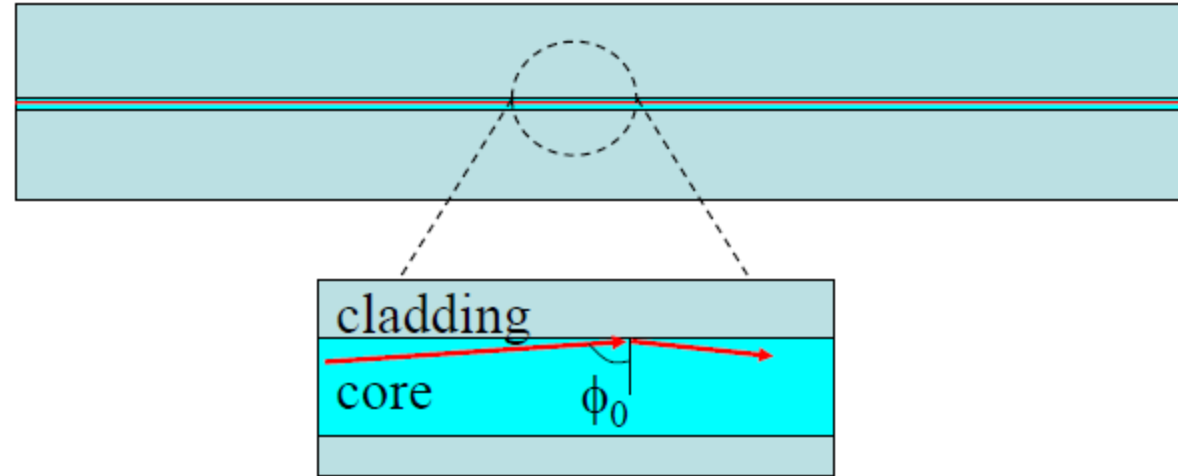
- This condition provides a rough estimate of a fundamental limitation of step-index multimode fibers.

(the smaller is the NA, the larger is the bit-rate distance product)

Bit-rate distance product

- The capacity of optical communications systems is frequently measured in terms of the bit rate-distance product.
- e.g. If a system is capable of transmitting 10 Mb/s over a distance of 1 km, it is said to have a bit rate-distance product of 10 (Mb/s)-km.
- This may be suitable for some local-area networks (LANs).
- Note that the same system can transmit 100 Mb/s along 100 m, or 1 Gb/s along 10 m, or 10 Gb/s along 1 m, or 100 Gb/s along 10 cm, 1 Tb/s along 1 cm

Single-mode fiber eliminates modal dispersion



- The main advantage of single-mode fibers is to propagate only one mode so that modal dispersion is absent.
- However, pulse broadening does not disappear altogether. The group velocity associated with the fundamental mode is frequency dependent within the pulse spectral linewidth because of **chromatic dispersion**.