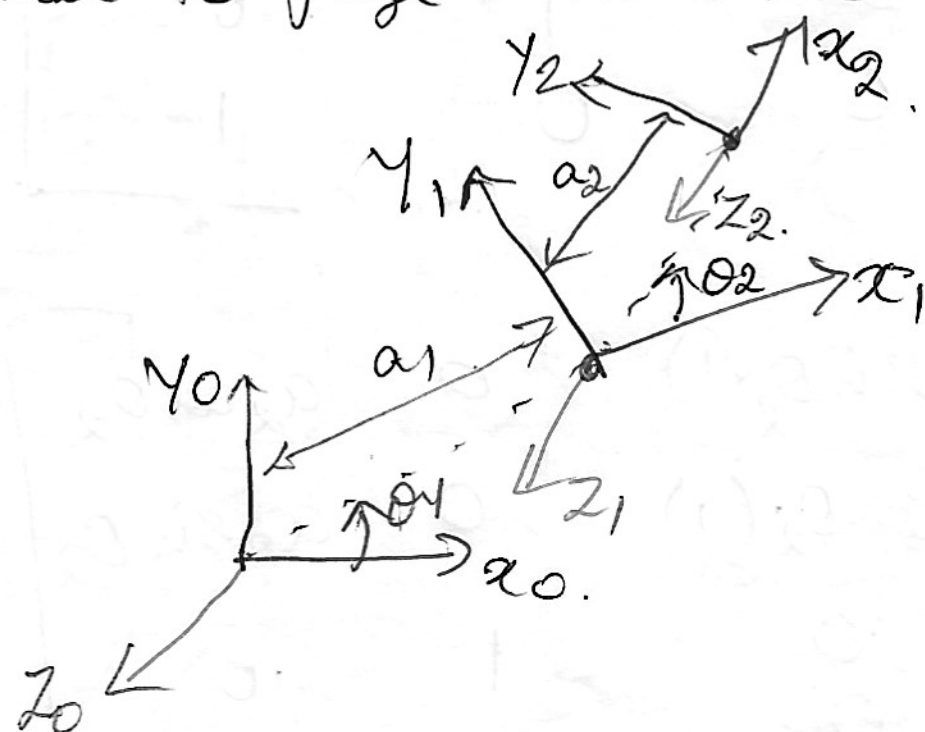


# Denavit Hartenberg:

Ex. 2 Consider 2-link planar arm.  $Z_0$  &  $Z_1$  are normal to page. Find the transformation matrix.



Solu: For the given Framing (frame positions) the D-H table is.

Link	$\theta$	$\alpha$	$\gamma$	$d$
1	$\theta_1$	0	$a_1$	0
2	$\theta_2$	0	$a_2$	0

$${}^0H_1 \rightarrow$$

$${}^0H_1 = \begin{bmatrix} \cos \theta_1 & -\sin \theta_1 \cos(0) & \sin \theta_1 \sin(0) & a_1 \\ \sin \theta_1 & -\cos \theta_1 \cos(0) & -\cos(\theta_1) \sin(0) & 0 \\ 0 & \sin(0) & \cos(0) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$\theta = \theta_1$   
 $\alpha = a_1$   
 $\gamma = d = 0$

$${}^0H_1 = \begin{bmatrix} \cos \theta_1 & -\sin \theta_1 & 0 & a_1 \cos \theta_1 \\ \sin \theta_1 & \cos \theta_1 & 0 & a_1 \sin \theta_1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^1H_2 = \begin{bmatrix} \cos \theta_2 & -\sin \theta_2 (1) & 0 & a_2 \cos \theta_2 \\ \sin \theta_2 & \cos \theta_2 (1) & 0 & a_2 \sin \theta_2 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$\theta = \theta_2$   $\alpha = 0$   
 $r = a_2$   $d = 0$

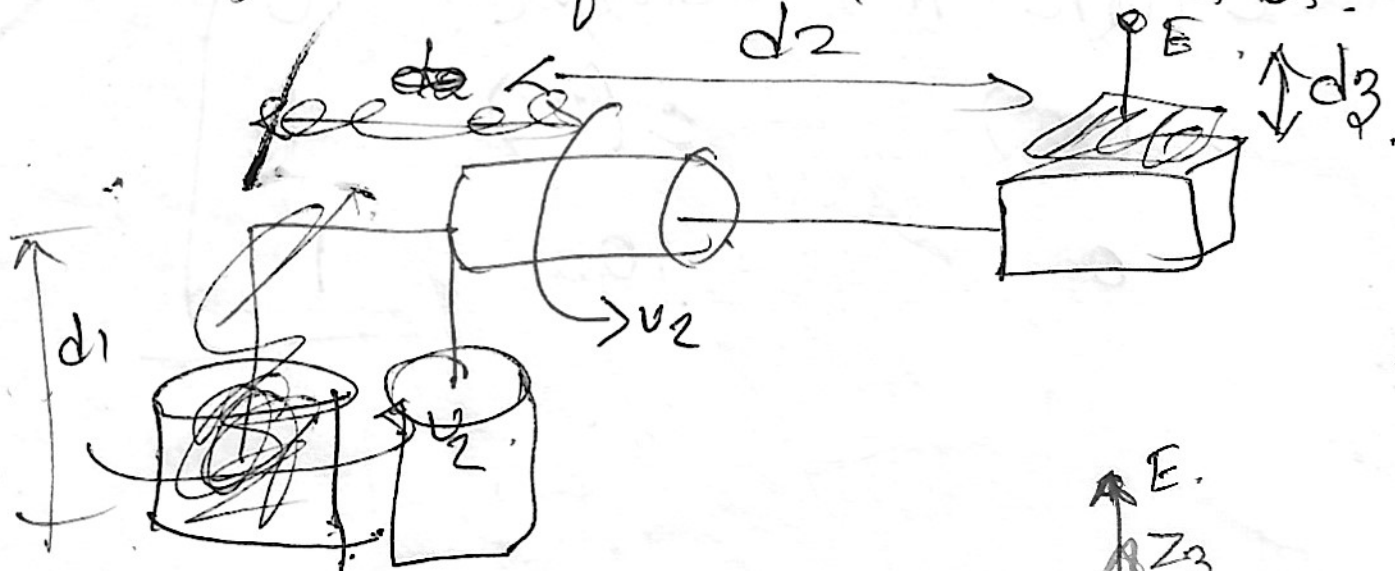
~~$${}^0H_2 = \begin{bmatrix} \cos \theta_1 \cos \theta_2 & -\sin \theta_1 \cos \theta_2 & 0 & a_1 \cos \theta_1 \cos \theta_2 \\ \cos \theta_1 \sin \theta_2 & -\sin \theta_1 \sin \theta_2 & 0 & a_1 \cos \theta_1 \sin \theta_2 \\ \sin \theta_1 \cos \theta_2 & \cos \theta_1 \cos \theta_2 & 1 & a_1 \sin \theta_1 \cos \theta_2 \\ \sin \theta_1 \sin \theta_2 & \cos \theta_1 \sin \theta_2 & 0 & a_1 \sin \theta_1 \sin \theta_2 \end{bmatrix}$$~~

$${}^0H_2 = {}^0H_1 \times {}^1H_2$$

$${}^0H_2 = {}^0H_1 \times {}^1H_2$$

# Inverse Kinematics

P3) DH - forward kinematics.

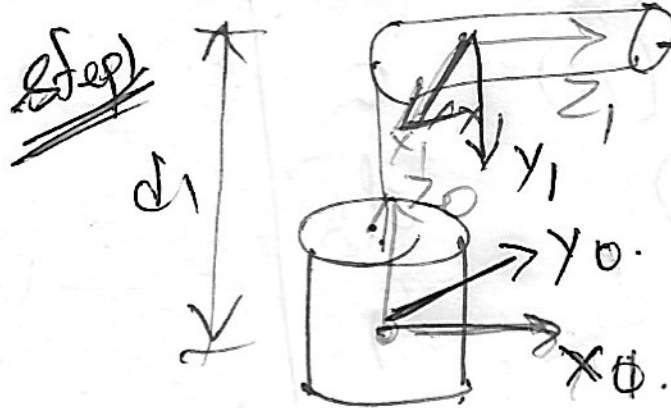


Joints = 3

Frames = 4

Rows = 3

Solution



	$\theta$	$\alpha$	$\alpha$	$d$	<u>Step 2</u>
1	$-90^\circ + \theta_1$	$-90^\circ$	0	$d_1$	
2	$v_2$	$90^\circ$	0	$d_2$	
3	0	0	0	$d_3$	

Step 3

$${}^{n-1}H_n = \begin{bmatrix} c(\theta_n) & -s(\theta_n)c(\alpha_n) & s(\theta_n)s(\alpha_n) & r_n c(\theta_n) \\ s(\theta_n) & -c(\theta_n)c(\alpha_n) & -c(\theta_n)s(\alpha_n) & r_n s(\theta_n) \\ 0 & s(\alpha_n) & c(\alpha_n) & d_n \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^0H_1 = \begin{bmatrix} \cos(v_1 - 90^\circ) & -s(v_1 - 90^\circ)c(-90^\circ) & s(v_1 - 90^\circ)s(-90^\circ) & 0 \\ \sin(v_1 - 90^\circ) & -c(v_1 - 90^\circ)c(-90^\circ) & -c(v_1 - 90^\circ)s(-90^\circ) & 0 \\ 0 & s(v_1 - 90^\circ) & c(-90^\circ) & d_1 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

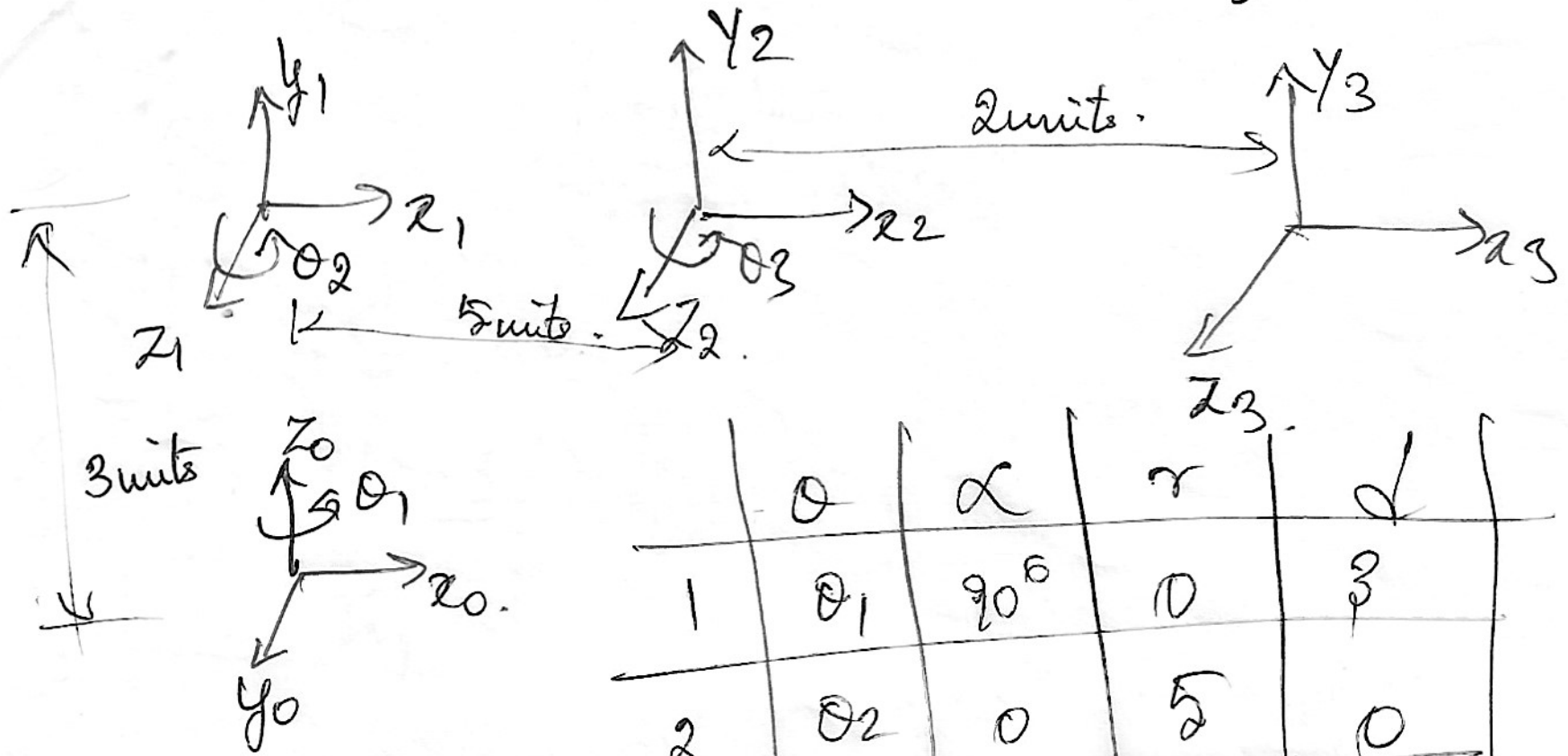
$${}^1H_2 = \begin{bmatrix} c(u_2) & -s(u_2)\cos(90^\circ) & s(u_2)s(90^\circ) & 0 \\ s(u_2) & c(u_2)c(90^\circ) & -c(u_2)s(90^\circ) & 0 \\ 0 & -s(90^\circ) & c(90^\circ) & d_2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^2H_3 = \begin{bmatrix} c(0) & -s(0)c(90^\circ) & s(0)\sin(90) & 0 \\ s(0) & -c(0)c(90^\circ) & -c(0)s(90^\circ) & 0 \\ 0 & s(90^\circ) & c(90) & d_3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^0H_3 = {}^0H_1 \times {}^1H_2 \times {}^2H_3.$$



P4). Find DH matrix & transformation.



	$\theta$	$\alpha$	$r$	$d$
1	$\theta_1$	$90^\circ$	0	3
2	$\theta_2$	0	5	0
3	$\theta_3$	0	2	0

$${}^0H_1 = \begin{bmatrix} \cos \theta_1 & 0 & \sin \theta_1 & 0 \\ \sin \theta_1 & 0 & -\cos \theta_1 & 0 \\ 0 & 1 & 0 & 3 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^1H_2 = \begin{bmatrix} \cos \theta_2 & -\sin \theta_2 & 0 & 2 \cos \theta_2 \\ \sin \theta_2 & \cos \theta_2 & 0 & 2 \sin \theta_2 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^2H_3 = \begin{bmatrix} \cos \theta_3 & -\sin \theta_3 & 0 & 2 \cos \theta_3 \\ \sin \theta_3 & \cos \theta_3 & 0 & 2 \sin \theta_3 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^0H_3 = {}^0H_1 \times {}^1H_2 \times {}^2H_3 = [ \quad ] [ \quad ] [ \quad ]$$

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