

**Question:Question: At  $t = 0$  a current of 2 amperes flows in an RLC circuit with resistance  $R = 40$  ohms, inductance  $L$ ...**

At  $t = 0$  a current of 2 amperes flows in an  $RLC$  circuit with resistance  $R = 40$  ohms, inductance  $L = 0.2$  henrys, and capacitance  $C = 10^{-4}$  farads. Find the current flowing in the circuit at  $t > 0$  if the initial charge on the capacitor is 1 coulomb. Assume that  $E(t) = 0$  for  $t > 0$ .

- Must start by writing a differential equation and solving it.

$$R = 40 \text{ ohm}$$

$$L = 0.2 \text{ henrys}$$

$$C = 10^{-4} \text{ farads}$$

$$E(t) = 0$$

Let  $q(t)$  be charge flowing at time  $t$

$$q(0) = 1 \text{ coulomb}$$

$$q'(0) = 0$$

$$Lq'' + Rq' + \frac{1}{C}q = E(t)$$

$$\Rightarrow 0.2q'' + 40q' + 10000q = 0$$

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auxiliary equation is

$$0.2r^2 + 40r + 10000 = 0$$

root  $r$  is  $-100 + 200i$ ,  $-100 - 200i$

solution is  $q(t) = e^{(-100t)} (c_1 \cos(200t) + c_2 \sin(200t))$

$$q'(t) = e^{(-100t)} (-200c_1 \sin(200t) + 200c_2 \cos(200t) - 100c_1 \cos(200t) - 100c_2 \sin(200t))$$

Put  $q(0) = 1$ ,  $q'(0) = 0$

$$1 = c_1$$

$$0 = 200 c_2 - 100 c_1$$

on solving

$$c_1 = 1, c_2 = 0.5$$

$$\text{hence } q(t) = e^{-100t} (1 \cos(200t) + 0.5 \sin(200t))$$

$$\text{Now } q(t) = e^{-100t} \left( \cos(200t) + \frac{\sin(200t)}{2} \right)$$

$$\Rightarrow \text{Current } i(t) = q'(t)$$

$$i(t) = -250 e^{-100t} \sin(200t) \quad \text{Answer}$$