

Register Number

Name

VIT<sup>®</sup>

Vellore Institute of Technology

(Deemed to be University under provision of UGC Act, 1956)

## Continuous Assessment Test - II, March 2023

### Open Book Examination

Programme	: B.Tech.	Semester	: WIN 2022 - 2023
Course	: Differential Equations and Transforms	Code	: BMAT102L
		Slot	: C2+TC2+TCC2
Faculty	: Dr. V. Parthiban Dr. Pankaj Shukla Dr. Somnath Bera Dr. Biswajit Mallick Dr. Kalyan Dr. A. Felix	Class Nbr	: CH2022235002171 CH2022235002172 CH2022235002173 CH2022235002590 CH2022235002591 CH2022235002704
Time	: 90 Mins.	Max.Marks	: 50

**Answer all the questions**

**(5 × 10 = 50 Marks)**

Q.No.	Question Description	Marks
1. a)	Find the Laplace transform of $f(t) = t^2 e^{-2t} \cos(5t)$	5
b)	Find the Laplace transform of $f(t) = \begin{cases} t-3, & 3 \leq t \leq 4 \\ 5-t, & 4 \leq t \leq 5 \end{cases}$	5
2.	Find the inverse Laplace transform of $\frac{s+4}{(s^2+8s+15)^2}$ .	10
3.	Solve $y'' - 7y' + 6y = e^t + \delta(t-2) + \delta(t-4)$ , $y(0) = 0$ , $y'(0) = 0$ using Laplace transform technique	10
4✓	Solve $u_x + 4u_t = -8t$ , $u(x, 0) = 0$ , $u(0, t) = 2t^2$ using Laplace transform technique.	10
5.	Find the Fourier series of the function $f(x) = x(2\pi - x)$ in $(0, 2\pi)$ with period $2\pi$ . Deduce the sum of the series $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots \infty$ .	10

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