

Continuous Assessment Test (CAT- II) - JUNE 2023

| Course | me : B. Tech | Semester | : Fall Inter Semester 2022-23 |
|---------|--|------------|--|
| Course | : Discrete Mathematics and Graph Theory | Code | : BMAT205L |
| Faculty | | Slot(s) | : C1+TC1+TCC1 |
| | Dr. Kalyan Manna, Dr. Avinash Kumar Mittal, Dr. Durga Nagrajan, Dr. Vidhya V, Dr. Devi Yamini S, Dr. Om Namah Shivay, Dr. Uma Maheswari S, Dr. Rajesh Kumar Mohapatra, Dr. Manigandla Prasannalakshmi, Dr. Sandip Dalui, Dr. Pulak Konar, Dr. Surath Ghosh, Dr. Lakshmanan S | Class Id | : CH2022232500280 CH2022232500287 CH2022232500292 CH2022232500297 |
| ime | : 90 Minutes | Max. Marks | - 50 |

Answer ALL the Questions (5 X 10 = 50 Marks)

| Q.No. | Sub. Sec. | Question Description | Marks |
|-------|--------------|----------------------|-------|
| | | | |

The number plates of cars must contain 3 letters of the alphabet denoting the place and area to which its owner belongs. This is to be followed by a three-digit number. How many different number plates can be formed if: (i) Repetition of letters and digits is not allowed. (ii) Repetition of letters and digits is allowed.

6. (i) Kyle wants to buy coffee and a doughnut. The local doughnut shop has five kinds of doughnuts for sale and sells four varieties of coffee in three sizes (as shown in the table).

| | Small | Medium | Large |
|------------|------------------|-------------------|------------------|
| Latte | small latte | medium latte | large latte |
| Mocha | small mocha | medium mocha | large mocha |
| Espresso | small espresso | medium espresso | large espresso |
| Cappuccino | small cappuccino | medium cappuccino | large cappuccino |

How many different orders could Kyle make?

(ii) Jasmine is holding three cards from a regular deck of playing cards. She tells you that they are all hearts, and that she is holding at least one of the two highest cards in the suit (Ace and King). If you wanted to list all of the possible sets of cards she might be holding, how long would your list be?

2. Using the method of undetermined coefficients, solve the recurrence relation.

$$a_{n+2} - 6a_{n+1} + 5a_n = 1 + n + 5^n, n \ge 0$$
 with $a_0 = 1; a_1 = 1$

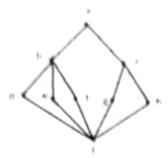
3. (i)Prove that
$$(a+b') \cdot (b+c') \cdot (c+a') = (a'+b) \cdot (b'+c) \cdot (c'+a)$$

(Using Boolean laws)
(ii)Simplify the Boolean expression: $ab + abc + a'b + ab'c$

Prove that the following Hasse Diagram represents a Lattice.

2+3





Also, check whether the lattice is (a) complemented or not (b) distributive or not. (Justification required for each part)

Consider the set $A = \{\{1\}, \{2\}, \{5\}, \{1,2\}, \{1,5\}, \{2,5\}, \{3,5\}, \{1,3,5\}, \{2,3,5\}\}$ with subset \subseteq as the relation.

- (a) Prove that (A, ⊆) is a POSET.
 - (b) Draw the Hasse diagram.

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- (c) Find the minimal, maximal, greatest, least element if it exists.
- (d) Find the upper bounds and least upper bound of {{2},{5}}, if it exists
- (e) Find the lower bounds and greatest lower bound of {{1,3,5},{2,3,5}} if it exists.

a. For the given incidence matrix

$$\begin{array}{c} e_1 \\ e_2 \\ e_3 \\ e_4 \\ e_5 \\ e_6 \\ e_6 \\ e_8 \end{array} \begin{pmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 & 0 \\ \end{array}$$

Identify the following.

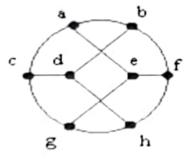
- (i) Isolated vertices
- (ii) Pendant vertices

(Justification required for each case)



(i)Check whether the degree sequence (6, 4, 3, 3, 2, 1, 1, 0) constitute a simple graph, if so, draw the graph, if not, add or delete exactly one vertex to make it a simple graph.

(ii) Check whether the following graph is planar. (Justification required)



4+2