

## FORCES AND GEOMETRY

volume constancy, (width, b)

$$bh_0v_0 = bhv = bh_fv_f$$

N - neutral/ no-slip point

P\_r - radial force

F - tangential frictional force

before N, v < v\_r

after  $N, v > v_r$ 

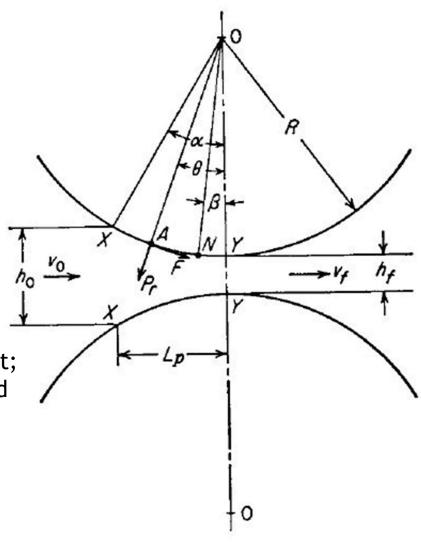
Vertical component of P\_r is Rolling Load, P

Contact area = L\_p \* b; L\_p - length of arc of contact;

h\_0 - h\_f = dell\_h - rolling draft or thickness reduced

$$L_p = \left[ R(h_0 - h_f) - \frac{(h_0 - h_f)^2}{4} \right]^{1/2} \approx \left[ R(h_0 - h_f) \right]^{1/2}$$

Specific roll pressure,  $p = P/A = P/(b.L_p)$ 



Pressure rises to a maximum at neutral point then falls.

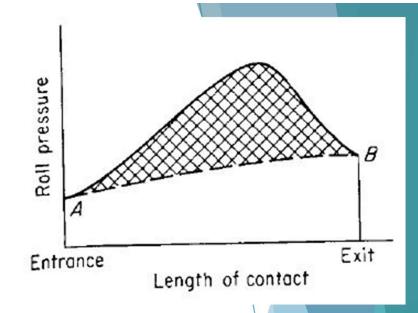
Why no sharp peak in the graph? Neutral point is not a line but a plane!

#### Features of the graph:

- Area under the curve is proportional to rolling load
- 2. Shaded region denotes force required to overcome frictional forces
- Unshaded portion represents the force required to deform metal

Angle between entrance plane and centerline of rolls is the bite angle, a

Equating the horizontal components of the radial and tangential forces, we get F = mu.P\_r



$$F\cos\alpha = P_r \sin\alpha$$

$$\frac{F}{P_r} = \frac{\sin\alpha}{\cos\alpha} = \tan\alpha$$

$$F = \mu P_r$$

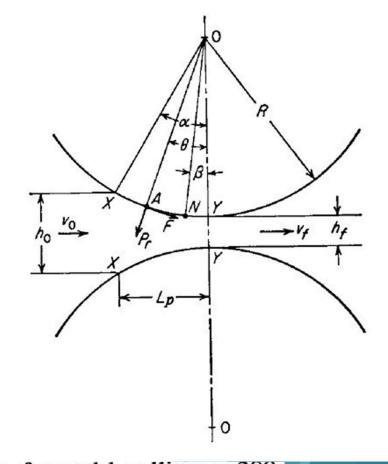
$$\mu = \tan\alpha$$

## MAX. THICKNESS REDUCTION

$$\tan \alpha = \frac{L_p}{R - \Delta h/2} \approx \frac{\sqrt{R\Delta h}}{R - \Delta h/2} \approx \sqrt{\frac{\Delta h}{R}}$$

$$\mu \ge \tan \alpha = \sqrt{\Delta h/R}$$

$$(\Delta h)_{\text{max}} = \mu^2 R$$



Solve Quickly!

Example Determine the maximum possible reduction for cold-rolling a 300 mm-thick slab when  $\mu = 0.08$  and the roll diameter is 600 mm. What is the maximum reduction on the same mill for hot rolling when  $\mu = 0.5$ ?

## **ELASTIC DISTORTION**

- BENDING OF ROLL
- 2. ROLL FLATTENING

$$R' = R \left[ 1 + \frac{CP'}{b(h_0 - h_f)} \right]$$

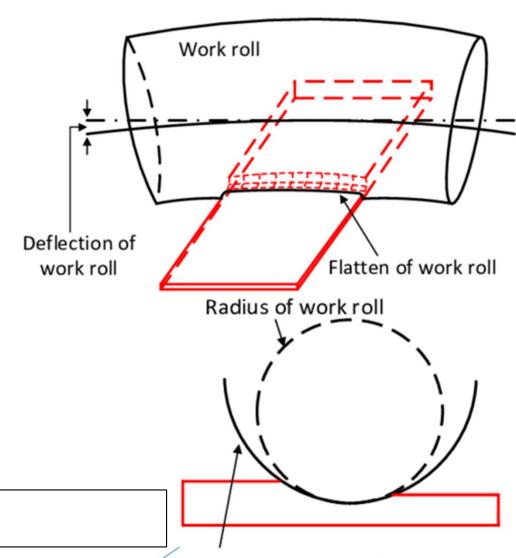
Roll flattening calculations are iterative

R' - new roll radius after roll flattening

P' - rolling load based on deformed roll radius

C = 16(1- nu<sup>2</sup>)pi.E [roll material parameter]

C = 2.16e-11 Pa^-1 for steel rolls



Answers to the Qn in previous slide:

(i) cold rolling: dell\_h\_max = 1.92 mm; (ii) hot rolling: dell\_h\_max = 75 mm

C2+TC2 Metal Forming Theory and Practice, School of Mechanical Engineering, Vellore Institute of Technology, Chennai

Flattening radius of work roll

## **ROLLING LOAD ANALYSIS**

#### Major parameters in rolling:

- Roll Diameter
- Deformation resistance of metal
- 3. Friction between rolls and workpiece
- 4. Presence of front and/or back tension in the plane of sheet

Y - flow stress in plane strain condition

Using slab analysis, the equation of average roll pressure is obtained as follows,

$$P = \begin{bmatrix} Y - (T_b + T_f) \\ \frac{\mu L_P}{h} \end{bmatrix} \begin{bmatrix} e^{\mu L_P} \\ \frac{\mu L_P}{h} \end{bmatrix}$$

$$P - average rolling pressure$$

$$Y - plane strain flow stress$$

$$T_b, T_f - back/front tensile stress$$

$$T_b - average sheet thickness$$

$$T_h = h_0 + h_f$$

$$Z$$

$$Now, P = P b \sqrt{R} \Delta h$$

# Question 1 - Roll Pressure without Roll Flattening

Consider the rolling of a sheet 15-cm wide from a thickness of 1.8mm to 1.2mm in a single pass by steel rolls 20 cm in diameter. Assume a friction coefficient of 0.10 and a flow stress of 125 MPa. Calculate the roll pressure if roll flattening is neglected.

Question: 1

Given:

(a) 
$$\vec{p} = \frac{r}{r} \left[ e^{\frac{r^2 r}{r}} - 1 \right]$$

$$\bar{h} = \frac{h_0 + h_f}{2} = \frac{1.8 + 1.2}{2} = 1.5 \text{ mm}$$

$$\frac{\mu Lp}{\bar{h}} = \frac{0.1 \times 7.7}{1.5} = 0.5133$$

$$\Rightarrow \bar{p} = \frac{125}{0.5133} \left[ e^{0.5133} - 1 \right]$$
 $\bar{p} = 163.35 \text{ MPa}$ 

The noll pressure, for above considered case, if noll flattening is neglected, is.,  $\bar{p} = 163.35$  MPa.

Rolling Load, P.

P = \bar{p}.b\sqrt{RAh}

= 163.35 \times 150 \times 7.7

= 188669.25 \times N

= 188.67 \times N

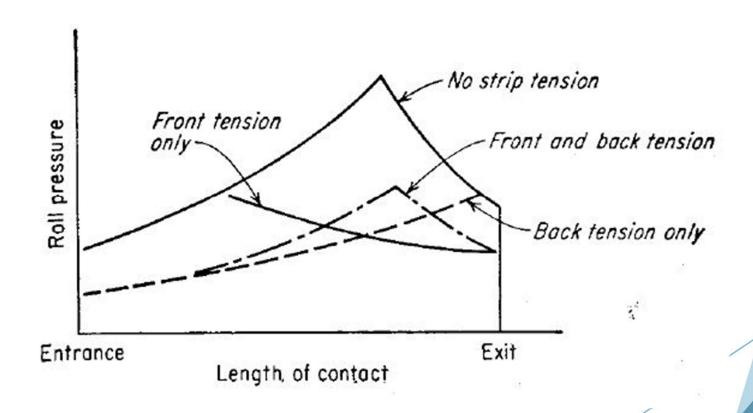
# Practice Problem - Roll pressure - Try later!

The plane-strain flow stress of a metal is 200 MPa. A sheet 0.60 m wide and 3 mm thick is to be cold rolled to 2.4 mm in a single pass using 30 cm diameter rolls. Assuming a coefficient of friction is 0.075,

- a) Compute the roll pressure.
- b) If front tension of 75 MPa were applied, what would be the average roll pressure?

Answer: (a) 988MPa, (b) 803 MPa

# EFFECT OF STRIP TENSION ON ROLL PRESSURE



Roll entrance to neutral point:

$$p_r = \frac{\sigma_0' h}{h_0} \left( 1 - \frac{\sigma_{xb}}{\sigma_{01}'} \right) e^{\mu (H_1 - H)}$$
 (17-19)

Neutral point to roll exit:

# THEORIES OF COLD ROLLING

$$p_{r} = \frac{\sigma_{0}' h}{h_{f}} \left( 1 - \frac{\sigma_{xf}}{\sigma_{02}'} \right) e^{\mu H}$$
 (17-20)

where

$$H = 2\left(\frac{R'}{h_f}\right)^{1/2} \tan^{-1} \left[ \left(\frac{R'}{h_f}\right)^{1/2} \theta \right]$$

and  $\sigma_{xb}$  = back tension  $\sigma_{xf}$  = front tension

Subscript 1 refers to a quantity evaluated at the roll-entrance plane, and subscript 2 refers to a quantity evaluated at the roll-exit plane.

#### THEORIES OF HOT ROLLING

 Ford and Alexander, slip line field analysis of hot rolling in non - ferrous alloys and steels

$$P = kbL_p \left( \frac{\pi}{2} + \frac{L_p}{h_0 + h_f} \right)$$

 $M_T = kbL_p^2 \left( 1.60 + 0.91 \frac{L_p}{h_0 + h_f} \right)$ 

2. Denton and Crane, hot forging of a slab between perfectly rough platens analogy

Hot-rolling:

$$P = kbL_p \left[ 1.31 + 0.53 \frac{L_p}{\left(h_0 h_f\right)^{1/2}} \right]$$

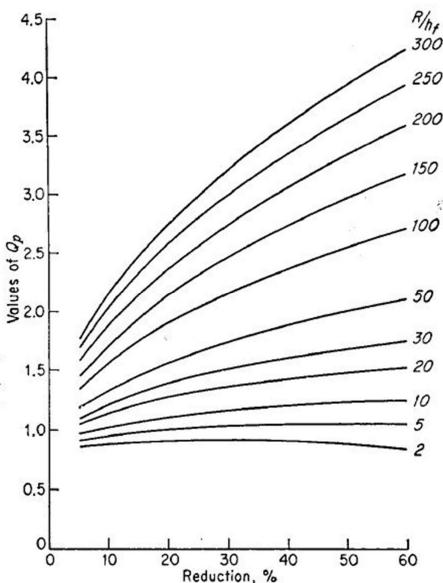
Hot-forging:

$$P = kbw \left[ 1.5 + 0.5 \frac{b}{h} \right]$$

3. Sims relation (shortened form of Orowan's equation and further mathematical simplification)

$$P = \sigma_0' b \left[ R \left( h_0 - h_f \right)^{1/2} \right] Q_p$$

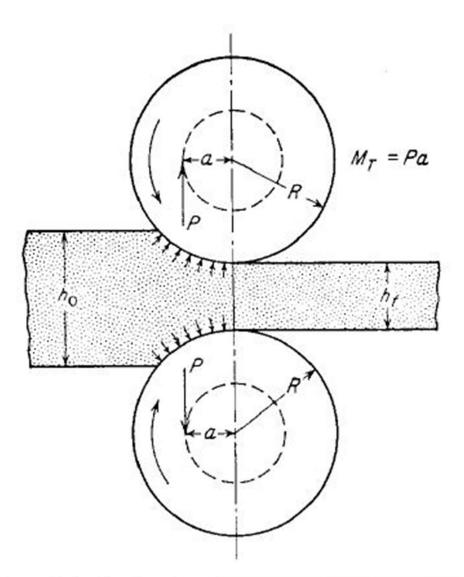
$$Q_{p} = \sqrt{\frac{h_{0}}{4\Delta h}} \left[ \pi \tan^{-1} \sqrt{\frac{\Delta h}{h_{f}}} - \sqrt{\frac{R}{h_{f}}} \ln \frac{h_{n}^{2}}{h_{0}h_{f}} \right] - \frac{\pi}{4}$$



# TORQUE AND POWER

#### Power Expenditure:

- 1. Energy needed to deform the metal
- 2. Energy needed to overcome frictional forces in bearings
- 3. Energy lost in pinion and power transmission system
- 4. Electrical losses in motors and generators



Calculating moment arm, a from the ratio of moment arm length to projected length of arc of contact

$$\lambda = \frac{a}{L_p} = \frac{a}{\left[R(h_0 - h_f)\right]^{1/2}}$$

 $\lambda$  is 0.5 for hot-rolling and 0.45 for cold-rolling

Torque = Total rolling load \* effective moment arm; where total rolling load is 2P for 2 rolls

$$M_{I} = 2Pa$$

The rolling load acts on the circle whose circumference is given by 2.pi.a; hence, work is given by the product of load with the distance travelled

Work = 
$$2(2\pi a)P$$

 $W = 4\pi a P N$ 

Power is the rate of doing work.

# Question 2 - Roll Torque

A 300 mm-wide aluminum alloy strip is hot-rolled in thickness from 20 to 15 mm. The rolls are 1 m in diameter and operate at 100 rpm. The uniaxial flow stress for the aluminum alloy can be expressed as  $140\epsilon^0.2$  (MPa). Determine the rolling load and the power required for this hot reduction.

## Solution

Question 2

Given: dluminium alloy, hot rolling 
$$b = 300 \text{ mm}$$
 $h_0 = 20 \text{ mm}$ 
 $h_1 = 15 \text{ mm}$ 
 $D = 1 \text{ m}$ ,  $R = 0.5 \text{ m} = 500 \text{ mm}$ 
 $N = 100 \text{ rpm}$ 
 $N = 140 \epsilon^{0.2} \text{ MPa}$ 

$$\mathcal{E}_{4} = \ln\left(\frac{h_{0}}{h_{4}}\right) = \ln\left(\frac{20}{15}\right) = 0.288$$

$$\vec{Y} = \frac{k\epsilon^{n}}{n+1} = \frac{140(0.288)}{0.2+1} = 90.95 \text{ MPa}$$

$$L_{p} = \sqrt{R}\Delta h = \sqrt{500(5)} = 50 \text{ mm}$$

For aluminium (non-ferrous) alloy,

use Ford and Alexander relation

$$k = \frac{7}{\sqrt{3}} = 52.51 \text{ MPa.}$$

$$P = 52.51 \times 300 \times 50 \left[ \frac{17}{2} + \frac{50}{20 + 15} \right]$$

= 2362452 N

similarly

= 
$$52.51 \times 300 \times (50) \left[ 1.60 + 0.91 \left( \frac{50}{20 + 15} \right) \right]$$

= 114 209 250 N-m

= 114.21 MN-m

For hot-rolling,  $\lambda = 0.5$ a = 7 Lp = 0.5(50) = 25 mm Power, W = 4 TTaPN =  $4\pi (25 \times 10^3) (2.36 \times 10^6) 100$ 60 = 1235693 W = 1.24 MW.

