```
In [ ]: # Essentials
        import numpy as np
        import pandas as pd
        # Plots
        import seaborn as sns
        import matplotlib.pyplot as plt
        # Models Regression
        import lightqbm as lqb
        # Models Classification
        from xgboost import XGBClassifier
        from sklearn.ensemble import RandomForestClassifier
        # Misc
        import math
        import shap
        from sklearn.preprocessing import PowerTransformer
        from sklearn.preprocessing import StandardScaler
        from sklearn.preprocessing import MinMaxScaler
        from sklearn import metrics
        from hyperopt import fmin, hp, tpe, Trials, space eval, STATUS OK
        from hyperopt.pyll import scope
        from sklearn.pipeline import Pipeline
        from sklearn.cluster import KMeans
        from sklearn.metrics import silhouette score
        # Feature Selection
        from sklearn.feature selection import VarianceThreshold
        from sklearn.base import BaseEstimator, TransformerMixin
        import warnings
        warnings.filterwarnings("ignore")
```

Utils

```
# ### Matriz de confusão com (tn,fp,fn,tp)
crosstab = metrics.confusion_matrix(yTrue, pred)

if len(pred) < 4:
    tn, fp, fn, tp = 0, 0, 0, 0

else:
    tn, fp, fn, tp = crosstab.ravel()

# Compute profit
profit = (tp*90 - fp*10)

# Compute profit per customer
profitCustomer = profit/len(pred)

if doubleAnalysis:
    return profitCustomer, profit

return profitCustomer</pre>
```

```
In [3]: def thresholdsCurve(y true = None, y proba = None):
              Calculate the best threshold to maximize profit
              Args:
                y true (np.array):
                y proba (np.array):
          1.1.1
          thresholds = np.arange(0.0, 1.0, 0.01)
          threshold_gain_max = 0.0
          gain score eval = list()
          gain score max = 0.0
          gain tp = 90
          gain fp = -10
          for threshold in thresholds:
            y pred = np.array(list(map(lambda proba: 1 if proba >= threshold else 0,
            tn, fp, fn, tp = metrics.confusion matrix(y true, y pred).ravel()
            total clientes = int(tp + tn + fp + fn)
            gain = round((tp * gain_tp + fp * gain_fp) / total_clientes, 2)
            gain score eval.append(gain)
            if gain >= gain score max and threshold >= threshold gain max:
              gain score max = gain
              threshold gain max = threshold
          plt.figure(figsize= (5, 5))
          sns.lineplot(x = thresholds, y = gain score eval, color= "red")
          plt.text(x = 0.45,
                   y = gain score max*1.1,
                   s = f"THRESHOLD: {threshold gain max:.2f},\nLucro Per. Cliente (F
```

```
bbox = {'facecolor': 'gray', 'alpha': 0.4, 'pad': 6}
)

plt.title("Curva Lucro Per. Cliente(R$) x THRESHOLD")
plt.legend(["Classe 1 - Insatisfeito"])
plt.ylim(0, gain_score_max*1.35)
plt.ylabel("Lucro Per. Cliente(R$)")
plt.xlabel("Thresholds")
plt.show()
```

Carregamento dos Dados

```
In [4]: dfTrain = pd.read_csv('train_features.csv')
yTrain = dfTrain.TARGET
dfTrain = dfTrain.drop(labels=['TARGET'], axis=1)

dfVal = pd.read_csv('val_features.csv')
yVal = dfVal.TARGET
dfVal = dfVal.drop(labels=['TARGET'], axis=1)

dfTest = pd.read_csv('test_features.csv')
```

Solução

1.0 - Classificação (Case A)

1.1 - Preparação do Dataset

1.2 - Ponto de Partida

Como base line vamos treinar uma simples árvore de decisão sem fazer nenhuma seleção de atribuitos ou tunning de hyperparametros.

```
In [11]: # Model base
    clRF = RandomForestClassifier(n_jobs = -1, class_weight='balanced')
    clRF.fit(dfTrainCLF, yTrain)
    preds = clRF.predict(dfValCLF)
    rfPerCustomer, rfProfit = scoringProfit(yVal, preds, True)

# Lucro caso a campanha impacte todos os clientes
    allCustomerProfitPerCustomer, allCustomerProfit = scoringProfit(yVal, [1 for

# Verificação do score máximo possível no treino
    maxProfitPerCustomer, maxProfit = (scoringProfit(yVal, yVal, True))

print(f"Lucro no modelo base R${rfProfit:,.2f}")
    print(f"Lucro por cliente no modelo base R$ {rfPerCustomer:,.2f}\n")

print(f"Lucro caso a capanha seja aplicada a todos os clientes R$ {allCustom print(f"Lucro por cliente caso a capanha seja aplicada a todos os clientes F

print(f"Lucro caso a capanha seja aplicada apenas aos clientes insatisfeitos print(f"Lucro por cliente caso a capanha seja aplicada apenas aos clientes i
```

Lucro no modelo base R\$1,040.00 Lucro por cliente no modelo base R\$ 0.07

Lucro caso a capanha seja aplicada a todos os clientes R\$ -88,300.00 Lucro por cliente caso a capanha seja aplicada a todos os clientes R\$ -6.22

Lucro caso a capanha seja aplicada apenas aos clientes insatisfeitos R\$ 48,2 40.00

Lucro por cliente caso a capanha seja aplicada apenas aos clientes insatisfe itos R\$ 3.40

1.3 - Busca dos Melhores Parâmetros

1.3.0 - LGBM

```
yPred = classifier.predict(dfValCLF)
             score = scoringProfit(yVal, yPred)
             return {
                 'loss': -score,
                 'status': STATUS OK,
             }
In [11]: spaceLGBM = {
             'n estimators': scope.int(hp.uniform('n estimators', 50, 5000)),
             'colsample bytree': hp.uniform('colsample bytree', 0.01, 1.0),
             'learning rate': hp.choice('learning rate', np.arange(0.05, 0.35, 0.02))
             'max depth': scope.int(hp.quniform('max depth', 3, 20, 1)),
             'min child weight': scope.int(hp.quniform('min child weight', 3, 20, 1))
             'subsample': hp.uniform('subsample', 0.01, 1.0),
             'reg lambda': hp.lognormal('reg lambda', 0.0, 1.0),
             'reg alpha': hp.lognormal('reg alpha', 0.0, 1.0),
In [12]: trials = Trials ()
         bestParamsLGBM = fmin(
             fn=objective,
             space=spaceLGBM,
             algo=tpe.suggest,
             trials=trials,
             max evals=1000
        100% | 1000/1000 [1:40:31<00:00, 6.03s/trial, best loss: -0.8421423537702
        6071
In [13]: print(bestParamsLGBM)
        {'colsample bytree': 0.33833779547527354, 'learning rate': 5, 'max depth': 1
        6.0, 'min child weight': 6.0, 'n estimators': 2482.3448603876004, 'reg alph
        a': 7.20937108380558, 'req lambda': 1.985448182110237, 'subsample': 0.075906
        31124333537}
         1.3.1 - XGBoost
In [14]: def objective(params):
             classifier = XGBClassifier(n_jobs = -1, objective='binary:logistic', ran
             model = Pipeline(
                             ('classifier', classifier)
             model.fit(dfTrainCLF, yTrain)
```

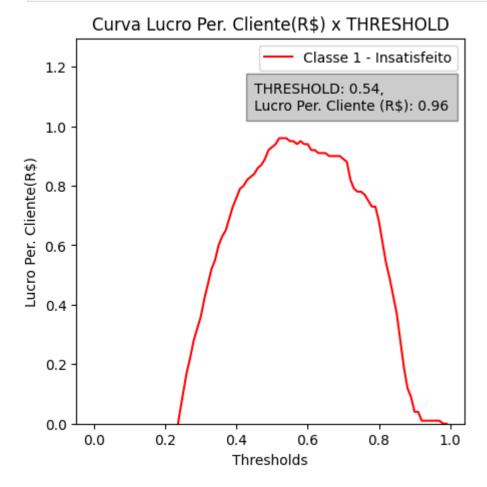
vPred = classifier.predict(dfValCLF)

```
score = scoringProfit(yVal, yPred)
             return {
                 'loss': -score,
                 'status': STATUS OK,
                 'booster': model.named steps['classifier'].get booster().attributes(
             }
In [15]: spaceXGB = {
             'n estimators': scope.int(hp.uniform('n estimators', 50, 5000)),
             'colsample bytree': hp.uniform('colsample bytree', 0.01, 1.0),
             'learning rate': hp.choice('learning rate', np.arange(0.05, 0.35, 0.02))
             'max depth': scope.int(hp.guniform('max depth', 3, 20, 1)),
             'scale pos weight': scope.int(hp.quniform('scale pos weight', 20, 30, 1)
             'min child weight': scope.int(hp.quniform('min child weight', 3, 20, 1))
             'subsample': hp.uniform('subsample', 0.01, 1.0),
             'reg lambda': hp.lognormal('reg lambda', 0.0, 1.0),
             'reg alpha': hp.lognormal('reg alpha', 0.0, 1.0)
In [16]: trials = Trials ()
         bestParamsXGB = fmin(
             fn=objective,
             space=spaceXGB,
             algo=tpe.suggest,
             trials=trials,
             max evals=1000
        100%| | 1000/1000 [54:26<00:00, 3.27s/trial, best loss: -0.9344608879492
        601]
In [17]: print(bestParamsXGB)
        {'colsample bytree': 0.3126403997344753, 'learning rate': 0, 'max depth': 9.
        0, 'min child weight': 4.0, 'n estimators': 469.3250670352471, 'reg alpha':
        0.6860970446487238, 'reg lambda': 3.6398478765329894, 'scale pos weight': 2
        0.0, 'subsample': 0.9817877351312972}
In [18]: print(trials.best_trial['result'])
        {'loss': -0.9344608879492601, 'status': 'ok', 'booster': {}}
         1.4 - Avaliar Melhor Modelo
         1.4.0 - XGBoost
In [19]: bestParamsXGB['learning_rate'] = np.arange(0.05, 0.35, 0.02)[0]
         bestParamsXGB['n estimators'] = int(bestParamsXGB['n estimators'])
         bestParamsXGB['max depth'] = int(bestParamsXGB['max depth'])
```

In [86]: classifierXGB = XGBClassifier(n jobs = -1, objective='binary:logistic', rand

classifierXGB.fit(dfTrainCLF, yTrain)

```
In [40]: yPred_prob = classifierXGB.predict_proba(dfValCLF)
In [41]: thresholdsCurve(yVal, yPred_prob)
```



1.4.1 - LGBM

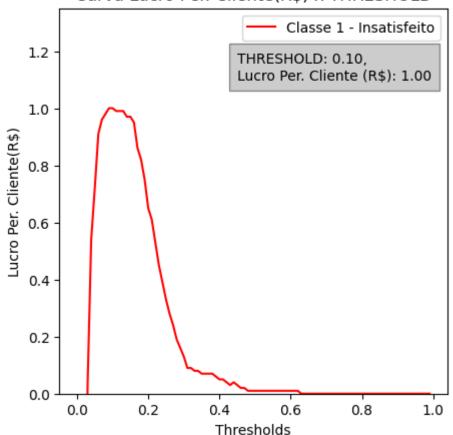
```
In [95]: bestParamsLGBM['learning_rate'] = np.arange(0.05, 0.35, 0.02)[5]
bestParamsLGBM['n_estimators'] = int(bestParamsLGBM['n_estimators'])
bestParamsLGBM['max_depth'] = int(bestParamsLGBM['max_depth'])
```

```
In [96]: classifierLGBM = lgb.LGBMClassifier(verbose = -1,
                                            n_{jobs} = -1,
                                            objective='binary',
                                            random state=424,
                                            **bestParamsLGBM)
In [97]: classifierLGBM.fit(dfTrainCLF, yTrain)
Out[97]:
                                      LGBMClassifier
         LGBMClassifier(colsample_bytree=0.33833779547527354,
                         learning_rate=0.15000000000000002, max_depth=16,
                        min_child_weight=6.0, n_estimators=2482, n_jobs=-1,
                        objective='binary', random_state=424, reg_alpha=7.20
         937108380558,
                        reg_lambda=1.985448182110237, subsample=0.0759063112
         4333537,
                        verbose=-1)
```

In [98]: yPred_prob = classifierLGBM.predict_proba(dfValCLF)

In [54]: thresholdsCurve(yVal, yPred_prob)

Curva Lucro Per. Cliente(R\$) x THRESHOLD



Entre os dois melhores modelos o modelo que melhor performou em relação a métrica de avaliação foi o LGBM. Importante destacar que avaliamos sem o class_weight e o resultado foi infinitamente inferior.

```
In [55]: yPred = yPred_prob[:,1] > 0.10
    profitClient, profit = scoringProfit(yVal, yPred, True)
    profitClientMax, profitMax = scoringProfit(yVal, yVal, True)

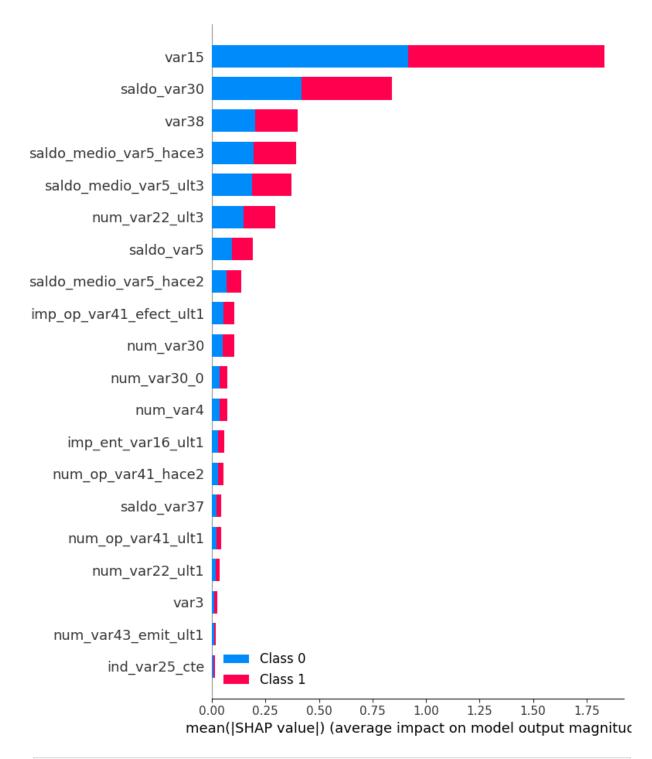
    print(f'Lucro máximo por cliente {profitClient:,.2f}')
    print(f'Lucro máximo da campanha: R$ {profit:,.2f}')
    print(f'Lucro máximo que poderia ser atingindo na campanha: R$ {profitMax:,.print(f'Lucro máximo em %: {profit/profitMax:.2%}')

    Lucro máximo por cliente 1.00
    Lucro máximo que poderia ser atingindo na campanha: R$ 48,240.00
    Lucro máximo que poderia ser atingindo na campanha: R$ 48,240.00
    Lucro máximo em %: 29.48%
```

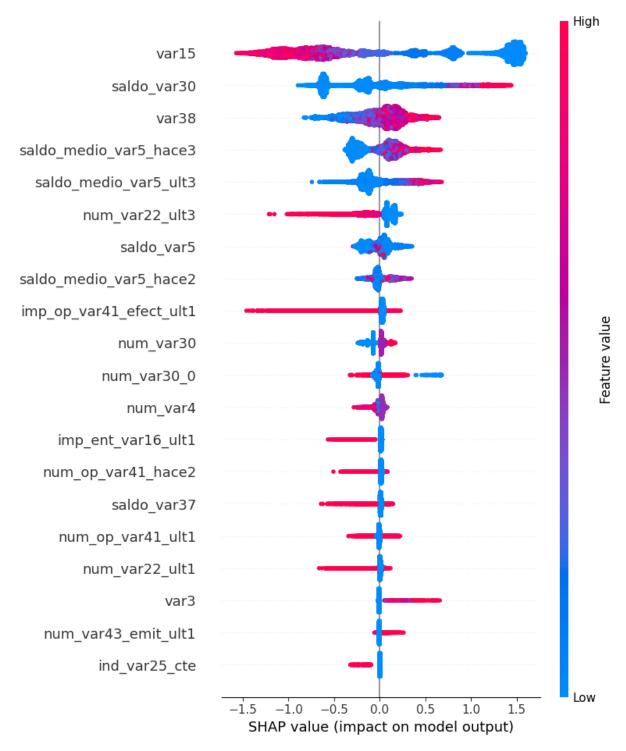
1.5 - Explicabilidade do Melhor Modelo (SHAP Values)

```
In [65]: shap.initjs()
    explainer = shap.TreeExplainer(classifierLGBM)
    shap_values = explainer.shap_values(dfValCLF)
```

In [66]: shap.summary_plot(shap_values, dfValCLF, feature_names=model.get_feature_nam



In [67]: shap.summary_plot(shap_values[0], dfValCLF, feature_names=model.get_feature_



Como podemos observar todas as variáveis são importantes para o modelo. Sendo as variáveis var15, saldo_var30, var38... as mais importantes

2.0 - Notas (Case B)

```
In [100... yPred_prob = classifierLGBM.predict_proba(dfTestCLF)
In [101... # ### Separar os clientes classificados como insatisfeitos pelo modelo
df_preds_1 = pd.DataFrame(yPred_prob_test[yPred_prob_test[:,1] > 0.10][:,1]
df_preds_0 = pd.DataFrame(yPred_prob_test[yPred_prob_test[:,1] <= 0.10][:,1]</pre>
```

```
# ### Dividir os registros classificados como satisfeitos em quartis baseado
decil_preds_0 = pd.qcut(df_preds_0[0].rank(method='first'), q = 4, labels =
pub_segmentado = np.concatenate((df_preds_1, decil_preds_0), axis=None)
segmentos, quantidade = np.unique(pub_segmentado, return_counts=True)

# ### Plot
plt.bar(segmentos, quantidade, color='red')
plt.title('Quantidade de publico por segmento');
print('A quantidade de publico no segmento 1 é menor pois trata-se do públic
```

A quantidade de publico no segmento 1 é menor pois trata-se do público categ orizado como insatisfeito pelo modelo



3.0 - Clustering (Agrupamento)

3

5

2

6000

4000

2000

1

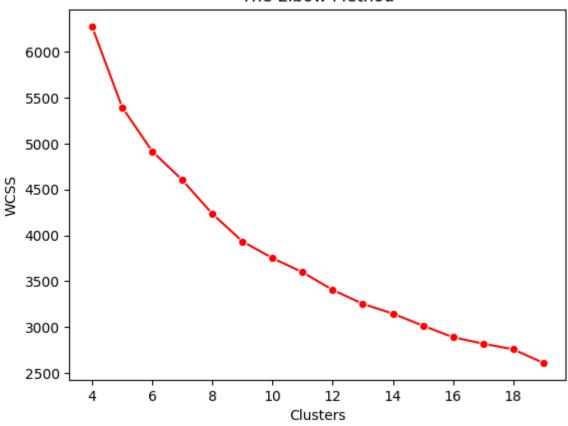
3.1 - Testar usando a normalização MinMaxScaler e todas as features

```
In [11]: # ### Scaler feature for clustering
    scaler = MinMaxScaler()
    scaler.fit(dfTrain)

# ### Apply in train and val
    xTrainScaledcaled = scaler.transform(dfTrain)
    xValScaled = scaler.transform(dfVal)
```

```
In [12]: minCluster = 4
         maxCluster = 20
         WCSS = []
         for nClusters in range(minCluster, maxCluster):
             # ### Train kmeans model
             kmeanModel = KMeans(n clusters = nClusters, random state = 424)
             kmeanModel.fit(xTrainScaledcaled)
             # ### Predict
             pred = kmeanModel.predict(xTrainScaledcaled)
             # ### Compute WCSS (Elbow)
             wcss.append(kmeanModel.inertia)
             # ### Compute silhouette score
             score = silhouette score(xTrainScaledcaled, pred)
             print(f'Silhouette Score for {nClusters} clusters: {score:.5f}')
        Silhouette Score for 4 clusters: 0.41712
        Silhouette Score for 5 clusters: 0.45717
        Silhouette Score for 6 clusters: 0.46655
        Silhouette Score for 7 clusters: 0.46847
        Silhouette Score for 8 clusters: 0.47283
        Silhouette Score for 9 clusters: 0.48264
        Silhouette Score for 10 clusters: 0.48210
        Silhouette Score for 11 clusters: 0.48380
        Silhouette Score for 12 clusters: 0.48181
        Silhouette Score for 13 clusters: 0.48411
        Silhouette Score for 14 clusters: 0.48820
        Silhouette Score for 15 clusters: 0.49153
        Silhouette Score for 16 clusters: 0.48568
        Silhouette Score for 17 clusters: 0.47026
        Silhouette Score for 18 clusters: 0.47893
        Silhouette Score for 19 clusters: 0.47660
In [13]: mycenters = pd.DataFrame({'Clusters' : range(minCluster, maxCluster), 'WCSS'
         sns.lineplot(x = 'Clusters', y = 'WCSS', data = mycenters, marker="o", color
         plt.title('The Elbow Method')
         plt.show()
```

The Elbow Method



```
In [14]:

def optimalNumberClusters(wcss):
    x1, y1 = 4, wcss[0]
    x2, y2 = 20, wcss[len(wcss)-1]

distances = []
    for i in range(len(wcss)):
        x0 = i+4
        y0 = wcss[i]
        numerator = abs((y2-y1)*x0 - (x2-x1)*y0 + x2*y1 - y2*x1)
        denominator = math.sqrt((y2 - y1)**2 + (x2 - x1)**2)
        distances.append(numerator/denominator)

return distances.index(max(distances)) + 4

print(f'Melhor número de clusters de acordo com o método Elbow: {optimalNumb}
```

Melhor número de clusters de acordo com o método Elbow: 9

3.1.0 - Com base no Elbow

```
In [23]: #### Avaliar com base no método Elbow
best_k = 9

model = KMeans(n_clusters = best_k, random_state = 424)
model.fit(xTrainScaledcaled)

cluster = model.predict(xValScaled)
```

```
df cluster = pd.DataFrame({'cluster': cluster}).join(yVal)
 df cluster.columns = ['labels','true target']
 data = pd.crosstab(df cluster['labels'],df cluster['true target'])
 data ['Ganho'] = data [1]*90
 data ['Perda'] = data[0]*10
 data ['Lucro'] = data [1]*90 - data[0]*10
 print('top 3 clusters para o kmeans')
 print(data.sort values(by='Lucro', ascending=False).head(3))
top 3 clusters para o kmeans
true target 0 1 Ganho Perda Lucro
labels
5
                             1290 -930
            129 4
                       360
3
            359 28
                             3590 -1070
                      2520
            190 0
                        0
                             1900 - 1900
```

3.1.1 - Com base na Silhueta Score

```
In [21]: best k = 15
         model = KMeans(n clusters = best k, random state = 424)
         model.fit(xTrainScaledcaled)
         cluster = model.predict(xValScaled)
         df cluster = pd.DataFrame({'cluster': cluster}).join(yVal)
         df cluster.columns = ['labels','true target']
         data = pd.crosstab(df cluster['labels'],df cluster['true target'])
         data ['Ganho'] = data [1]*90
         data ['Perda'] = data[0]*10
         data ['Lucro'] = data [1]*90 - data[0]*10
         print('top 3 clusters para o kmeans')
         print(data.sort values(by='Lucro', ascending=False).head(3))
        top 3 clusters para o kmeans
        true target 0 1 Ganho Perda Lucro
        labels
                    705 143 12870 7050
                                             5820
        0
        14
                     72
                          7
                                630
                                      720
                                              - 90
                           2
                      36
                                180
                                       360
                                             -180
```

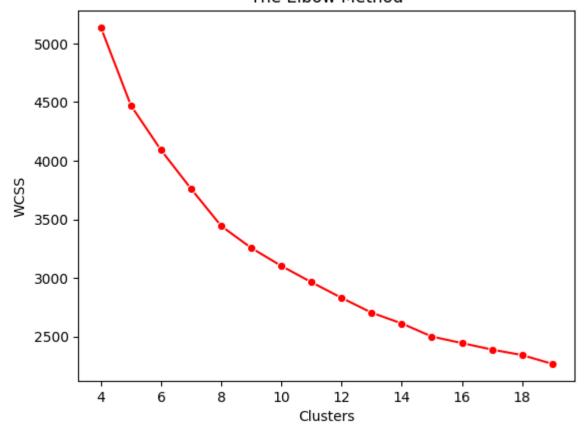
3.2 - Testar usando a normalização MinMaxScaler e removendo as variáveis binárias

```
In [29]: dfTrain.nunique()
```

```
195
Out[29]: var3
         var15
                                       81
         imp ent var16 ult1
                                      513
                                      289
         imp op var41 efect ult1
         ind var1 0
                                       2
         ind var25 cte
                                        7
         num var4
         num op var41 hace2
                                       48
                                       58
         num op var41 ult1
         num var30 0
                                       11
         num var30
                                       5
         num var37 med ult2
                                       15
         saldo var5
                                     9592
         saldo var30
                                    13848
         saldo var37
                                     3301
         imp aport var13 hace3
                                      187
         num var22 ult1
                                       15
                                       29
         num var22 ult3
                                        4
         num meses var8 ult3
         num var43 emit ult1
                                       10
         saldo medio var5 hace2
                                    12021
         saldo medio var5 hace3
                                    5801
         saldo medio var5 ult3
                                    14479
         saldo medio var8 hace3
                                      304
                                    46609
         var38
         dtype: int64
In [57]: dfTrainDrop = dfTrain.drop(labels=['ind_var1_0', 'ind_var25_cte'] , axis=1,
         dfValDrop = dfVal.drop(labels=['ind var1 0', 'ind var25 cte'] , axis=1, inpl
In [58]: # ### Scaler feature for clustering
         scaler = MinMaxScaler()
         scaler.fit(dfTrainDrop)
         # ### Apply in train and val
         xTrainScaledcaled = scaler.transform(dfTrainDrop)
         xValScaled = scaler.transform(dfValDrop)
In [59]: minCluster = 4
         maxCluster = 20
         WCSS = []
         for nClusters in range(minCluster, maxCluster):
             # ### Train kmeans model
             kmeanModel = KMeans(n clusters = nClusters, random state = 424)
             kmeanModel.fit(xTrainScaledcaled)
             # ### Predict
             pred = kmeanModel.predict(xTrainScaledcaled)
             # ### Compute WCSS (Elbow)
             wcss.append(kmeanModel.inertia )
             # ### Compute silhouette score
```

```
score = silhouette score(xTrainScaledcaled, pred)
             print(f'Silhouette Score for {nClusters} clusters: {score:.5f}')
        Silhouette Score for 4 clusters: 0.44628
        Silhouette Score for 5 clusters: 0.46062
        Silhouette Score for 6 clusters: 0.46468
        Silhouette Score for 7 clusters: 0.47107
        Silhouette Score for 8 clusters: 0.48019
        Silhouette Score for 9 clusters: 0.48148
        Silhouette Score for 10 clusters: 0.48342
        Silhouette Score for 11 clusters: 0.47561
        Silhouette Score for 12 clusters: 0.47724
        Silhouette Score for 13 clusters: 0.47215
        Silhouette Score for 14 clusters: 0.46838
        Silhouette Score for 15 clusters: 0.46909
        Silhouette Score for 16 clusters: 0.46981
        Silhouette Score for 17 clusters: 0.46919
        Silhouette Score for 18 clusters: 0.45965
        Silhouette Score for 19 clusters: 0.47256
In [60]: mycenters = pd.DataFrame({'Clusters' : range(minCluster, maxCluster), 'WCSS'
         sns.lineplot(x = 'Clusters', y = 'WCSS', data = mycenters, marker="o", color
         plt.title('The Elbow Method')
         plt.show()
```

The Elbow Method



```
In [61]: def optimalNumberClusters(wcss):
    x1, y1 = 4, wcss[0]
    x2, y2 = 20, wcss[len(wcss)-1]
```

```
distances = []
for i in range(len(wcss)):
    x0 = i+4
    y0 = wcss[i]
    numerator = abs((y2-y1)*x0 - (x2-x1)*y0 + x2*y1 - y2*x1)
    denominator = math.sqrt((y2 - y1)**2 + (x2 - x1)**2)
    distances.append(numerator/denominator)

return distances.index(max(distances)) + 4

print(f'Melhor número de clusters de acordo com o método Elbow: {optimalNumb}
```

Melhor número de clusters de acordo com o método Elbow: 9

3.2.0 - Com base no Elbow

```
In [62]: best k = 9
         model = KMeans(n clusters = best k, random state = 424)
         model.fit(xTrainScaledcaled)
         cluster = model.predict(xValScaled)
         df cluster = pd.DataFrame({'cluster': cluster}).join(yVal)
         df cluster.columns = ['labels','true target']
         data = pd.crosstab(df cluster['labels'],df cluster['true target'])
         data ['Ganho'] = data [1]*90
         data ['Perda'] = data[0]*10
         data ['Lucro'] = data [1]*90 - data[0]*10
         print('top 3 clusters para o kmeans')
         print(data.sort_values(by='Lucro', ascending=False).head(3))
        top 3 clusters para o kmeans
        true target 0 1 Ganho Perda Lucro
        labels
        1
                    764 153 13770 7640 6130
                    266 25 2250 2660 -410
       6
                    196
                        0 0
                                     1960 - 1960
```

3.2.1 - Com base na Silhueta Score

```
In [63]: best_k = 10

model = KMeans(n_clusters = best_k, random_state = 424)
model.fit(xTrainScaledcaled)

cluster = model.predict(xValScaled)

df_cluster = pd.DataFrame({'cluster': cluster}).join(yVal)
df_cluster.columns = ['labels','true_target']

data = pd.crosstab(df_cluster['labels'],df_cluster['true_target'])
```

```
data ['Ganho'] = data [1]*90
data ['Perda'] = data[0]*10
data ['Lucro'] = data [1]*90 - data[0]*10
print('top 3 clusters para o kmeans')
print(data.sort_values(by='Lucro', ascending=False).head(3))

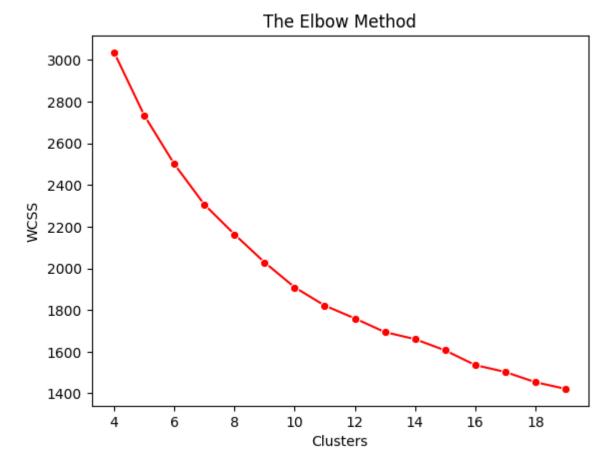
top 3 clusters para o kmeans
true_target 0 1 Ganho Perda Lucro
labels
9 765 152 13680 7650 6030
7 268 25 2250 2680 -430
8 48 0 0 480 -480
```

3.3 - Testar usando a normalização MinMaxScaler e removendo as variáveis com menos de 10 valores distitos

```
In [31]: dfTrainDrop = dfTrain.drop(labels=['ind_var1_0', 'ind_var25_cte', 'num_var4']
         dfValDrop = dfVal.drop(labels=['ind var1 0', 'ind var25 cte', 'num var4', 'r
In [35]: # ### Scaler feature for clustering
         scaler = MinMaxScaler()
         scaler.fit(dfTrainDrop)
         # ### Apply in train and val
         xTrainScaledcaled = scaler.transform(dfTrainDrop)
         xValScaled = scaler.transform(dfValDrop)
In [36]: minCluster = 4
         maxCluster = 20
         wcss = []
         for nClusters in range(minCluster, maxCluster):
             # ### Train kmeans model
             kmeanModel = KMeans(n clusters = nClusters, random state = 424)
             kmeanModel.fit(xTrainScaledcaled)
             # ### Predict
             pred = kmeanModel.predict(xTrainScaledcaled)
             # ### Compute WCSS (Elbow)
             wcss.append(kmeanModel.inertia)
             # ### Compute silhouette score
             score = silhouette_score(xTrainScaledcaled, pred)
             print(f'Silhouette Score for {nClusters} clusters: {score:.5f}')
```

```
Silhouette Score for 4 clusters: 0.51940
Silhouette Score for 5 clusters: 0.51334
Silhouette Score for 6 clusters: 0.52355
Silhouette Score for 7 clusters: 0.45830
Silhouette Score for 8 clusters: 0.45901
Silhouette Score for 9 clusters: 0.46099
Silhouette Score for 10 clusters: 0.47009
Silhouette Score for 11 clusters: 0.47650
Silhouette Score for 12 clusters: 0.42342
Silhouette Score for 13 clusters: 0.47931
Silhouette Score for 14 clusters: 0.42142
Silhouette Score for 15 clusters: 0.34102
Silhouette Score for 16 clusters: 0.42897
Silhouette Score for 17 clusters: 0.41503
Silhouette Score for 18 clusters: 0.41653
Silhouette Score for 19 clusters: 0.41708
```

```
In [37]: mycenters = pd.DataFrame({'Clusters' : range(minCluster, maxCluster), 'WCSS'
    sns.lineplot(x = 'Clusters', y = 'WCSS', data = mycenters, marker="o", color
    plt.title('The Elbow Method')
    plt.show()
```



```
In [38]:
    def optimalNumberClusters(wcss):
        x1, y1 = 4, wcss[0]
        x2, y2 = 20, wcss[len(wcss)-1]

    distances = []
    for i in range(len(wcss)):
```

```
x0 = i+4
y0 = wcss[i]
numerator = abs((y2-y1)*x0 - (x2-x1)*y0 + x2*y1 - y2*x1)
denominator = math.sqrt((y2 - y1)**2 + (x2 - x1)**2)
distances.append(numerator/denominator)

return distances.index(max(distances)) + 4

print(f'Melhor número de clusters de acordo com o método Elbow: {optimalNumb}
```

Melhor número de clusters de acordo com o método Elbow: 10

3.3.0 - Com base no Elbow

```
In [39]: best k = 10
         model = KMeans(n clusters = best k, random state = 424)
         model.fit(xTrainScaledcaled)
         cluster = model.predict(xValScaled)
         df cluster = pd.DataFrame({'cluster': cluster}).join(yVal)
         df cluster.columns = ['labels','true target']
         data = pd.crosstab(df cluster['labels'],df cluster['true target'])
         data ['Ganho'] = data [1]*90
         data ['Perda'] = data[0]*10
         data ['Lucro'] = data [1]*90 - data[0]*10
         print('top 3 clusters para o kmeans')
         print(data.sort values(by='Lucro', ascending=False).head(3))
       top 3 clusters para o kmeans
       true target 0 1 Ganho Perda Lucro
       labels
                   47 0 0 470 -470
       9
                    191 11
                              990 1910 -920
       8
                    112 1 90 1120 -1030
       3
```

3.3.1 - Com base na Silhueta Score

```
In [40]: best_k = 6

model = KMeans(n_clusters = best_k, random_state = 424)
model.fit(xTrainScaledcaled)

cluster = model.predict(xValScaled)

df_cluster = pd.DataFrame({'cluster': cluster}).join(yVal)
df_cluster.columns = ['labels', 'true_target']

data = pd.crosstab(df_cluster['labels'],df_cluster['true_target'])

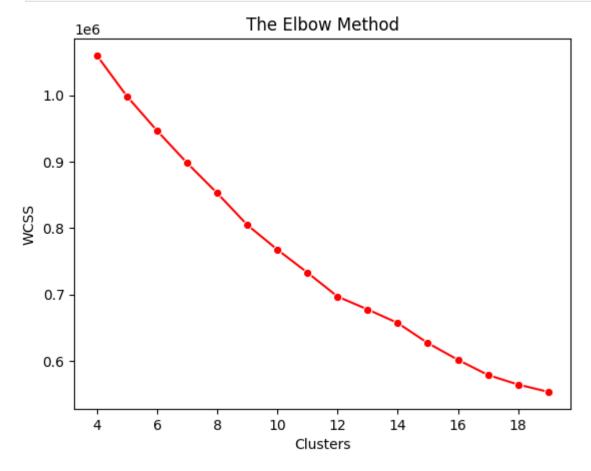
data ['Ganho'] = data [1]*90
data ['Perda'] = data[0]*10
```

3.4 - Testar usando a normalização StandardScaler e todas as features

```
In [41]: # ### Scaler feature for clustering
         scaler = StandardScaler()
         scaler.fit(dfTrain)
         # ### Apply in train and val
         xTrainScaledcaled = scaler.transform(dfTrain)
         xValScaled = scaler.transform(dfVal)
In [44]: minCluster = 4
         maxCluster = 20
         wcss = []
         for nClusters in range(minCluster, maxCluster):
             # ### Train Kmeans
             kmeanModel = KMeans(n clusters = nClusters, random state = 424)
             kmeanModel.fit(xTrainScaledcaled)
             # ### Predict
             pred = kmeanModel.predict(xTrainScaledcaled)
             # ### Compute WCSS (Elbow)
             wcss.append(kmeanModel.inertia )
             # ### Compute silhouette score
             score = silhouette score(xTrainScaledcaled, pred)
             print(f'Silhouette Score for {nClusters} clusters: {score:.5f}')
```

```
Silhouette Score for 4 clusters: 0.56280
Silhouette Score for 5 clusters: 0.44995
Silhouette Score for 6 clusters: 0.29691
Silhouette Score for 7 clusters: 0.30027
Silhouette Score for 8 clusters: 0.31074
Silhouette Score for 9 clusters: 0.31307
Silhouette Score for 10 clusters: 0.31758
Silhouette Score for 11 clusters: 0.32416
Silhouette Score for 12 clusters: 0.33168
Silhouette Score for 13 clusters: 0.33153
Silhouette Score for 14 clusters: 0.33531
Silhouette Score for 15 clusters: 0.34208
Silhouette Score for 16 clusters: 0.34364
Silhouette Score for 17 clusters: 0.35333
Silhouette Score for 18 clusters: 0.36269
Silhouette Score for 19 clusters: 0.35715
```

```
In [45]: mycenters = pd.DataFrame({'Clusters' : range(minCluster, maxCluster), 'WCSS'
    sns.lineplot(x = 'Clusters', y = 'WCSS', data = mycenters, marker="o", color
    plt.title('The Elbow Method')
    plt.show()
```



```
In [46]:
    def optimalNumberClusters(wcss):
        x1, y1 = 4, wcss[0]
        x2, y2 = 20, wcss[len(wcss)-1]

    distances = []
    for i in range(len(wcss)):
```

```
x0 = i+4
y0 = wcss[i]
numerator = abs((y2-y1)*x0 - (x2-x1)*y0 + x2*y1 - y2*x1)
denominator = math.sqrt((y2 - y1)**2 + (x2 - x1)**2)
distances.append(numerator/denominator)

return distances.index(max(distances)) + 4

print(f'Melhor número de clusters de acordo com o método Elbow: {optimalNumb}
```

Melhor número de clusters de acordo com o método Elbow: 12

3.4.0 - Com base no Elbow

```
In [47]: best k = 12
          model = KMeans(n clusters = best k, random state = 424)
          model.fit(xTrainScaledcaled)
          cluster = model.predict(xValScaled)
          df cluster = pd.DataFrame({'cluster': cluster}).join(yVal)
          df cluster.columns = ['labels','true target']
          data = pd.crosstab(df cluster['labels'],df cluster['true target'])
          data ['Ganho'] = data [1]*90
          data ['Perda'] = data[0]*10
          data ['Lucro'] = data [1]*90 - data[0]*10
          print('top 3 clusters para o kmeans')
          print(data.sort values(by='Lucro', ascending=False).head(3))
         top 3 clusters para o kmeans
         true target 0 1 Ganho Perda Lucro
         labels

    14
    1
    90
    140
    -50

    29
    0
    0
    290
    -290

    300
    300

         9
         3
                       39 1 90
                                         390 -300
         8
```

3.4.1 - Com base na Silhueta Score

```
In [48]: best_k = 4

model = KMeans(n_clusters = best_k, random_state = 424)
model.fit(xTrainScaledcaled)

cluster = model.predict(xValScaled)

df_cluster = pd.DataFrame({'cluster': cluster}).join(yVal)
df_cluster.columns = ['labels', 'true_target']

data = pd.crosstab(df_cluster['labels'],df_cluster['true_target'])

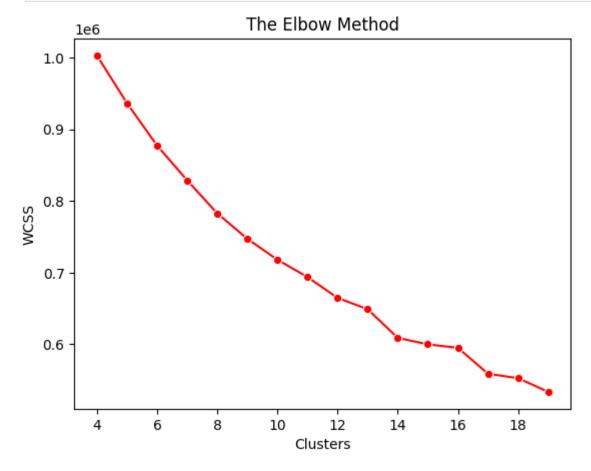
data ['Ganho'] = data [1]*90
data ['Perda'] = data[0]*10
```

3.5 - Testar usando a normalização yeojohnson e todas as features

```
In [49]: # ### Scaler feature for clustering
         scaler = PowerTransformer(method='yeo-johnson')
         scaler.fit(dfTrain)
         # ### Apply in train and val
         xTrainScaledcaled = scaler.transform(dfTrain)
         xValScaled = scaler.transform(dfVal)
In [50]: minCluster = 4
         maxCluster = 20
         wcss = []
         for nClusters in range(minCluster, maxCluster):
             # ### Train kmeans model
             kmeanModel = KMeans(n clusters = nClusters, random state = 424)
             kmeanModel.fit(xTrainScaledcaled)
             # ### Predict
             pred = kmeanModel.predict(xTrainScaledcaled)
             # ### Compute WCSS (Elbow)
             wcss.append(kmeanModel.inertia )
             # ### Compute silhouette score
             score = silhouette score(xTrainScaledcaled, pred)
             print(f'Silhouette Score for {nClusters} clusters: {score:.5f}')
```

```
Silhouette Score for 4 clusters: 0.39075
Silhouette Score for 5 clusters: 0.21144
Silhouette Score for 6 clusters: 0.22606
Silhouette Score for 7 clusters: 0.24022
Silhouette Score for 8 clusters: 0.24570
Silhouette Score for 9 clusters: 0.26244
Silhouette Score for 10 clusters: 0.25647
Silhouette Score for 11 clusters: 0.24959
Silhouette Score for 12 clusters: 0.27540
Silhouette Score for 13 clusters: 0.25305
Silhouette Score for 14 clusters: 0.28694
Silhouette Score for 15 clusters: 0.20484
Silhouette Score for 16 clusters: 0.26093
Silhouette Score for 17 clusters: 0.26627
Silhouette Score for 18 clusters: 0.21308
Silhouette Score for 19 clusters: 0.26636
```

```
In [51]: mycenters = pd.DataFrame({'Clusters' : range(minCluster, maxCluster), 'WCSS'
    sns.lineplot(x = 'Clusters', y = 'WCSS', data = mycenters, marker="o", color
    plt.title('The Elbow Method')
    plt.show()
```



```
In [52]: def optimalNumberClusters(wcss):
    x1, y1 = 4, wcss[0]
    x2, y2 = 20, wcss[len(wcss)-1]

    distances = []
    for i in range(len(wcss)):
```

```
x0 = i+4
       y0 = wcss[i]
        numerator = abs((y2-y1)*x0 - (x2-x1)*y0 + x2*y1 - y2*x1)
        denominator = math.sqrt((y2 - y1)**2 + (x2 - x1)**2)
        distances.append(numerator/denominator)
    return distances.index(max(distances)) + 4
print(f'Melhor número de clusters de acordo com o método Elbow: {optimalNumb
```

Melhor número de clusters de acordo com o método Elbow: 9

3.5.0 - Com base no Elbow

```
In [53]: best k = 9
         model = KMeans(n clusters = best k, random state = 424)
         model.fit(xTrainScaledcaled)
         cluster = model.predict(xValScaled)
         df cluster = pd.DataFrame({'cluster': cluster}).join(yVal)
         df cluster.columns = ['labels','true target']
         data = pd.crosstab(df cluster['labels'],df cluster['true target'])
         data ['Ganho'] = data [1]*90
         data ['Perda'] = data[0]*10
         data ['Lucro'] = data [1]*90 - data[0]*10
         print('top 3 clusters para o kmeans')
         print(data.sort values(by='Lucro', ascending=False).head(3))
       top 3 clusters para o kmeans
       true target 0 1 Ganho Perda Lucro
       labels
                   93 7 630 930 -300
       3
                    276 25 2250
       6
                                    2760 -510
                    357 2 180 3570 -3390
       5
```

3.5.1 - Com base na Silhueta Score

```
In [54]: best k = 4
         model = KMeans(n clusters = best k, random state = 424)
         model.fit(xTrainScaledcaled)
         cluster = model.predict(xValScaled)
         df cluster = pd.DataFrame({'cluster': cluster}).join(yVal)
         df_cluster.columns = ['labels','true_target']
         data = pd.crosstab(df cluster['labels'],df cluster['true target'])
         data ['Ganho'] = data [1]*90
         data ['Perda'] = data[0]*10
```

```
data ['Lucro'] = data [1]*90 - data[0]*10
print('top 3 clusters para o kmeans')
print(data.sort_values(by='Lucro', ascending=False).head(3))
```

```
top 3 clusters para o kmeans
true target
                0
                     1
                       Ganho
                               Perda Lucro
labels
1
              355
                    31
                         2790
                                3550
                                        -760
0
             1430
                    10
                          900
                               14300 - 13400
3
                               22580 -16190
             2258
                    71
                         6390
```

O melhor resultado encontrado foi usando a normalização MinMaxScaler e removendo as variáveis binárias, usando o K com base na silhuete score (3.2.1). Onde encontramos um cluster com um bom lucro e os demais com pouca perda. Sendo os labels 7,8 e 9 os principais clusters.Para visualizar toda a solução basta acessar: https://github.com/vitorgodeiro/DataMaster