

IMD0033 - Probabilidade

Aula 07 - NumPy

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Março, 2018



Agenda

- Motivação
- Introdução sobre NumPy
- Criação de estruturas multidimensionais
- Leitura de arquivos
- Tipos de dados
- Comparando dados
- Funções agregadas
- Vantagens & Desvantagens

Atualizar o repositório

```
git clone https://github.com/ivanovitchm/imd0033_2018_1.git
```

Ou

```
git pull
```

Motivação

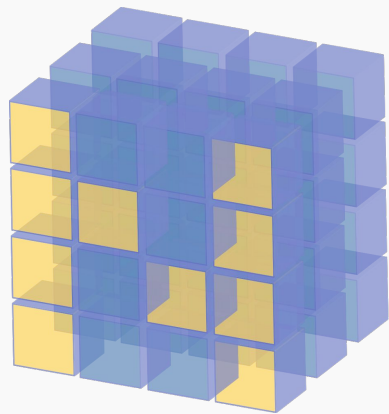
```
areas = ["hallway", 11.25, "kitchen", 18.0, "living room", 20.0]
```

Trabalhar com **Listas** em Python tem várias vantagens:

- Armazenar tipos diferentes
- Podem diminuir e crescer dinamicamente

Mas....

- Para suportar essa flexibilidade, **Listas** consomem mais memória
- Baixo desempenho para lidar com grande volumes de dados
- Não realizam operações matemáticas entre listas



NumPy

A biblioteca NumPy é o núcleo da computação científica em Python. NumPy fornece alto desempenho para operações para estruturas multidimensionais com a flexibilidade de uso encontrada nas Listas.

<https://goo.gl/0eWPy6>

Criando vetores multidimensionais

1-dimensional array

	a
a[0]	0
a[1]	3
a[2]	105
a[3]	30
a[4]	1

2-dimensional array

	b				
	b[0,0]	b[0,1]	b[0,2]	b[0,3]	b[0,4]
b[0,0]	0	3	105	30	1
b[1,0]	0	3	105	30	1
b[2,0]	0	3	105	30	1

```
import numpy as np
```

```
a = np.array([0,3,105,30,1])
```

```
b = np.array([[0,3,105,30,1],[0,3,105,30,1],[0,3,105,30,1]])
```

Imprimindo a dimensão das estruturas

```
vector = np.array([1, 2, 3, 4])  
print(vector.shape) #output: (4,)  
matrix = np.array([[5, 10, 15], [20, 25, 30]])  
print(matrix.shape) #output: (2, 3)
```


Utilizando NumPy para leitura de arquivos

```
import numpy  
data = numpy.genfromtxt("data.csv", delimiter=",")
```



World Health Organization

<http://apps.who.int/gho/data/view.main.52160>

"world_alcohol.csv"

Here's what each column represents:

- **Year** -- the year the data in the row is for.
- **WHO Region** -- the region in which the country is located.
- **Country** -- the country the data is for.
- **Beverage Types** -- the type of beverage the data is for.
- **Display Value** -- the number of liters, on average, of the beverage type a citizen of the country drank in the given year.

Analisar o conjunto de dados

world_alcohol

Cabeçalho

```
array([[ nan, nan, nan,
       [ 1.98600000e+03, nan, nan],
         nan, 0.00000000e+00],
       [ 1.98600000e+03, nan, nan,
         nan, 5.00000000e-01],
       ...,
       [ 1.98600000e+03, nan, nan,
         nan, 2.54000000e+00],
       [ 1.98700000e+03, nan, nan,
         nan, 0.00000000e+00],
       [ 1.98600000e+03, nan, nan,
         nan, 5.15000000e+00]])
```

nan,

String

Quando NumPy é incapaz de transformar o tipo do dado para numérico (nan)

Lendo o dado corretamente

```
world_alcohol = np.genfromtxt("world_alcohol.csv", delimiter="," , dtype="U75", skip_header=1)

[['1986' 'Western Pacific' 'Viet Nam' 'Wine' '0']
 ['1986' 'Americas' 'Uruguay' 'Other' '0.5']
 ['1985' 'Africa' 'Cte d'Ivoire' 'Wine' '1.62']
 ...,
 ['1986' 'Europe' 'Switzerland' 'Spirits' '2.54']
 ['1987' 'Western Pacific' 'Papua New Guinea' 'Other' '0']
 ['1986' 'Africa' 'Swaziland' 'Other' '5.15']]
```

Comparando arrays

```
vector = np.array([5, 10, 15, 20])  
vector == 10
```

```
array([False,  True, False, False], dtype=bool)
```

```
matrix = np.array([[5, 10, 15],  
                   [20, 25, 30],  
                   [35, 40, 45]])  
matrix == 25
```

```
array([[False, False, False],  
       [False,  True, False],  
       [False, False, False]], dtype=bool)
```

Funções agregadas

- `sum()`
- `mean()`
- `median()`
- `max()`
- `min()`



Executa funções sobre uma determinada dimensão do array

Funções agregadas

```
vector = np.array([5, 10, 15, 20])  
vector.sum()
```

50

```
matrix = np.array([  
                    [5, 10, 15],  
                    [20, 25, 30],  
                    [35, 40, 45]  
                ])  
matrix.sum(axis=1)
```

array([30, 75, 120])

<https://goo.gl/0eWPy6>

NumPy

The NumPy library is the core library for scientific computing in Python. It provides a high-performance multidimensional array object, and tools for working with these arrays.

Use the following import convention:



```
>>> import numpy as np
```

NumPy Arrays

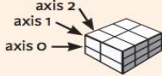
1D array

1	2	3
---	---	---

2D array

axis 1	1	5	2	3
axis 0	4	5	6	6

3D array



Creating Arrays

```
>>> a = np.array([1,2,3])
>>> b = np.array([(1.5,2,3), (4,5,6)], dtype = float)
>>> c = np.array([[(1.5,2,3), (4,5,6)], [(3,2,1), (4,5,6)]], dtype = float)
```

Initial Placeholders

```
>>> np.zeros((3,4))
>>> np.ones((2,3,4),dtype=np.int16)
>>> d = np.arange(10,25,5)

>>> np.linspace(0,2,9)

>>> e = np.full((2,2),7)
>>> f = np.eye(2)
>>> np.random.random((2,2))
>>> np.empty((3,2))
```

Create an array of zeros
Create an array of ones
Create an array of evenly spaced values (step value)
Create an array of evenly spaced values (number of samples)
Create a constant array
Create a 2x2 identity matrix
Create an array with random values
Create an empty array

I/O

Saving & Loading On Disk

```
>>> np.save('my_array', a)
>>> np.savez('array.npz', a, b)
>>> np.load('my_array.npy')
```

Saving & Loading Text Files

```
>>> np.loadtxt("myfile.txt")
>>> np.genfromtxt("my_file.csv", delimiter=',')
>>> np.savetxt("myarray.txt", a, delimiter=" ")
```

Data Types

>>> np.int64	Signed 64-bit integer types
>>> np.float32	Standard double-precision floating point
>>> np.complex	Complex numbers represented by 128 floats
>>> np.bool	Boolean type storing TRUE and FALSE values
>>> np.object	Python object type
>>> np.string	Fixed-length string type
>>> np.unicode_	Fixed-length unicode type

Inspecting Your Array

<pre>>>> a.shape >>> len(a) >>> b.ndim >>> e.size >>> b.dtype >>> b.dtype.name >>> b.astype(int)</pre>	Array dimensions Length of array Number of array dimensions Number of array elements Data type of array elements Name of data type Convert an array to a different type
---	---

Asking For Help

```
>>> np.info(np.ndarray.dtype)
```

Array Mathematics

Arithmetic Operations

<pre>>>> g = a - b array([[-0.5, 0., 0.], [-3., -3., -3.]]) >>> np.subtract(a,b) >>> b + a array([[2.5, 4., 6.], [5., 7., 9.]]) >>> np.add(b,a) >>> a / b array([[0.66666667, 1., 1.], [0.25, 0.4, 0.5]]) >>> np.divide(a,b) >>> a * b array([[1.5, 4., 9.], [4., 10., 18.]]) >>> np.multiply(a,b) >>> np.exp(b) >>> np.sqrt(b) >>> np.sin(a) >>> np.cos(b) >>> np.log(a) >>> e.dot(f) array([[7., 7.]])</pre>	Subtraction Subtraction Addition Addition Division Division Multiplication Multiplication Exponentiation Square root Print sines of an array Element-wise cosine Element-wise natural logarithm Dot product
---	--

Comparison

<pre>>>> a == b array([[False, True, True], [False, False, False]], dtype=bool) >>> a < 2 array([True, False, False], dtype=bool) >>> np.array_equal(a, b)</pre>	Element-wise comparison Element-wise comparison Array-wise comparison
--	---

Aggregate Functions

<pre>>>> a.sum() >>> a.min() >>> b.max(axis=0) >>> b.cumsum(axis=1) >>> a.mean() >>> b.median() >>> a.corrcoef() >>> np.std(b)</pre>	Array-wise sum Array-wise minimum value Maximum value of an array row Cumulative sum of the elements Mean Median Correlation coefficient Standard deviation
--	--

Copying Arrays

<pre>>>> h = a.view() >>> np.copy(a) >>> h = a.copy()</pre>	Create a view of the array with the same data Create a copy of the array Create a deep copy of the array
--	--

Sorting Arrays

<pre>>>> a.sort() >>> c.sort(axis=0)</pre>	Sort an array Sort the elements of an array's axis
--	---

Subsetting, Slicing, Indexing

Also see This

Subsetting

```
>>> a[2]
3
>>> b[1,2]
6.0
```

1	2	3
1	5	2
4	5	6

Select the element at the 2nd index
Select the element at row 0 column 2 (equivalent to `b[1][2]`)

Slicing

```
>>> a[0:2]
array([1., 2])
>>> b[0:2,1]
array([ 2.,  5.])
```

1	2	3
1	5	2
4	5	6

Select items at index 0 and 1
Select items at rows 0 and 1 in column 1

```
>>> b[:1]
array([[1.5, 2., 3.]])
>>> c[1,...]
array([[ 3.,  2.,  1.],
       [ 4.,  5.,  6.]])
```

1	2	3
1	5	2
4	5	6

Select all items at row 0 (equivalent to `b[0:1, :]`)
Same as `[1, :, :]`

```
>>> a[::-1]
array([3., 2., 1])
```

Reversed array a

Boolean Indexing

```
>>> a[a<2]
array([1])
```

1	2	3
---	---	---

Select elements from a less than 2

Fancy Indexing

```
>>> b[[1, 0, 1, 0]], [0, 1, 2, 0]]
array([[ 4.,  2.,  6.,  1.5])
>>> b[[1, 0, 1, 0]][:, [0,1,2,0]]
array([[ 4.,  5.,  6.,  4.],
       [ 4.5,  5.5,  6.,  4.5],
       [ 1.5,  2.,  3.,  1.5]])
```

Select elements (1,0), (0,1), (1,2) and (0,0)
Select a subset of the matrix's rows and columns

Array Manipulation

Transposing Array

```
>>> i = np.transpose(b)
>>> i.T
```

Permute array dimensions
Permute array dimensions

Changing Array Shape

```
>>> b.ravel()
>>> g.reshape(3,-2)
```

Flatten the array
Reshape, but don't change data

Adding/Removing Elements

```
>>> h.resize((2,6))
>>> np.append(h,g)
>>> np.insert(a, 1, 5)
>>> np.delete(a, [1])
```

Return a new array with shape (2,6)
Append items to an array
Insert items in an array
Delete items from an array

Combining Arrays

```
>>> np.concatenate((a,d),axis=0)
array([ 1.,  2.,  3., 10, 15, 20])
>>> np.vstack((a,b))
array([[ 1.,  2.,  3.],
       [ 1.5,  2.,  3.],
       [ 4.,  5.,  6.]])
>>> np.r_[e,f]
>>> np.hstack((e,f))
array([[ 7.,  7.,  1.,  0.],
       [ 7.,  7.,  0.,  1.]])
>>> np.column_stack((a,d)
array([[ 1., 10],
       [ 2., 15],
       [ 3., 20]])
>>> np.c_[a,d]
```

Concatenate arrays
Stack arrays vertically (row-wise)
Stack arrays vertically (row-wise)
Stack arrays horizontally (column-wise)
Create stacked column-wise arrays
Create stacked column-wise arrays

Splitting Arrays

```
>>> np.hsplit(a,3)
(array([1]),array([2]),array([3]))
>>> np.vsplit(c,2)
[array([[ 1.5,  2.,  1.],
       [ 4.,  5.,  3.]])],
 array([[ 3.,  2.,  1.],
       [ 4.,  5.,  6.]])])
```

Split the array horizontally at the 3rd index
Split the array vertically at the 2nd index



NumPy - Pros & Contra

Pros

- Fácil e flexível para computação científica
- Acesso rápido e flexível ao dado (slicing, indexing)
- Conversão de tipos rapidamente

Contra

- Todos os dados devem ser do mesmo tipo
- Colunas e linhas são acessadas por números

Desafio (WHO)?



World Health
Organization