

KB  $\cup \{\neg\alpha\}$ :

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| 01. $[\neg(\text{joe} = \text{sally})]$   | 11. $[\neg C(t), (t = \text{joe}), (t = \text{sally}), (t = \text{bill}), (t = \text{ellen})]$ |
| 02. $[\neg(\text{joe} = \text{bill})]$    | 12. $M(\text{joe}, \text{sally})$  |
| 03. $[\neg(\text{joe} = \text{ellen})]$   | 13. $S(\text{bill}, \text{ellen})$   |
| 04. $[\neg(\text{sally} = \text{bill})]$  | 14. $[\neg M(u_1, u_2), \neg C(u_1), C(u_2)]$  |
| 05. $[\neg(\text{sally} = \text{ellen})]$ | 15. $[\neg M(v_1, v_2), M(v_2, v_1)]$  |
| 06. $[\neg(\text{bill} = \text{ellen})]$  | 16. $[\neg M(v_3, v_3)]$   |
| 07. $[C(\text{joe})]$                     | 17. $[\neg S(w_1, w_2), S(w_2, w_1)]$  |
| 08. $[C(\text{sally})]$                   | 18. $[\neg S(w_3, w_4), \neg M(w_3, w_4)]$   |
| 09. $[C(\text{bill})]$                    | 19. $[\neg M(v_4, v_5), (v_6 = v_4), \neg M(v_6, v_5)]$  |
| 10. $[C(\text{ellen})]$                   | 20. $[M(\text{ellen}, h)]$   |

Resolução:

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| 20'. $[M(h, \text{ellen})]$   | 15 $\{v_1 / \text{ellen}, v_2 / h\}, 20$                                   |
| 21. $[\neg C(\text{ellen}), C(h)]$  | 14 $\{u_1 / \text{ellen}, u_2 / h\}, 20$                                   |
| 22. $[C(h)]$  | 10, 21   |
| 23. $[(h = \text{joe}), (h = \text{sally}), (h = \text{bill}), (h = \text{ellen})]$ | 11 $\{t / h\}, 22$   |
| 24. $[\neg(x_1 = y_1), \neg(x_2 = y_2), \neg M(x_1, x_2), M(y_1, y_2)]$             | igualdade: subst. em pred.   |
| 25. $[\neg(\text{ellen} = y_1), \neg(h = y_2), M(y_1, y_2)]$                        | 20, 24 $\{x_1 / \text{ellen}, x_2 / h\}$                                   |
| 26. $[\neg(\text{ellen} = \text{ellen}), \neg(h = \text{ellen})]$                   | 16 $\{v_3 / \text{ellen}\}, 25 \{y_1 / \text{ellen}, y_2 / \text{ellen}\}$ |
| 27. $[(z = z)]$   | igualdade: reflex.   |
| 28. $[\neg(h = \text{ellen})]$  | 26, 27 $\{z / \text{ellen}\}$  |
| 29. $[(h = \text{joe}), (h = \text{sally}), (h = \text{bill})]$                     | 23, 28   |
| 30. $[\neg M(\text{bill}, \text{ellen})]$   | 13, 18 $\{w_3 / \text{bill}, w_4 / \text{ellen}\}$                         |
| 31. $[\neg(x_1 = \text{bill}), \neg(x_2 = \text{ellen}), \neg M(x_1, x_2)]$         | 24 $\{y_1 / \text{bill}, y_2 / \text{ellen}\}, 30$                         |
| 32. $[\neg(h = \text{bill}), \neg(\text{ellen} = \text{ellen})]$                    | 20', 31 $\{x_1 / h, x_2 / \text{ellen}\}$                                  |
| 33. $[\neg(h = \text{bill})]$   | 27 $\{z / \text{ellen}\}, 32$  |
| 34. $[(h = \text{joe}), (h = \text{sally})]$  | 29, 33   |
| 35. $[(v_6 = \text{joe}), \neg M(v_6, \text{sally})]$                               | 12, 19 $\{v_4 / \text{joe}, v_5 / \text{sally}\}$                          |
| 36. $[\neg(x_3 = x_4), (x_4 = x_3)]$  | igualdade: simetria  |
| 37. $[\neg(\text{ellen} = \text{joe})]$   | 3, 36 $\{x_3 / \text{ellen}, x_4 / \text{joe}\}$                           |
| 38. $[\neg M(\text{ellen}, \text{sally})]$  | 35 $\{v_6 / \text{ellen}\}, 37$  |
| 39. $[\neg(x_1 = \text{ellen}), \neg(x_2 = \text{sally}), \neg M(x_1, x_2)]$        | 24 $\{y_1 / \text{ellen}, y_2 / \text{sally}\}, 38$                        |
| 40. $[\neg(\text{ellen} = \text{ellen}), \neg(h = \text{sally})]$                   | 20, 39 $\{x_1 / \text{ellen}, x_2 / h\}$                                   |
| 41. $[\neg(h = \text{sally})]$  | 27 $\{z / \text{ellen}\}, 40$  |
| 42. $[(h = \text{joe})]$  | 34, 41   |
| 43. $[M(\text{sally}, \text{joe})]$   | 12, 15 $\{v_1 / \text{joe}, v_2 / \text{sally}\}$                          |
| 44. $[(v_6 = \text{sally}), \neg M(v_6, \text{joe})]$                               | 19 $\{v_4 / \text{sally}, v_5 / \text{joe}\}, 43$                          |
| 45. $[\neg(\text{ellen} = \text{sally})]$   | 5, 36 $\{x_3 / \text{sally}, x_4 / \text{ellen}\}$                         |
| 46. $[\neg M(\text{ellen}, \text{joe})]$  | 44 $\{v_6 / \text{ellen}\}, 45$  |
| 47. $[\neg(x_1 = \text{ellen}), \neg(x_2 = \text{joe}), \neg M(x_1, x_2)]$          | 24 $\{y_1 / \text{ellen}, y_2 / \text{joe}\}, 46$                          |
| 48. $[\neg(\text{ellen} = \text{ellen}), \neg(h = \text{joe})]$                     | 20, 47 $\{x_1 / \text{ellen}, x_2 / h\}$                                   |
| 49. $[\neg(h = \text{joe})]$  | 27 $\{z / \text{ellen}\}, 48$  |
| 50. $[ ]$   | 42, 49   |