

# Lecture 6: Representation Learning

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Deep Learning Course, Winter 2023-2024

# Announcements

Deadline for Homework 1 is **Friday, December 15, 23:59**

- Please submit your solutions and code in Fenix.
- No late days allowed!!
- Solutions will be posted the day after.

# Today's Roadmap

Today's lecture is about:

- Representation learning.
- Principal component analysis (PCA) and auto-encoders.
- Denoising auto-encoders.
- Distributed representations.
- Word embeddings and negative sampling.
- Multilingual and contextual word embeddings.

# Outline

## ① Representation Learning

Hierarchical Compositionality

Distributed Representations

Auto-Encoders

Word Embeddings

## ② Conclusions

# Representations

- A key feature of NNs is their ability to **learn representations**  $\phi(x)$
- Standard linear models require **manually engineered features**  $\phi(x)$
- **Representations** are useful for several reasons:
  - (i) They can make our models **more expressive and more accurate**
  - (ii) They may allow **transferring** representations from one task to another
- We talked about (i) when discussing the multi-layer perceptron
- In this lecture, we'll focus on (ii)

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# Hierarchical Compositionality

Key Idea: deep(er) NNs learn **coarse-to-fine** representation layers.

## Vision:

- pixels → edges → textons → motifs → parts → objects → scenes

## Speech:

- samples → spectral bands → formants → motifs → phonemes → words

## Text:

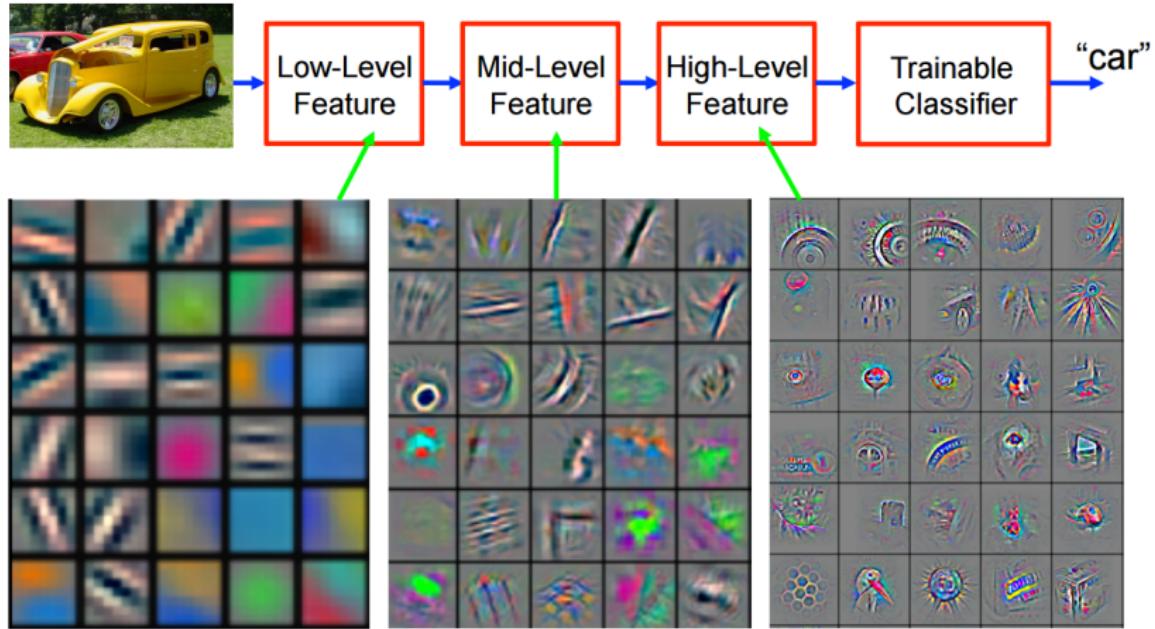
- characters → words → phrases → sentences → stories

(Inspired by Marc'Aurelio Ranzato and Yann LeCun)

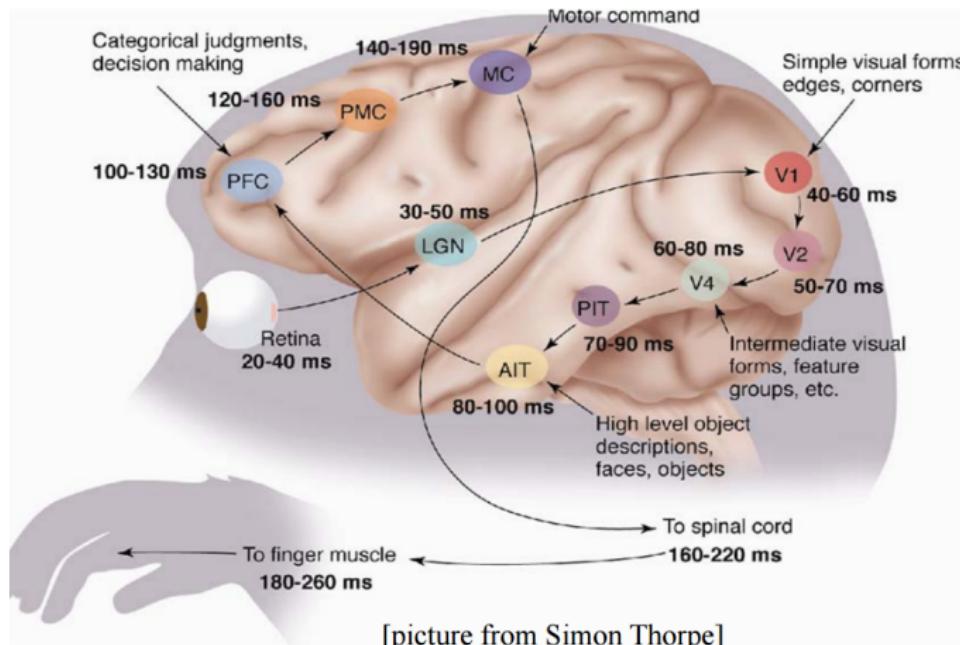
# Hierarchical Compositionality

Feature visualization of convolutional NNs trained on ImageNet

(Zeiler and Fergus, 2013)



# The Mammalian Visual Cortex is Hierarchical



(LGN = lateral geniculate nucleus; PIT = posterior inferotemporal area; AIT = anterior inferotemporal area; PFC = prefrontal cortex; PMC = premotor cortex; MC = motor cortex)

## What Is Learned in Each Layer

- Layers closer to inputs learn **low-level representations** (corners, edges)
- Layers farther away from inputs learn **more abstract representations** (shapes, forms, objects)
- This holds, not only for images, but also text, sounds, ...

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# Distributed Representations (Hinton, 1984)

This is a central concept in neural networks.

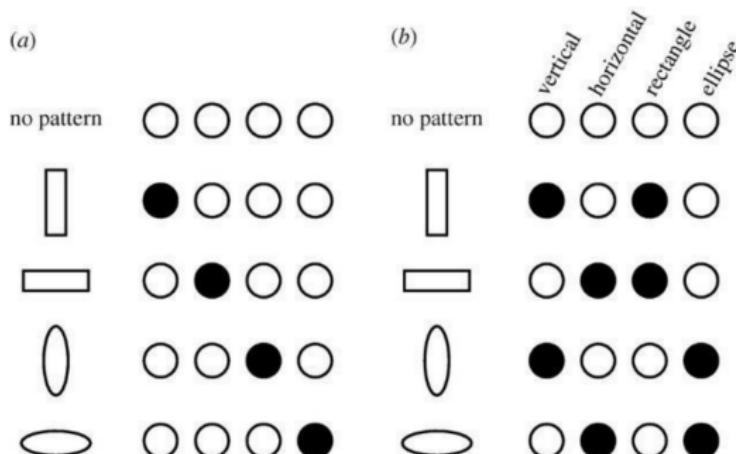
## Key questions:

- How can a NN so effectively **represent objects**, if it has only a few **hidden units** (i.e. much fewer than possible objects)?
- What is each **hidden unit** actually **representing**?
- How can a NN **generalize** to objects that it has not seen before?

# Local vs Distributed Representations

Consider two alternative representations:

- Local (one-hot) representations (one dimension per object)
- Distributed representations (one dimension per property)



(Inspired by Moontae Lee and Dhruv Batra)

# Distributed Representations

**Key idea:** no single neuron “encodes” everything; groups of neurons (e.g. in the same hidden layer) work together!

cf. the **grandmother cell**



jolyon.co.uk

# The Power of Distributed Representations

- Distributed representations are **more compact** (there can be  $O(\exp N)$  objects combining  $N$  properties)
- They are also **more powerful**, as they can generalize to unseen objects in a meaningful way:

Local	 = VR + HR + HE = ?
Distributed	 = V + H + E ≈ 

(Inspired by Moontae Lee and Dhruv Batra)

# The Power of Distributed Representations

- Hidden units should capture **diverse properties** of objects (not all capturing the same property)
- Usually ensured by random initialization of the weights
- Initializing all the units to the same weights would never break the symmetry!
- **Side note:** a NN computes the same function if we permute the hidden units within a layer (order doesn't matter, only diversity)

**Next:** how to learn useful object representations from raw inputs (no labels)?

## Example: Unsupervised Pre-Training

- Training deep NNs (with many hidden layers) can be challenging
- This has been a major difficulty with NNs for a long time
- Initialize hidden layers using **unsupervised learning** (Erhan et al., 2010):
  - Force network to **represent latent structure** of input distribution
  - Encourage hidden layers to **encode** that structure
  - This can be done with an **auto-encoder!**

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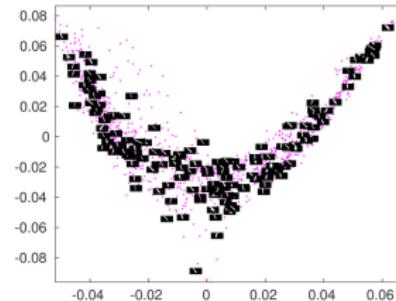
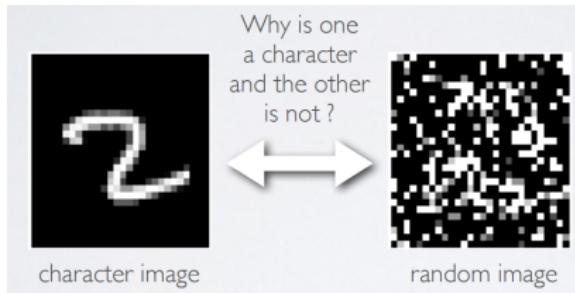
Auto-Encoders

Word Embeddings

## ② Conclusions

# Data Manifold

**Key idea:** learn the **manifold** (what is this?) where the input objects live



(Image credit: Hugo Larochelle)

Learn representations that encode well points in that **manifold**

# Auto-Encoders

**Auto-encoder:** feed-forward NN trained to reproduce its input at the output

- Encoder:  $\mathbf{h}(\mathbf{x}) = \mathbf{g}(\mathbf{Wx} + \mathbf{b})$

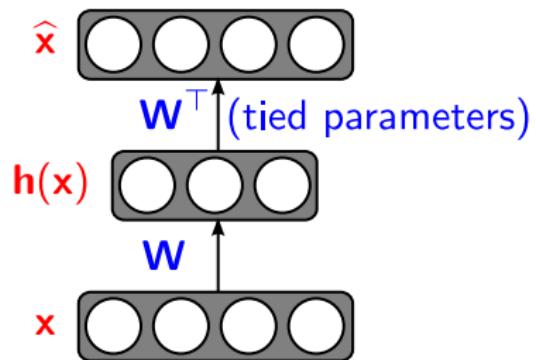
- Decoder:  $\hat{\mathbf{x}} = \mathbf{W}^\top \mathbf{h}(\mathbf{x}) + \mathbf{c}$

- Loss function (for  $\mathbf{x} \in \mathbb{R}^D$ ):

$$L(\hat{\mathbf{x}}; \mathbf{x}) = \|\hat{\mathbf{x}} - \mathbf{x}\|^2$$

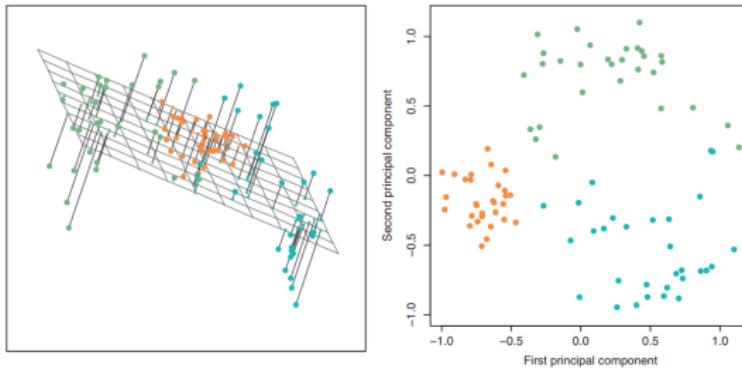
- Objective (dropping the biases):

$$\widehat{\mathbf{W}} = \arg \min_{\mathbf{W}} \sum_i \|\mathbf{W}^\top \mathbf{g}(\mathbf{Wx}_i) - \mathbf{x}_i\|^2$$



# The Simplest Auto-Encoder: Linear

What happens if the activation function  $g$  is linear?



**FIGURE 10.2.** Ninety observations simulated in three dimensions. Left: the first two principal component directions span the plane that best fits the data. It minimizes the sum of squared distances from each point to the plane. Right: the first two principal component score vectors give the coordinates of the projection of the 90 observations onto the plane. The variance in the plane is maximized.

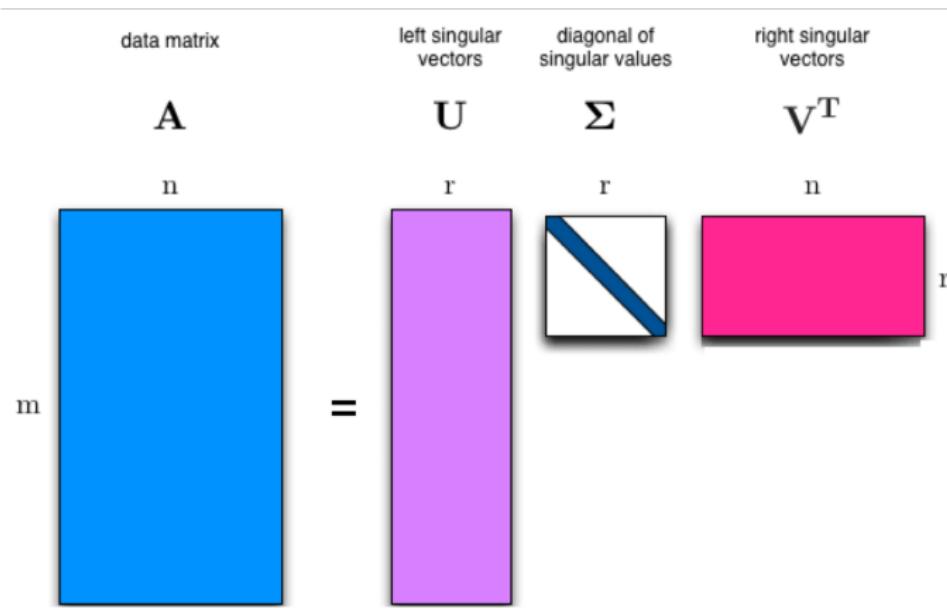
(From “An Introduction to Statistical Learning” by James, Witten, Hastie, Tibshirani)

# An Important Tool: Singular Value Decomposition

- Any rank- $r$  matrix  $\mathbf{A} \in \mathbb{R}^{m \times n}$  can be written as  $\mathbf{A} = \mathbf{U}\Sigma\mathbf{V}^T$ 
  - ✓ columns of  $\mathbf{U} \in \mathbb{R}^{m \times r}$  are an orthonormal basis of  $\mathcal{R}(\mathbf{A})$ ;
  - ✓ columns of  $\mathbf{V} \in \mathbb{R}^{n \times r}$  are an orthonormal basis of  $\mathcal{R}(\mathbf{A}^T)$ ;
  - ✓  $\Sigma = \text{diag}(\sigma_1, \dots, \sigma_r)$  is a  $r \times r$  diagonal matrix;
  - ✓  $\sigma_1, \dots, \sigma_r$  are square roots of the eigenvalues of  $\mathbf{A}^T\mathbf{A}$  or  $\mathbf{A}\mathbf{A}^T$ ;
  - ✓  $\sigma_1, \dots, \sigma_r$  are called **singular values**.
- Orthonormality of  $\mathbf{U}$  and  $\mathbf{V}$ :  $\mathbf{U}^T\mathbf{U} = \mathbf{I}$  and  $\mathbf{V}^T\mathbf{V} = \mathbf{I}$ .

# Singular Value Decomposition (SVD)

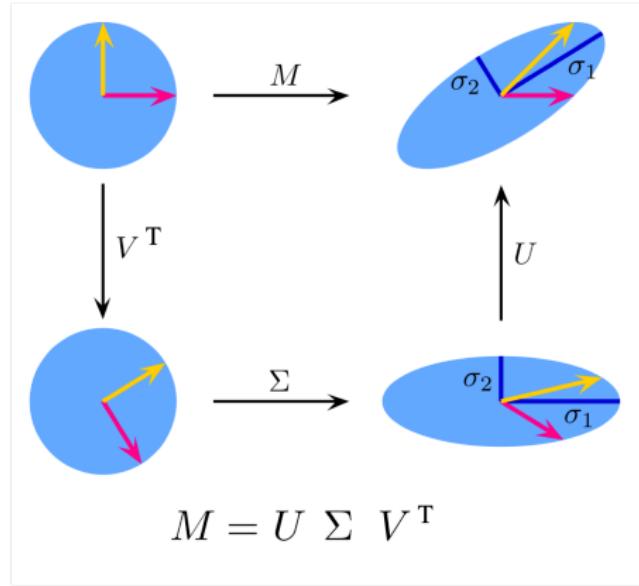
- $\mathbf{A} = \mathbf{U}\Sigma\mathbf{V}^T$ , where  $\mathbf{U} \in \mathbb{R}^{m \times r}$  and  $\mathbf{V} \in \mathbb{R}^{n \times r}$ .



Picture credits: Mukesh Mithrakumar

# Singular Value Decomposition (SVD)

- $M = U\Sigma V^T$ , where  $U \in \mathbb{R}^{m \times r}$  and  $V \in \mathbb{R}^{n \times r}$ .



Picture credits: Wikipedia

## Linear Auto-Encoder

Let  $\mathbf{X} \in \mathbb{R}^{N \times D}$  be the data matrix ( $N > D$ ),

Assume  $\mathbf{W} \in \mathbb{R}^{K \times D}$  with  $K < D$  (no biases, assuming  $\mathbf{X}$  is centred)

We want to minimize

$$\sum_{i=1}^N \|\mathbf{x}_i - \hat{\mathbf{x}}_i\|_2^2 = \|\mathbf{X} - \hat{\mathbf{X}}\|_F^2 = \|\mathbf{X} - \mathbf{X}\mathbf{W}^\top \mathbf{W}\|_F^2$$

where  $\|\cdot\|_F^2$  is the Frobenius matrix norm and  $\mathbf{W}^\top \mathbf{W}$  has rank  $K$ .

From the [Eckart-Young theorem](#), the minimizer is [truncated SVD](#) of  $\mathbf{X}^\top$ :

$$\hat{\mathbf{X}}^\top = \mathbf{U}_K \Sigma_K \mathbf{V}_K^\top,$$

where  $\Sigma_K$  is a diagonal matrix containing the top  $K$  singular values of  $\mathbf{X}^\top$ , and the columns of  $\mathbf{U}_K$  are the corresponding left singular vectors.

The solution is  $\mathbf{W} = \mathbf{U}_K^\top$ , which gives as desired:

$$\hat{\mathbf{X}}^\top = \mathbf{W}^\top \mathbf{W} \mathbf{X}^\top = \mathbf{U}_K \mathbf{U}_K^\top \mathbf{U} \Sigma \mathbf{V}^\top = \mathbf{U}_K \Sigma_K \mathbf{V}_K^\top.$$

This is called [principle component analysis \(PCA\)](#)

# PCA: EigenFaces

$$\begin{bmatrix} x^{(n)} \end{bmatrix} = \alpha_1 \begin{bmatrix} u_1 \end{bmatrix} + \dots + \alpha_p \begin{bmatrix} u_p \end{bmatrix}$$

Diagram illustrating PCA decomposition:

- A grayscale portrait of a man is shown.
- An arrow labeled "PCA" points from the portrait to a vertical vector of coefficients  $\begin{bmatrix} \alpha_1 \\ \vdots \\ \alpha_p \end{bmatrix}$ .
- The right side of the equation shows the reconstruction of the image as a sum of  $p$  components. Each component is a scalar coefficient  $\alpha_i$  multiplied by a grayscale face template  $u_i$ .
- A 4x6 grid of 24 grayscale face templates is shown below the equation.
- Red arrows point from the terms  $\alpha_1 u_1$  and  $\alpha_p u_p$  in the equation to the first and last columns of the template grid, respectively, illustrating how these components capture the most variance in the data.

# Auto-Encoders

PCA fits a **linear manifold** (affine space) to the data

By using **non-linear** activations, we obtain more sophisticated codes (i.e. representations).

We need some sort of **regularization** to:

- encourage a smooth representation (small perturbations of the input will lead to similar representations)
- avoid overfitting to the training data

# Some Variants of Auto-Encoders

- **Sparse auto-encoders:** use many hidden units, but add a  $\ell_1$  regularization term to encourage **sparse representations** of the input
- **Denoising auto-encoders:** regularize by adding noise to the input; the goal is to learn a **smooth representation function** that allows to output the denoised input (inspired by image denoising)
- **Stacked auto-encoders:** several auto-encoders on top of each other
- **Variational auto-encoders:** a generative probabilistic model that minimizes a variational bound (this will be covered in another lecture!)

# Regularized Auto-Encoders

- To regularize auto-encoders, **regularization** may be added to the loss
- The goal is then to minimize  $L(\hat{x}; x) + \Omega(h, x)$
- For example:
  - regularizing the code  $\Omega(h, x) = \lambda \|h\|^2$
  - regularizing the derivatives  $\Omega(h, x) = \lambda \sum_i \|\nabla_x h_i\|^2$
- The encoder and decoder parameters may be shared or not.

# Sparse Auto-Encoders

- Most auto-encoders learn low-dimensional codes, e.g., they reduce input dimensionality (bottleneck shape  $K < D$ ).
- One exception are **sparse auto-encoders**:
  - Sparse auto-encoders incorporate a sparsity penalty  $\Omega(\mathbf{h})$  on the code layer, e.g.,  $\Omega(\mathbf{h}) = \lambda \|\mathbf{h}\|_1$
  - Typically the number of hidden units is large, e.g., larger than the input dimension
  - The sparsity penalty encourages sparse codes, where most hidden units are inactive.

# Stochastic Auto-Encoders

- In this case, the encoder and decoder are not deterministic functions, but involve some noise/randomness
- Uses distribution  $p_{\text{encoder}}(\mathbf{h} \mid \mathbf{x})$  for the encoder and a distribution  $p_{\text{decoder}}(\mathbf{x} \mid \mathbf{h})$  for the decoder
- The auto-encoder can be trained to minimize
  - $-\log p_{\text{decoder}}(\mathbf{x} \mid \mathbf{h})$ .

# Denoising Auto-Encoders

- Use a perturbed version of the input,  $\tilde{x} = x + n$ , where  $n$  is random noise (e.g. Gaussian noise  $n \sim \mathcal{N}(0, \sigma^2 I)$ )
- Instead of minimizing  $\frac{1}{2}\|\hat{x} - x\|^2$ , minimize  $\frac{1}{2}\|\hat{x} - \tilde{x}\|^2$
- This is a form of implicit regularization that ensures **smoothness**: it forces the system to represent well not only the data points, but also their perturbations

# Denoising Auto-Encoders

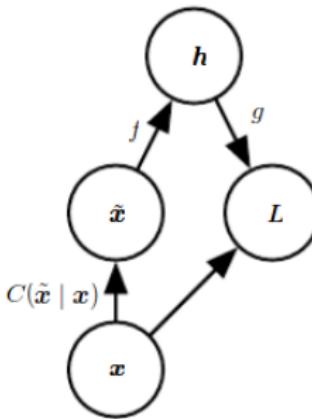


Figure 14.3: The computational graph of the cost function for a denoising autoencoder, which is trained to reconstruct the clean data point  $\mathbf{x}$  from its corrupted version  $\tilde{\mathbf{x}}$ . This is accomplished by minimizing the loss  $L = -\log p_{\text{decoder}}(\mathbf{x} | \mathbf{h} = f(\tilde{\mathbf{x}}))$ , where  $\tilde{\mathbf{x}}$  is a corrupted version of the data example  $\mathbf{x}$ , obtained through a given corruption process  $C(\tilde{\mathbf{x}} | \mathbf{x})$ . Typically the distribution  $p_{\text{decoder}}$  is a factorial distribution whose mean parameters are emitted by a feedforward network  $g$ .

(From Goodfellow et al.'s book.)

# Denoising Auto-Encoders

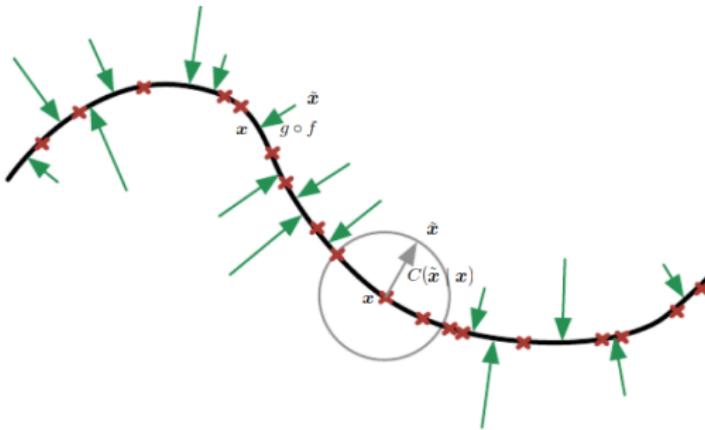


Figure 14.4: A denoising autoencoder is trained to map a corrupted data point  $\tilde{x}$  back to the original data point  $x$ . We illustrate training examples  $x$  as red crosses lying near a low-dimensional manifold, illustrated with the bold black line. We illustrate the corruption process  $C(\tilde{x} | x)$  with a gray circle of equiprobable corruptions. A gray arrow demonstrates how one training example is transformed into one sample from this corruption process. When the denoising autoencoder is trained to minimize the average of squared errors  $\|g(f(\tilde{x})) - x\|^2$ , the reconstruction  $g(f(\tilde{x}))$  estimates  $\mathbb{E}_{x, \tilde{x} \sim p_{\text{data}}(x)C(\tilde{x}|x)}[x | \tilde{x}]$ . The vector  $g(f(\tilde{x})) - \tilde{x}$  points approximately toward the nearest point on the manifold, since  $g(f(\tilde{x}))$  estimates the center of mass of the clean points  $x$  that could have given rise to  $\tilde{x}$ . The autoencoder thus learns a vector field  $g(f(x)) - x$  indicated by the green arrows. This vector field estimates the score  $\nabla_x \log p_{\text{data}}(x)$  up to a multiplicative factor that is the average root mean square reconstruction error.

# Why Do We Use Auto-Encoders?

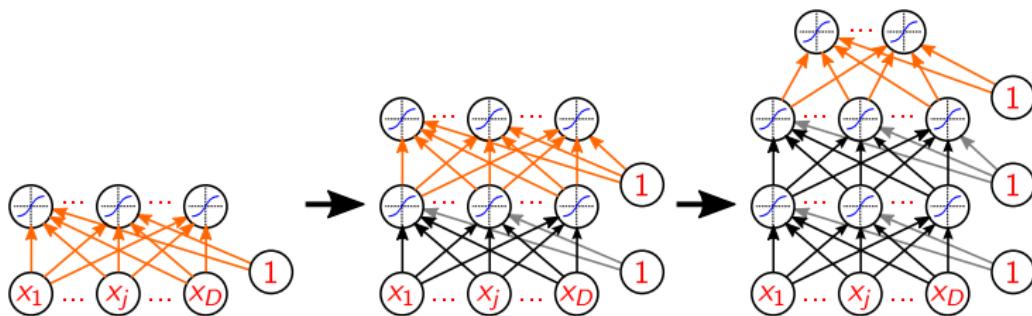
Historically, training deep neural networks was hard

One of the initial successful uses of auto-encoders was for **unsupervised pre-training** (Erhan et al., 2010).

# Unsupervised Pre-Training

A greedy, layer-wise procedure:

- train one layer at a time, from first to last, with unsupervised criterion (e.g. an auto-encoder)
- fix the parameters of previous hidden layers
- previous layers viewed as feature extraction



Pre-training initializes the parameters in a region such that the near local optima overfit less the data.

# Fine-Tuning

Once all layers are pre-trained:

- add output layer
- train the whole network using supervised learning

Supervised learning is performed as in a regular feed-forward network:

- forward propagation, backpropagation, and update
- all parameters are “tuned” for the supervised task at hand
- representation is adjusted to be more discriminative

# Other Applications of Auto-Encoders

- Dimensionality reduction
- Information retrieval and semantic hashing (via binarizing the codes)
- Conversion of discrete inputs to low-dimensional continuous space

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Word Embeddings

## ② Conclusions

# Word Representations

- Learning representations of **words in natural language**;
- Also called **word embeddings**;
- An extremely successful application of representation learning;
- Still an active area of research;
- Essential ingredient of modern **large language models** (LLMs).

# Distributional Similarity

Key idea: represent a word by means of its neighbors

- “*You shall know a word by the company it keeps*” (J. R. Firth, 1957)
- One of the most successful ideas of modern statistical NLP!

For example:

- Adjectives are normally surrounded by nouns
- Words like *book*, *newspaper*, *article*, are commonly surrounded by *reading*, *read*, *writes*, but not by *flying*, *eating*, *sleeping*

# Word Embeddings

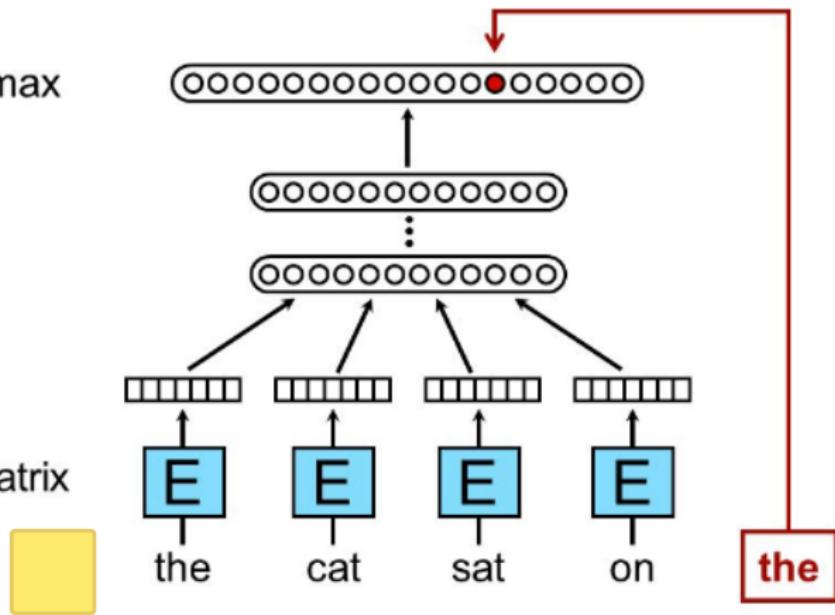
- Obtain (lower dimensional) **vector representations** of words.
- Two possible methods:
  - ✓ Factorization of a co-occurrence word/context matrix (latent semantic analysis, etc.)
  - ✓ Directly learn low-dimensional vectors by training a network to *predict* the context of a given word
- We focus on the latter, namely **word2vec** (Mikolov et al., 2013), which follows previous ideas (Bengio et al., 2003; Collobert et al., 2011).

# Neural Language Model (Bengio et al., 2003)

Hinge Loss // Softmax

Hidden Layers?

Word Embedding Matrix



(Image credits: Quoc Le)

## Neural Language Model (Bengio et al., 2003)

**Embedding matrix:** assigns a vector to every word in the vocabulary.

Learning the embeddings:

- Each word is associated with a vector (**word embedding**)
- Given the **context** (previous  $K$  words), predict the next word
- The word embeddings in the context window are **concatenated** into a vector that is fed to **neural network**
- The output layer is a huge **softmax** assigning probabilities to each word in the vocabulary
- The network is trained by **SGD with backpropagation** including the embedding matrix.

Variants of this model outperform smoothed  $K$ -th order Markov models

## Some Insights

- Often, we are not concerned with language modelling (the addressed task), but with the **quality of the embeddings** learned
- If we don't care about language modelling,
  - ✓ We don't need to have a "left-to-right model" where we try to predict the next word given the context
  - ✓ We don't need to predict the probability of every word, just make sure that the true word is more likely than a random one
- These insights underlie the word2vec model of Mikolov et al. (2013).

## Word2Vec (Mikolov et al., 2013)

- Considers a context window **around** each word in the sentence.
- **Word2vec** comes with two variants:
  - ✓ **skip-gram**: predict surrounding context words in a window of length  $m$  of every word
  - ✓ **continuous bag-of-words (CBOW)**: predict the central word from the context
- We focus on the skip-gram model (more widely used).

## Skip-Gram

- **Objective:** maximize the log probability of any context word given the central word:

$$J(\Theta) = \frac{1}{T} \sum_{t=1}^T \sum_{-m \leq j \leq m, j \neq 0} \log p_\Theta(x_{t+j} | x_t)$$

- There are 2 sets of parameters (2 embedding matrices)  $\Theta = (\mathbf{u}, \mathbf{v})$ :
  - ✓ Embeddings  $\mathbf{u}_o$  for each word  $o$  appearing as the center word
  - ✓ Embeddings  $\mathbf{v}_c$  for each word  $c$  appearing as context of another word
- Uses a **log-bilinear model**:  $p_\Theta(x_{t+j} = c | x_t = o) \propto \exp(\mathbf{u}_o^\top \mathbf{v}_c)$
- Every word gets two vectors
- In the end, we use the  $\mathbf{u}$  as the word embeddings, discarding  $\mathbf{v}$

# The Large Vocabulary Problem

- Recall that

$$p_{\Theta}(x_{t+j} = c \mid x_t = o) = \frac{\exp(\mathbf{u}_o^T \mathbf{v}_c)}{\sum_{c'} \exp(\mathbf{u}_o^T \mathbf{v}_{c'})}$$

- This is a softmax over the entire vocabulary (often  $> 50000$ )
- With large vocabularies, this leads to very slow training. Possible workarounds:
  - ✓ Stochastic sampling
  - ✓ Noise contrastive estimation
  - ✓ Negative sampling
- More details in <https://arxiv.org/pdf/1410.8251.pdf>
- We focus on **negative sampling**.

# Negative Sampling

## Key idea:

- Replace the huge softmax by **binary logistic regressions** for a true pair (center word, word in the context window) and  $k$  random pairs (center word, random word):

$$J_t(\Theta) = \log \sigma(\mathbf{u}_o^\top \mathbf{v}_c) + \sum_{i=1}^k \log \sigma(-\mathbf{u}_o^\top \mathbf{v}_{j_i}), \quad j_i \sim P(x)$$

- Several strategies for sampling the random words (uniform, unigram frequency, etc.)
- Negative sampling is a simple form of unsupervised pre-training.

# Linear Relationships

- Word embeddings are good at encoding dimensions of similarity
- Word analogies can be solved well simply via subtraction in the embedding space
- Syntactically:

$$\mathbf{x}_{\text{apple}} - \mathbf{x}_{\text{apples}} \approx \mathbf{x}_{\text{car}} - \mathbf{x}_{\text{cars}} \approx \mathbf{x}_{\text{family}} - \mathbf{x}_{\text{families}}$$

- Semantically:

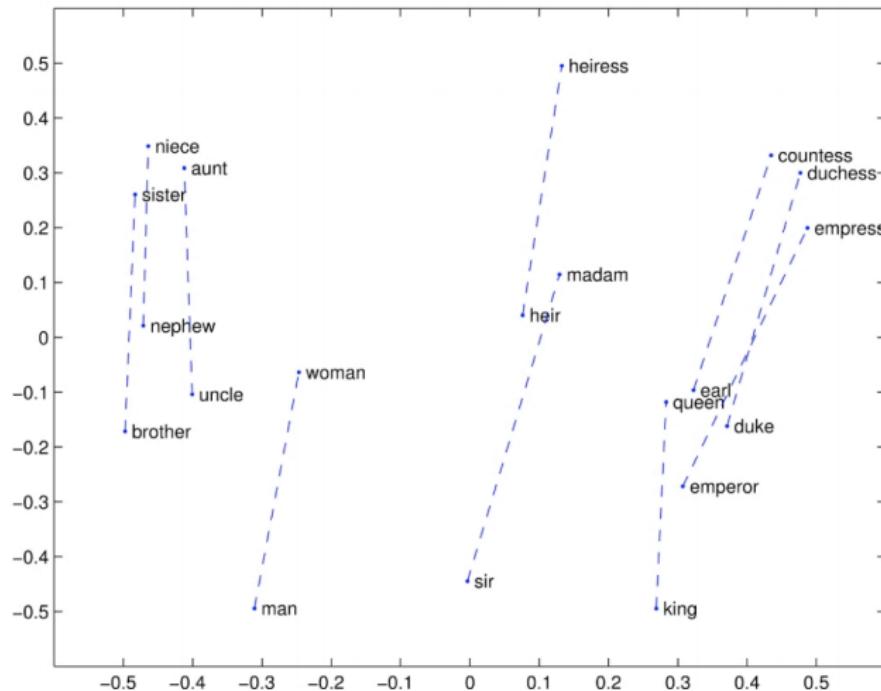
$$\mathbf{x}_{\text{shirt}} - \mathbf{x}_{\text{clothing}} \approx \mathbf{x}_{\text{chair}} - \mathbf{x}_{\text{furniture}}$$

$$\mathbf{x}_{\text{king}} - \mathbf{x}_{\text{man}} \approx \mathbf{x}_{\text{queen}} - \mathbf{x}_{\text{woman}}$$

# Visualization

- Typical embedding dimensions are in the hundreds (e.g. 300)
- How can we visualize these embeddings?
- Simple way: project them in 2D with something like PCA
- Most used: t-SNE (*t*-distributed stochastic neighbor embedding (Maaten and Hinton, 2008))  
<https://lvdmaaten.github.io/tsne>

# Word Analogies (Mikolov et al., 2013)



(Slide credit to Richard Socher)

## Other Methods for Obtaining Word Embeddings

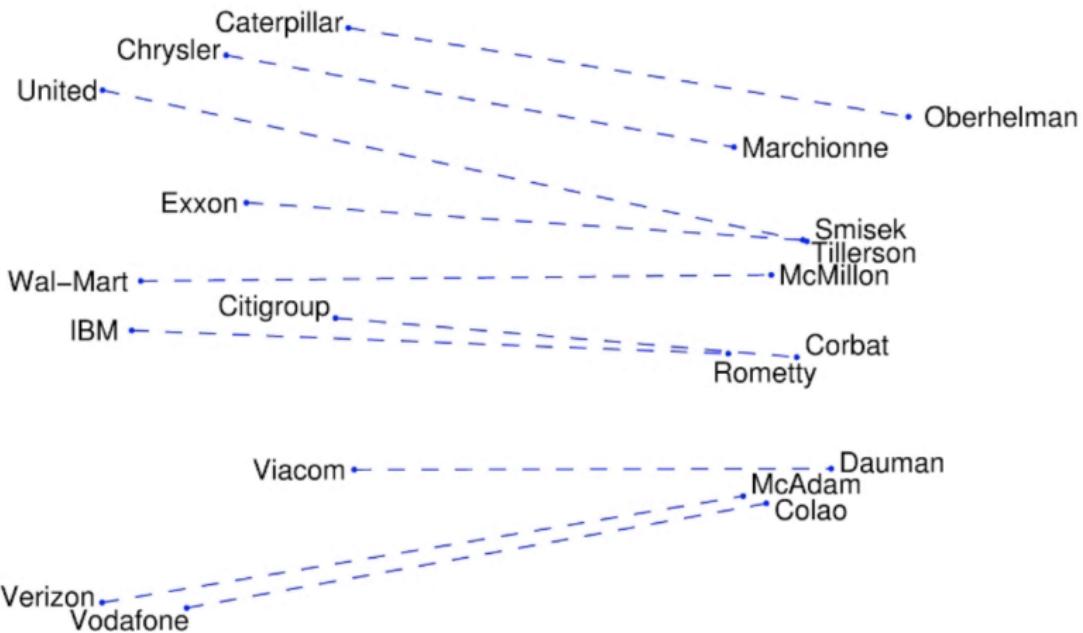
**GloVe:** Global Vectors for Word Representation (Pennington et al., 2014)

- <https://nlp.stanford.edu/projects/glove>
- Training is performed on aggregated global word-word co-occurrence statistics from a corpus

**FastText** (Bojanowski et al., 2016): embeds also character  $n$ -grams for generating embeddings for out-of-vocabulary words

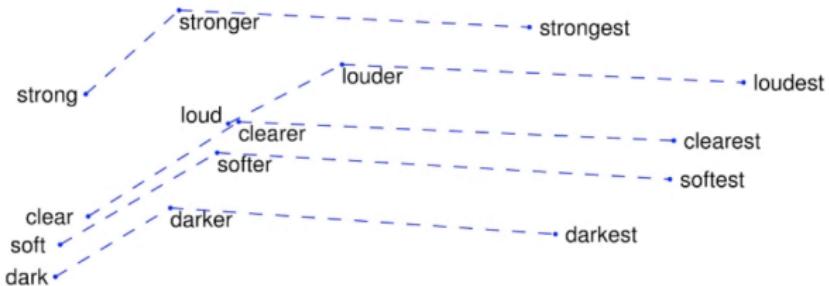
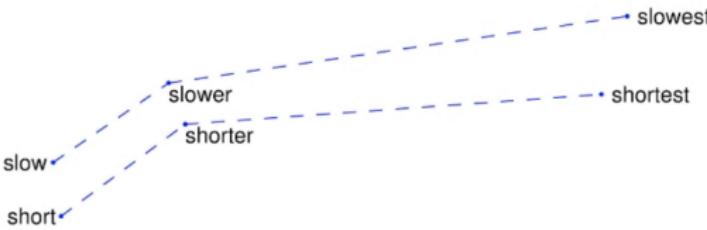
- <https://fasttext.cc> (from FAIR)
- open-source, free, lightweight library that allows users to learn text representations and text classifiers
- contains multi-lingual word vectors for 157 different languages

# GloVe Visualizations: Company → CEO



(Slide credit to Richard Socher)

# GloVe Visualizations: Superlatives



(Slide credit to Richard Socher)

# Word Embeddings: Some Open Problems

- Can we have word embeddings for multiple languages in the same space?
- How to capture **Polysemy**? (e.g., bank, star, spring, pupil, ...)
- These word embeddings are static, can we compute them **on-the-fly**, depending on the context?

# Cross-Lingual Word Embeddings

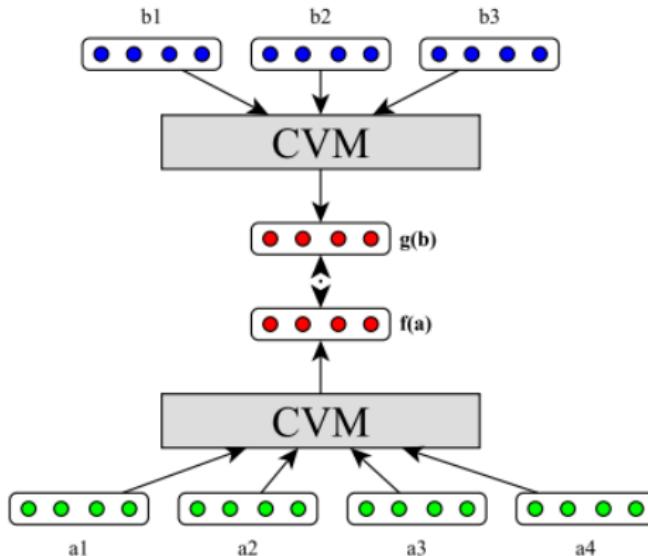


Figure 1: Model with parallel input sentences  $a$  and  $b$ . The model minimises the distance between the sentence level encoding of the bitext. Any composition functions (CVM) can be used to generate the compositional sentence level representations.

(From Hermann and Blunsom (2014).)

# Cross-Lingual Word Embeddings

- Use a corpus of parallel sentences in two languages
- Define a composition function to obtain a sentence representation given word embeddings
- Apply a loss function that encourages the sentence representations in the two languages to be similar
- Negative sampling works here too: true pair vs fake pair.

# Cross-Lingual Word Embeddings

## Other approaches:

- Define a bilingual dictionary and apply canonical correlation analysis (Faruqui and Dyer, 2014)
- Task-specific embeddings with convex optimization (Ferreira et al., 2016)
- Learn the two embeddings separately, and then apply a linear transformation to put them in a shared space (Artetxe et al., 2017)
- Adversarial training (Lample et al., 2018)

This is a very active area of research!

# Contextual Embeddings

- Words can have different meanings, depending on the context
- In 2018, a model called ELMo learned **context-dependent embeddings** and achieved impressive results on 6 NLP downstream tasks (Peters et al., 2018)

## Key ideas:

- ✓ Pre-train a BiLSTM language model on a large dataset (we'll see in a later class what this is)
- ✓ Save **all** the encoder parameters at all layers, not only the embeddings
- ✓ Then, for your downstream task, tune a scalar parameter for each layer, and pass **the entire sentence** through this encoder.

## BERT, GPT, etc.

Some time later, a transformer-based model (BERT) achieved even better performance:

### **BERT: Pre-training of Deep Bidirectional Transformers for Language Understanding**

**Jacob Devlin   Ming-Wei Chang   Kenton Lee   Kristina Toutanova**

Google AI Language

{jacobdevlin, mingweichang, kentonl, kristout}@google.com

Huge improvements in multiple NLP tasks!

(Trained on 64 TPU chips!!)

Other related models include GPT-2, GPT-3, etc.

This will be covered in a later lecture!

# Outline

## ① Representation Learning

Hierarchical Compositionality

Distributed Representations

Auto-Encoders

Word Embeddings

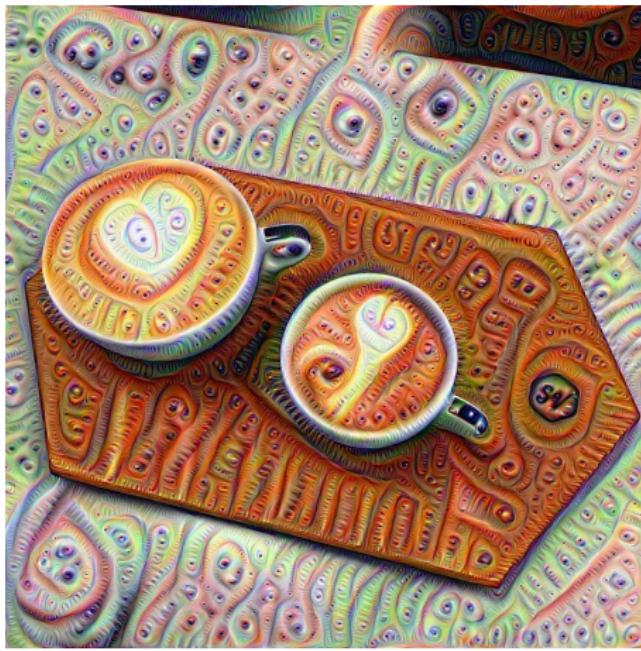
## ② Conclusions

# Conclusions

- Neural nets learn internal representations that can be transferred across tasks
- Distributed representations are exponentially more compact and allow generalizing to unseen objects
- Deeper neural nets exhibit hierarchical compositionality: upper level layers learn more abstract/semantic representations than bottom level layers
- Auto-encoders are an effective means for learning representations
- Word embeddings are continuous representations of words that are extremely useful in NLP

# Thank you!

Questions?



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