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## Questions

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### Not

1/1 point (graded)

Alyssa and Ben are studying the recursive datatype for Boolean formulas.

Ben suggests changing the `Not` variant from `Not(formula:Formula)` to `Not(var:Variable)`. Which of these formulas should Alyssa offer as a counterexamples?


- ☐  $(P \vee Q) \wedge (\neg P \vee R)$
- ☐  $(P \vee Q) \wedge (P \vee \neg R)$
- ☐  $(P \vee Q) \wedge (\neg P \vee \neg R)$
- ☒  $(P \vee Q) \wedge \neg(P \vee R)$
- ☒  $\neg((P \vee Q) \wedge (P \vee R))$



#### Explanation

With this change, Ben can only represent negated variables, not negated (sub-)formulas.

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### Pair

1/1 point (graded)

When we write `Environment = ImList<Variable x Boolean>`, we mean that an `Environment` is implemented as an `ImList` of two-element tuples (a.k.a. pairs) where the first element is a `Variable` and the second is a `Boolean`.

Then we wrote statements like:

```
lookup(Cons((var, val), rest), x) = if var = x then val else lookup(rest, x)
```

which says: when we look up `x` in an `Environment` whose first pair is `(var, val)`, if `var` is `x`, return `val`, otherwise keep looking for `x` in the `rest` of the `Environment` (which is just an `ImList` of these pairs).

Unlike Python, Java does not have tuples. What could we do instead to store these tuples?

- ☐ `Environment = ImList< List< Variable, Boolean>>`
- ☐ `Environment = ImList< List< String, Boolean>>`
- ☒ `Environment = ImList< List< Object>>`
- ☐ `Environment = ImList< Variable[]>`
- ☐ `Environment = ImList< Boolean[]>`

☐ Environment = ImList< String[]>

☒ Environment = ImList< Object[]>

**Explanation**  
The first two options are not valid Java: `List`’s have only one type of thing in them. And we need to store two different types, so the `Object` list and array are the only options that work.

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### Pair problems

0/1 point (graded)

The solutions for storing pairs in the previous question are pretty bad. What do they *not* provide?

☒ static checking of the types of objects in the pair

☒ dynamic checking of the types of objects in the pair

☒ static checking of the number of objects in the pair

☒ dynamic checking of the number of objects in the pair

☒ static checking that we only access valid indices in the pair

☐ dynamic checking that we only access valid indices in the pair

**Explanation**  
Lists and arrays provide dynamic out-of-bounds checking, but that’s it. Storing these pairs as sequences of `Object`’s is not a good design.

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### Pair progress

4/4 points (graded)

Let’s define an abstract datatype `Pair<T, U>` to store pairs of values. This is another generic type: the first element of the pair is of some unknown type we’ll call `T`, and the second is of unknown type `U`. For Boolean formula environments, we will use `Pair<Variable, Boolean>`.

This ADT will be characterized by two operations: `first`, to retrieve the first element in the pair, and `second`, to retrieve the second element.

To work on the concrete implementation, we’ll write a datatype definition:

```
Pair<T, U> = Pair(first:T, second:U)
```

Pair has only one concrete variant.

Fill in the blanks to define operations:

```
first : FIRST_INPUTS -> FIRST_OUTPUTS
second : SECOND_INPUTS -> SECOND_OUTPUTS
```

FIRST\_INPUTS

☒ Pair< T, U>

☐ T

☐ U

☐ first

☐ t

☐ u



FIRST\_OUTPUTS

☐ Pair< T, U>

☒ T

☐ U

☐ first

☐ t

☐ u



SECOND\_INPUTS

☒ Pair< T, U>

☐ T

☐ U

☐ second

☐ t

☐ u



SECOND\_OUTPUTS

☐ Pair< T, U>

☐ T

☒ U

☐ second

☐ t

☐ u



Explanation

These function definitions are in terms of types, so names like `first`, `t`, etc. are out. The input is a `Pair` (probably these will be instance methods, and it will be `this`), and the output is the first or second element, which are of arbitrary, unknown types `T` and `U`.

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