

## LE1.2.1: Entropy

pontos 3 / 3 (sem classificação)

Please compute the entropy associated with each the following random variables. You may find it helpful to use the built-in calculator -- click the icon in the lower righthand corner of the page. It supports the function "log2(...)" which computes the log-base-2 of its argument. You can type in an entire expression to evaluate, e.g., ".3\*log2(1/.3) + .7\*log2(1/.7)". Answers that include decimal places must be within 10% of the correct solution to be marked correct.

A) The flip of an unfair coin, where  $p(\text{heads}) = 0.999$  and  $p(\text{tails}) = 0.001$ .

Entropy (in bits):

✓ Answer: .0114

Explanation

$$\begin{aligned}\text{Entropy} &= p(\text{heads}) \cdot \log_2\left(\frac{1}{p(\text{heads})}\right) + p(\text{tails}) \cdot \log_2\left(\frac{1}{p(\text{tails})}\right) \\ &= 0.999 \cdot \log_2(1/0.999) + 0.001 \cdot \log_2(1/0.001) = .0114\end{aligned}$$

B) The random choice of one of the 16 hex digits, where the probability of choosing any particular digit is  $1/16$ .

Entropy (in bits):

✓ Answer: 4

Explanation

$$\begin{aligned}\text{Entropy} &= \sum_{i=0}^{15} p_i \cdot \log_2\left(\frac{1}{p_i}\right) \\ &= \frac{1}{16} * \log_2\left(\frac{1}{\frac{1}{16}}\right) + \frac{1}{16} * \log_2\left(\frac{1}{\frac{1}{16}}\right) + \dots + \frac{1}{16} * \log_2\left(\frac{1}{\frac{1}{16}}\right) \\ &= 16 * \frac{1}{16} * \log_2(16) = 4\end{aligned}$$

C) The quiz grade of a randomly-chosen student, where in the 100-student class the grade distribution was 27 A's, 38 B's, 23 C's, 8 D's, and 4 F's.

Entropy (in bits):

✓ Answer: 2.005

Explanation

Entropy =  $0.27 \cdot \log_2(100/27) + 0.38 \cdot \log_2(100/38) + 0.23 \cdot \log_2(100/23) + 0.08 \cdot \log_2(100/8) + 0.04 \cdot \log_2(100/4)$

Enviar

**i** Answers are displayed within the problem

## Discussion






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**Topic:** 1. Basics of Information / LE1.2

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- |                                                                                     |                                                                                                                                                                                   |      |
|-------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|
|    | <u>[typo] missing word</u><br>"each the following", should be "each of the following" #typo                                                                                       | 1 ▼  |
|    | <u>B outcome.</u><br>ha. B got me. listen to my better judgement :)                                                                                                               | 5 ▼  |
|  | <u>2 bits are sufficient for question (C)???</u><br>we have five grades, So we require 3 bits to represent 5 grades i.e 000 for A,001 for B,010 for C,01...                       | 2 ▼  |
|  | <u>Shannon's Information Formula Not Intuitive</u><br>For an unfair coin flip, where $p(\text{heads}) = 0.999$ and $p(\text{tail})=0.001$ and the coin is flipped once, If I w... | 11 ▼ |
|  | <u>Computational Power</u><br>Tremendous computational power of the calculator at the bottom of the page. With this computati...                                                  | 1 ▼  |