

Stacks and Procedures: 1

12 points possible (ungraded)

Harry Hapless is a friend struggling to finish his Lab; knowing that you completed it successfully, he asks your help understanding the operation of the quicksort procedure, which he translated from the Python code given in the lab handout:

```
def quicksort(array, left, right):
    if left < right:
        pivotIndex = partition(array, left, right)
        quicksort(array, left, pivotIndex-1)
        quicksort(array, pivotIndex+1, right)
```

You recall from your lab that each of the three arguments and the local variable are 32-bit binary integers. You explain to Harry that quicksort returns no value, but is called for its effect on the contents of a region of memory dictated by its argument values. Harry asks some questions about the possible effect of the call **quicksort(0×1000, 0×10, 0×100)**:

0

9

0

2F0

94C

F94

1

2

3

4

8

0

2F0

F24

FCC

2F0

0

9

9
 8
 7
 2F0
 F48
 FF0
 BP → 2F0
 0
 8
 6
 SP →

1. Given the above call to **quicksort**, what is the region of memory locations (outside of the stack) that might be changed?

Lowest memory address possibly effected: 0x

Answer: 1040

Highest memory address possibly effected: 0x

Answer: 1400

Explanation

The lowest memory address where an element of the array is stored is $\text{array}[\text{left}] = 0 \times 1000 + 4 \times 0 \times 10 = 0 \times 1040$. The highest memory address of the array is $\text{array}[\text{right}] = 0 \times 1000 + 4 \times 0 \times 100 = 0 \times 1400$.

Harry's translation of quicksort to Beta assembly language appears above on the right.

2. What register did Harry choose to hold the value of the variable **pivotIndex**?

Register holding pivotIndex value: R

Answer: 4

```

quicksort:
    PUSH(LP)
    PUSH(BP)
    MOVE(SP, BP)
    PUSH(R1)
    PUSH(R2)
    PUSH(R3)
    PUSH(R4)

    LD(BP, -12, R1)
    LD(BP, -16, R2)
aa:    LD(BP, -20, R3)

    CMPLT(R2, R3, R0)
    BF(R0, qx)

    PUSH(R3)
    PUSH(R2)
    PUSH(R1)
    BR(partition, LP)
    DEALLOCATE(3)
    MOVE(R0, R4)
xx:

    SUBC(R4, 1, R0)
    PUSH(R0)
    PUSH(R2)
    PUSH(R1)
    BR(quicksort, LP)
    DEALLOCATE(3)

    PUSH(R3)
    ADDC(R4, 1, R0)
    PUSH(R0)
    PUSH(R1)
    BR(quicksort, LP)
bb:    DEALLOCATE(3)

qx:    POP(R4)
        POP(R3)
        POP(R2)
        POP(R1)
cc:    MOVE(BP, SP)
        POP(BP)
        POP(LP)
        JMP(LP)
  
```

Explanation

If you look at the **MOVE(R0, R4)** that comes 2 instructions after the call to partition, you see that the result of partition (R0) is moved to R4. The variable that receives the result of partition is **pivotIndex**.

After loading and assembling this code in BSim, Harry has questions about its translation to binary.

3. Give the hex value of the 32-bit machine instruction with the tag **aa** in the program to the right.

Hex translation of instruction at aa: 0x

Answer: 607BFFEC

Explanation

The assembled format of the instruction **LD(BP, -20, R3)** is:

opcode | Rc | Ra | literal = LD | R3 | R27 | -20

= 011000 00011 11011 0xFFEC = 0110 0000 0111 1011 0xFFEC = 0x607BFFEC

Harry tests his code, which seems to work fine. He questions whether it could be shortened by simply eliminating certain instructions.

4. Would Harry's quicksort continue to work properly if the instruction at **bb** were eliminated? If the instruction at **cc** were eliminated? Indicate which, if any, of these instructions could be deleted.

OK to delete instruction at bb?

☐ Yes

☒ No
✓

OK to delete instruction at cc?

☒ Yes
✓

☐ No

Explanation

If you remove the DEALLOCATE instruction at label **bb**, then you would end up popping the wrong values at label **qx**.

If you remove the MOVE(BP, SP) instruction at label **cc**, everything will still work because there were no local variables allocated in the implementation of this procedure so SP already equals BP after you pop the used registers.

Harry runs his code on one of the Lab test cases, which executes a call to **quicksort(Y, 0, X)** via a **BR(quicksort, LP)** at address **0x948**. Harry halts its execution just as the instruction following the **xx** tag is about to be executed. The contents of a region of memory containing the topmost locations on the stack is shown to the right.

5. What are the arguments to the current quicksort call? Use the stack trace shown above to answer this question.

Arguments: array = 0x

Answer: 2F0

left = 0x

Answer: 7

right = 0x

Answer: 8

Explanation

The stack frame for one call to **quicksort** is:

Right

Left

Array

LP

BP

R1

R2

R3

R4

The three arguments (array, left, and right) are put on the stack in reverse order. Then we store the LP, then the BP and then R1-R4 so that we can use those registers within our procedure.

Since we are told that the program halts at the **xx** label, we know that we just deallocated the 3 arguments for the partition procedure call and are now ready to continue with the recursive quicksort calls. This means that the SP is pointing immediately following a full stack frame. This information helps us label our stack as follows:

0	
9	Right
9	Left
2F0	Array
94C	LP
F94	BP
1	R1
2	R2
3	R3
4	R4
8	Right
0	Left
2F0	Array
F24	LP
FCC	BP
2F0	R1
0	R2
9	R3
9	R4
8	Right
7	Left
2F0	Array
F48	LP
FF0	BP
BP → 2F0	R1
0	R2
8	R3
6	R4

SP →

The current quicksort call is the bottom most one. We see that the arguments for that call are array = 0×2F0, Left = 7, and Right = 8.

6. What is the value **X** in the original call **quicksort(Y, 0, X)**?

Value of X in original call: 0x

Answer: 9

Explanation

Since we are told that the original call to the **quicksort** procedure is from a branch instruction at address 0x948, we know that the LP register from that initial call holds the address of the instruction following that branch which is 0x94C. If we search our stack trace for LP = 0x94C, we see that the topmost stack frame corresponds to that original call to **quicksort**. The arguments in that stack frame are the arguments to the original call to **quicksort**. X is the value of right which is 9.

7. What were the contents of R4 when the original call to **quicksort(Y, 0, X)** was made?

Contents of R4 at original call: 0x

Answer: 4

Explanation

Since we know that the top stack frame corresponds to the original call to **quicksort**, we know that the original contents of register R4 was 4.

8. What is the address of the instruction tagged **bb** in the program?

HEX value of bb: 0x

Answer: F48

Explanation

Looking at the various stack frames in our stack trace, we see that in one of the calls to quicksort LP = 0xF24 and in the other LP = 0xF48. The instruction tagged **bb** corresponds to the second call to **quicksort** where LP = 0xF48.

Submit

i Answers are displayed within the problem

Stacks and Procedures: 2

11 points possible (ungraded)

The following C program implements a function (ffo) of two arguments, returning an integer result. The assembly code for the procedure is shown on the right, along with a partial stack trace showing the execution of **ffo(0xDECAF,0)**. The execution has been halted just as the Beta is about to execute the instruction labeled **rtn**, i.e., the value of the Beta's program counter is the address of the first instruction in POP(R1). In the C code below, note that "**v>>1**" is a logical right shift of the value v by 1 bit.

```
// bit position of left-most 1
int ffo(unsigned v, int b) {
    if (v == 0) ???;
    else return ffo(v>>1,b+1);
}
```

BP →

0x000F
0x001B
0x0208
0x012C
0x001B
0x0010
0x000D
0x0208
0x0140
0x000D
0x0011
0x0006
0x0208
0x0154
0x0006
0x0012
0x0003

ffo:	PUSH(LP) PUSH(BP) MOVE(SP,BP) PUSH(R1)
	LD(BP,-16,R0) LD(BP,-12,R1)
xxx:	BEQ(R1,rtn)
	ADDC(R0,1,R0) PUSH(R0) SHRC(R1,1,R1) PUSH(R1) BR(ffo,LP) DEALLOCATE(2)
rtn:	POP(R1) MOVE(BP,SP) POP(BP) POP(LP) JMP(LP)

1. Examining the assembly

language for ffo, what is the appropriate C code for ??? in the C representation for ffo?

C code for ???:

☐ return v

☒ return b



☐ return 0

☐ return ffo(v>>1,b)

Explanation

If we follow the assembly code, we see that the two **LD** operations load the arguments b into R0 and v into R1. At label 'xxx', we then check if R1 = 0 and if so return. The value returned is always in R0 which was just loaded with b, so that means that we are returning b when v = 0.

2. What value will be returned from the procedure call `ffo(3,100)`?

Value returned from procedure call `ffo(3,100)`:

Answer: 102

Explanation

$\text{ffo}(3,100) = \text{ffo}(1,101) = \text{ffo}(0,102) = 102.$

3. What are the values of the arguments in the call to `ffo` from which the Beta is about to return? Please express the values in hex or write "CAN'T TELL" if the value cannot be determined.

Value of argument `v` or "CAN'T TELL": 0x

Answer: 6

Value of argument `b` or "CAN'T TELL": 0x

Answer: 11

Explanation

The stack frame for one call to **`ffo`** is:

b

v

LP

BP

R1

The two argument (*v*, *b*) are put on the stack in reverse order. Then we store the LP, then the BP and then any registers that we will use to compute intermediate data (*R1*) so that they can be restored at the end of the procedure call.

We know that the value immediately above the current BP, is the old BP. Using that information, we can fill in the elements of each stack frame in our trace as follows.

0x000F ***b***

0x001B ***v***

0x0208 ***LP***

0x012C ***BP***

0x001B ***R1***

0x0010 ***b***

0x000D ***v***

0x0208 ***LP***

0x0140 BP
0x000D R1
0x0011 b
0x0006 v
0x0208 LP
0x0154 BP
BP → **0x0006** R1
0x0012
0x0003

The program stops just before we execute the instruction labelled **rtn**, this means that we have not yet popped R1 off of the stack. So we are at our bottom-most stack frame where v = 0x6 and b = 0x11.

4. Determine the specified values at the time execution was halted. Please express each value in hex or write "CAN'T TELL" if the value cannot be determined.

Value in R1 or "CAN'T TELL": 0x

Answer: 3

Value in BP or "CAN'T TELL": 0x

Answer: 168

Value in LP or "CAN'T TELL": 0x

Answer: 208

Value in SP or "CAN'T TELL": 0x

Answer: 16C

Value in PC or "CAN'T TELL": 0x

Answer: 20C

Explanation

Using the labeled stack trace that we just produced in part C, we can also determine the addresses where these stack trace elements are stored in memory by making use of the stored BP values.

Starting from the bottom of the trace, we find an old BP = 0x0154. The old BP points to the previous saved copy of R1, so we can label the previous R1 element, 0x000D as being at address 0x0154. From there, we can add/subtract 4 to determine the remaining addresses.

The resulting labeled stack with addresses is:

	Hex Value	Variable	Hex address
	$0x000F$	b	
	$0x001B$	v	
	$0x0208$	LP	
	$0x012C$	BP	
	$0x001B$	R1	
	$0x0010$	b	
	$0x000D$	v	
	$0x0208$	LP	
	$0x0140$	BP	
	$0x000D$	R1	0×154
	$0x0011$	b	0×158
	$0x0006$	v	$0 \times 15C$
	$0x0208$	LP	0×160
	$0x0154$	BP	0×164
$BP \rightarrow$	$0x0006$	R1	0×168
	$0x0012$		$0 \times 16C$
	$0x0003$		

This tells us that $BP = 0 \times 168$, and $LP = 0 \times 208$. We also know that just before executing the instruction at label **rtm**, we have not yet popped $R1$, so that means that the SP is one location below the current BP , and therefore $SP = 0 \times 16C$. $R1$ contains the value of the previously popped $R1$, which means that if we are about to pop the value 0×0006 into $R1$, the previous value popped into $R1$ is 0×0006 shifted to the right by 1 which is 0×0003 . Finally, we need to determine the value of PC . PC points to the **rtm** instruction. We know that LP stores the return address from the call to `ffo` (the address of the `DEALLOCATE(2)` instruction), since $LP = 0208$, we know that the `DEALLOCATE` instruction is at address 0×208 . This means that the **rtm** label is at address $0 \times 20C$, so $PC = 0 \times 020C$.

5. What is the address of the BR instruction for the original call to ffo(0xDECAF,0)? Please express the value in hex or "CAN'T TELL".

Address of the original BR, or "CAN'T TELL": 0x

Answer: CAN'T TELL

Explanation

From the stack trace we see that all the stored LP values are the same, 0x0208. We know that this is the return address of the recursive call to ffo, which means that we don't have any information in this stack trace about the return address of the original call to ffo, so the answer is CAN'T TELL.

6. A 6.004 student modifies ffo by removing the DEALLOCATE(2) macro in the assembly compilation of the ffo procedure, reasoning that the MOVE(BP,SP) will perform the necessary adjustment of stack pointer. She runs a couple of tests and verifies that the modified ffo procedure still returns the same answer as before. Does the modified ffo obey our procedure call and return conventions?

Does modified ffo obey call/return conventions?

Answer: No

Explanation

Our procedure call and return conventions require all registers to be restored to their original value except for R0 which should contain the correct answer. If the DEALLOCATE(2) macro is removed from the code, then the value of R1 would not be restored correctly. The value of v would be popped into R1 upon each return sequence of ffo.

i Answers are displayed within the problem

Stacks and Procedures: 3

13 points possible (ungraded)

It was mentioned in lecture that recursion became a popular programming construct following the adoption of the stack as a storage allocation mechanism, ca. 1960. But the Greek mathematician Euclid, always ahead of his time, used recursion in 300 BC to compute the greatest common divisor of two integers. His elegant algorithm, translated to C from the ancient greek, is shown below:

```
int gcd(int a, int b) {  
    if (a == b) return a;  
    if (a > b) return gcd(a-b, b);  
    else return gcd(a, b-a);  
}
```

The procedure **gcd(a, b)** takes two positive integers **a** and **b** as arguments, and returns the greatest positive integer that is a factor of both **a** and **b**.

Note that the base case for this recursion is when the two arguments are equal (`==` in C tests for equality), and that there are two recursive calls in the body of the procedure definition.

Although Euclid's algorithm has been known for millennia, a recent archeological dig has uncovered a new document which appears to be a translation of the above C code to Beta assembly language, written in Euclid's own hand. The Beta code is known to work properly, and is shown below.

```
gcd:    PUSH(LP)
        PUSH(BP)
        MOVE(SP, BP)
        PUSH(R1)
        PUSH(R2)
        LD(BP, -12, R0)
        LD(BP, -16, R1)
        CMPEQ(R0, R1, R2)
        BT(R2, L1)
        CMPL(R0, R1, R2)
xxx:    BT(R2, L2)
        PUSH(R1)
        SUB(R0, R1, R2)
        PUSH(R2)
        BR(gcd, LP)
        DEALLOCATE(2)
        BR(L1)

L2:     SUB(R1, R0, R2)
        PUSH(R2)
        PUSH(R0)
        BR(gcd, LP)
        DEALLOCATE(2)

L1:     POP(R2)
        POP(R1)
yyy:    MOVE(BP, SP)
        POP(BP)
        POP(LP)
        JMP(LP)
```

1. Give the 32-bit binary translation of the **BT(R2,L2)** instruction at the label **xxx**
opcode (6 bits): 0b

Rc (5 bits): 0b

Ra (5 bits): 0b

literal (16 bits): 0b

2. One historian studying the code, a Greek major from Harvard, questions whether the **MOVE(BP, SP)** instruction at **yyy** is really necessary. If this instruction were deleted from the assembly language source and re-translated to binary, would the shorter Beta program still work properly?

Still works?

Select an option ▼

```
main:  CMOVE(0x104, SP)
        PUSH(R17)
        PUSH(R18)
        BR(gcd, LP)
zzz:   HALT()
```

At a press conference, the archeologists who discovered the Beta code give a demonstration of it in operation. They use the test program shown above to initialize SP to hex **0x104**, and call gcd with two positive integer arguments from **R17** and **R18**. Unfortunately, the values in these registers have not been specified.

Address in Hex Data in Hex

100 :	104
104 :	18
108 :	9
10C :	D8
110 :	D4
114 :	EF
118 :	BA
11C :	F
120 :	9
124 :	78
128 :	114
12C :	18
130 :	F
134 :	6
138 :	9

13C :	78
140 :	12C
144 :	<i>F</i>
148 :	6
14C :	6
150 :	3
154 :	58
158 :	144
<i>SP</i> → 15C :	6

They start their program on a computer designed to approximate the computers of Euclid's day (think of Moore's law extrapolated back to 300 BC!), and let it run for a while. Before the call to gcd returns, they stop the computation just as the instruction at **yyy** is about to be executed, and examine the state of the processor.

They find that **SP** (the stack pointer) contains **0x15C**, and the contents of the region of memory containing the stack as shown **(in HEX)** to the right.

You note that the instruction at **yyy**, about to be executed, is preparing for a return to a call from gcd(a,b).

3. What are the values of **a** and **b** passed in the call to gcd which is about to return?
Answer in HEX.

Args to current call: a=0x

b = 0x

4. What are the values of **a** and **b** passed in the *original* call to gcd, from registers **R17** and **R18**? Answer in HEX.

Args to original call: a=0x

b = 0x

5. What is the address corresponding to the tag **zzz:** of the **HALT()** following the original call to **gcd**?

Address of zzz: (HEX): 0x

6. What is the address corresponding to the tag **L1**: in the assembly b for **gcd**?

Address of L1: (HEX): 0x

7. What value will be returned (in R0) as the result of the original call to **gcd**?

Value returned to original caller: (HEX): 0x

8. What was the value of R2 at the time of the original call to gcd?

Original value in R2: (HEX): 0x

Submit

Stacks and Procedures: 4

15 points possible (ungraded)

You are given the following listing of a C program and its translation to Beta assembly code:

```
int f(int x, int y)
    int a = x - 1; b = x + y;
    if (x == 0) return y;
    return f(a, ???)
```



```
f:    PUSH(LP)
      PUSH(BP)
mm:   MOVE(SP, BP)
      PUSH(R1)
      PUSH(R2)
      LD(BP, -16, R0)
yy:   LD(BP, -12, R1)
      BEQ(R1, xx)
      SUBC(R1, 1, R2)
      ADD(R0, R1, R1)
      PUSH(R1)
      PUSH(R2)
      BR(f, LP)
zz:   DEALLOCATE(2)
      LD(BP, -16, R1)
      ADD(R1, R0, R0)
      PUSH(R0)
ww:   PUSH(R2)
      BR(f, LP)
      DEALLOCATE(2)
xx:   POP(R2)
      POP(R1)
      POP(BP)
      POP(LP)
      JMP(LP)
```

1. Fill in the binary value of the **LD** instruction stored at the location tagged **yy** in the above program.

opcode (6 bits): 0b

Rc (5 bits): 0b

Ra (5 bits): 0b

literal (16 bits): 0b

2. Suppose the MOVE instruction at the location tagged **mm** were eliminated from the above program. Would it continue to run correctly?

Still works fine?

☐ Yes

☐ Can't Tell

☐ No

3. What is the missing expression designated by **???** in the C program above.

☐ b

☐ y

☐ y + f(a,b)

☐ f(a,b)

The procedure f is called from location 0xFC and its execution is interrupted during a recursive call to f, just prior to the execution of the instruction tagged **xx**. The contents of a region of memory, including the stack, are shown to the left.

NB: All addresses and data values are shown in hex. The **BP** register contains **0x494**, and **SP** contains **0x49C**.

Address in Hex Contents in Hex

448	2
44C	4
450	7
454	3
458	2
45C	100
460	D4
464	3
468	4
46C	5

470	1
474	50
478	???
47 <i>C</i>	5
480	1
484	<i>B</i>
488	0
48 <i>C</i>	70
490	47 <i>C</i>
<i>BP</i> → 494	5
498	0
<i>SP</i> → 49 <i>C</i>	

4. What are the arguments to the *most recent* active call to **f**?

Most recent arguments (HEX): x = 0x

$$y = 0x$$

5. What value is stored at location **0x478**, shown as **???** in the listing to the left?

Contents 0x478 (HEX): 0x

6. What are the arguments to the *original* call to **f**?

Original arguments (HEX): x = 0x

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$$y = 0x$$

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7. What value is in the **LP** register?

Contents of LP (HEX): 0x

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8. What value was in **R1** at the time of the original call?

Contents of R1 (HEX): 0x

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9. What value is in **R0**?

Value currently in R0 (HEX): 0x

10. What is the hex address of the instruction tagged **ww**?

Address of ww (HEX): 0x?

Submit

Stacks and Procedures: 5

17 points possible (ungraded)

The **wfps** procedure determines whether a string of left and right parentheses is well balanced, much as your Turing machine of Lab 4 did. Below is the code for the **wfps** ("well-formed paren string") procedure in C, as well as its translation to Beta assembly code.

```
int STR[100];                // string of parens

int wfps(int i,               // current index in STR
          int n)              // LPARENs to balance

{ int c = STR[i];             // next character
  int new_n;                   // next value of n
  if (c == 0)                  // if end of string,
    return (n == 0);           //   return 1 iff n == 0
  else if (c == 1)             // on LEFT PAREN,
    new_n = n+1;               //   increment n
  else {                       // else must be RPAREN
    if (n == 0) return 0;       // too many RPARENS!
    xxxxx; }                   // MYSTERY CODE!
  return wfps(i+1, new_n);     // and recurse.
}
```

```

STR:  . = .+4*100
wfps: PUSH(LP)
      PUSH(BP)
      MOVE(SP, BP)
      ALLOCATE(1)
      PUSH(R1)
      LD(BP, -12, R0)
      MULC(R0, 4, R0)
      LD(R0, STR, R1)
      ST(R1, 0, BP)
      BNE(R1, more)
      LD(BP, -16, R0)
      CMPEQC(R0, 0, R0)
rtn:  POP(R1)
      MOVE(BP, SP)
      POP(BP)
      POP(LP)
      JMP(LP)
more: CMPEQC(R1, 1, R0)
      BF(R0, rpar)
      LD(BP, -16, R0)
      ADDC(R0, 1, R0)
      BR(par)
rpar: LD(BP, -16, R0)
      BEQ(R0, rtn)
      ADDC(R0, -1, R0)
par:  PUSH(R0)
      LD(BP, -12, R0)
      ADDC(R0, 1, R0)
      PUSH(R0)
      BR(wfps, LP)
      DEALLOCATE(2)
      BR(rtn)

```

wfps expects to find a string of parentheses in the integer array stored at **STR**. The string is encoded as a series of **32-bit integers** having values of

- **1** to indicate a left paren,
- **2** to indicate a right paren, or
- **0** to indicate the end of the string.

These integers are stored in consecutive 32-bit locations starting at the address **STR**.

wfps is called with two arguments:

1. The first, **i**, is the index of the start of the part of **STR** that this call of **wfps** should examine. Note that indexes start at 0 in C. For example, if **i** is 0, then **wfps** should examine the entire string in **STR** (starting at the first character, or **STR[0]**). If **i** is

2. The second argument, **n**, is zero in the original call; however, it may be nonzero in recursive calls.

Note that the compiler may use some simple optimizations to simplify the assembly-language version of the code, while preserving equivalent behavior.

1. Fill in the binary value of the instruction stored at the location tagged **more** in the above assembly-language program.

☐ Yes

☐ No

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○ *BP* – 16

○ *BP* – 12

○ *BP* – 8

 $\bigcirc \text{ } BP + 0$ $\bigcirc \text{ } BP + 4$

○ $BP + 8$

○ *NA*

3. Is the variable `new_n` from the C program stored as a local variable in the stack frame?

☐ Yes

☐ No

If so, give its (signed) offset from BP; else select "NA".

○ *BP* – 16

○ *BP* – 12

○ *BP* – 8

 $\bigcirc \text{ } BP + 0$

○ $BP + 4$

○ $BP + 8$

☐ *NA*

4. What is the missing C source code represented by xxxxx in the given C program?

☐ `n = n + 1`
☐ `n = n - 1`
☐ `new_n = n + 1`
☐ `new_n = n - 1`
☐ `new_n = n`

The procedure **wfps** is called from an external procedure and its execution is interrupted during a recursive call to **wfps**, just prior to the execution of the instruction labeled **rtn**. The contents of a region of memory are shown below. At this point, **SP** contains 0×1D8, and **BP** contains 0×1D0.

NOTE: All addresses and data values are shown in hexadecimal.

Address in Hex Contents in Hex

188:	7
18C:	4A8
190:	0
194:	0
198:	458
19C:	D4
1A0:	1
1A4:	D8
1A8:	1
1AC:	1
1B0:	3B8
1B4:	1A0
1B8:	2
1BC:	1
1C0:	0
1C4:	2
1C8:	3B8

1CC: 1B8

BP→1D0: **2**

1D4: **2**

SP→1D8: 0

5. What are the arguments to the *most recent* active call to **wfpps**?

Most recent arguments (HEX): i = 0x

n = 0x

6. What are the arguments to the *original* call to **wfps**?

Original arguments (HEX): i = 0x

n = 0x

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7. What value is in **R0** at this point?

Contents of R0 (HEX): 0x

8. How many parens (left and right) are in the string stored at STR (starting at index 0)? Give a number, or **"CAN'T TELL"** if the number can't be determined from the given information.

Length of string, or "CAN'T TELL":

☐ Can't Tell

9. What is the hex address of the instruction tagged **par**?

Address of par (HEX): 0x

10. What is the hex address of the **BR** instruction that called **wfps** originally?

Address of original call (HEX): 0x

Submit

Stacks and Procedures: 6

13 points possible (ungraded)

You've taken a summer internship with BetaSoft, the worlds largest supplier of Beta software. They ask you to help with their library procedure **sqr(j)**, which computes the square of a non-negative integer argument **j**. Because so many Betas don't have a multiply instruction, they have chosen to compute **sqr(j)** by adding up the first **j** odd integers, using the C code below and its translation to Beta assembly language to the left.

```
int sqr(j) {
    int s = 0;
    int k = j;
    while (k != 0) {
        s = s + nthodd(k);
        k = k - 1;
    }
    return s;
}

int nthodd(n) {
    if (n == 0) return 0;
    return ???;
}
```

You notice that the **sqr** procedure takes an integer argument **j**, and declares two local integer variables **s** and **k** (initialized to zero and **j**, respectively).

The body of **sqr** is a loop that is executed repeatedly, decrementing the value of **k** at each iteration, until **k** reaches zero. Each time through the loop, the local variable **s** incremented by the value of the **k**th odd integer, a value that is computed by an auxiliary procedure **nthodd**.

1. What is the missing expression shown as **???** in the C code defining **nthodd** above?

What is the missing expression denoted ??? in above C code:

```

sqr:    PUSH (LP)
        PUSH (BP)
        MOVE (SP, BP)
        ALLOCATE(2)
        PUSH (R1)
        ST(R31, 0, BP)
        LD (BP, -12, R0)
        ST(R0, 4, BP)
loop:   LD(BP, 4, R0)
        BEQ(R0, done)
        PUSH(R0)
        SUBC(R0, 1, R0)
        ST(R0, 4, BP)
        BR(nthodd, LP)
        DEALLOCATE(1)
        LD(BP, 0, R1)
        ADD(R0, R1, R1)
        ST(R1, 0, BP)
        BR(loop)
done:   LD(BP, 0, R0)
        POP(R1)
        DEALLOCATE(2)
        MOVE(BP, SP)
        POP(BP)
        POP(LP)
        JMP(LP)

nthodd: PUSH (LP)
        PUSH (BP)
        MOVE (SP, BP)
        LD (BP, -12, R0)
        BEQ(R0, zero)
        ADD(R0, R0, R0)
        SUBC(R0, 1, R0)
zero:   MOVE(BP, SP)
        POP(BP)
        POP(LP)
        JMP(LP)

```

2. What variable in the C code, if any, is loaded into R0 by the LD instruction tagged **loop**? Answer "none" if no such value is loaded by this instruction.

Value loaded by instruction at loop:, or "none":

Using a small test program to run the above assembly code, you begin computing **sqr(X)** for some positive integer **X**, and stop the machine during its execution. You notice, from the value in the PC, that the instruction tagged **zero** is about to

be executed. Examining memory, you find the following values in a portion of the area reserved for the Beta's stack.

F0: *F4*
 F4: *5*
 F8: *EC*
 FC: *D4*
 100: *15*
 104: *1*
 108: *DECAF*
 10C: *2*
 110: *4C*
 114: *100*
 BP¹¹⁸: *0*
 →

NB: All values are in HEX! Give your answers in hex, or write "CAN'T TELL" if you can't tell.

You notice that BP contains the value **0×118**.

3. What argument (in hex) was passed to the current call to **nthodd**? Answer "CAN'T TELL" if you can't tell.

HEX Arg to nthodd, or "CAN'T TELL": 0x

4. What is the value **X** that was passed to the original call to **sqr(X)**? Answer "CAN'T TELL" if you can't tell.

HEX Arg X to sqr, or "CAN'T TELL": 0x

5. What is the hex value in **SP**? Answer "CAN'T TELL" if you can't tell.

HEX Value in SP, or "CAN'T TELL": 0x

6. What is the current value of the variable **k** in the C code for **sqr**? Answer "CAN'T TELL" if you can't tell.

HEX Value of k in sqr, or "CAN'T TELL": 0x

7. The test program invoked **sqr(X)** using the instruction **BR(sqr,LP)**. What is the address of that instruction? Answer "CAN'T TELL" if you can't tell.

HEX Address of BR instruction that called sqr, or "CAN'T TELL": 0x

8. What value was in R1 at the time of the call to **sqr(X)**? Answer “CAN'T TELL” if you can't tell.

HEX Value in R1 at call to sqr, or “CAN'T TELL”: 0x

Your boss at BetaSoft, Les Ismoore, suspects that some of the instructions in the Beta code could be eliminated, saving both space and execution time. He hands you an annotated listing of the code (shown below), identical to the original assembly code but with some added tags.

```

sqr:    PUSH (LP)
        PUSH (BP)
        MOVE (SP, BP)
        ALLOCATE(2)
        PUSH (R1)
        ST(R31, 0, BP)
        LD (BP, -12, R0)
        ST(R0, 4, BP)
loop:   LD(BP, 4, R0)
        BEQ(R0, done)
        PUSH(R0)
        SUBC(R0, 1, R0)
        ST(R0, 4, BP)
        BR(nthodd, LP)
        DEALLOCATE(1)
        LD(BP, 0, R1)
        ADD(R0, R1, R1)
        ST(R1, 0, BP)
        BR(loop)
done:   LD(BP, 0, R0)
        POP(R1)
q1:     DEALLOCATE(2)
        MOVE(BP, SP)
        POP(BP)
        POP(LP)
        JMP(LP)
nthodd: PUSH (LP)
q5:     PUSH (BP)
q2:     MOVE (SP, BP)
        LD (BP, -12, R0)
        BEQ(R0, zero)
        ADD(R0, R0, R0)
        SUBC(R0, 1, R0)
zero:   MOVE(BP, SP)
        POP(BP)
        POP(LP)
        JMP(LP)

```

Les proposes several optimizations, each involving just the deletion of one or more instructions from the annotated code. He asks, in each case, whether the resulting code would still work properly. For each of the following proposed deletions, select “OK” if the code would still work after the proposed deletion, or “NO” if not. For each question, **assume that the proposed deletion is the ONLY change** (i.e., you needn’t consider combinations of proposed changes).

9. Delete the instruction tagged **q1**.

Proposed deletion OK or NO?

☐ OK☐ NO

10. Delete the instruction tagged **q2**.

Proposed deletion OK or NO?

☐ OK☐ NO

11. Delete the instruction tagged **loop**.

Proposed deletion OK or NO?

☐ OK☐ NO

12. Delete the instruction tagged **zero**.

Proposed deletion OK or NO?

☐ OK☐ NO

After some back-and-forth with Les, he proposes to replace **nthodd** with a minimalist version that avoids much of the standard procedure linkage boilerplate:

```
nthodd: LD (SP, NNN, R0)
        BEQ(R0, zero)
        ADD(R0, R0, R0)
        SUBC(R0, 1, R0)
zero:   JMP(LP)
```

He's quite sure this code will work, but doesn't know the appropriate value for **NNN**.

13. What is the proper value for the constant **NNN** in the shortened version of **nthodd**?

Appropriate value for NNN (in decimal):

Submit

Stacks and Procedures: 7

15 points possible (ungraded)

You are given the following listing of a C program and its translation to Beta assembly code:

```
// Mystery function:
int f(int x, int y) {
    int a = (x+y) >> 1;
    if (a == 0) return y;
    else return ???;
}
```

(Recall that $a \gg b$ means a shifted b bits to the right, propagating – ie, preserving -- sign)

- Fill in the binary value of the BR instruction stored at the location tagged **yy** in the above program.

opcode (6 bits): 0b

Rc (5 bits): 0b

Ra (5 bits): 0b

literal (16 bits): 0b

```
f:  PUSH(LP)
    PUSH(BP)
    MOVE(SP, BP)
    PUSH(R1)
    PUSH(R2)
    LD(BP, -12, R1)
    LD(BP, -16, R0)
    ADD(R0, R1, R2)
    SRAC(R2, 1, R2)

xx:  BEQ(R2, bye)

    SUB(R1, R2, R1)
    PUSH(R1)
    PUSH(R0)

yy:  BR(f, LP)
    DEALLOCATE(2)
    ADD(R2, R0, R0)

bye: POP(R2)
    POP(R1)
zz:  MOVE(BP, SP)
    POP(BP)
    POP(LP)
    JMP(LP)
```


2. Suppose the MOVE instruction at the location tagged **zz** were eliminated from the above program. Would it continue to run correctly?

Still works fine?

☐ YES

☐ NO

3. What is the missing expression designated by **???** in the C program above.

☐ $f(y, a)$

☐ $a + f(y, x)$

☐ $a + f(y, x-a)$

☐ $f(x, -a)$

☐ $f(y, -a)$

The procedure **f** is called from an external procedure and its execution is interrupted during a recursive call to **f**, just prior to the execution of the instruction tagged **bye**. The contents of a region of memory are shown below.

NB: All addresses and data values are shown in hex. The **BP** register contains **0x250**, **SP** contains **0x258**, and **R0** contains **0x5**.

204:	<i>CC</i>
208:	<i>4</i>
20C:	<i>7</i>
210:	<i>6</i>
214:	<i>7</i>
218:	<i>E8</i>
21C:	<i>D4</i>
220:	<i>BAD</i>
224:	<i>BABE</i>
228:	<i>1</i>

22C **6**230 **54**

234

238 **1**23C **6**240 **3**244 **1**248 **54**24C **238*****BP***²⁵⁰: **3**

→

254 **3*****SP***²⁵⁸: **−1**

→

4. What are the arguments to the *most recent* active call to **f**?

Most recent arguments (HEX): x = 0x**y = 0x**

5. Fill in the missing value in the stack trace.
6. What are the arguments to the *original* call to **f**?

Original arguments (HEX): x = 0x**y = 0x**

7. What value is in the **LP** register?

Contents of LP (HEX): 0x

8. What value was in **R1** at the time of the original call?

Contents of R1 (HEX): 0x

9. What value will be returned in R0 as the value of the original call? [HINT: You can figure this out without getting the C code right!].

Value returned to original caller (HEX): 0x

10. What is the hex address of the instruction tagged **yy**?

Address of yy (HEX): 0x

Submit

Stacks and Procedures: 8

15 points possible (ungraded)

You are given the following listing of a C program and its translation to Beta assembly code:

```
int f(int x, int y) {
    int a = (x+y) >> 2;
    if (a == 0) return x;
    else return y + f(a, x+a);
}
```

(Recall that $a \gg b$ means a shifted b bits to the right, propagating -- ie, preserving -- sign)

1. Fill in the binary value of the BEQ instruction stored at the location tagged **laby** in the above program.

opcode (6 bits): 0b

Rc (5 bits): 0b

Ra (5 bits): 0b

```
f:    PUSH(LP)
      PUSH(BP)
      MOVE(SP, BP)
      PUSH(R1)
      LD(BP, -12, R0)
      LD(BP, -16, R1)
      ADD(R0, R1, R1)
      SRAC(R1, 2, R1)
laby: BEQ(R1, laby)

      ADD(R0, R1, R0)
      PUSH(R0)
      PUSH(R1)
      BR(f, LP)
      DEALLOCATE(2)

labz: LD(BP, -16, R1)
      ADD(R1, R0, R0)

labx: POP(R1)
      MOVE(BP, SP)
      POP(BP)
      POP(LP)
      JMP(LP)
```

- Offset of x (in decimal), or “NONE”:**

- Offset of variable a, or “NONE”:**

NB: All addresses and data values are shown in hex. The SP contains 0x1C8.

184:	4
188:	7
18C:	3
190:	5
194:	<i>D0</i>
198:	<i>D4</i>
19C:	<i>D8</i>
1A0:	7
1A4	2
1A8	<i>4C</i>
1AC	<i>19C</i>
1B0	2
1B4	4
1B8	2
1BC	<i>4C</i>

→

-

-

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In the stack trace, I expected to see a value of R0 right after the value of R1 since we have a "P...	
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Is it just me, or does the stack of question set 4 have a small error? There is a small section at Q...	
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Per the explanation, the result of a recursive call to f is returned in R0. How does it get there?	
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In the answer it's stated that the value of R1 at the time the program is halted is 0×03, given pre...	
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In the program given in stack and procedure:2 under rtn label, if we remove the instruction MOV...	
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In the case of recursion, how will the program know that stack discipline has been achieved? Is...	
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The explanation for part E says: "This means that the BP is pointing immediately following a full...	
[STAFF] Typo on "CAN'T TELL"	3
When stating problems, e.g. Problem 2, question C > Please express the values in hex or write "...	

