CPE 4196

Lecture 4: Machine Learning

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Machine Learning

- Supervised: We are given input samples (X) and output samples (y) of a function y = f(X). We would like to "learn" f, and evaluate it on new data. Types:
 - Classification: y is discrete (class labels).
 - Regression: y is continuous, e.g. linear regression.
- Unsupervised: Given only samples X of the data, we compute a function f such that y = f(X) is "simpler".
 - Clustering: y is discrete
 - Y is continuous: Matrix factorization, Kalman filtering, unsupervised neural networks.

Machine Learning

Supervised:

- Is this image a cat, dog, car, house?
- How would this user score that restaurant?
- Is this email spam?

Unsupervised

- Cluster some hand-written digit data into 10 classes.
- What are the top 20 topics in Twitter right now?
- Separate groups of patients into 2 groups.

Techniques

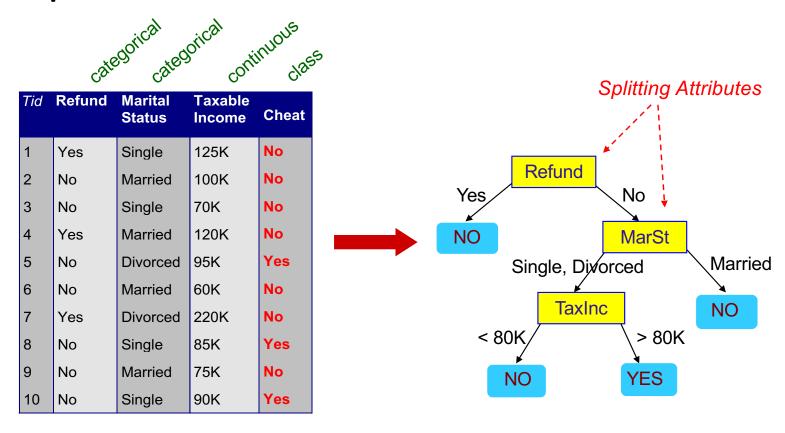
- Supervised Learning:
 - Decision Trees
 - Naïve Bayes
 - kNN (k Nearest Neighbors)
 - Support Vector Machines
- Unsupervised Learning:
 - Clustering

Classification: Definition

- Given a collection of records (*training set*)
 - Each record contains a set of *attributes*, one of the attributes is the *class*.
- Find a *model* for class attribute as a function of the values of other attributes.
- Goal: <u>previously unseen</u> records should be assigned a class as accurately as possible.
 - A *test set* is used to determine the accuracy of the model. Usually, the given data set is divided into training and test sets, with training set used to build the model and test set used to validate it.

Decision Trees

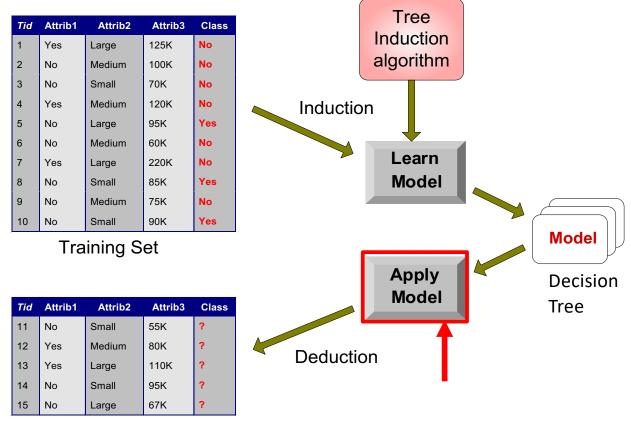
Example of a Decision Tree



Training Data

Model: Decision Tree

Decision Tree Classification Task



Test Set

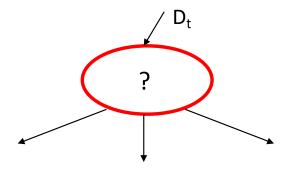
Decision Tree Induction

- Many Algorithms:
 - Hunt's Algorithm (one of the earliest)
 - CART
 - ID3, C4.5
 - SLIQ, SPRINT

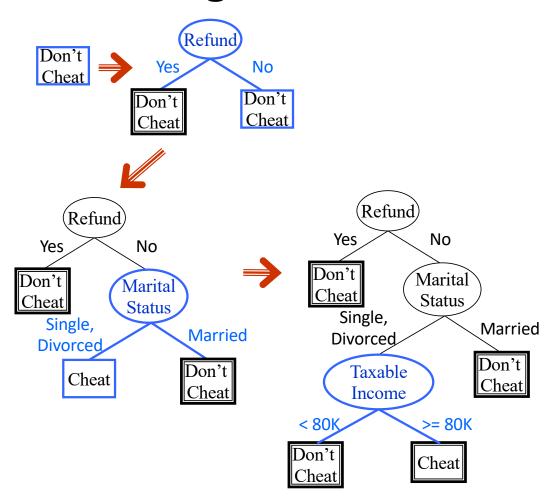
General Structure of Hunt's Algorithm

- Let D_t be the set of training records that reach a node t
- General Procedure:
 - If D_t contains records that belong the same class y_t , then t is a leaf node labeled as y_t
 - If D_t is an empty set, then t is a leaf node labeled by the default class, y_d
 - If D_t contains records that belong to more than one class, use an attribute test to split the data into smaller subsets.
 - Recursively apply the procedure to each subset.

Tid	Refund	Marital Status	Taxable Income	Cheat
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes



Hunt's Algorithm



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Tree Induction

- Greedy strategy.
 - Split the records based on an attribute test that optimizes certain criterion.
- Issues
 - Determine how to split the records
 - How to specify the attribute test condition?
 - How to determine the best split?
 - Determine when to stop splitting

How to Specify Test Condition?

- Depends on attribute types
 - Nominal
 - Ordinal
 - Continuous
- Depends on number of ways to split
 - 2-way split
 - Multi-way split

Splitting Based on Nominal Attributes

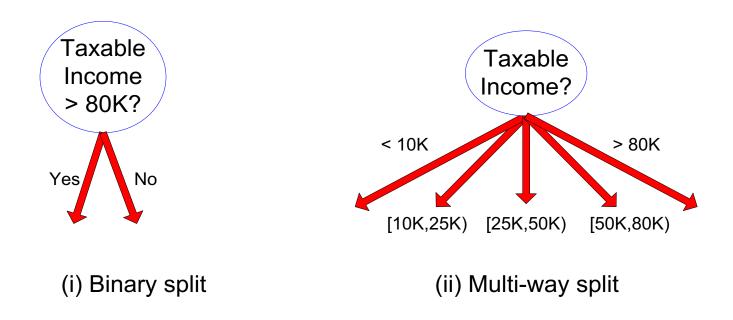
Multi-way split: Use as many partitions as distinct values.



Binary split: Divides values into two subsets.
 Need to find optimal partitioning.



Splitting Based on Continuous Attributes



How to determine the Best Split

- Greedy approach:
 - Nodes with homogeneous class distribution are preferred
- Need a measure of node impurity:

C0: 5 C1: 5

Non-homogeneous,

High degree of impurity

C0: 9

C1: 1

Homogeneous,

Low degree of impurity

Measures of Node Impurity

• Gini Index

Entropy

Misclassification error

Measure of Impurity: GINI

• Gini Index for a given node t :

$$GINI(t) = 1 - \sum_{j} [p(j|t)]^{2}$$

(NOTE: p(j | t) is the relative frequency of class j at node t).

- Maximum $(1-1/n_c)$ when records are equally distributed among all classes, implying least interesting information
- Minimum (0.0) when all records belong to one class, implying most interesting information

C1	0	
C2	6	
Gini=0.000		

C1	1	
C2	5	
Gini=0.278		

C1	2	
C2	4	
Gini=0.444		

C1	3	
C2	3	
Gini=0.500		

Splitting Based on GINI

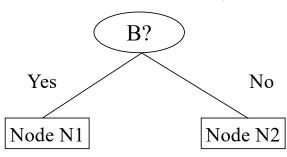
- Used in CART, SLIQ, SPRINT.
- When a node p is split into k partitions (children), the quality of split is computed as,

$$GINI_{split} = \sum_{i=1}^{k} \frac{n_i}{n} GINI(i)$$

where, n_i = number of records at child i, n = number of records at node p.

Binary Attributes: Computing GINI Index

- Splits into two partitions
- Effect of Weighing partitions:
 - Larger and Purer Partitions are sought for.



	Parent	
C1	6	
C2	6	
Gini = 0.500		

$= 1 - (5/7)^2 - (2/7)^2$ $= 0.408$
Gini(N2) = $1 - (1/5)^2 - (4/5)^2$ = 0.32

Gini(N1)

	N1	N2	
C1	5	1	
C2	2	4	
Gini _{split} =0.371			

Categorical Attributes: Computing Gini Index

- For each distinct value, gather counts for each class in the dataset
- Use the count matrix to make decisions

Multi-way split

	CarType		
	Family Sports Luxury		
C1	1	2	1
C2	4	1	1
Gini_{split}	0.393		

Two-way split (find best partition of values)

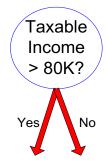
	CarType		
	{Sports, Luxury} {Family}		
C1	3	1	
C2	2	4	
Gini _{split}	0.400		

	CarType		
	{Sports} {Family Luxury		
C1	2	2	
C2	1	5	
Gini _{split}	0.419		

Continuous Attributes: Computing Gini Index

- Use Binary Decisions based on one value
- Several Choices for the splitting value
 - Number of possible splitting values
 - = Number of distinct values
- Each splitting value has a count matrix associated with it
 - Class counts in each of the partitions, A < v and >= v
- Simple method to choose best v
 - For each v, scan the database to gather count matrix and compute its Gini index
 - Computationally Inefficient! Repetition of work.

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1	Yes	Single	125K	No
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9	No	Married	75K	No
10	No	Single	90K	Yes



Continuous Attributes: Computing Gini Index

- For efficient computation: for each attribute,
 - Sort the attribute on values
 - Linearly scan these values, each time updating the count matrix and computing GINI index
 - Choose the split position that has the least GINI index

	Cheat	No			No		N	No Y		s Ye		s	Yes		No		No		o N			No	
·			Taxable Income																				
Sorted Values	\longrightarrow	60			70		7	75		85			9	5 10		00 12		20 1:		25		220	
Split Positions	\longrightarrow	55		6	65		72		80		87		92		97		110		22	172		230	
		<=	>	<=	>	<=	^	<=	^	\=	>	<=	>	<=	>	<=	>	<=	>	<=	>	<=	>
	Yes	0	3	0	3	0	3	0	3	1	2	2	1	3	0	3	0	3	0	3	0	3	0
	No	0	7	1	6	2	5	3	4	3	4	3	4	3	4	4	3	5	2	6	1	7	0
	Gini	0.420		0.4	0.400 0.37		375	0.343		0.417		0.400		<u>0.300</u>		0.343		0.375		0.400		0.420	

Alternative Splitting Criteria based on INFO

Entropy at a given node t:

$$Entropy(t) = -\sum_{j} p(j \mid t) \log p(j \mid t)$$

(NOTE: p(j | t) is the relative frequency of class j at node t).

- Measures homogeneity of a node.
 - Maximum ($\log n_c$) when records are equally distributed among all classes implying least information
 - Minimum (0.0) when all records belong to one class, implying most information
- Entropy based computations are similar to the GINI index computations

Examples for computing Entropy

$$Entropy(t) = -\sum_{j} p(j \mid t) \log_{2} p(j \mid t)$$

$$P(C1) = 0/6 = 0$$
 $P(C2) = 6/6 = 1$

Entropy =
$$-0 \log 0 - 1 \log 1 = -0 - 0 = 0$$

$$P(C1) = 1/6$$
 $P(C2) = 5/6$

Entropy =
$$-(1/6) \log_2 (1/6) - (5/6) \log_2 (1/6) = 0.65$$

$$P(C1) = 2/6$$
 $P(C2) = 4/6$

Entropy =
$$-(2/6) \log_2 (2/6) - (4/6) \log_2 (4/6) = 0.92$$

Splitting Based on INFO...

Information Gain:

$$GAIN_{split} = Entropy(p) - \left(\sum_{i=1}^{k} \frac{n_{i}}{n} Entropy(i)\right)$$

Parent Node, p is split into k partitions; n_i is number of records in partition i

- Measures Reduction in Entropy achieved because of the split. Choose the split that achieves most reduction (maximizes GAIN)
- Used in ID3 and C4.5
- Disadvantage: Tends to prefer splits that result in large number of partitions, each being small but pure.

Splitting Based on INFO...

• Gain Ratio:

$$GainRATIO_{split} = \frac{GAIN_{split}}{SplitINFO}$$

$$SplitINFO = -\sum_{i=1}^{k} \frac{n_{i}}{n} \log \frac{n_{i}}{n}$$

Parent Node, p is split into k partitions n_i is the number of records in partition i

- Adjusts Information Gain by the entropy of the partitioning (SplitINFO).
 Higher entropy partitioning (large number of small partitions) is penalized!
- Used in C4.5
- Designed to overcome the disadvantage of Information Gain

Splitting Criteria based on Classification Error

Classification error at a node t :

$$Error(t) = 1 - \max_{i} P(i \mid t)$$

- Measures misclassification error made by a node.
 - Maximum $(1-1/n_c)$ when records are equally distributed among all classes, implying least interesting information
 - Minimum (0.0) when all records belong to one class, implying most interesting information

Examples for Computing Error

$$Error(t) = 1 - \max_{i} P(i \mid t)$$

$$P(C1) = 0/6 = 0$$
 $P(C2) = 6/6 = 1$

Error =
$$1 - \max(0, 1) = 1 - 1 = 0$$

$$P(C1) = 1/6$$
 $P(C2) = 5/6$

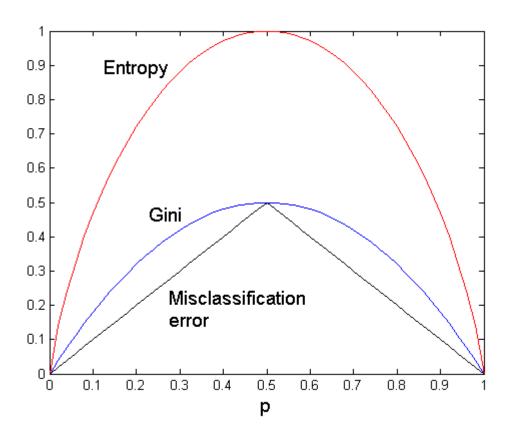
Error =
$$1 - \max(1/6, 5/6) = 1 - 5/6 = 1/6$$

$$P(C1) = 2/6$$
 $P(C2) = 4/6$

Error =
$$1 - \max(2/6, 4/6) = 1 - 4/6 = 1/3$$

Comparison among Splitting Criteria

For a 2-class problem:



Tree Induction

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- Issues
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Stopping Criteria for Tree Induction

- Stop expanding a node when all the records belong to the same class
- Stop expanding a node when all the records have similar attribute values
- Early termination

Decision Tree Based Classification

Advantages:

- Inexpensive to construct
- Extremely fast at classifying unknown records
- Easy to interpret for small-sized trees
- Accuracy is comparable to other classification techniques for many simple data sets

Example: C4.5

- Simple depth-first construction.
- Uses Information Gain
- Sorts continuous attributes at each node.
- Needs entire data to fit in memory.
- Unsuitable for large datasets.
 - Needs out-of-core sorting.
- You can download the software from: http://www.rulequest.com/Personal/