# NHL Structural Model

### **NHL**

```
#loading required libraries
library(tidyverse)
## -- Attaching core tidyverse packages ----- tidyverse 2.0.0 --
## v dplyr
              1.1.2
                        v readr
                                    2.1.4
              1.0.0
                                    1.5.0
## v forcats
                        v stringr
## v ggplot2
              3.4.2
                                    3.2.1
                      v tibble
## v lubridate 1.9.2
                        v tidyr
                                    1.3.0
## v purrr
              1.0.1
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                    masks stats::lag()
## i Use the conflicted package (<a href="http://conflicted.r-lib.org/">http://conflicted.r-lib.org/</a>) to force all conflicts to become error
library(RCurl)
##
## Attaching package: 'RCurl'
## The following object is masked from 'package:tidyr':
##
      complete
library(ggplot2)
#the data
library(RCurl)
link <- getURL("https://raw.githubusercontent.com/M-ttM/Basketball/master/gamedata.csv")</pre>
nhl <- read.csv(text = link)</pre>
head(nhl)
          Date
                           Visitor G
                                                    Home G.1 X Att. LOG Notes
## 1 2017-10-04
                    Calgary Flames 0
                                         Edmonton Oilers 3
                                                                18347 2:34
## 2 2017-10-04
                   St. Louis Blues 5 Pittsburgh Penguins 4 OT 18652 2:38
                                                                             NA
## 3 2017-10-04 Philadelphia Flyers 5
                                         San Jose Sharks 3 17562 2:27
## 4 2017-10-04 Toronto Maple Leafs 7
                                           Winnipeg Jets 2 15321 2:33
                                                                             NA
                                           Anaheim Ducks 5
## 5 2017-10-05
                   Arizona Coyotes 4
                                                                17174 2:38
                                                                             NA
## 6 2017-10-05 Nashville Predators 3
                                           Boston Bruins 4
                                                                17565 2:39
                                                                             NΑ
WEIBULL DISTRIBUTION
install.packages("fitdistrplus")
## Installing package into '/opt/r'
## (as 'lib' is unspecified)
```

```
library(fitdistrplus)

## Loading required package: MASS

##

## Attaching package: 'MASS'

## The following object is masked from 'package:dplyr':

##

## select

## Loading required package: survival

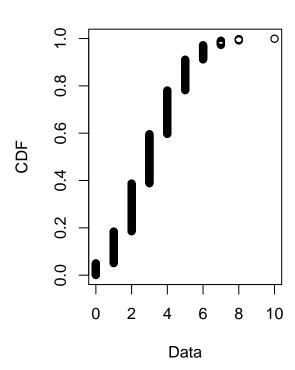
nhl <- nhl %>% mutate(GHadj = G.1+.5, GAadj = G+.5)

plotdist(nhl$G.1, histo = TRUE, demp = TRUE)
```

# **Empirical density**

# Density Data

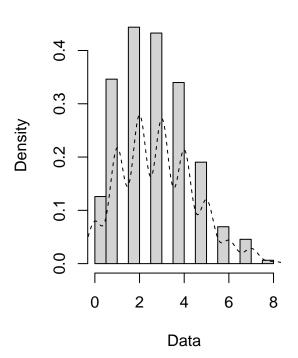
# **Cumulative distribution**

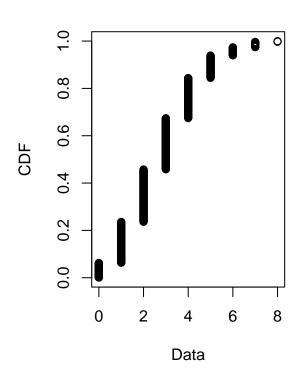


plotdist(nhl\$G, histo = TRUE, demp = TRUE)

# **Empirical density**

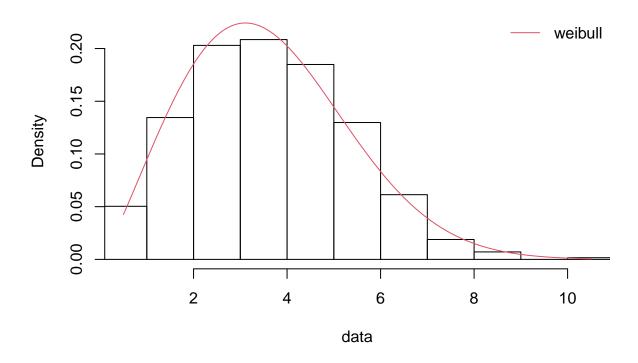
# **Cumulative distribution**





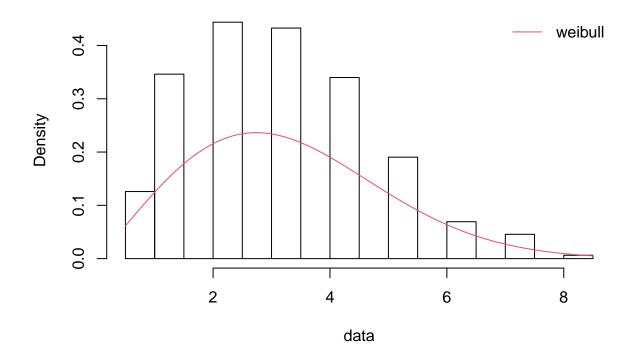
```
fit.GH <- fitdist(nhl$GHadj, "weibull")</pre>
summary(fit.GH)
## Fitting of the distribution 'weibull 'by maximum likelihood
## Parameters :
##
         estimate Std. Error
## shape 2.203528 0.04907325
## scale 4.089189 0.05467170
## Loglikelihood: -2470.345
                               AIC: 4944.689
                                                 BIC: 4954.985
## Correlation matrix:
##
            shape
                     scale
## shape 1.000000 0.305757
## scale 0.305757 1.000000
fit.GA <- fitdist(nhl$GAadj, "weibull")</pre>
summary(fit.GA)
## Fitting of the distribution ' weibull ' by maximum likelihood
## Parameters :
         estimate Std. Error
## shape 2.090796 0.04641639
## scale 3.738554 0.05272833
                               AIC: 4806.073
## Loglikelihood: -2401.036
                                                 BIC: 4816.368
## Correlation matrix:
             shape
                       scale
## shape 1.0000000 0.3083788
## scale 0.3083788 1.0000000
```

# Histogram and theoretical densities



denscomp(fit.GA)

# Histogram and theoretical densities



## WINS PER SEASON PER EXTRA GOAL PER GAME

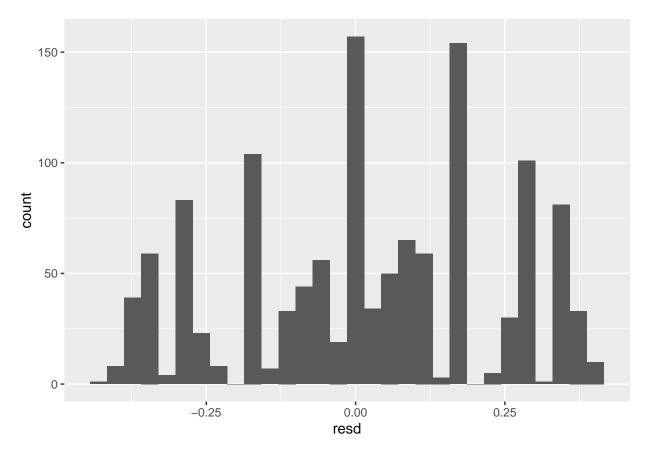
```
WP = GF^{\hat{}}(a) / [GF^{\hat{}}(a) + GA^{\hat{}}(a)]
slope = (a * GF^(a-1) * GA^(a)) / (GF^(a) + GA^{(a))}(2)
a = shape = 2.2
count <- nhl %>%
  group_by(Home) %>%
  summarize(GF = sum(G.1), GA = sum(G))
a = 2.2
count <- count %>%
  mutate(WP = (GF^(a)/(GF^(a) + GA^(a)))) \%\%
  arrange(desc(WP))
count <- count %>%
  mutate(Slope = (a * GF^(a-1) * GA^(a)) / (GF^(a) + GA^(a))^(2))
count <- count %>%
  mutate(xWpS = Slope * 82)
print(count)
## # A tibble: 31 x 6
##
      Home
                                GF
                                       GA
                                             WP
                                                   Slope xWpS
                                                   <dbl> <dbl>
##
      <chr>>
                             <int> <int> <dbl>
```

```
159 101 0.731 0.00272 0.223
## 1 Winnipeg Jets
## 2 Minnesota Wild
                           137 90 0.716 0.00327 0.268
## 3 Colorado Avalanche
                           146 98 0.706 0.00313 0.256
## 4 Vegas Golden Knights 147 103 0.686 0.00322 0.264
## 5 Boston Bruins
                           148 104 0.685 0.00321 0.263
## 6 Pittsburgh Penguins
                         151 110 0.668 0.00323 0.265
## 7 Washington Capitals
                        138 103 0.656 0.00360 0.295
## 8 Nashville Predators
                          143 107 0.654 0.00348 0.285
## 9 Toronto Maple Leafs
                           144 109 0.649 0.00348 0.286
## 10 Dallas Stars
                           128
                               99 0.638 0.00397 0.326
## # i 21 more rows
```

### PER GAME PREDICTION

```
a = 2.2
nhl <- nhl %>%
 mutate(WP = (G.1^(a)/(G.1^(a) + G^(a))),
        diff = G.1 - G,
        Win = ifelse(diff>0, 1, 0)) \%
 arrange(desc(WP))
print(head(nhl))
##
                           Visitor G
                                                      Home G.1 X Att. LOG Notes
          Date
## 1 2017-10-04
                    Calgary Flames 0
                                           Edmonton Oilers
                                                             3 18347 2:34
## 2 2017-10-05 Philadelphia Flyers 0
                                         Los Angeles Kings
                                                             2 18230 2:37
                                                                               NA
## 3 2017-10-06 New York Islanders O Columbus Blue Jackets
                                                             5 18595 2:25
                                                                               NA
## 4 2017-10-07 Nashville Predators 0
                                       Pittsburgh Penguins
                                                            4 18645 2:38
                                                                               NA
## 5 2017-10-08 Montreal Canadiens 0
                                          New York Rangers
                                                            2 18006 2:29
                                                                               NA
                                            Buffalo Sabres
## 6 2017-10-24
                 Detroit Red Wings 0
                                                            1 16882 2:32
    GHadj GAadj WP diff Win
##
## 1
      3.5
            0.5 1
## 2
      2.5
            0.5 1
                          1
## 3
      5.5
            0.5 1
## 4
      4.5
            0.5 1
                          1
## 5
      2.5
            0.5
                      2
## 6
      1.5
            0.5 1
                      1
nhl <- nhl %>%
 mutate(resd = Win - WP)
ggplot(nhl, aes(resd)) +
 geom_histogram()
```

## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



From the plot above, we can understand the predictive ability of the Pythagorean Wins Model. It predicts around 150 estimates with the correct win probability, this means that through goals scored and conceded in the game, 150 times the model predicts the correct probability as the result of the game. If we divide the plot in half from the 0 point, we can see that it is asymmetric, with the positive residuals having a higher probability, this implies that it predicts a higher win probability than the actual result more times than it does a lower one. There are clear modes in the distribution - 0, -.2, .2, -.3, .3, and so on. It is to be noted that everything on the left of 1 had a positive probability but a value for 0 which implies either a tie or a loss. The probability associated with such a game is never predicted higher than 50%. For wins, it ranges above the 50% point (depending on goals scored and conceded).

### LOGISTIC REGRESSION

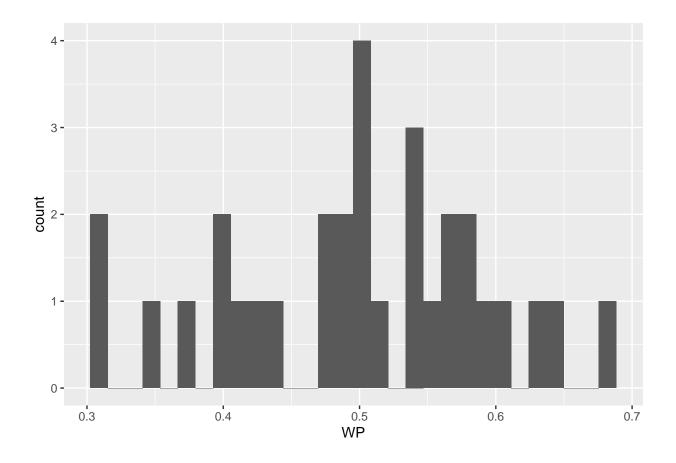
A logistic regression with two variables - Goals For and Goals Against will be used to predict the winning probability of a team. It predicts the odds for a success, in this context, a win given the variables. Therefore, intuitively, considering similar level of teams, will have the same coefficient affecting the probability of winning a game as a goal being scored must have the same but opposite implication on the chances of a team winning. Otherwise, goals scored are valued higher than goals conceded. Therefore it will just use the difference in the two values to increase the odds in relation to the coefficient value as per its slope. In a pythagorean model, there is a scale and shape which help in understanding and modelling such situations better than logistic regression.

# NHL PREDICTION

#the data
library(RCurl)

```
link <- getURL("https://raw.githubusercontent.com/M-ttM/Basketball/master/allrecords2.csv")
nhl1 <- read.csv(text = link)</pre>
head(nhl1)
##
    X
          Team GF_mid GA_mid OTL_mid W_mid L_mid GP_mid GF GA OTL W L
## 1 1
                  144
                        142
                                  9
                                      25
                                            17
                                                   51 235 216 13 44 25
      Anaheim
## 2 2
       Arizona
                  118
                        172
                                  9
                                      12
                                            29
                                                   50 208 256 12 29 41
                                      29
                                                   48 270 214 12 50 20
## 3 3
       Boston
                 157
                        119
                                  8
                                            11
## 4 4 Buffalo
                        163
                                  9
                                      14
                                            26
                                                   49 199 280 12 25 45
                 114
## 5 5 Calgary
                  137
                        135
                                  8
                                      25
                                            16
                                                   49 218 248 10 37 35
## 6 6 Carolina
                                                   49 228 256 11 36 35
                  137
                        154
                                  8
                                      22
                                            19
second half WP using first half pf/pa and Weibull distribution estimate.
a = 2.2
nhl1 <- nhl1 %>%
 mutate(WP = (GF_mid^(a)/(GF_mid^(a) + GA_mid^(a))),
        W_pred = W_mid + (82-GP_mid)*WP) %>%
 arrange(desc(WP))
print(head(nhl1))
##
     Х
            ## 1 26 Tampa Bay
                   175
                                   3
                                        34
                                              12
                                                     49 296 236
                                                                 5 54 23
## 2 3
          Boston
                                                     48 270 214 12 50 20
                   157
                          119
                                        29
                                              11
                                    8
## 3 29
           Vegas
                   164
                          128
                                    4
                                        32
                                              12
                                                     48 272 228
                                                                7 51 24
## 4 31 Winnipeg
                   164
                                   8
                                        29
                                                     50 277 218 10 52 20
                          136
                                              13
## 5 17 Nashville
                   145
                          123
                                   7
                                        29
                                              11
                                                     47 267 211 11 53 18
                                   4
                                        28
                                                    50 235 225
                                                                8 42 32
## 6 10
          Dallas
                   155
                          134
                                              18
##
           WP
                W_pred
## 1 0.6770481 56.34259
## 2 0.6478653 51.02742
## 3 0.6330304 53.52303
## 4 0.6015351 48.24912
## 5 0.5895266 49.63343
## 6 0.5793944 46.54062
ggplot(nhl1, aes(WP)) +
 geom_histogram()
```

## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



second half WP for each team by running a regression using the first half wins/pf/pa data, and using the predicted values.

```
fit.1 <- lm(W ~ GF_mid + GA_mid, data = nhl1)</pre>
summary(fit.1)
##
## lm(formula = W ~ GF_mid + GA_mid, data = nhl1)
##
## Residuals:
                       Median
        Min
                  1Q
                                    3Q
                                            Max
## -10.7825 -2.8040 -0.3477
                                3.1952 10.0873
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 44.11887
                          14.86803
                                     2.967 0.006089 **
                           0.06148
                                     4.244 0.000218 ***
## GF_mid
                0.26093
## GA_mid
               -0.28259
                           0.06138 -4.604 8.18e-05 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.647 on 28 degrees of freedom
## Multiple R-squared: 0.7027, Adjusted R-squared: 0.6815
\#\# F-statistic: 33.1 on 2 and 28 DF, p-value: 4.207e-08
```

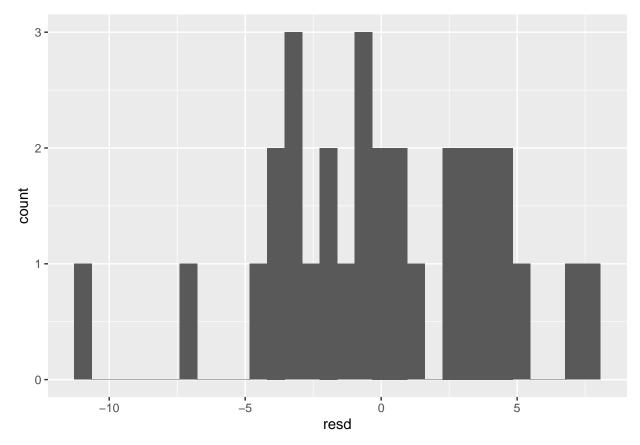
# Which predictions does better at predicting the second half of the season?

```
nhl1 <- nhl1 %>%
  mutate(resd = W_pred - W)

nhl1$resd_l <- resid(fit.1)

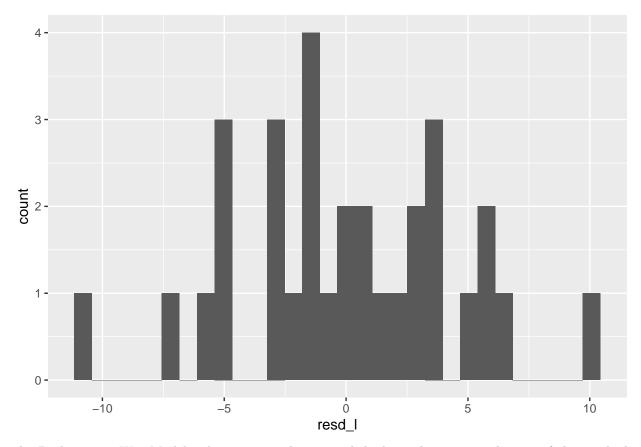
ggplot(nhl1, aes(resd)) +
  geom_histogram()</pre>
```

## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



```
ggplot(nhl1, aes(resd_l)) +
  geom_histogram()
```

## `stat\_bin()` using `bins = 30`. Pick better value with `binwidth`.



The Pythagorean Win Model is better at prediction with higher values at 0 and more of the residuals centered around 0 and within the 5 win error range. FOr the regressions, the residuals are more dispersed and less percentage is in the -5 to 5 error range. It also has more outliers in the residuals distribution.