

1. Assuming the professor asks 1 question:

$$p = 1 - \frac{1}{15} = 0.933$$

probability that no student will have to answer more than 1 question:

$$p = 1 - \frac{8}{15} = \frac{7}{15} = 0.467$$

$$2. \quad N = 5 \times 4 \times 8 \times 7 \times 1$$

\uparrow
odd

\uparrow
odd
unique

\uparrow
any
Unique

\nearrow
 \nearrow

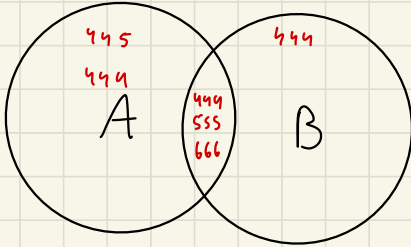
$$5 \times 4 \times 8 \times 7 \times 1 = 1120$$

$$\text{total combination probability} = \frac{1120}{10000} = 0.112$$

$$0.112 \times \frac{5}{8} = 0.07$$

3. $A \in \begin{bmatrix} 444 \\ 555 \\ 666 \\ 445 \\ 456 \\ \vdots \end{bmatrix}$

$B \in \begin{bmatrix} 444 \\ 555 \\ 666 \\ 111 \\ 222 \\ \vdots \end{bmatrix}$



→ they are dependent

4. total flushes probability in a suit:
 $13C_5 = 1287$

↓ 4 suits

total flushes = $1287 \cdot 4 = 5148$

So $\frac{5148}{52C_5} = \frac{5148}{258690} = 0.00198$
 5 cards from deck → \uparrow probability

5. $P(S) = 0.7 \rightarrow$ Probability of Win w/ Superstar
 $P(WS) = 0.5 \rightarrow$ P of Win w/o Superstar
 $P(S) \text{ play} = 0.75 \rightarrow$ P of Superstar playing
 $P(\text{win}) = 0.8 \text{ (4/5)}$

$$\begin{aligned} P(\text{Team}) &= P(S) (1 - P(WS)) + (P(WS) (1 - P(S))) \\ &= (0.7) (0.5) + (0.5) (0.3) \\ &= 0.5 \end{aligned}$$

$$\begin{aligned} P(\text{Play}) &= P(\text{win}) \cdot [P(S) (1 - P(\text{Team})) + P(WS) P(\text{Team})] \\ &= 0.8 \cdot [0.7 \cdot 0.5 + 0.5 \cdot 0.5] \\ &= 0.48 \text{ she played those 5 games} \\ &\quad 48\% \end{aligned}$$