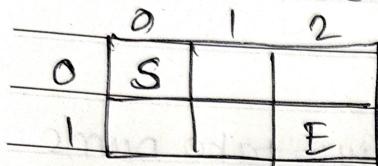


26/6/2023

Grid Unique Paths →

problem states that we can move only right bottom direction.



In recursion we can traverse all possible combinations.

At first we are at

(0,0) position (Index) ③

(we can move bottom or right)

In recursion

Left part is executed first

→ (0,0)

right

bottom

①

②

③

(1,0)

bottom

right

④

⑤

⑥

(2,0) X

You can not
move further
bcz this is out of
our boundary

out of
boundary

⑦

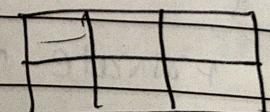
⑧

End point
So this is one
of our path

Initially, $i=0, j=0$

$n=1, m=2$

for $\binom{2}{3}$,
math X



Base condn $\rightarrow i \geq n \text{ or } j \geq m$

return 0;

when $i = n-1$ & $j = m-1$

return 1.

```
int countPaths(int i, int j, int n, int m){  
    if (i == (n-1) && j == (m-1)) return 1;  
    if (i >= n || j >= m) return 0;  
    else return countPaths(i+1, j) + countPaths(i, j+1);
```

Time complexity \rightarrow

It's going to be exponential in nature as we are going to try all possible combinations

Space complexity also will be exponential bcz we are going to use stack space in recursion.

Optimal solution (DP)

Recursive to DP

Exponential time complexity to quadratic T.C.

2 states (01) (11) (10) at max value of i can be n & value of j can be m .

Total no. of combⁿ of states will be $[n \times m]$

This where DP solⁿ comes in.

Create Hash Table of $(n \times m)$

Initialize everything as $\frac{-1}{2}$

| | | | |
|---|----|----|----|
| 0 | -1 | -1 | -1 |
| 1 | -1 | -1 | -1 |

We can see that we already fig. answers out somewhere else & answer you got i. Instead of calling recursive funn' as bottom & the right, we can use stored val. This what dp is: repeating the past without actually computing it.

Suboverlapping problems → You encounter the same state in some other part of recursion tree & you don't call recursion for that instead you use the val. stored in D.P. hashtable.

To convert recursive code to D.P. code
for that we need to carry 1 Hash table

base cond'n & if cond'n is same

if ($i == (n-1)$ && $j == (m-1)$) return 1
if ($i >= n$ || $j >= m$) return 0;

if ($dp[i][j] \neq -1$) return $dp[i][j]$

else return $dp[i][j] = countPath(i+1, j, dp)$

+ $countPath(i, j+1, dp);$

}

T.C. $O(N \times M)$

S.C. $O(N \times M)$