

FINAL LAB TEST MDSC-103P

1. Wilson Problem: Wilson Manufacturing produces both baseballs and softballs, which it wholesales to vendors around the country. Its facilities permit the manufacture of a maximum of 500 dozen baseballs and a maximum of 500 dozen softballs each day. The cowhide covers for each ball are cut from the same processed cowhide sheets. Each dozen baseballs require five square feet of cowhide (including waste), whereas, one dozen softballs require six square feet of cowhide (including waste). Wilson has 3600 square feet of cowhide sheets available each day. Production of baseballs and softballs includes making the inside core, cutting and sewing the cover, and packaging. It takes about one minute to manufacture a dozen baseballs and two minutes to manufacture a dozen softballs. A total of 960 minutes is available for production daily. The prices for a dozen baseball and a dozen softball are 7 and 10 dollars respectively. Answer the following:

a) Formulate the problem in the Excel file and generate the sensitivity analysis.

Microsoft Excel 16.0 Sensitivity Report

Worksheet: [Book1]Sheet1

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Variable Cells

		Final	Reduced	Objective	Allowable	Allowable
Cell	Name	Value	Cost	Coefficient	Increase	Decrease
\$C\$4	x1	360	0	7	1.333333333	2
\$D\$4	x2	300	0	10	4	1.6

Constraints

		Final	Shadow	Constraint	Allowable	Allowable
Cell	Name	Value	Price	R.H. Side	Increase	Decrease
\$E\$5	c1	660	0	1000	1E+30	340
\$E\$6	c2	3600	1	3600	1200	720
\$E\$7	c3	960	2	960	240	240

b) Write on cost coefficient sensitivity analysis.

The cost sensitivity analysis tells us how the cost coefficient affect the optimality of the the given linear programming problem,the cost coefficient can be solved for an linear programming problem using an excel solver,from the cost coefficient analysis we can tell about the reduced cost and the shadow price , the shadow price tells us that at one unit of time how the materials used so that it makes an impact in the objective function

The shadow price is given by

Shadow
Price
0
1
2

The reduced cost is

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Reduced Cost
0
0

The allowable decrease for the x_1 is 2 and the allowable increase for the x_1 is 1.333

The allowable decrease for the x_2 is 1.6 and allowable increase for the x_2 is 4

x_1 -baseballs

x_2 -softballs

The cost function tells us what impact will it make if there is like for example 10 per cent increase the material how it affect the optimality

If a new material is introduced how it effect the optimality etc

c) Write on Right Hand Side Sensitivity Analysis

The right hand side of the sensitivity analysis tells us how the changes in the right hand side make the changes in the optimality of the programme this is a case in the post optimal analysis the allowable decrease or increase in the constraints

We have three constraints c_1 , c_2 and c_3

The allowable decrease for the c_1 is 340

The allowable decrease for the c_2 is 720

The allowable decrease for the c_3 is 240

The allowable increase for the constraints are given by

Allowable Increase
1E+30
1200
240

2. Consider the following problem:

$$f(x_1, x_2) = 4x_1 + 6x_2 - 2x_1^2 - 2x_1x_2 - 2x_2^2$$

a) Write a program to visualize the above function.

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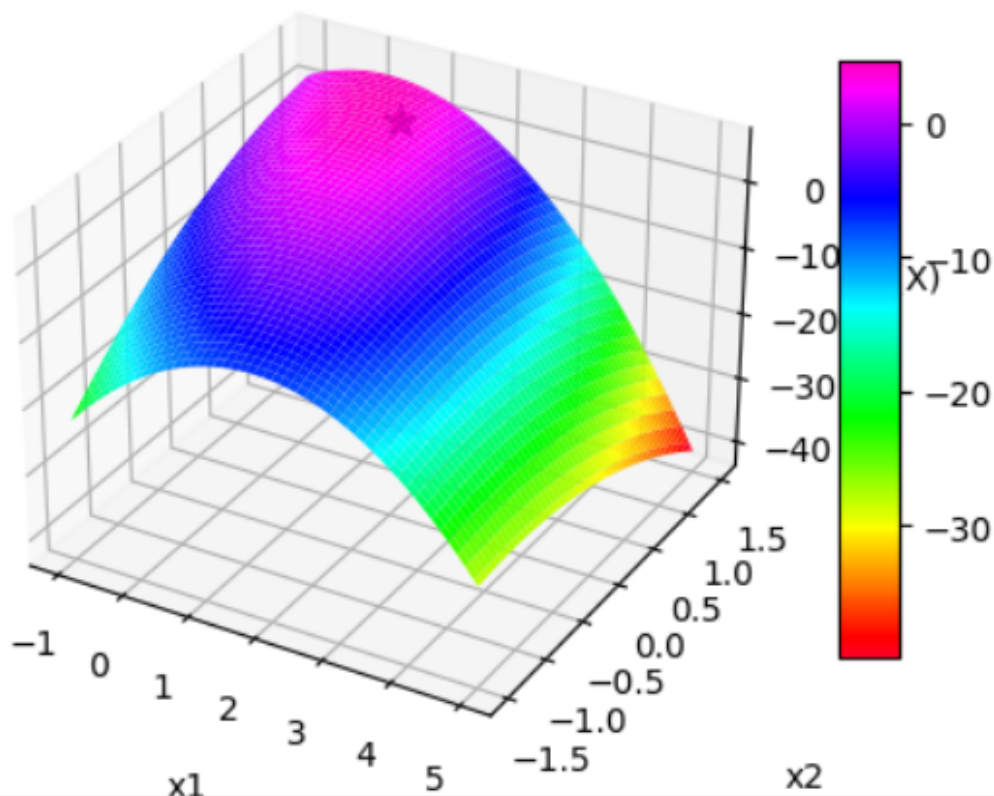
```
import numpy as np
import matplotlib.pyplot as plt
import scipy as sp
from scipy.special import gamma
```

$$\diamond (x_1, x_2) = 4x_1 + 6x_2 - 2x_1^2 - 2x_1x_2 - 2x_2^2$$

```
[8] from mpl_toolkits.mplot3d import Axes3D
f=lambda x1,x2:(4*x1+6*x2-2*x1**2-2*x1*x2-2*x2**2) # writing the function using lambda
x2=np.linspace(-1.5,1.5,100) #x2 will take 100 equal data points ranging from 1.5 to 1.5
x1=np.linspace(-1,5,100)# x1 will take the 100 equal data points from -1 to 5

X,Y=np.meshgrid(x1,x2) #creating a mesh grid for the x1 and x2
F=f(X,Y)
```

```
fig=plt.figure(figsize=(12,8)) #we are plotting the the figure size is of the ratio of 12 ,8
ax=plt.subplot(1,2,1,projection='3d')
ax.scatter3D(1,1,f(1,1),c="black",marker="*",s=100)
surf = ax.plot_surface(X,Y,F, cmap= 'gist_rainbow')
fig.colorbar(surf,shrink=0.4, aspect=10)
# set axes label
ax.set_xlabel('x1', labelpad=10)
ax.set_ylabel('x2', labelpad=30)
ax.set_zlabel('f(x)', labelpad=10)
plt.show()
```



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b) Write an iterative program to maximize the function

```
f=lambda x1,x2:-(4*x0+6*x1-2*x0**2-2*x0*x1-2*x1**2)
x0=1
x1=5
delta=1*10**(-5)
eta=x0-x1
learning_rate=0.1

#grad function
def gradf(x):
    return -(4*x0+6*x1-2*x0**2-2*x0*x1-2*x1**2)

x1=x0-eta*gradf(x0)
x0=x1
a=[]

for i in range(0,100):
    x1=x0-eta*gradf(x0)
    x0=x1
    if gradf(x0)<delta:
        break

print(x1)
    #graph plot with x,f(x) values with the plot function
plt.scatter(a,f(np.array(a)))
plt.plot(x,f(x))
plt.title("plot for all the x ,f(x) values")
plt.xlabel("x")
plt.ylabel("f(x)")
plt.show()
```