# 3.5 Year PhD Progress Review

Vivek Katial

2024-05-28

1. Introduction

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- 2. Aims and Objectives

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- 3. Key Contributions

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- 7. Feedback!

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- Among prominent VQAs, Quantum Approximate Optimization
  Algorithm (QAOA) and Variational Quantum Eigensolver (VQE)
  are widely studied.
- 3. The main area of focus in this thesis is to study the instance dependence of QAOAs to better understand and stress test its performance.

#### MaxCut Problem

Partition a graph G=(V,E) into two sets S and  $V\setminus S$  such that the number of edges between the two sets is maximised.

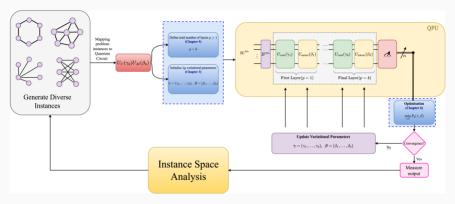
$$\max_{\mathbf{x}} \sum_{(i,j) \in E} w_{ij} (1 - x_i x_j)$$

where  $x_i \in \{-1, 1\}$  and  $w_{ij}$  is the weight of edge (i, j).



Figure 1: An example of a six-node MaxCut problem

### QAOA + Our Focus



**Figure 2:** A schematic representation of the parameter optimisation process in QAOA.

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- 3. Circuit Depth Selection: What is the optimal number of layers for QAOA, considering the trade-off between resource requirements and performance? What is the impact of instance characteristics on the dependence between layers p and p+1?
- 4. Classical Optimisers: Which classical optimisers are most effective in the hybrid optimisation phase of QAOA, and how do they impact solution quality?

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  - Presenting the findings at OPTIMA-CON 2024.

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- Development of Software for Managing Experimental Workloads
  - A toolkit for automated and reproducible research experiments on HPC clusters, enhancing research scalability and reproducibility in computational research.

# Results

# Instance Space Analysis (ISA)

$$\begin{bmatrix} Z_1 \\ Z_2 \end{bmatrix} = \begin{bmatrix} -0.5225 & 0.2301 \\ -0.5939 & 0.7398 \\ 0.3977 & -0.2637 \\ -0.1423 & -0.2023 \\ -0.0091 & 0.5056 \\ 0.4226 & -0.0190 \\ 0.0843 & 0.6528 \\ -0.0033 & -0.0937 \\ -0.2002 & -0.3513 \\ 0.3448 & -0.3839 \end{bmatrix}$$

algebraic connectivity average distance clique number diameter maximum degree maximum weighted degree number of edges radius skewness weight weighted average clustering

# Instance Space Analysis (ISA) - Sources

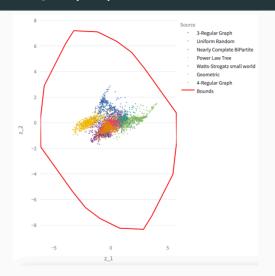


Figure 3: Source Distribution for MaxCut Instances

# Instance Space Analysis (ISA) – Features

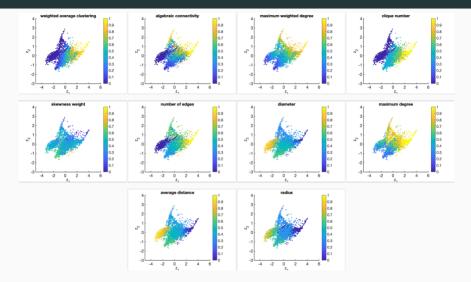


Figure 4: Feature Distribution for MaxCut Instances

# Instance Space Analysis (ISA) – Algorithm Performance

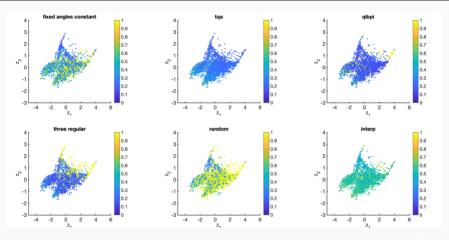


Figure 5: Algorithm Performance for MaxCut Instances (globally normalised)

# Instance Space Analysis (ISA) – Algorithm Footprints

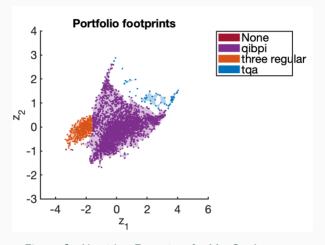


Figure 6: Algorithm Footprints for MaxCut Instances

# Instance Space Analysis (ISA) – SVM

Algorithm	Avg Perf (all instances)	Std Perf (all instances)	Probability of Good
Constant	34323.017	47394.475	0.032
INTERP	6082.428	22217.419	0.001
QIBPI	6749.427	25023.466	0.709
Random	62812.688	48268.844	0.005
3-Regular	16989.979	37511.188	0.448
TQA	2138.589	14257.964	0.111
Oracle	27.734	59.506	1.000
SVM Selector	4998.899	21721.862	0.767

Table 1: Performance Metrics for Different Algorithms

# Results

#### Results

Lets look at results from other experiments interactively!

Link here: ISA Visualisation

# Thesis Update

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Writing has started (~100 pages through...)

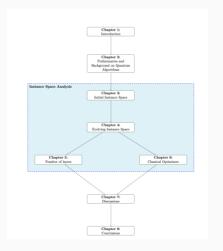


Figure 7: Thesis Structure

# Thesis Update

- Chapter 1: Introduction
  - Complete (Draft Stage)
- Chapter 2: Background and Preliminaries on Quantum Algorithms
  - Writing in progress (60-70% Complete)
- Chapter 3: Instance Space Analysis for QAOA Parameter Initialisation
  - Almost Complete, Needs Revision (Update Results)
- Chapter 4: Evolving Instances for QAOA Using Genetic Algorithms
  - Writing in progress, Needs Revision (Update Results)

# Thesis Update (continued)

- Chapter 5: The Role of Circuit Depth in QAOA
  - Results Complete, Writing Not Started
- Chapter 6: Evaluating Classical Optimisers for QAOA
  - Results Complete, Writing Not Started
- Chapter 7: Conclusions and Future Work
  - Conclusion, Not Started

# Thesis Completion Plan

#### Thesis GANTT Chart

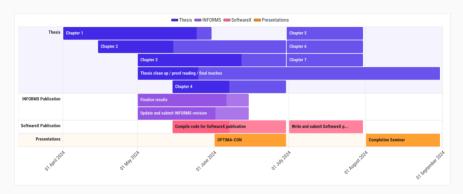


Figure 8: PhD GANTT Chart

# Primary Focus in June: Submit revision to INFORMS and finalise SoftwareX submission

Finalise revisions for INFORMS and submit (by June 15th)

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- Chapter 4: Complete writing, revise and update results, review and edit

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#### Other tasks

Submit SoftwareX paper

#### Primary Focus: Thesis Writing and revising

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#### Other tasks

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#### Other tasks

- Submit SoftwareX paper
- OPTIMA-CON presentation
- Conduct any additional experiments required for thesis completion

## Month 3: August

# Primary Focus: Thesis Writing and revising

• Final revisions and edits

# Month 3: August

- Final revisions and edits
- Prepare and hopefully submit!

# Feedback and Questions for

**Discussion** 

1. Stipend and Scholarship: My current scholarship ends in June 2024 (next week). I've applied for the COVID-19 productivity-loss extension but haven't received a response yet. Any support would be appreciated. I applied for the shorter extension (16 weeks instead of 26), but I'm open to suggestions or advice. This extension would last until 23rd September, which I believe is more than enough time to get everything done. Link here.

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Thank you!