Report on Time Series Data Training using RNN’s

Dataset Overview

The dataset used in this project is the "jena_climate_2009_2016" dataset, containing time-series data of various climate measurements recorded from 2009 to 2016. The dataset includes features such as temperature, air pressure, humidity, and wind speed, among others. These features are crucial for analyzing and predicting weather patterns.

- Total Samples: 41,808
- Features: 14 (including variables like temperature, pressure, humidity, wind speed, etc.)
- Target Variable: Temperature
- Data Split:
  - Training Set: 70%
  - Validation Set: 15%
  - Test Set: 15%

Preprocessing involved scaling each feature between 0 and 1 to ensure the data was ready for model training without scale-induced biases.

Model Architectures and Process

Several model architectures were employed to evaluate their performance on this time-series forecasting task. Each model was trained for 5 epochs, with performance evaluated using the Mean Absolute Error (MAE) on the test set. Here is a brief description of each model:

1. Bidirectional LSTM (50 and 100 units): A Bidirectional Long Short-Term Memory model captures both past and future context for each timestamp. By comparing the model with 50 and 100 units, we tested how increased capacity impacts accuracy.

2. Stacked LSTM (50_50 and 100_50 units): A Stacked LSTM model with two layers, designed to capture more complex temporal relationships by stacking layers. Different configurations (e.g., 50_50 and 100_50) were used to understand the effect of varying layer sizes.

3. Conv-LSTM (50 and 100 units): A model combining Convolutional Neural Networks (CNN) with LSTM layers, leveraging spatial and temporal feature extraction. This was tested with both 50 and 100 units in the LSTM layer.

4. Stacked Conv-LSTM: Similar to Conv-LSTM but with additional layers, aiming to capture a deeper relationship by stacking multiple CNN and LSTM layers.

5. Advanced LSTM with Dropout: An LSTM model with dropout regularization to address potential overfitting. Dropout layers were applied to regularize the network by randomly deactivating neurons during training.

6. Advanced Bidirectional LSTM with Dropout: An extension of the Bidirectional LSTM model with dropout, adding regularization to prevent overfitting.

Process:
- The models were trained on the scaled training set for 5 epochs each, with validation loss recorded at each epoch.
- After training, MAE on the test set was recorded for each model to evaluate performance.

Results and Discussion

The table below summarizes the test Mean Absolute Error (MAE) for each model:

Model	Test MAE
Bidirectional LSTM (50)	0.1749
Bidirectional LSTM (100)	0.1327
Stacked LSTM (50_50)	0.1955
Stacked LSTM (100_50)	0.2093
Conv-LSTM (50)	0.2084
Conv-LSTM (100)	0.1431
Stacked Conv-LSTM	0.1624
Advanced LSTM with Dropout	0.1444
Advanced Bidirectional LSTM with Dropout	0.1692

Key Observations:
- Best Performing Model: The Bidirectional LSTM with 100 units achieved the lowest MAE (0.1327), suggesting it effectively captured temporal dependencies in the time series data.
- Effect of Bidirectional Layers: The Bidirectional LSTM models performed better than regular LSTMs and even the Conv-LSTM models, indicating that learning both past and future contexts simultaneously benefits weather forecasting tasks.
- Impact of Dropout Regularization: Models with dropout (e.g., Advanced LSTM with Dropout and Advanced Bidirectional LSTM with Dropout) showed slight improvement in generalization, but did not outperform the Bidirectional LSTM model without dropout. This suggests that while dropout helps in regularizing, it may slightly hinder capturing sequential dependencies in a highly temporal dataset.
- Effect of Convolutional Layers: Conv-LSTM models performed moderately well, but their performance was slightly lower than bidirectional models. This might be due to the convolutional layers introducing noise or failing to fully capture the sequential patterns in the time-series data.

Conclusion

In this experiment, various recurrent neural network architectures were compared for the task of climate time-series forecasting. The Bidirectional LSTM with 100 units model performed best, achieving the lowest test MAE. This result emphasizes the advantage of bidirectional networks in time-series forecasting, where capturing both past and future context is beneficial.

The addition of dropout regularization did not significantly improve performance, possibly due to the short training period of only 5 epochs. Models with convolutional layers showed moderate performance, indicating they may not be as effective as purely recurrent layers for this dataset.

Importing Libraries

In [1]:
```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
from sklearn.preprocessing import MinMaxScaler
from tensorflow import keras
from tensorflow.keras import layers
from tensorflow.keras.models import Sequential
from sklearn.metrics import mean_absolute_error
```

Load the dataset

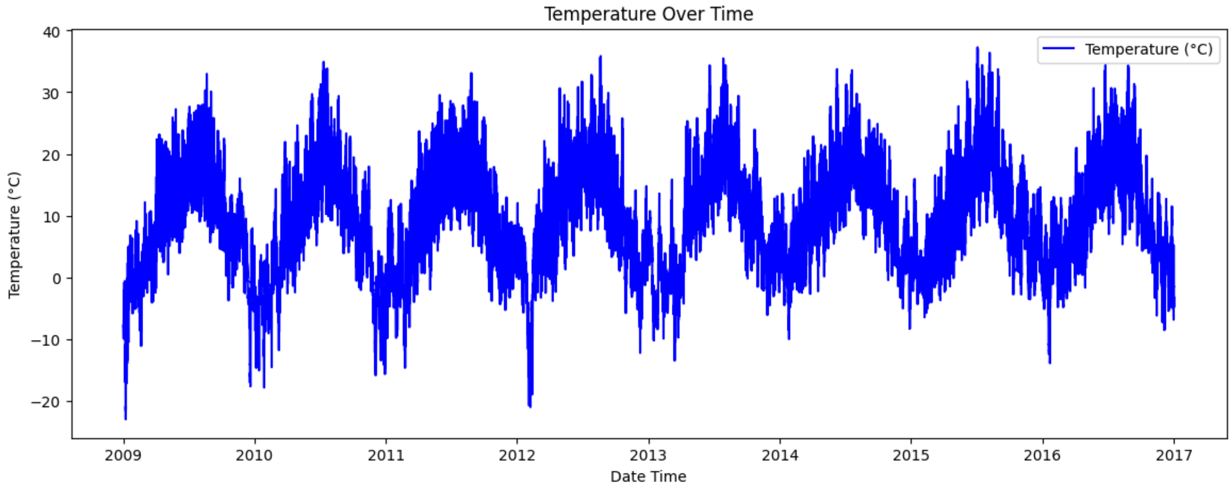
In [2]:
```
# Load the dataset
data = pd.read_csv('jena_climate_2009_2016.csv')
data['Date Time'] = pd.to_datetime(data['Date Time'], format='%d.%m.%Y %H:%M:%S', dayf
data.set_index('Date Time', inplace=True)
```

Select a target variable

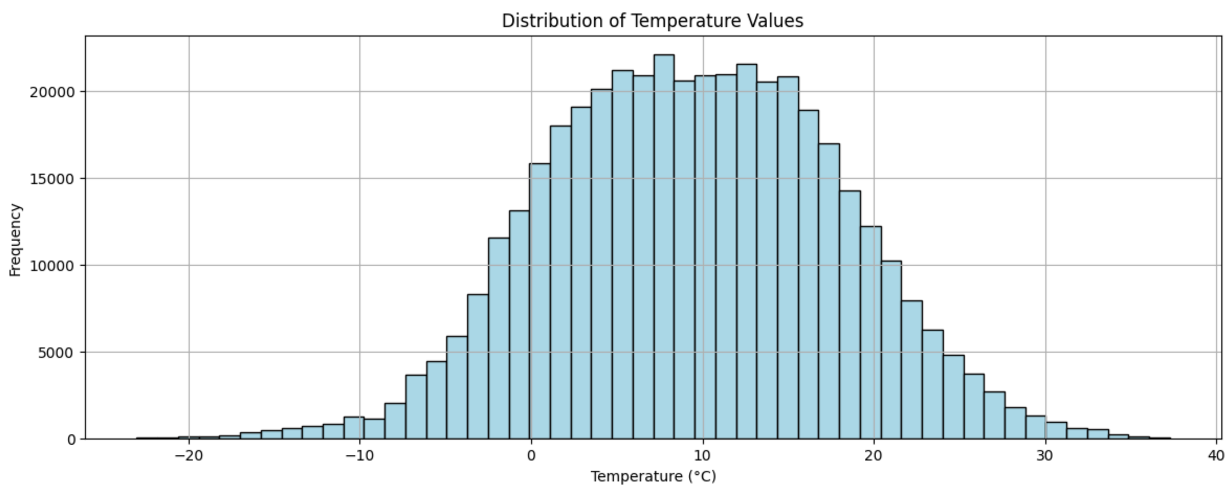
In [3]:
```
# Select a target variable
target_column = 'T (degC)'
data = data[target_column]
```

Data Analysis Plots

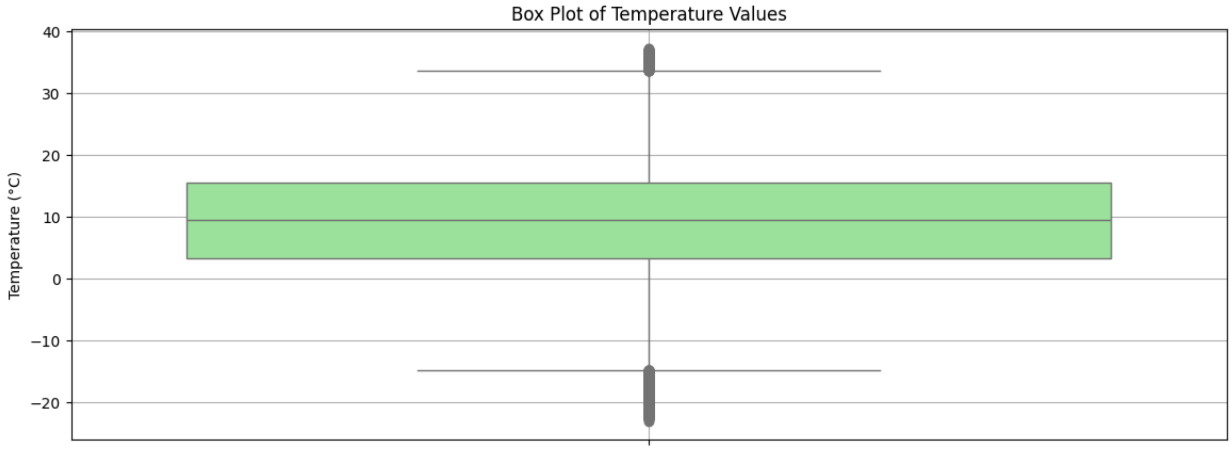
In [4]:
```
# Data Analysis Plots
# 1. Time Series Plot
plt.figure(figsize=(14, 5))
plt.plot(data.index, data, label='Temperature (°C)', color='blue')
plt.title('Temperature Over Time')
plt.xlabel('Date Time')
plt.ylabel('Temperature (°C)')
plt.legend()
plt.show()
```



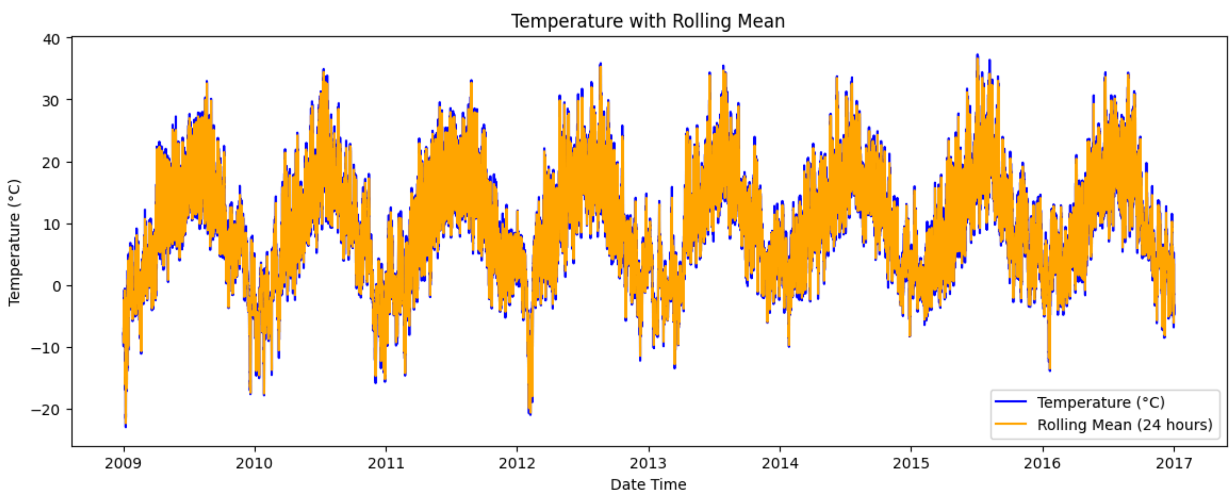
In [5]:
```
# 2. Histogram
plt.figure(figsize=(14, 5))
plt.hist(data, bins=50, color='lightblue', edgecolor='black')
plt.title('Distribution of Temperature Values')
plt.xlabel('Temperature (°C)')
plt.ylabel('Frequency')
plt.grid()
plt.show()
```



In [6]:
```
# 3. Box Plot
plt.figure(figsize=(14, 5))
sns.boxplot(data=data, color='lightgreen')
plt.title('Box Plot of Temperature Values')
plt.ylabel('Temperature (°C)')
plt.grid()
plt.show()
```



In [7]:
```
# 4. Rolling Mean
rolling_mean = data.rolling(window=24).mean()
plt.figure(figsize=(14, 5))
plt.plot(data.index, data, label='Temperature (°C)', color='blue')
plt.plot(data.index, rolling_mean, label='Rolling Mean (24 hours)', color='orange')
plt.title('Temperature with Rolling Mean')
plt.xlabel('Date Time')
plt.ylabel('Temperature (°C)')
plt.legend()
plt.show()
```



Data Pre processing

In [8]:
```
# Normalize the data
scaler = MinMaxScaler(feature_range=(0, 1))
data_scaled = scaler.fit_transform(data.values.reshape(-1, 1))
```

In [9]:
```
# Create sequences for training
def create_sequences(data, time_step=1):
    X, y = [], []
    for i in range(len(data) - time_step):
        X.append(data[i:(i + time_step), 0])
        y.append(data[i + time_step, 0])
    return np.array(X), np.array(y)
```

In [10]:
```
# Define the time step
time_step = 48
X, y = create_sequences(data_scaled, time_step)
X = X.reshape(X.shape[0], X.shape[1], 1)
```

Data Splitting

In [11]:
```
# Split the dataset into training, validation, and test sets
train_size = int(len(X) * 0.7)
val_size = int(len(X) * 0.15)
X_train, X_val, X_test = X[:train_size], X[train_size:train_size + val_size], X[train_
y_train, y_val, y_test = y[:train_size], y[train_size:train_size + val_size], y[train_
```

Model Training

In [12]:
```
# Function to build and train models
def build_and_train_model(model_name, model):
    print(f"Training {model_name} model...")
    model.fit(X_train, y_train, epochs=5, batch_size=32, validation_data=(X_val, y_val
    predictions = model.predict(X_test)
    predictions = scaler.inverse_transform(predictions)

    # Plot results
    true_values = scaler.inverse_transform(y_test.reshape(-1, 1))

    # True vs Predicted Plot
    plt.figure(figsize=(14, 5))
    plt.plot(data.index[-len(y_test):], true_values, label='True Values', color='blue'
    plt.plot(data.index[-len(predictions):], predictions, label='Predictions', color='
    plt.title(f'{model_name} - Temperature Prediction')
    plt.xlabel('Date Time')
    plt.ylabel('Temperature (°C)')
    plt.legend()
    plt.show()

    # Residual Plot
    residuals = true_values - predictions
    plt.figure(figsize=(14, 5))
    plt.plot(data.index[-len(y_test):], residuals, label='Residuals', color='purple')
    plt.axhline(0, color='black', linestyle='--')
    plt.title(f'{model_name} - Residuals')
    plt.xlabel('Date Time')
    plt.ylabel('Residuals (°C)')
    plt.legend()
    plt.show()

    # Distribution of Residuals
    plt.figure(figsize=(14, 5))
    plt.hist(residuals, bins=50, color='lightblue', edgecolor='black')
    plt.title(f'{model_name} - Distribution of Residuals')
    plt.xlabel('Residuals (°C)')
    plt.ylabel('Frequency')
    plt.grid()
    plt.show()
```

```python
    # Calculate MAE
    mae = mean_absolute_error(true_values, predictions)
    print(f'{model_name} MAE: {mae:.4f}')
    return mae
```

In [13]:

```python
# Define and train enhanced models
models = {
    "Bidirectional_LSTM_50": Sequential([
        layers.Bidirectional(layers.LSTM(50, return_sequences=True), input_shape=(X_tr
        layers.Bidirectional(layers.LSTM(50)),
        layers.Dense(1)
    ]),

    "Bidirectional_LSTM_100": Sequential([
        layers.Bidirectional(layers.LSTM(100, return_sequences=True), input_shape=(X_t
        layers.Bidirectional(layers.LSTM(100)),
        layers.Dense(1)
    ]),

    "Stacked_LSTM_50_50": Sequential([
        layers.LSTM(50, return_sequences=True, input_shape=(X_train.shape[1], 1)),
        layers.LSTM(50, return_sequences=True),
        layers.LSTM(50),
        layers.Dense(1)
    ]),

    "Stacked_LSTM_100_50": Sequential([
        layers.LSTM(100, return_sequences=True, input_shape=(X_train.shape[1], 1)),
        layers.LSTM(50),
        layers.Dense(1)
    ]),

    "Conv_LSTM_50": Sequential([
        layers.Conv1D(filters=64, kernel_size=3, activation='relu', input_shape=(X_tra
        layers.MaxPooling1D(pool_size=2),
        layers.LSTM(50),
        layers.Dense(1)
    ]),

    "Conv_LSTM_100": Sequential([
        layers.Conv1D(filters=64, kernel_size=3, activation='relu', input_shape=(X_tra
        layers.MaxPooling1D(pool_size=2),
        layers.LSTM(100),
        layers.Dense(1)
    ]),

    "Stacked_Conv_LSTM": Sequential([
        layers.Conv1D(filters=64, kernel_size=3, activation='relu', input_shape=(X_tra
        layers.MaxPooling1D(pool_size=2),
        layers.LSTM(50, return_sequences=True),
        layers.LSTM(50),
        layers.Dense(1)
    ]),

    "Advanced_LSTM_with_Dropout": Sequential([
        layers.LSTM(100, return_sequences=True, input_shape=(X_train.shape[1], 1)),
        layers.Dropout(0.2),
        layers.LSTM(50),
```

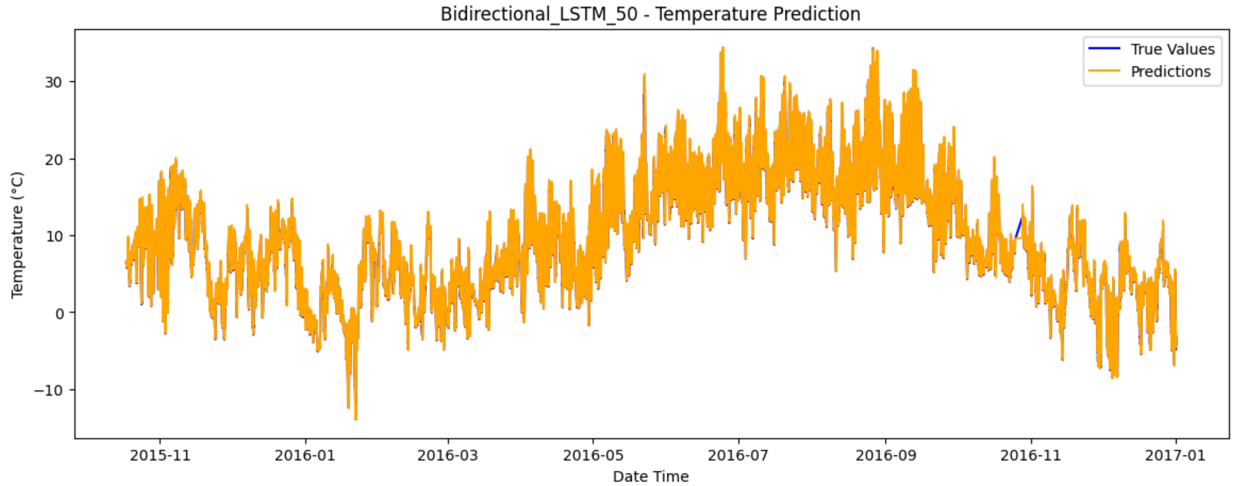
```
        layers.Dense(1)
    ]),

    "Advanced_Bidirectional_LSTM_with_Dropout": Sequential([
        layers.Bidirectional(layers.LSTM(100, return_sequences=True), input_shape=(X_t
        layers.Dropout(0.2),
        layers.Bidirectional(layers.LSTM(50)),
        layers.Dense(1)
    ])
}
```

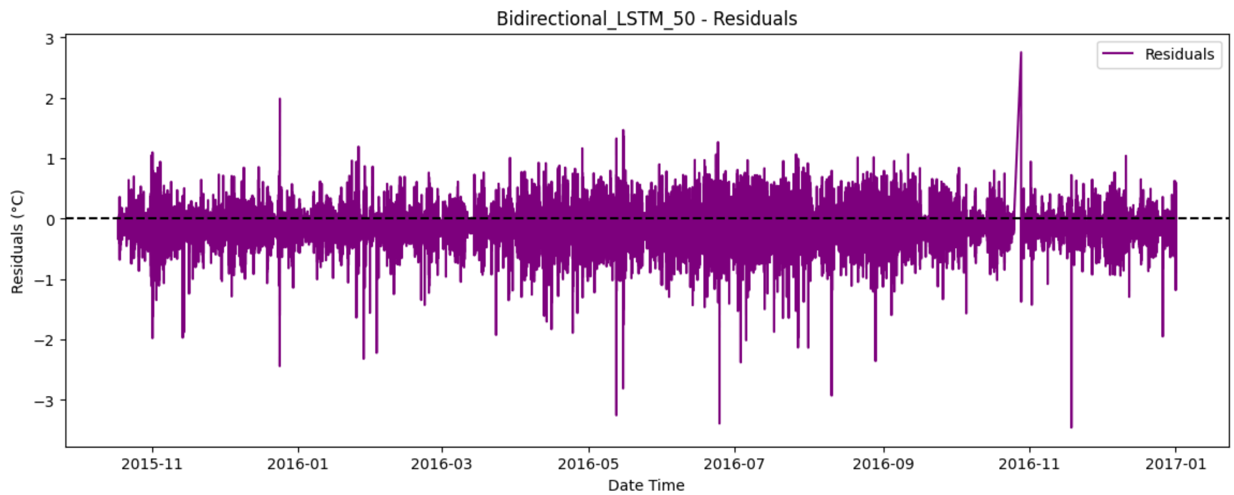
```
/usr/local/lib/python3.10/dist-packages/keras/src/layers/rnn/bidirectional.py:107: Us
erWarning: Do not pass an `input_shape`/`input_dim` argument to a layer. When using S
equential models, prefer using an `Input(shape)` object as the first layer in the mod
el instead.
  super().__init__(**kwargs)
/usr/local/lib/python3.10/dist-packages/keras/src/layers/rnn/rnn.py:204: UserWarning:
Do not pass an `input_shape`/`input_dim` argument to a layer. When using Sequential m
odels, prefer using an `Input(shape)` object as the first layer in the model instead.
  super().__init__(**kwargs)
/usr/local/lib/python3.10/dist-packages/keras/src/layers/convolutional/base_conv.py:1
07: UserWarning: Do not pass an `input_shape`/`input_dim` argument to a layer. When u
sing Sequential models, prefer using an `Input(shape)` object as the first layer in t
he model instead.
  super().__init__(activity_regularizer=activity_regularizer, **kwargs)
```

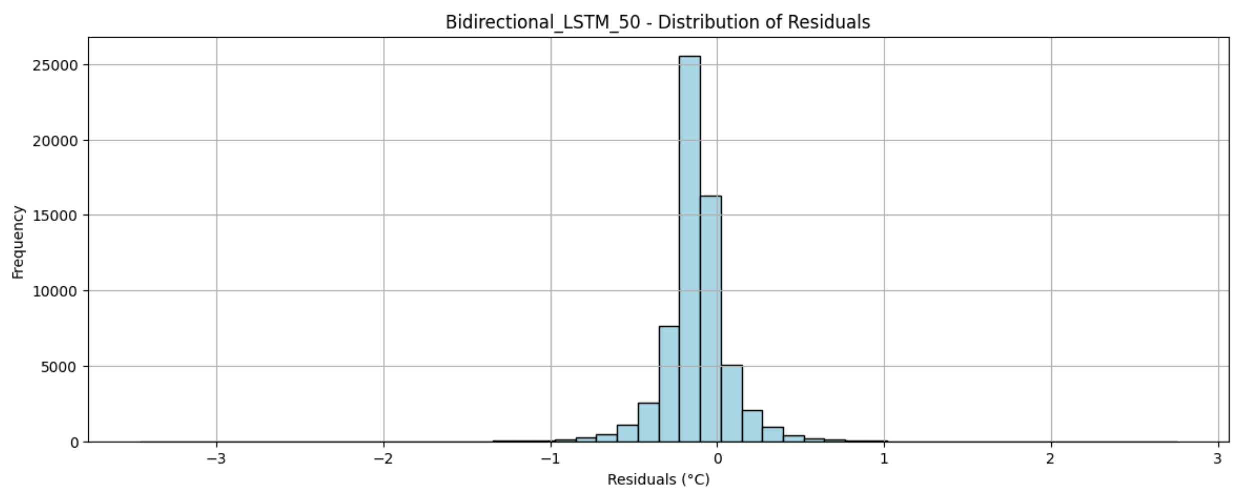
In [14]:

```
# Compile and train all enhanced models
for model_name, model in models.items():
    model.compile(optimizer='adam', loss='mean_squared_error')
    mae = build_and_train_model(model_name, model)
```

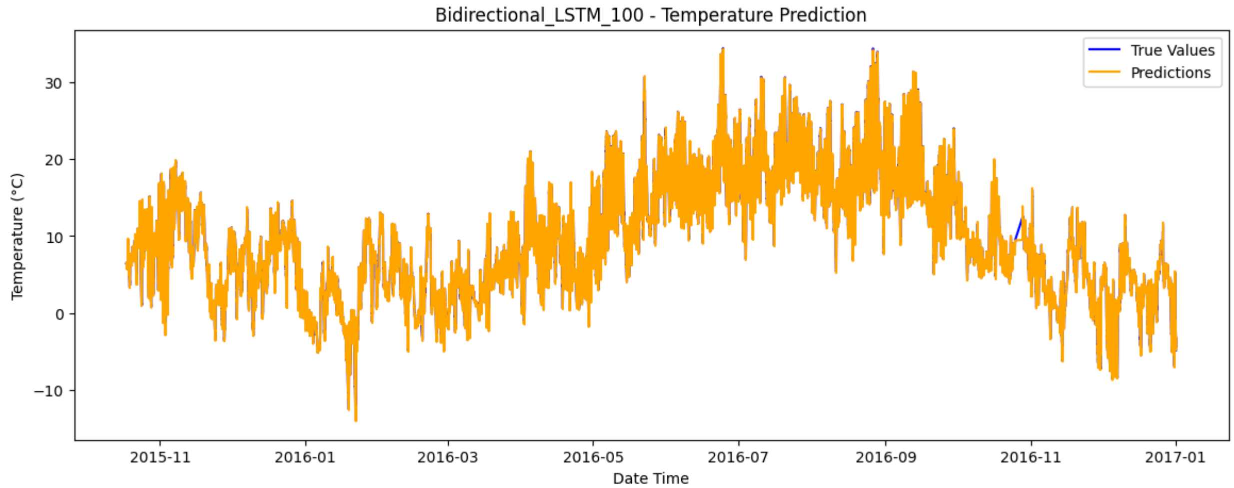
```
Training Bidirectional_LSTM_50 model...
Epoch 1/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 132s 14ms/step - loss: 0.0012 - val_loss: 5.3375e-05
Epoch 2/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 139s 14ms/step - loss: 2.3356e-05 - val_loss: 1.2361e-
05
Epoch 3/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 142s 14ms/step - loss: 1.6299e-05 - val_loss: 1.7306e-
05
Epoch 4/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 125s 14ms/step - loss: 1.5304e-05 - val_loss: 1.3788e-
05
Epoch 5/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 125s 14ms/step - loss: 1.4943e-05 - val_loss: 1.6129e-
05
1972/1972 ━━━━━━━━━━━━━━━━━━━━ 9s 4ms/step
```

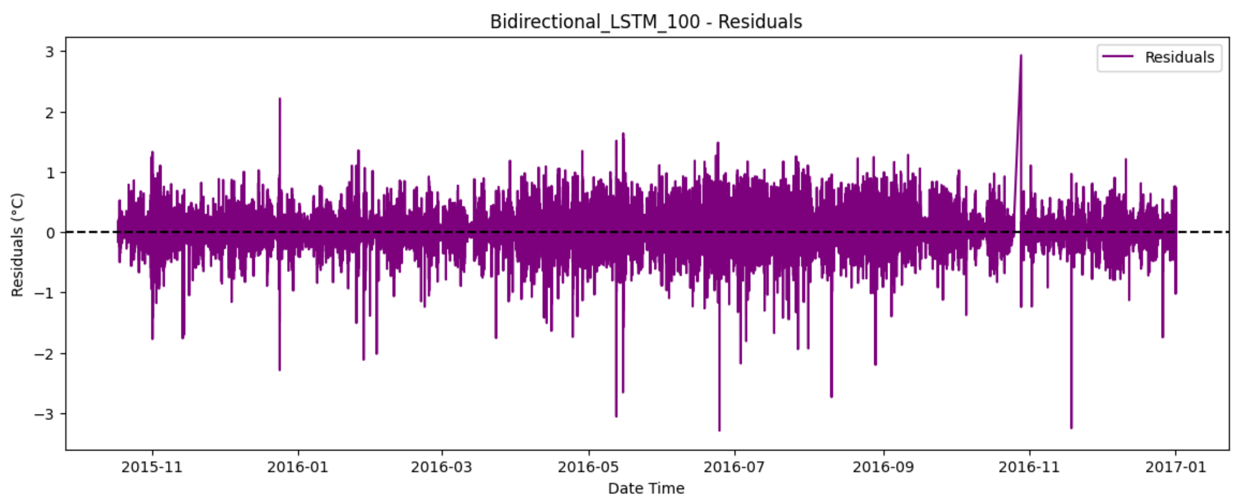

Bidirectional_LSTM_50 - Temperature Prediction
True Values
Predictions
Temperature (°C)
30
20
10
0
−10
2015-11
2016-01
2016-03
2016-05
2016-07
2016-09
2016-11
2017-01
Date Time

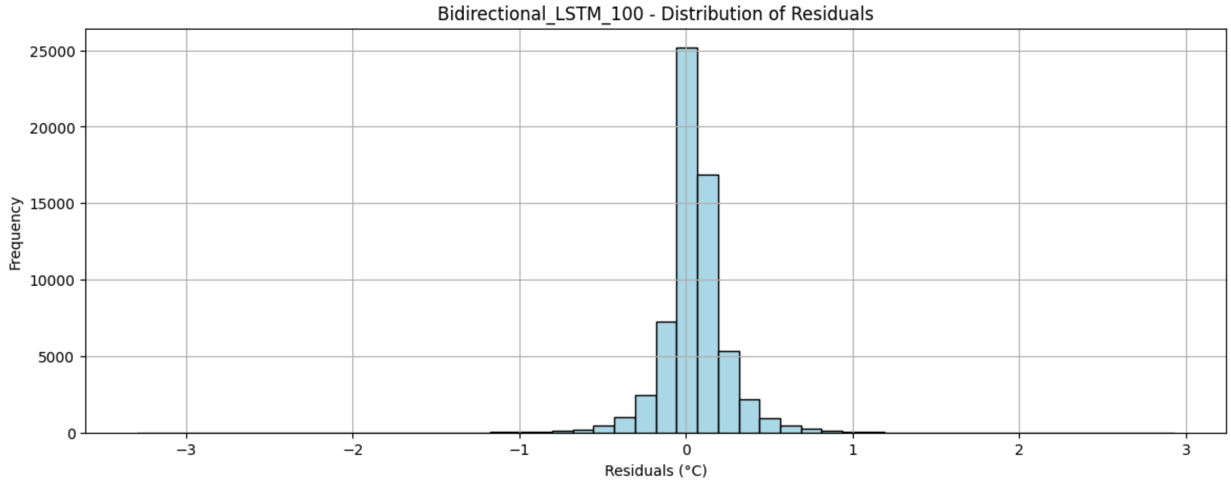

Bidirectional_LSTM_50 - Residuals
Residuals
Residuals (°C)
3
2
1
0
−1
−2
−3
2015-11
2016-01
2016-03
2016-05
2016-07
2016-09
2016-11
2017-01
Date Time


Bidirectional_LSTM_50 - Distribution of Residuals
Frequency
25000
20000
15000
10000
5000
0
−3
−2
−1
0
1
2
3
Residuals (°C)

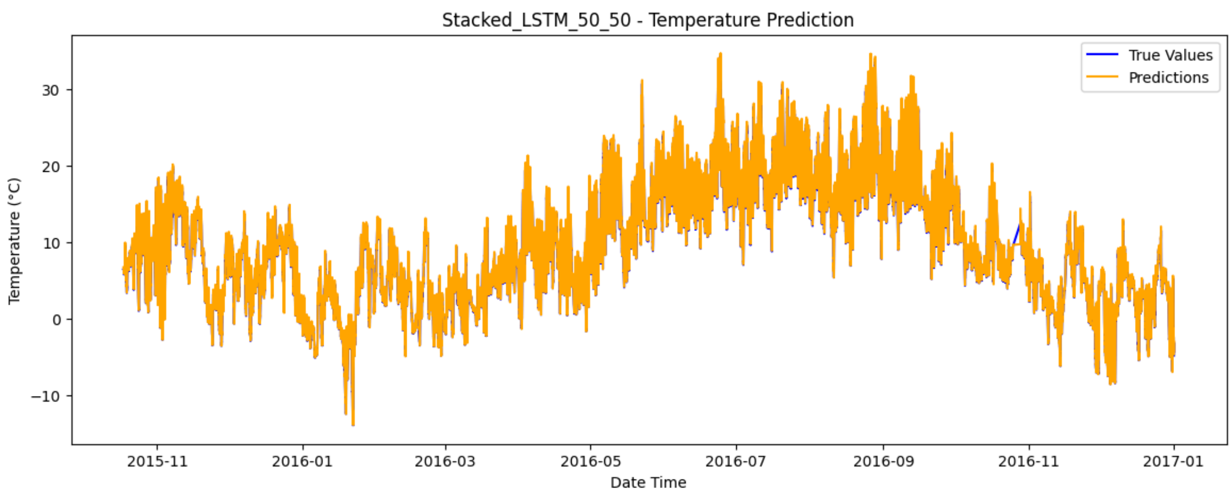
```
Bidirectional_LSTM_50 MAE: 0.1749
Training Bidirectional_LSTM_100 model...
Epoch 1/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 133s 14ms/step - loss: 8.8118e-04 - val_loss: 1.4765e-05
Epoch 2/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 142s 14ms/step - loss: 2.0256e-05 - val_loss: 2.1802e-05
Epoch 3/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 142s 14ms/step - loss: 1.6521e-05 - val_loss: 1.4544e-05
Epoch 4/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 142s 14ms/step - loss: 1.5370e-05 - val_loss: 1.2581e-05
Epoch 5/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 131s 14ms/step - loss: 1.4676e-05 - val_loss: 1.2740e-05
1972/1972 ━━━━━━━━━━━━━━━━━━━━ 11s 5ms/step
```

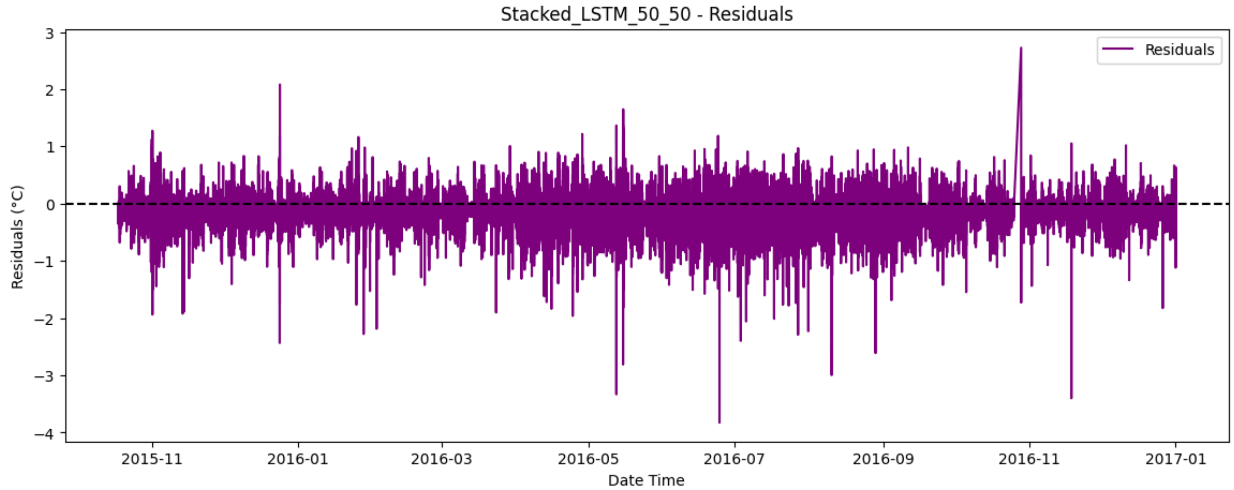


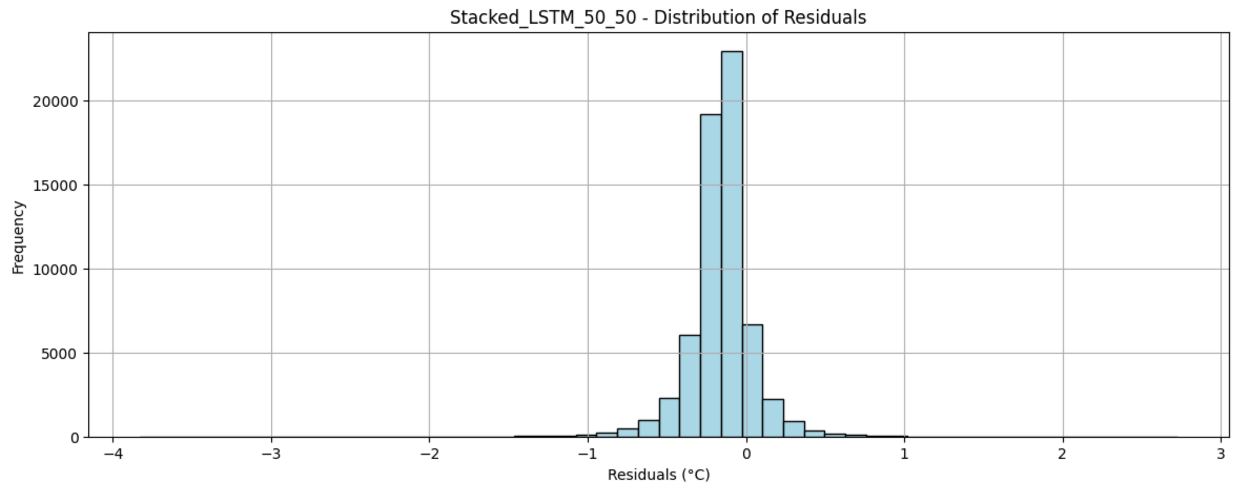




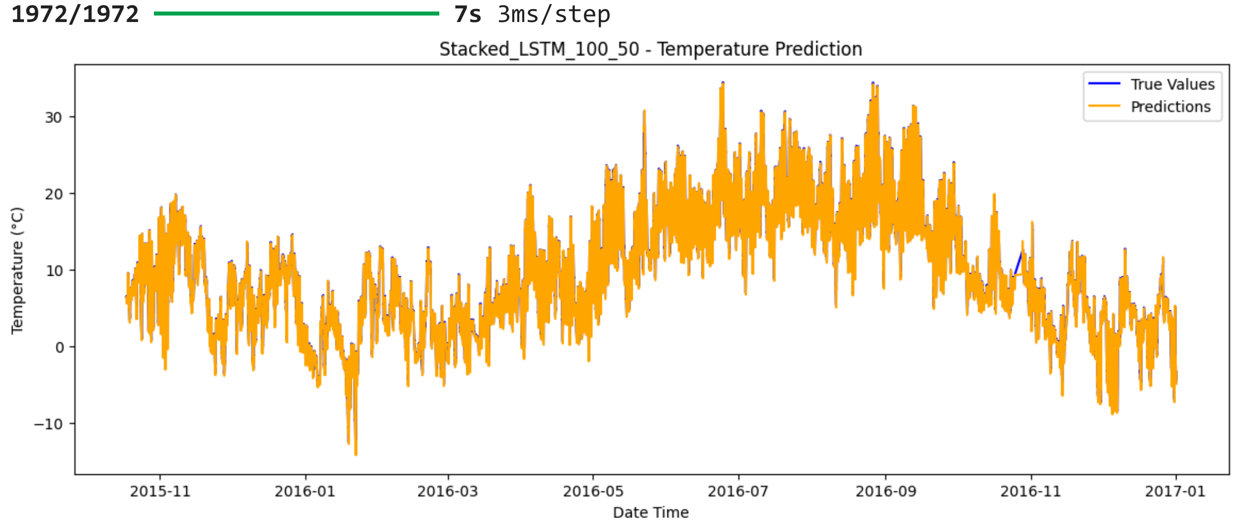

```
Bidirectional_LSTM_100 MAE: 0.1327
Training Stacked_LSTM_50_50 model...
Epoch 1/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 106s 11ms/step - loss: 0.0012 - val_loss: 1.5214e-05
Epoch 2/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 104s 11ms/step - loss: 2.1015e-05 - val_loss: 4.8905e-
05
Epoch 3/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 104s 11ms/step - loss: 1.7043e-05 - val_loss: 1.2252e-
05
Epoch 4/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 106s 12ms/step - loss: 1.5548e-05 - val_loss: 1.4831e-
05
Epoch 5/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 103s 11ms/step - loss: 1.5233e-05 - val_loss: 1.9987e-
05
1972/1972 ━━━━━━━━━━━━━━━━━━━━ 7s 4ms/step
```

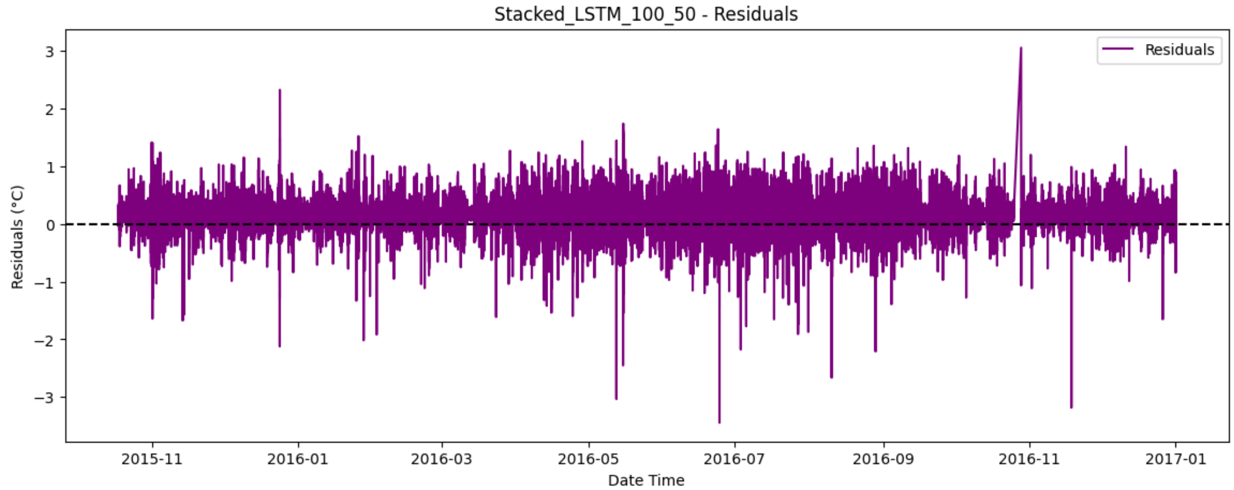


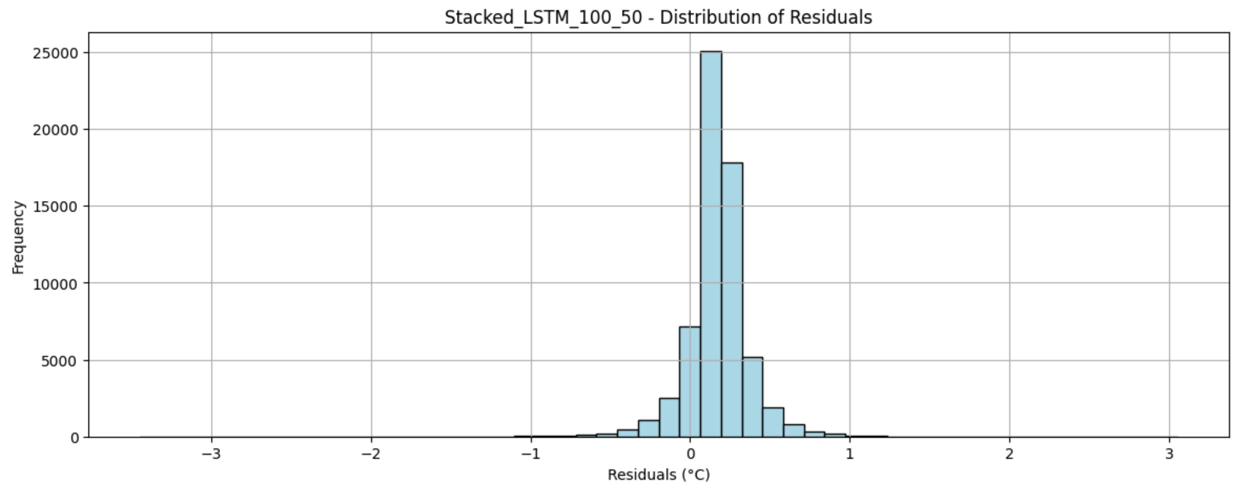




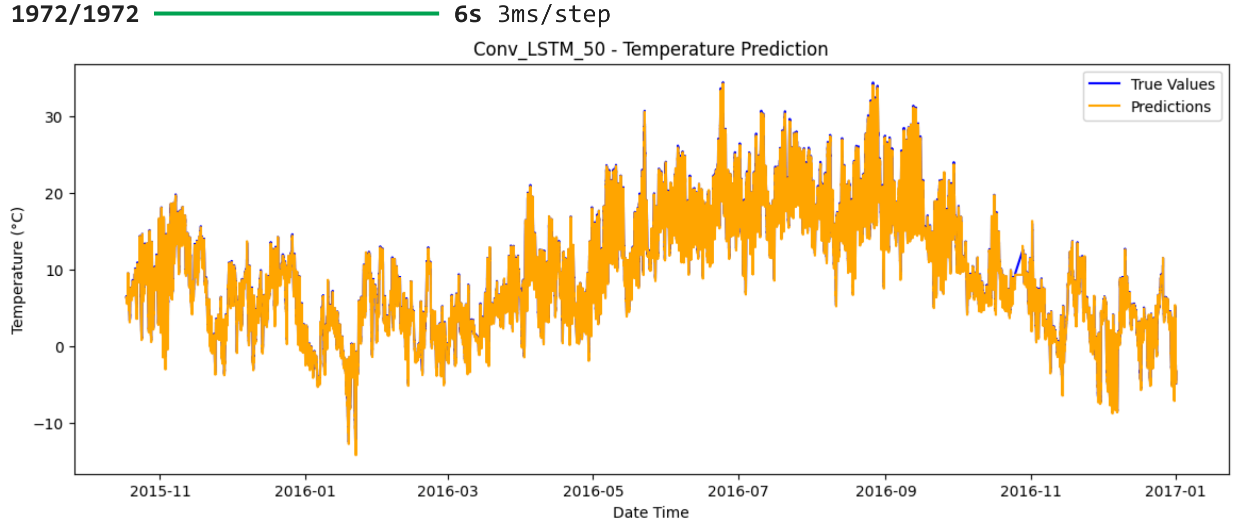

```
Stacked_LSTM_50_50 MAE: 0.1955
Training Stacked_LSTM_100_50 model...
Epoch 1/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 81s 9ms/step - loss: 9.0394e-04 - val_loss: 1.5288e-05
Epoch 2/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 82s 9ms/step - loss: 1.8080e-05 - val_loss: 1.5883e-05
Epoch 3/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 80s 8ms/step - loss: 1.5874e-05 - val_loss: 1.2578e-05
Epoch 4/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 81s 9ms/step - loss: 1.4559e-05 - val_loss: 1.3982e-05
Epoch 5/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 81s 9ms/step - loss: 1.4630e-05 - val_loss: 1.9952e-05
1972/1972 ━━━━━━━━━━━━━━━━━━━━ 7s 3ms/step
```

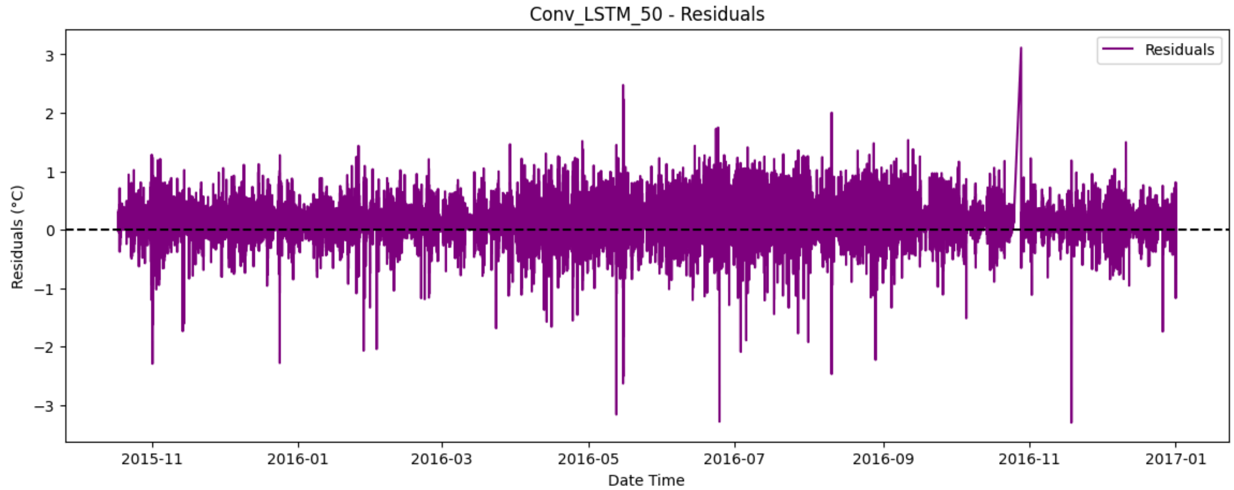


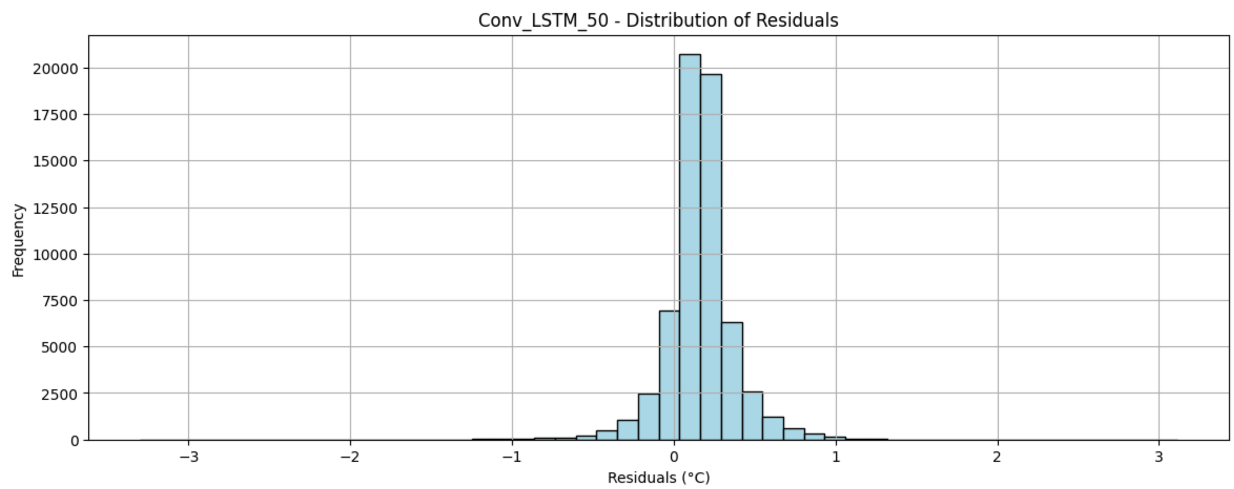




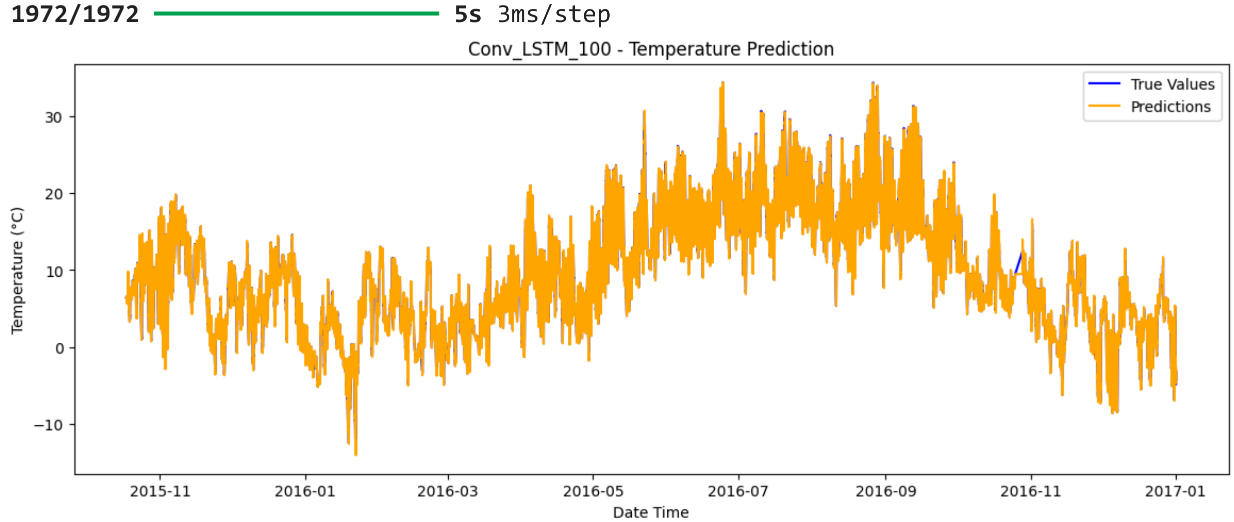

```
Stacked_LSTM_100_50 MAE: 0.2093
Training Conv_LSTM_50 model...
Epoch 1/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 58s 6ms/step - loss: 8.7930e-04 - val_loss: 2.1990e-05
Epoch 2/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 54s 6ms/step - loss: 2.8326e-05 - val_loss: 2.0212e-05
Epoch 3/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 82s 6ms/step - loss: 2.3102e-05 - val_loss: 2.0023e-05
Epoch 4/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 84s 6ms/step - loss: 1.8703e-05 - val_loss: 2.2838e-05
Epoch 5/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 80s 6ms/step - loss: 1.7576e-05 - val_loss: 2.2036e-05
1972/1972 ━━━━━━━━━━━━━━━━━━━━ 6s 3ms/step
```

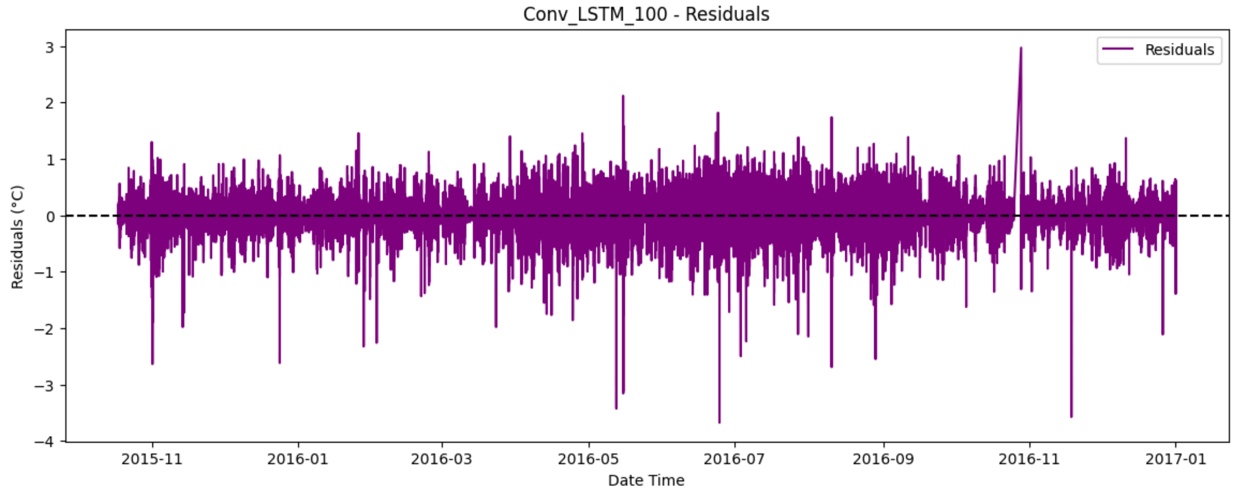


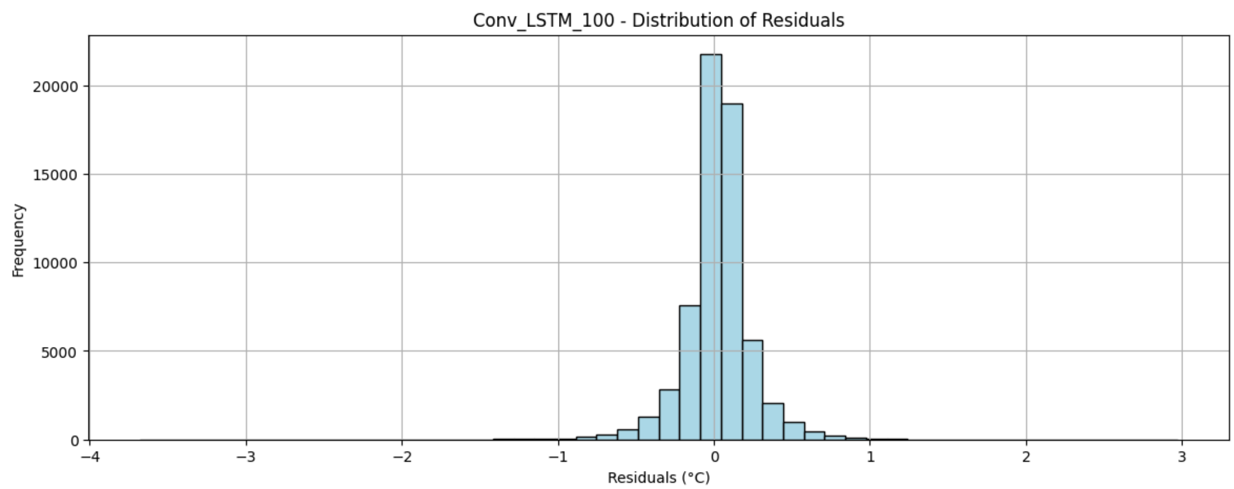




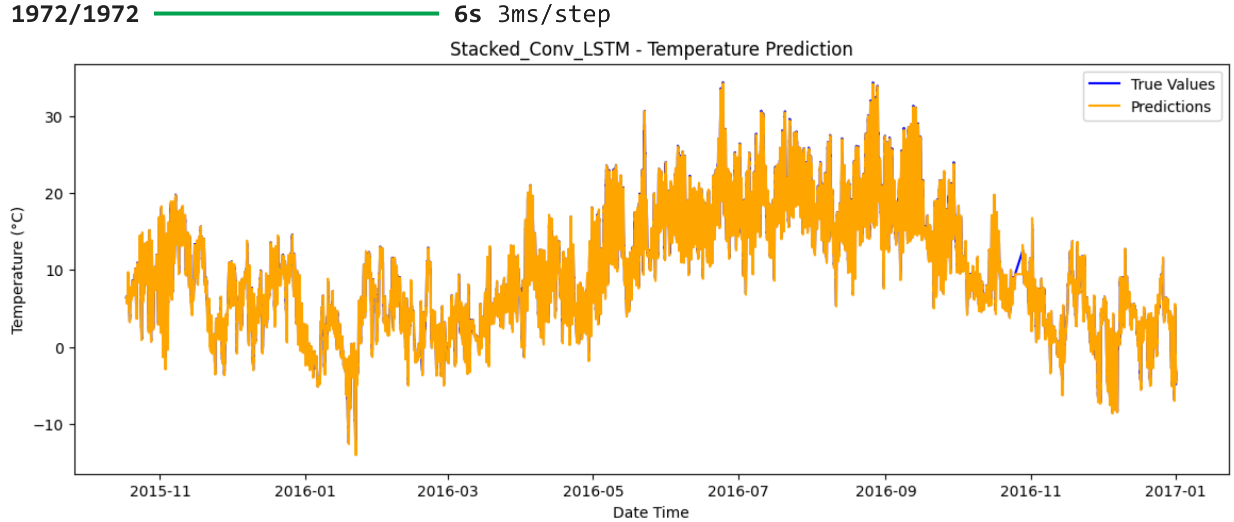

```
Conv_LSTM_50 MAE: 0.2084
Training Conv_LSTM_100 model...
Epoch 1/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 56s 6ms/step - loss: 0.0014 - val_loss: 2.0363e-05
Epoch 2/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 82s 6ms/step - loss: 2.6092e-05 - val_loss: 1.7784e-05
Epoch 3/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 58s 6ms/step - loss: 2.2489e-05 - val_loss: 1.6751e-05
Epoch 4/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 81s 6ms/step - loss: 1.9814e-05 - val_loss: 1.8026e-05
Epoch 5/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 82s 6ms/step - loss: 1.9084e-05 - val_loss: 1.4800e-05
1972/1972 ━━━━━━━━━━━━━━━━━━━━ 5s 3ms/step
```

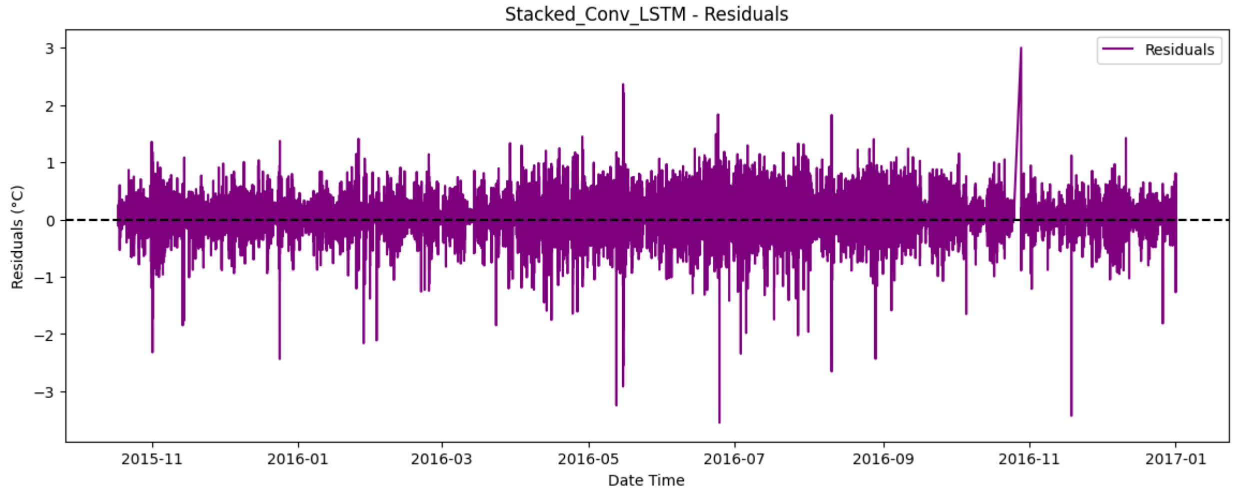


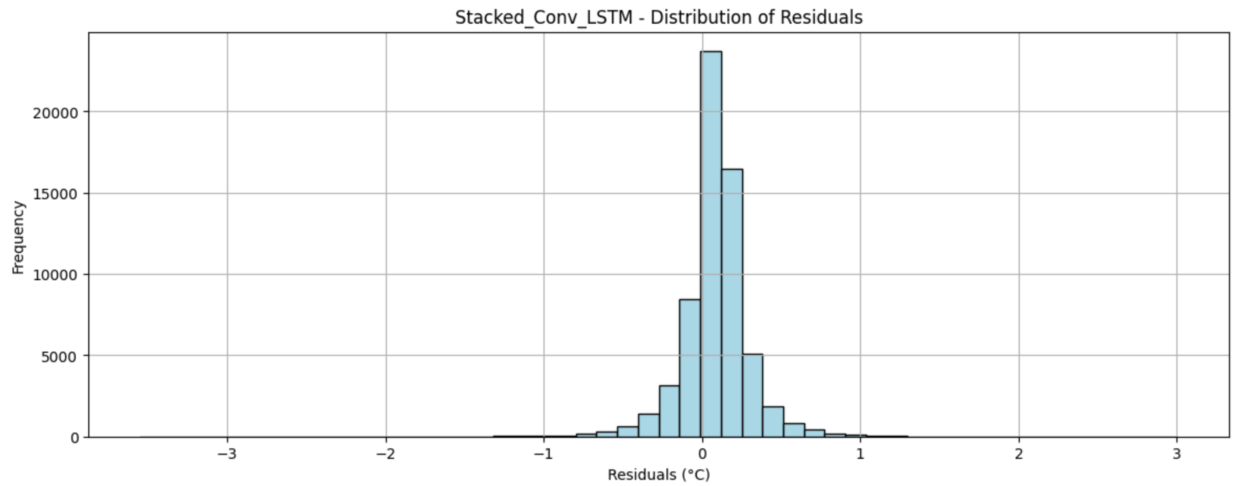




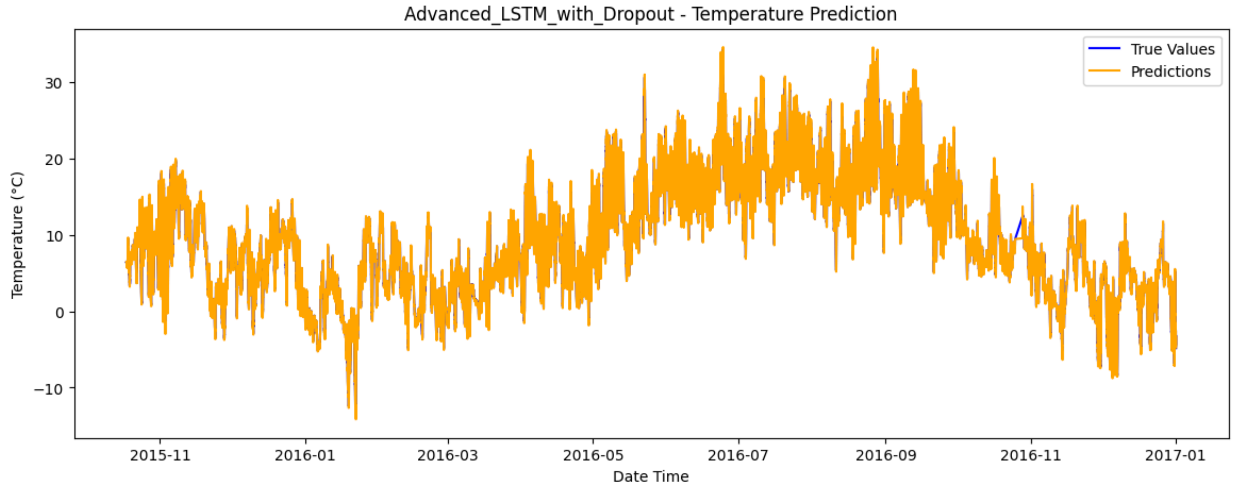

```
Conv_LSTM_100 MAE: 0.1431
Training Stacked_Conv_LSTM model...
Epoch 1/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 77s 8ms/step - loss: 0.0012 - val_loss: 2.5279e-05
Epoch 2/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 84s 8ms/step - loss: 2.8347e-05 - val_loss: 1.5515e-05
Epoch 3/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 84s 9ms/step - loss: 2.0687e-05 - val_loss: 1.5823e-05
Epoch 4/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 80s 9ms/step - loss: 1.9194e-05 - val_loss: 2.4945e-05
Epoch 5/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 79s 8ms/step - loss: 1.8738e-05 - val_loss: 1.6209e-05
1972/1972 ━━━━━━━━━━━━━━━━━━━━ 6s 3ms/step
```

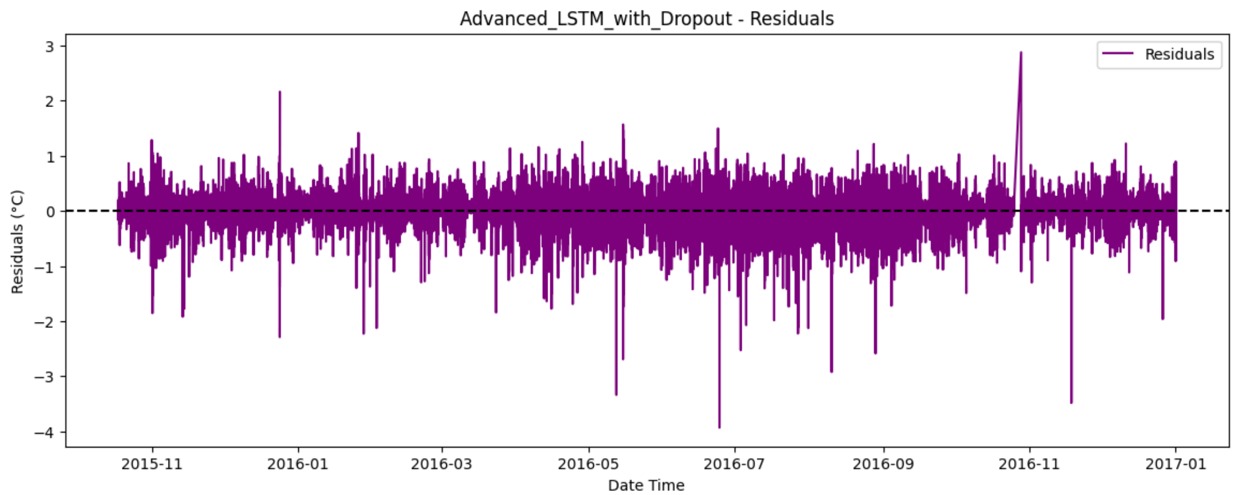


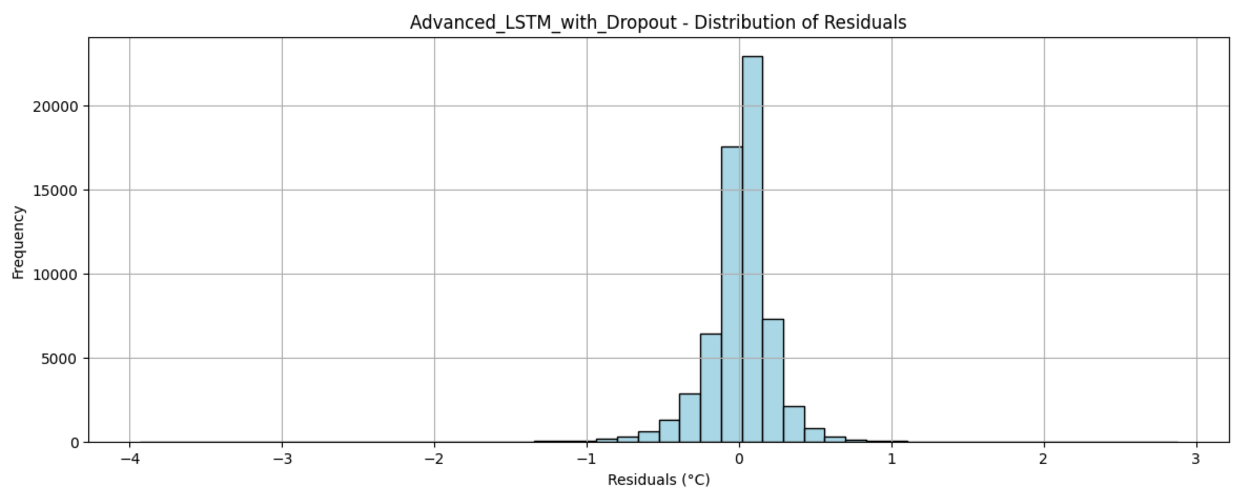




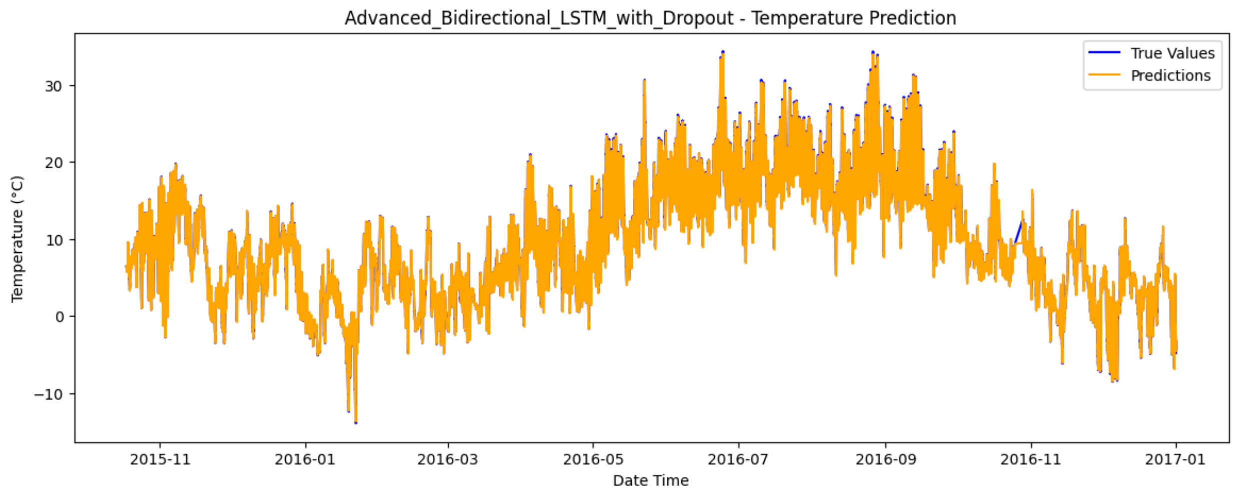

```
Stacked_Conv_LSTM MAE: 0.1624
Training Advanced_LSTM_with_Dropout model...
Epoch 1/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 96s 10ms/step - loss: 0.0012 - val_loss: 2.5050e-05
Epoch 2/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 88s 10ms/step - loss: 3.7990e-05 - val_loss: 1.2951e-0
5
Epoch 3/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 141s 9ms/step - loss: 3.0471e-05 - val_loss: 1.2633e-0
5
Epoch 4/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 142s 10ms/step - loss: 2.7372e-05 - val_loss: 1.7204e-
05
Epoch 5/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 143s 10ms/step - loss: 2.5713e-05 - val_loss: 1.4179e-
05
1972/1972 ━━━━━━━━━━━━━━━━━━━━ 7s 3ms/step
```

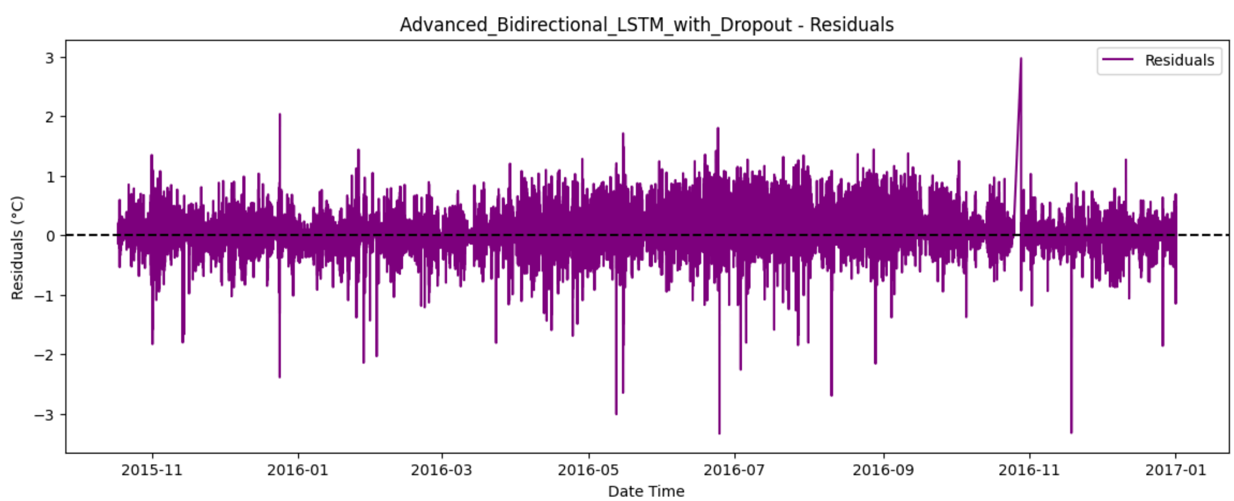

Advanced_LSTM_with_Dropout - Temperature Prediction
True Values
Predictions
Temperature (°C)
Date Time
2015-11
2016-01
2016-03
2016-05
2016-07
2016-09
2016-11
2017-01

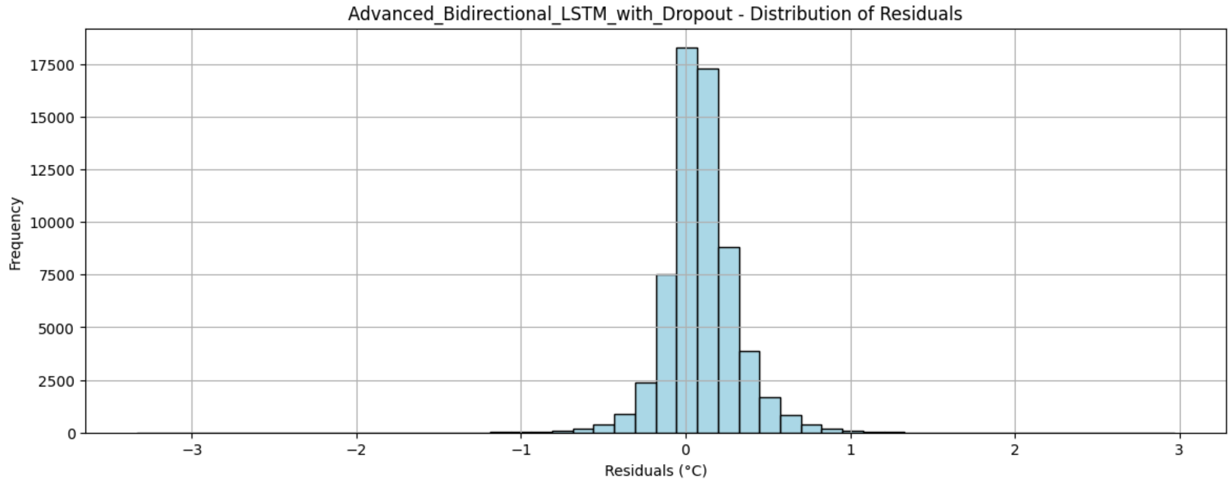

Advanced_LSTM_with_Dropout - Residuals
Residuals
Residuals (°C)
Date Time
2015-11
2016-01
2016-03
2016-05
2016-07
2016-09
2016-11
2017-01


Advanced_LSTM_with_Dropout - Distribution of Residuals
Frequency
Residuals (°C)

```
Advanced_LSTM_with_Dropout MAE: 0.1444
Training Advanced_Bidirectional_LSTM_with_Dropout model...
Epoch 1/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 152s 16ms/step - loss: 8.6533e-04 - val_loss: 3.9261e-
05
Epoch 2/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 150s 16ms/step - loss: 3.8655e-05 - val_loss: 1.9457e-
05
Epoch 3/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 202s 16ms/step - loss: 2.8121e-05 - val_loss: 2.0239e-
05
Epoch 4/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 199s 16ms/step - loss: 2.5980e-05 - val_loss: 3.1008e-
05
Epoch 5/5
9199/9199 ━━━━━━━━━━━━━━━━━━━━ 148s 16ms/step - loss: 2.4396e-05 - val_loss: 1.7915e-
05
1972/1972 ━━━━━━━━━━━━━━━━━━━━ 12s 6ms/step
```








```
Advanced_Bidirectional_LSTM_with_Dropout MAE: 0.1692
```