

KMP algorithm

Pre processing: lps array

longest prefix that is also a suffix.

→ a b c d a b c

prefix: a, ab, abc, abcd, abcda, abcdab, ~~abcdabc~~suffix: c, bc, abc, dabc, cdabc, bcdabc, ~~abcdabc~~

lps[i] → longest prefix that is also a suffix for string 0 → i.

	0	1	2	3	4	5	6	7	8	9
P ₁ :	a	b	c	d	a	b	e	a	b	f

lps: 0 0 0 0 1 2 0 1 2 0

abcdabeab

		1	2	3	4	5	6	7	8	9	10
P ₂ :	a	b	c	d	e	a	b	f	a	b	c

lps: 0 0 0 0 0 1 2 0 1 2 3

		1	2	3	4	5	6	7	8	9	10	11
P ₃ :	a	a	b	c	a	d	a	a	b	e		

lps: 0, 1, 0, 0, 1, 0, 1, 2, 3, 0

		1	2	3	4	5	6	7	8	9	10	11	12
P ₄ :	a	a	a	a	b	a	a	c	d				

lps: 0 1 2 3 0 1 2 0 0

KMP eg. i ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓

String: a b a b a b a b a b a b d

Pat: a b a b d

lps:

0	0	1	2	0
---	---	---	---	---

↑ ↑ ↑ ↑

if (string[i] == pat[j+1]) {
 i++;
 j++;
 }

mismatch:
 → j = lps[j] until j=0
 else i++

Pre processing
 Compute LPS:

- 1) int len = 0; lps[0] = 0; i = 1;
- 2) while (i < pat.length()) {
 - a) if (pat[i] == pat[len]) {

len++
 lps[i] = len;
 i++
 - b) else {
 - i) if (len != 0) len = lps[len-1];
 - ii) else lps[i] = 0; i++;

↓ ↓ ↓ ↓ ↓ ↓ ↓

a b c d e a b f a b c

lps

0	0	0	0	0	1	2	0	1	2	3
---	---	---	---	---	---	---	---	---	---	---

i len

x q 0

z 10 x

3 11 2

11 0 x 2 3

5

6

7

8

KMP Search
 (pat, text)

n = length of text

↓ ↓ ↓ ↓ ↓

a a a a b

i ↓

(pat, txt)

- 1) $m = \text{length of pat}, N = \text{length of txt}$
- 2) Create lps array and run Compute LPS.
- 3) $i=0, j=0$

while $((N-i) \geq (M-j)) \{$

if (pat[j] == txt[i])
 $i++; j++;$

if (j == m)

 return true;

else if $(i < N \ \&\& \ \text{pat}[j] \neq \text{txt}[i]) \{$

 if (j != 0)

$j = \text{lps}[j-1];$

 else

$i++$

}

a a a a b
 ↑ ↑
a a b
0 1 0