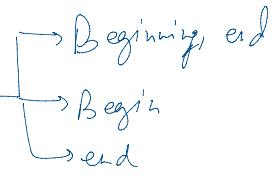


2 pointers

1) Need to know where to place the pointer.



2) Need to know how to move the pointers.

Smallest sequence with given Primes

Prime

$$\underbrace{A=2}_{\text{---}} \quad \underbrace{B=3}_{\text{---}} \quad \underbrace{C=5}_{\text{---}} \quad \boxed{D=7}$$

$$2 \rightarrow 2$$

$$\overbrace{2, 3, 4, 5, 6, 8, 9}^{\text{---}}$$

$$3 \rightarrow 3$$

$$4 \rightarrow \underline{2 \times 2}$$

$$5 \rightarrow 5$$

$$6 \rightarrow 2 \times 3$$

$$7 \rightarrow 7$$

$$8 \rightarrow 2 \times 2 \times 2$$

$$9 \rightarrow 3 \times 3$$

1) Take a number  $\text{num} = 2$  and a vector  $\langle \text{id} \rangle \text{ ans}$ .

2) Till size of  $\text{ans} < D$ :

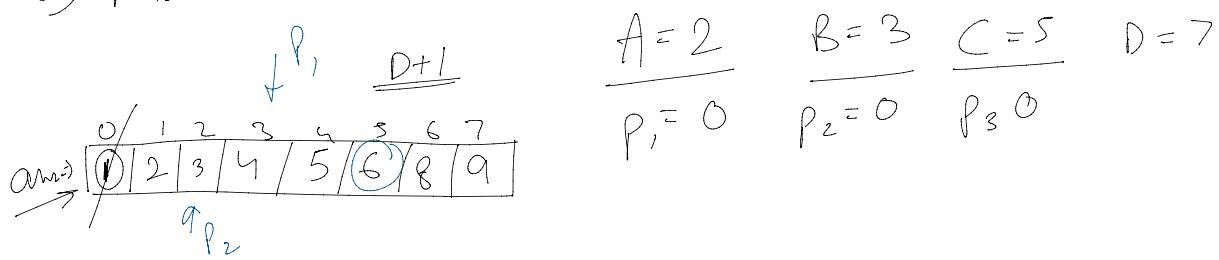
a) Prime factorize  $\text{num}$

b) check if all prime factors are from  $A, B, C$ :

i) If yes: add to  $\text{ans}$ .

c) num++

3) Return ans.



a) Insert 1 into ans.

b) Loop till size of ans = D+1.

1) find min( $\underline{\text{ans}[P_1] \times A}$ ,  $\underline{\text{ans}[P_2] \times B}$ ,  $\underline{\text{ans}[P_3] \times C}$ ).  $\rightarrow$  num

2) Insert num into ans.

3) If ( $\text{num} = \underline{\text{ans}[P_1] \times A}$ )  $P_1++$ .

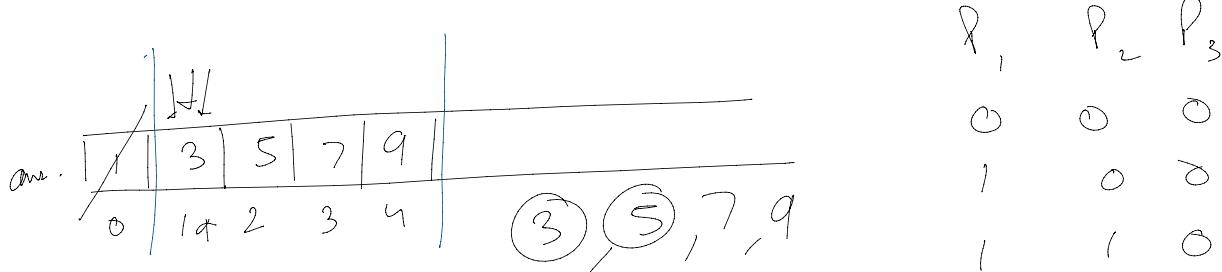
4) If ( $\text{num} = \underline{\text{ans}[P_2] \times B}$ )  $P_2++$ .

5) If ( $\text{num} = \underline{\text{ans}[P_3] \times C}$ )  $P_3++$ .

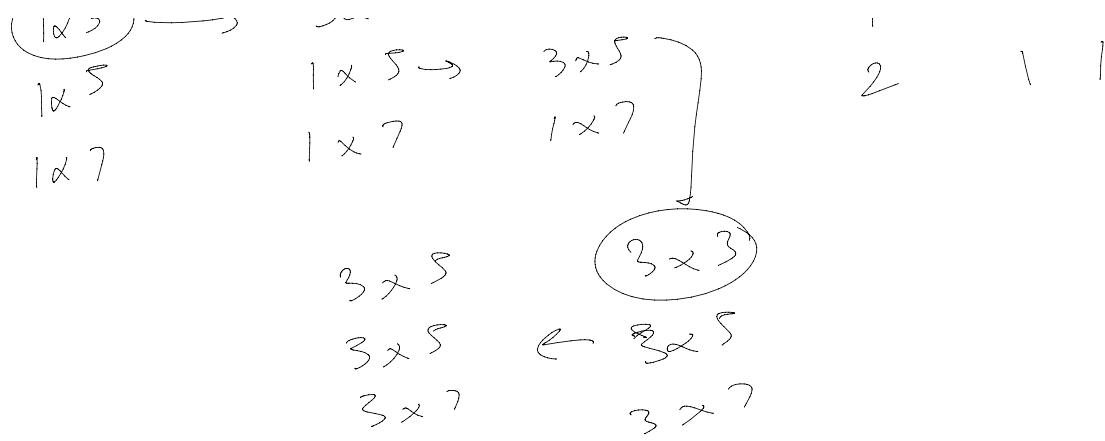
c) Remove 1<sup>st</sup> element from ans.

d) Return ans.

$$A=3 \quad B=5 \quad C=7 \quad D=4$$



$$\begin{array}{c} 1 \times 3 \\ 1 \times 5 \end{array} \rightarrow \begin{array}{c} 3 \times 3 \\ 1 \times 5 \rightarrow 3 \times 5 \end{array} \quad \begin{array}{c} 3 \times 3 \\ 3 \times 5 \end{array}$$



Diff K

$A: \begin{bmatrix} 1 & 3 & 5 \\ 0 & 1 & 2 \end{bmatrix}$  sorted

$i \neq j \wedge A[i] - A[j] = B$

$B: 4$

$5 - 1 = 4$   
for (int  $j=0; j < A.size(); j++$ ) {  
 for (int  $i=j+1; i < A.size(); i++$ ) {  
 if ( $A[i] - A[j] == B$ ) {  
 return true;  
 }  
}

$\begin{bmatrix} 1 & 3 & 5 \\ 0 & 1 & 2 \end{bmatrix}$   
j  
i  
0, 1, 2

$O(n^2)$

3

3  
return false;

$A: \begin{bmatrix} 1 & 3 & 5 & 6 & 10 & 25 & 36 \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 \end{bmatrix}$

$B=20$   
22

If I do  $P_1++$  (difference  $\uparrow$ ) .

$$\begin{array}{c} \cancel{P_1 = 0} \\ P_2 = 1 \end{array}$$

If I do  $P_2--$  (difference  $\downarrow$ ) .

$$P_1++ \rightarrow \uparrow$$

$$P_2++ \rightarrow \uparrow$$

1)  $P_1 = 0, P_2 = 1.$

2) while ( $P_2 < A.size()$ )

a) If ( $A[P_2] - A[P_1] == B$ ) return true

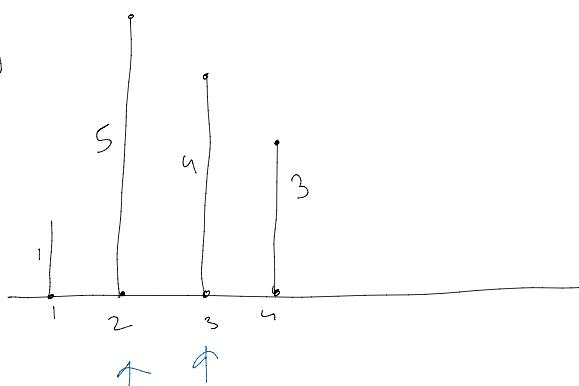
b) else if ( $A[P_2] - A[P_1] > B$ )  $P_1++;$  Time:  $O(n)$

c) else if ( $A[P_2] - A[P_1] < B$ )  $P_2++;$  Space:  $O(1)$

3) Return false .

Container with most water

$$\Rightarrow [1, 5, 4, 3]$$



$$3 \times 1 \Rightarrow 3$$

$$1 \times 2 \Rightarrow 2$$

$$\boxed{3 \times 2 = 6}$$

$$4 \times 1 = \textcircled{4}$$

$$\text{ans} = 0;$$

```

ans = 0;
for (int i=0; i < A.size(); i++) {
    for (int j=i+1; j < A.size(); j++) {
        ans = max (ans, min(A[i], A[j]) * (j-i));
    }
}

```

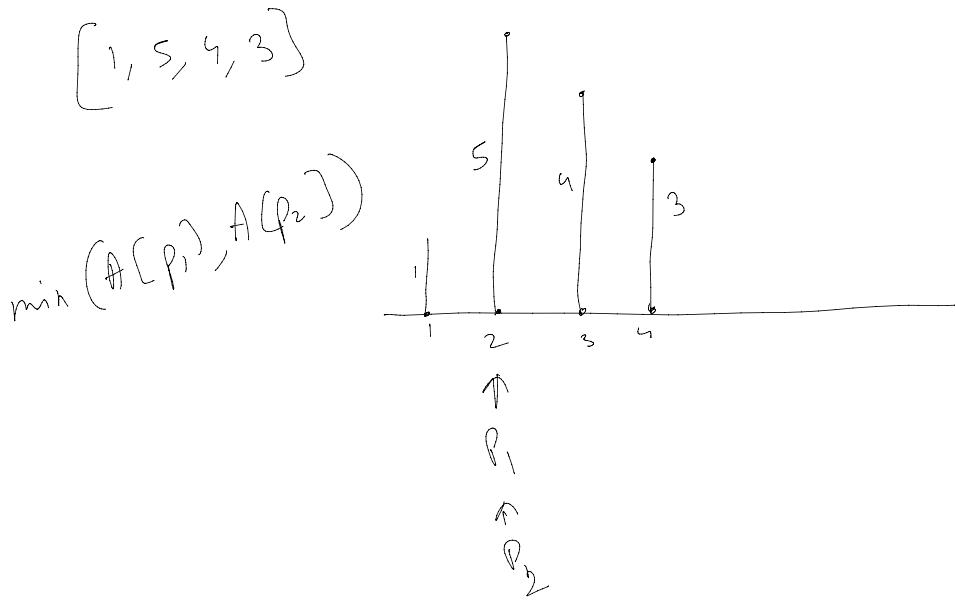
3

T:  $O(n^2)$

3

S:  $O(1)$

return ans;



$$1) P_1 = 0, P_2 = A.size() - 1.$$

$$2) ans = 0 \quad T: O(N)$$

$$3) while (P_1 < P_2) \quad S: O(1)$$

$$a) ans = \max (ans, \min (A[P_1], A[P_2]) * (P_2 - P_1));$$

$$b) if (A[P_1] < A[P_2]) \quad P_1++;$$

b) if ( $A[p_1] < A[p_2]$ )  $P_1++;$   
c) else  $P_2--;$

4) Return ans.

Minimize the absolute difference

3 return arr;

$$A = \{1, 4\} \quad i = 0, 1 \quad j = 0, 1 \quad k = 0, 1 \quad (1, 6, 2), (1, 6, 3)$$

$A : \{1, 4\}$	0	0	0, 1	$(1, 6, 2), (1, 6, 3)$
$B : \{6, 9\}$		1	0, 1	$(1, 9, 2), (1, 9, 3)$
$C : \{2, 3\}$		1	0, 1	$(4, 6, 2), (4, 6, 3)$
		1	0, 1	$(4, 9, 2), (4, 9, 3)$

$$A \left[ \begin{matrix} 1, 4, 5, 8, 10 \\ 0, 1, 2, 3, 4 \end{matrix} \right] \quad \downarrow P_1 \quad \downarrow P_2$$

$$B \left[ \begin{matrix} 6, 9, 15 \\ 0, 1, 2 \end{matrix} \right] \quad \downarrow P_3$$

$$C \left[ \begin{matrix} 2, 3, 6, 6 \\ 0, 1, 2, 3 \end{matrix} \right]$$

$$\frac{|\max(a, b, c) - \min(a, b, c)|}{\max(a, b, c) - \min(a, b, c)}$$

$$A \downarrow - B \uparrow$$

$$6 - 1 \rightarrow 5$$

$$6 - 2 \rightarrow 4$$

$$6 - 3 \rightarrow 3$$

1) Put  $P_1=0, P_2=0, P_3=0$

2) Move the points pointing to the minimum value.

3) Optimize the given function.

Create pairs in array divisible by K

$$\left[ 2, 2, 1, 7, 5, 3 \right]$$

$$R = 4$$

$$\left[ \begin{matrix} 1, 2, 2, 3, 5, 7 \\ \uparrow \quad \uparrow \quad \uparrow \end{matrix} \right]$$

$$(1, 3)$$

$$\boxed{(2, 2)}$$

$$3$$

$(2, 2)$   
 $(7, 1)$   
 $(5, 3)$   
 $(7, 5)$   
 $(3, 1)$

Sparre

4

$ans = 0;$   
 $\text{for}(\text{int } i=0; i < A.\text{size}(); i++) \{$

$\text{for}(\text{int } j=i+1; j < A.\text{size}(); j++) \{$   $T: O(n^2)$   
 $\text{if}((A[i] + A[j]) \% R == 0) \{$   $S: O(1)$

$ans++;$

3

3

return ans;

$\begin{matrix} \downarrow & \downarrow & \downarrow & \downarrow & \downarrow \\ (2, 2, 1, 7, 5, 3) \end{matrix}$

5, 5, 3

0 1 2 3  
1 0 2 1 0 1

$\begin{matrix} \downarrow & \downarrow & \downarrow \\ (1) & (2) & (3) \\ \downarrow & \downarrow & \downarrow \\ 0 & 1 & 0 & 1 & 0 \end{matrix}$

$2C_2$

$R = n$

$n \% n$   
 $0, 1, 2, 3$

②

$$\left( \frac{a \% n}{n} + \frac{b \% n}{n} \right) \% n = \underline{(a+b)} \% n$$

1, 5      7, 3

$(\underline{i} + \underline{j}) \% n$

ab

$$a \% n = i \quad b \% n = j$$

$$a = (pn+i) \quad b = (qn+j)$$

$$( (n \% n + i) \% n + (q \% n + j) \% n ) \% n = \underline{(pn+i+qn+j)} \% n$$

$$\left( \frac{(p_n+i)\%n + (q_n+j)\%n}{(i+j)\%n} \right) \%n = \left( \frac{p_n+i+q_n+j}{i+j} \right) \%n$$

$$(i+j)\%n = ((p+q)n + i+j) \%n$$

$$LHS = RHS$$

$$\begin{array}{ccccccc} & + & + & + & + & + & + \\ 0 & 1 & 2 & 3 & 4 & 5 & 6 \\ \textcircled{a} \boxed{b/c/d/e/f/g} & & & & & & \end{array} \quad R = 7$$

$7, 21 \rightarrow 28$

$$bg + cf + de + ac_2$$

$$\begin{array}{cccccc} & 2 & 1 & 7 & 8 & 8 \\ & + & & & & + \\ 0 & 1 & 2 & 3 & & \\ \boxed{0/2/2/2} & & & & & \end{array} \quad 2 \times 2 \Rightarrow 4 \quad \begin{array}{c} 2x1 \\ \hline x \\ \boxed{5} \end{array}$$

$$\begin{array}{ccccc} & + & + & + & + \\ 0 & 1 & 2 & 3 & 4 \\ \boxed{a/b/c/d/e} & & & & \end{array} \quad R = 5$$

$$\Rightarrow cd + be + \frac{a(a-1)}{2}$$