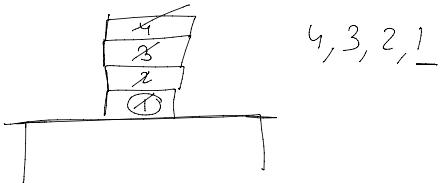


Stacks & Queues

Stacks

FIFO → First in Last out



- push : add an element.
 - pop : remove an element
 - peek : see-the top element.
- Time complexity
 $O(1)$

Evaluate reverse polish notation

$$\underline{2 + 3 * 10} = 32$$

2 3 10 * +



$$3 \times 10 = \underline{30}$$

$$30 + 2 = 32$$

$$4 + 2 \rightarrow 42 +$$

$$3 - 6 \rightarrow \underline{36} -$$

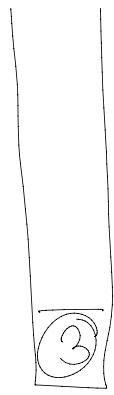
$$\underline{4} \underline{2} \pm \underline{3} =$$

$$4 + 2 = 2 + 4$$

$$\underline{4} - \underline{2} \neq \underline{2} - \underline{4}$$

$$6 - 3$$

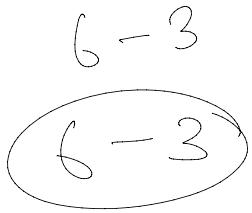
$$4 \underline{2} \pm \underline{3} =$$



$$\begin{array}{r} 4+2=6 \\ \hline \end{array}$$

$$6-3$$

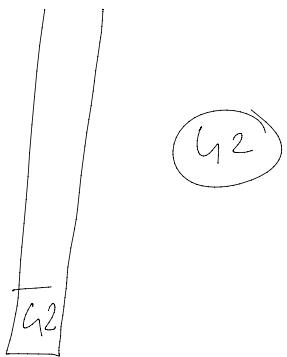
$$3-6$$



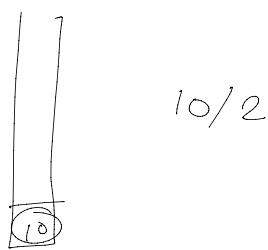
$$4 + \underline{5} \neq \underline{4} + 6 \neq 3$$

$$+ + + + + + +$$

$$454 * + 63 * +$$



$$\Rightarrow 510 2/+$$



1) Create a stack.

2) Iterate through the input.

3) If it is an operand, push it into the stack.

4) If it is an operator:

int num = stack.top;

$y_1 > y$

```
int num1 = stack.top();
stack.pop();
```

```
int num2 = stack.top();
stack.pop();
stack.push(num2 operator num1)
```

5) return stack.top;

Nearest smaller element

$[4, 5, 2, 10, 8]$

$[-1, 4, -1, 2, 2]$

$[1, 2, 3]$

Brute force $\underline{\mathcal{O}(n^2)}$ $\times [-1, 1, 1]$ $\min = 1$

int arr[A.size()] = {-1};

```
for(int i=0; i < A.size(); i++) {
```

```
    for(int j=i-1; j>=0; j--) {
```

```
        if(A[j] < A[i]) {
```

```
            arr[i] = A[j];
```

```
            break;
```

3
3
3

return arr;

$i \downarrow \uparrow \downarrow \uparrow \downarrow$
 $[4, 5, 2, 10, 8]$

$0 \uparrow 2 \uparrow 3 \uparrow 4$
 $[-1, 4, -1, 2, 2]$

$i \uparrow \downarrow \uparrow \downarrow \uparrow$
 $[9, 3, 5, 6, 4]$

$\Rightarrow [-1, -1, 3, 5, 3]$

$\downarrow \uparrow \downarrow \uparrow \downarrow$

$\left[\begin{smallmatrix} & & & & & \\ 4, 5, 2, 10, 8 \end{smallmatrix} \right]$

$\left[\begin{smallmatrix} -1, 4, -1, 2, 2 \end{smallmatrix} \right]$

T: $O(n)$
 S: $O(n)$



- > Remove all $-l$ th elements \geq current element
- > Put stack top into $-l$ th ans.
- > Put $-l$ th current element into stack.

create a stack, put -1 into it.

```

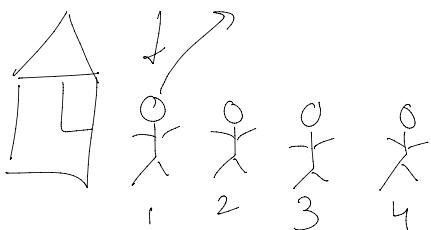
for(int i=0; i<A.size(); i++) {
    while(stack.top() >= A[i])
        stack.pop();
}
    
```

$ans[i] = stack.top$
 $stack.push(A[i]);$

}

return ans;

Queue



FIFO

first in first out

1) Enqueue : Add element to queue

Time complexity
 $\sim O(1)$

- 1) Enqueue : Add element to queue → Time complexity
 2) Deque : Remove element from queue → $O(1)$
 3) front : See the front element

Sliding window maximum

$[1, 3, -1, -3, 5, 3, 6, 7]$ $R = 3$

$[3, 3, 5, 5, 6, 7]$

R

$\boxed{1}$

Double ended queue (stack + queue) : ~~Q F L R~~

- 1) Add front
- 2) Add back
- 3) Remove front
- 4) Remove back

- 5) front
- 6) last

$O(1)$

$\boxed{1, 3, -1} -3, 5, 3, 6, 7$

- > remove all elements less than current element from back.
- > remove all elements out of window from the front
- > Add current element at the back.

$\rightarrow [6] 7)$

$[3, 3, 5, 5, 6, 7]$

maintain a queue with indices instead of values.

$$T: O(N) \quad S: O(N)$$

Reverse first k elements of a queue

$$\left[1, 2, 3, 4, 5 \right] \quad k=3 \quad \Rightarrow \left[3, 2, 1, 4, 5 \right]$$

$$\left[3, 2, 1, 4, 5 \right]$$

