

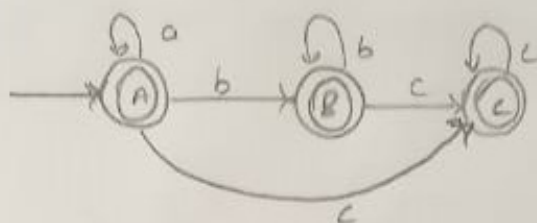
Consider the state $q_2 \in (Q_2)$

on input a $\delta(q_2, a) = \emptyset$

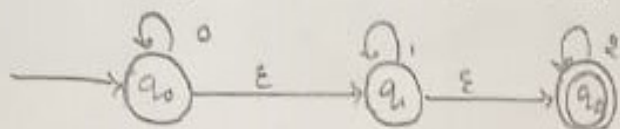
on input b $\delta(q_2, b) = \emptyset$

on input c $\delta(q_2, c) = \text{error}$ $(Q_2) = \{q_2, \delta(c)\}$.

δ	a	b	c
x A	A	B	C
x B	\emptyset	B	C
x C	\emptyset	\emptyset	C



→ The ϵ -closure of q denoted by $\epsilon\text{closure}(q)$ is the set of all state which are reachable from q on ϵ -transition only. It is recursively defined as: state p is in $\epsilon\text{closure}(q)$ i.e., $\epsilon\text{closure}(q) = q \cup \{p \mid \text{if } \epsilon\text{closure}(q) \text{ contains } p \text{ and if there is a transition from state } p \text{ to state } r \text{ labeled } \epsilon, \text{ then state } p \text{ also in } \epsilon\text{closure}(q)\}$



$$\epsilon\text{closure}(q_0) = \{q_0, q_1, q_2\} \dots A$$

consider the state $\{q_0, q_1, q_2\}$
on input 0

$$\begin{aligned}\delta(\{q_0, q_1, q_2\}, 0) &= \epsilon\text{closure}(\{q_0\}) \\ &= \{q_0, q_1, q_2\} \dots (A)\end{aligned}$$

On input 1

$$\begin{aligned}\delta(\{q_0, q_1, q_2\}, 1) &= \epsilon\text{closure}(q_1) \\ &= \{q_1, q_2\} \dots (B)\end{aligned}$$

on input 2

$$\begin{aligned}\delta(\{q_0, q_1, q_2\}, 2) &= \epsilon\text{closure}(\{q_2\}) \\ &= \{q_2\} \dots (C)\end{aligned}$$

consider the state $\{q_1, q_2\}$

on input 0

$$\delta(\{q_1, q_2\}, 0) = \epsilon\text{closure}(\{q_1\}) = \emptyset$$

on input 1

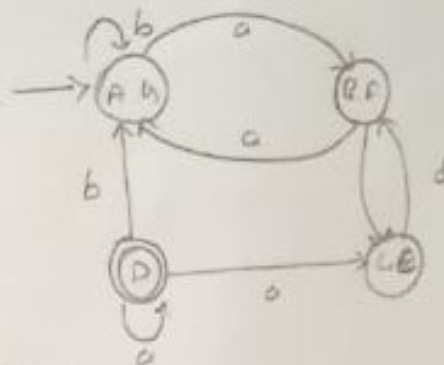
$$\delta(\{q_1, q_2\}, 1) = \epsilon\text{closure}(\{q_1, q_2\}) = \emptyset$$

on input 2

$$\begin{aligned}\delta(\{q_1, q_2\}, 2) &= \epsilon\text{closure}(\{q_2\}) \\ &= \{q_2\} \dots (C)\end{aligned}$$

$$\begin{aligned}\text{on input } 2 &= \delta(\{q_1, q_2\}, 2) = \epsilon\text{closure}(\{q_2\}) \\ &= \{q_2\} \dots (C)\end{aligned}$$

(L, G) (D, G) (B, D)
 (E, F) (D, G) ~~(A, F, E)~~
 (F, G) (D, F) (F, G)
 (E, H) (G, F) (E, G)
 (F, G) (G, G) (E, D)
 (G, H) (F, G) (D, G)



11) Give the Difference b/w DFA, NFA & E-NFA

DFA

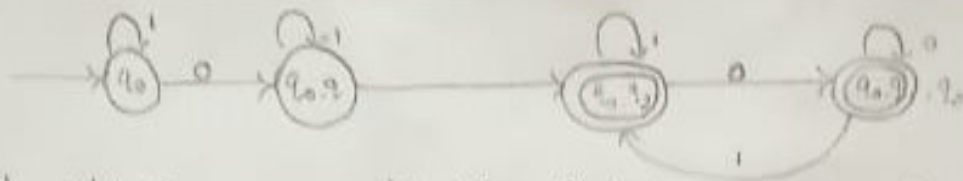
NFA

E-NFA

- | | | |
|---|---|---|
| 1) The DFA is 5-tuple
$M = (Q, \Sigma, \delta, q_0, F)$
where Q is finite state
Σ is Alphabet set of input
$\delta: Q \times \Sigma \rightarrow Q$
q_0 : start state
F : final state | 1) An NFA is 5-tuple
$(Q, \Sigma, \delta, q_0, F) = M$
where Q is finite state
Σ is Alphabet set of input
$\delta: Q \times \Sigma \rightarrow 2^Q$
q_0 : start state | 1) An E-NFA is 5-tuple
$- e$
$M = (Q, \Sigma, \delta, q_0, F)$
where Q is finite state
Σ is Alphabet set of input
$\delta = Q \times (\Sigma \cup \epsilon) \rightarrow 2^Q$
q_0 : start state |
| 2) less no of transition | 2) Relatively less no of transition | 2) Relatively more transition when compared with NFA |
| 3) Difficult to construct | 3) Easy to construct | 3) Easy to construct using regular expression. |

12) Define ϵ -closure and also find the ϵ -closure for the following & convert it to DFA,





10% obtain two distinguishable table for automaton and then minimise the state of following DFA.

δ	a	b
A	B	A
B	A	C
C	D	B
D	D	A
E	D	F
F	G	E
G	F	G
H	G	D

	B	C	D	E	F	G	H
B							
C							
D	+	+	+				
E						x	
F						x	
G						x	
H						x	

δ	a	b
(A.B)	(A.B)	(A.C)
(A.C)	(B.D)	(A.B)
(A.E)	(B.D)	(A.F)
(A.F)	(B.G)	(A.E)
(A.G)	(B.F)	(A.G)
(A.H)	(B.G)	(A.D)
(B.C)	(A.D)	(C.F)
(B.F)	(A.G)	(C.E)
(B.G)	(A.F)	(C.G)
(B.H)	(A.G)	(C.E)
(B.G)	(A.F)	(C.E)
(B.H)	(A.G)	(C.E)
(C.E)	(D.D)	(B.F)
(C.F)	(D.G)	(B.E)

	B	C	D	E	F	G	H
B							
C	+	+					
D	+	+	+				
E	+	+					
F							
G				+	+	+	
H	+	+	+	+	+	+	+

δ	0	1
q_0	$\{q_0, q_1\}$	q_0
q_1	\emptyset	q_2
q_2	q_2	q_2

$\rightarrow q_0$ is the start state of NFA $[q_0]$ is the start of DFA

$$\rightarrow \Sigma = \{0, 1\}$$

for state $\{q_0\}$ $I, S = 0$

$$I_1 = 1$$

$$\delta_0(\{q_0\}, 0) = \{q_0, q_1\}$$

$$\delta_0(\{q_0\}, 1) = \{q_0\}$$

for state $\{q_0, q_1\}$

$$I, S = 0$$

$$\delta_0(\{q_0, q_1\}, 0) = \delta_N(\{q_0, q_1\}, 0)$$

$$= \delta_N(\{q_0\}, 0) \cup \delta_N(\{q_1\}, 0)$$

$$= \{q_0, q_1\} \cup \{\emptyset\}$$

$$= \{q_0, q_1\}$$

For state $\{q_0, q_1, q_2\}$: $I, S = 0$

$$\delta_0(\{q_0, q_1, q_2\}, 0) = \delta_N(\{q_0, q_1, q_2\}, 0)$$

$$= \delta_N(\{q_0\}, 0) \cup \delta_N(\{q_1\}, 0) \cup \delta_N(\{q_2\}, 0)$$

$$= \{q_0, q_1\} \cup \{\emptyset\} \cup \{q_2\}$$

$$= \{q_0, q_1, q_2\}$$

$$I, S = 1$$

$$\delta_0(\{q_0, q_1, q_2\}, 1) = \delta_N(\{q_0, q_1, q_2\}, 1)$$

$$= \delta_N(\{q_0\}, 1) \cup \delta_N(\{q_1\}, 1) \cup \delta_N(\{q_2\}, 1)$$

$$= \{q_0\} \cup \{\emptyset\} \cup \{q_2\}$$

$$= \{q_0, q_2\}$$

$$\emptyset = \{q_0\}, \{q_0, q_1\}, \{q_0, q_2\}, \{q_0, q_1, q_2\}$$

$$I = \{0, 1\}$$

$$q_0 = \text{start state}$$

$$I, S = \{q_0, q_1, q_2\}$$

$$= \emptyset \cup q_2$$

$$= \{q_0, q_2\}$$

for state $\{q_0, q_2\}$

$$I, s = 0$$

$$\delta_0(\{q_0, q_2\}, 1) = \delta_N(\{q_0, q_2\}, 1)$$

$$= \delta_N(\{q_0\}, 1) \cup \delta_N(\{q_2\}, 1)$$

$$= \{q_0\} \cup \{q_2\}$$

$$= \{q_0, q_2\}$$

for state $\{q_1, q_2\}$

$$I, s = 0$$

$$\delta_0(\{q_1, q_2\}, 0) = \delta_N(\{q_1, q_2\}, 0)$$

$$= \delta_N(\{q_1\}, 0) \cup \delta_N(\{q_2\}, 0)$$

$$= \{q_0, q_1\} \cup \{\emptyset\} \cup \{q_2\}$$

$$= \{q_0, q_1, q_2\}$$

$$I, s = 1$$

$$\delta_0(\{q_1, q_2\}, 1) = \delta_N(\{q_1, q_2\}, 1)$$

$$= \delta_N(\{q_1\}, 1) \cup \delta_N(\{q_2\}, 1)$$

$$\delta \quad 0 \quad 1$$

$$\emptyset \quad \emptyset \quad \emptyset$$

$$q_0 \quad \{q_0, q_1\} \quad \{q_1\}$$

$$q_1 \quad \{\emptyset\} \quad \{q_2\}$$

$$q_2 \quad \{q_2\} \quad \{q_2\}$$

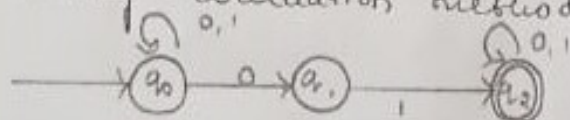
$$(q_0, q_1) \quad \{q_0, q_1\} \quad \{q_0, q_1\}$$

$$(q_0, q_2) \quad \{q_0, q_1, q_2\} \quad (q_0, q_2)$$

$$(q_1, q_2) \quad \{q_2\} \quad \{q_2\}$$

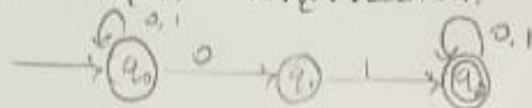
$$(q_0, q_1, q_2) \quad \{q_0, q_1, q_2\} \quad (q_0, q_2)$$

Lazy evaluation method



Q) Convert the following NFA to DFA
 i) subject construction.
 ii) Lazy evaluation method.

i) subject construction.



δ 0 1

q_0 $\{q_0, q_1\}$ q_0

q_1 \emptyset q_2

q_2 q_2 q_2

Step 1: q_0 is start state.

Step 2: $\Sigma = \{0, 1\}$

Step 3: $Q_N = \{q_0, q_1, q_2\}$

$Q_0 = \{\emptyset, \{q_0\}, \{q_1\}, \{q_2\}, \{q_0, q_1\}, \{q_1, q_2\}, \{q_0, q_2\}, \{q_0, q_1, q_2\}\}$

Step 4: final state from above subset.

$F_0 = \{\{q_2\}, \{q_0, q_2\}, \{q_1, q_2\}, \{q_0, q_1, q_2\}\}$

For state \emptyset .

Input symbol = 0

$\delta(\emptyset, 0) = \emptyset$

Input symbol = 1

$\delta_N(\emptyset, 1) = \emptyset$

For state q_0

Input symbol = 0

Input = 1

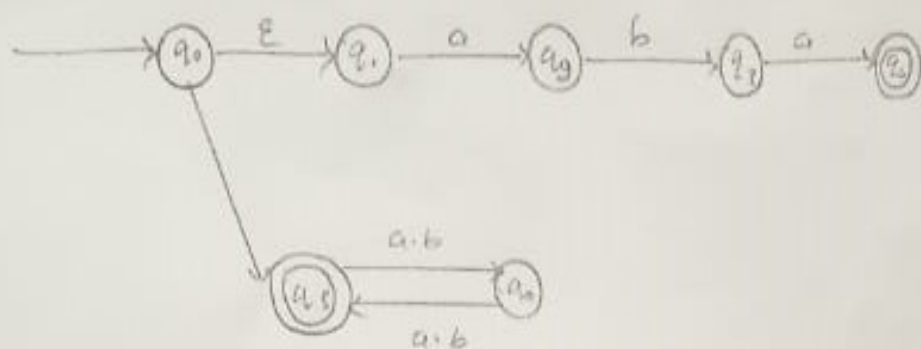
for state $\{q_0, q_1\}$

$\delta^*(q_0, 1) = \{q_0\}$

$$\begin{aligned}
 \delta_0(\{q_0, q_1, 0\}) &= \delta_N(\{q_0, q_1, 0\}) \\
 &= \delta_N(\{q_1, 0\}) \cup \delta_N(\{q_0, 0\}) \\
 &= \{q_0, q_1\} \cup \emptyset \\
 &= \{q_0, q_1\}
 \end{aligned}$$

$\therefore I_0 = 1$

$$\begin{aligned}
 \delta_0(\{q_0, q_1, 1\}) &= \delta_N(\{q_0, q_1, 1\}) \\
 &= \delta_N(\{q_0, 1\}) \cup \delta_N(\{q_1, 1\})
 \end{aligned}$$



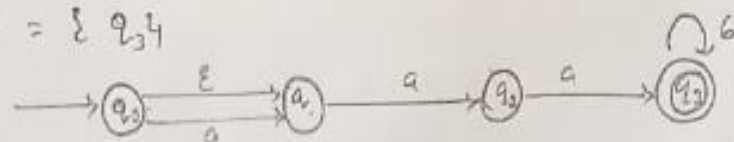
δ	a	b	ϵ
q_0	ϕ	ϕ	$\{q_0, q_1\}$
q_1	q_2	ϕ	ϕ
q_2	ϕ	q_3	ϕ
q_3	q_4	ϕ	ϕ
q_4	ϕ	ϕ	ϕ
q_5	q_6	q_6	ϕ
q_6	ϕ	ϕ	ϕ

pp2 $L = \{w \in \{a, b\}^* : w \text{ is made up of an optional } a \text{ followed by zero 'a' and max 'b's'}$

$$\Sigma = \{a, b\}.$$

$$Q = \{q_0, q_1, q_2, q_3\}.$$

$$F = \{q_3\}$$

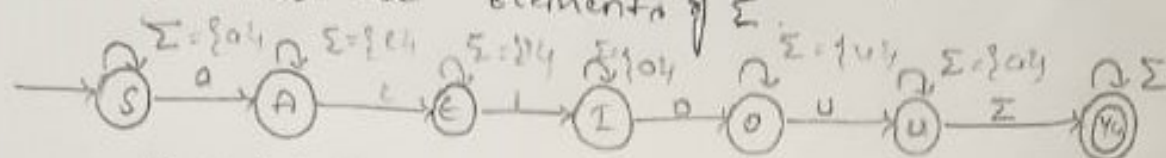


δ	a	b	ϵ
q_0	q_1	ϕ	q_1
q_1	q_2	ϕ	ϕ
q_2	q_3	ϕ	ϕ
q_3	q_3	q_3	ϕ

Start state = q_0 final state = q_7

x) $L = \{ w : w \in \{a, z\}^*$ all five vowels a, e, i, o, u, occur in alphabet order }

$\rightarrow \Sigma = \{a\}$ means all the elements of Σ except a' & let label ' Σ ' mean all elements of Σ .



$Q = \{s, a, e, i, o, u, y\}$

$S, t = \{s\}$

final state = $\{y\}$

$\Sigma = \{a, e, i, o, u\}$

δ	a	e	i	o	u
s	A	ϕ	ϕ	ϕ	ϕ
A	ϕ	e	ϕ	ϕ	ϕ
e	ϕ	ϕ	i	ϕ	ϕ
i	ϕ	ϕ	ϕ	o	ϕ
o	ϕ	ϕ	ϕ	ϕ	u
y	A	ϕ	ϕ	ϕ	ϕ

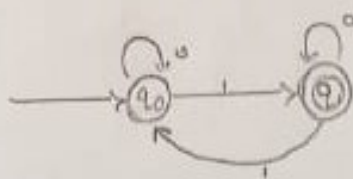
xii) $L = \{ w \in \{a, b\}^* : w \text{ has odd parity} \}$

$\Sigma = \{a, b\}$

$Q = \{q_0, q_1\}$

$F, t = \{q_1\}$

$S, s = \{q_0\}$



δ

q_0

q_1

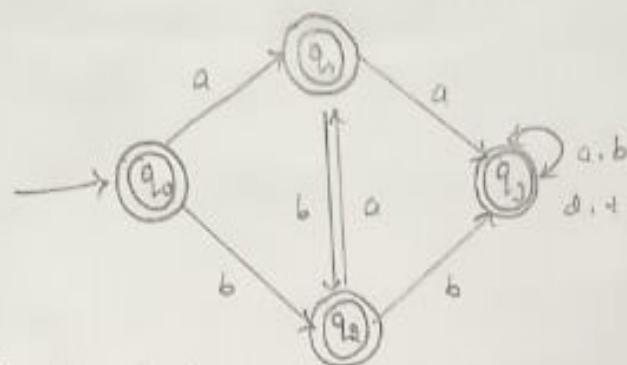
8) Design the E-non determinat^{finite} finite automata for the following

$L = \{ w \in \{a, b\}^* : w = ab^* \text{ or } [w] \text{ is even} \}$

$\Sigma = \{a, b\}$

$Q = \{q_0, q_1, q_2, q_3, q_4, q_5, q_6\}$

$F = \{q_4, q_6\}$



$$Q = \{q_0, q_1, q_2, q_3\}$$

Start state = q_0

Final state = $\{q_1, q_2\}$

d. s $\{q_3\}$

δ a b

q_0 q_1 q_2

q_1 q_3 q_2

q_2 q_1 q_3

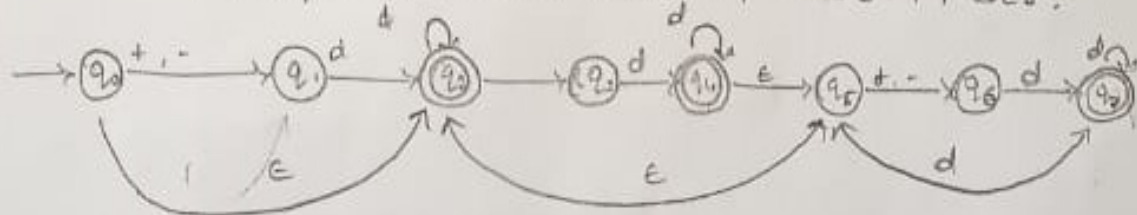
q_3 q_3 q_3

Ex) $L = \{w : w \text{ is the string representing a floating point number}\}$

* A floating point number is an optional sign, followed by a decimal number followed by an optional exponent.

* A decimal number may be of the form x or $x.y$, where x & y are non-empty string of decimal digits.

* An integer is a non-empty string of decimal digits.
So, for e.g. these strings represents floating point numbers
 $+3.0, 3.0, 0.3e1, 0.3e+1, -0.3e+1, -3e8$.



$$Q = \{q_0, q_1, q_2, q_3, q_4, q_5, q_6, q_7\} \quad \Sigma = \{+, -, d, e\}$$

In this we have used the short bond ϵ to stand for any one of the decimal digits (0-9) & we have created the dead state to avoid across crossing each other.

δ	a	b
q_0	q_1	q_3
q_1	q_2	q_1
q_2	q_2	q_1
q_3	q_3	q_3

iii DFA to accept string of a's & b's having odd number of a's and even no of b's

q_a = odd no of a's

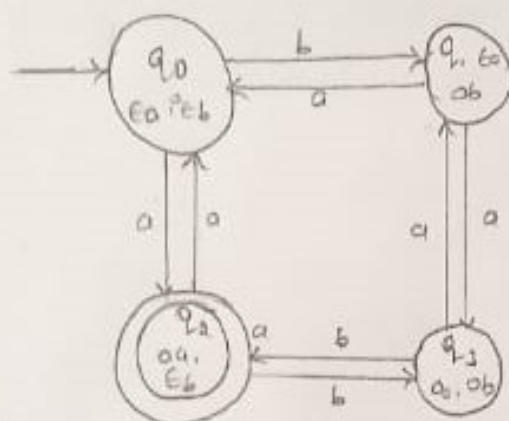
e_b = even no of b's

o_b = odd no of b's

o_a = even no of a's

$$\Sigma = \{a, b\}$$

$$Q = \{ (o_a, e_b), (e_a, o_b), (o_a, o_b), (e_a, e_b) \}$$



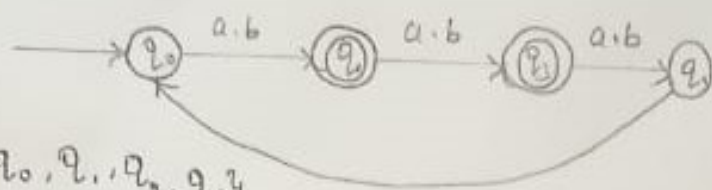
$$F = \{ o_a, e_b \}$$

δ	a	b
$\rightarrow q_0$	q_2	q_1
q_1	q_3	q_2
q_2	q_0	q_3
q_3	q_1	q_2

iv: $L = \{ w \in \{a, b\}^* : \text{no two consecutive characters are same} \}$

$$\Sigma = \{ a, b, ab, ba \}$$

VP) $L = \{ w : |w| \bmod 4 \neq 0 \}$ where $\Sigma = \{a, b\}$.
 $\Rightarrow \Sigma = \{a, b\}$



$$Q = \{q_0, q_1, q_2, q_3\}$$

$$F = \{q_1, q_2, q_3\}$$

$$\delta(q_0, a) = q_1 \quad \delta(q_1, (a, b)) = q_2 \quad \delta(q_2, (a, b)) = q_3$$

$$\delta(q_0, b) = q_1$$

$$\delta(q_3, (a, b)) = q_0$$

$$\delta \quad a \quad b$$

$$q_0 \quad q_1 \quad q_2$$

$$q_1 \quad q_2 \quad q_3$$

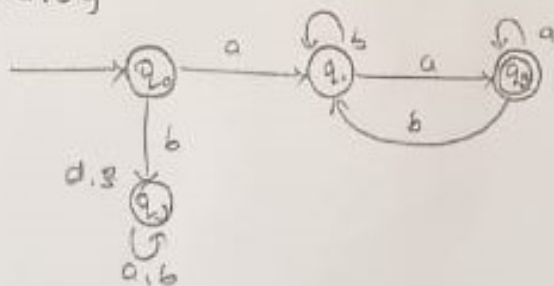
$$q_2 \quad q_3 \quad q_0$$

$$q_3 \quad q_0 \quad q_1$$

VP) $L = \{ awa \mid w \in (a+b)^+ \}$

$S = \{aaa, aab, aba, abab, ababa, \dots\}$

$\Sigma = \{a, b\}$



$$Q = \{q_0, q_1, q_2\}$$

$$F = \{q_2\}$$

$$\delta(q_0, a) = q_1 \quad \delta(q_1, a) = q_2 \quad \delta(q_2, a) = q_2$$

$$\delta(q_0, b) = q_3 \quad \delta(q_1, b) = q_3 \quad \delta(q_2, b) = q_1$$

$$\delta(q_3, a) = q_2$$

$$\delta(q_3, b) = q_3$$

* Minimum string $s = \{ab + \text{or } ba\}$

$$\Sigma = \{a, b\}$$

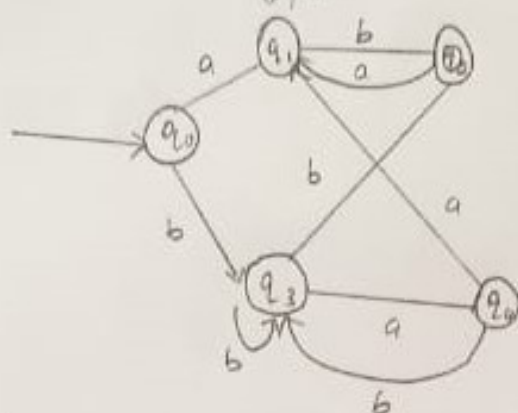
$$\Gamma = \{a, \Sigma, \delta, q_0, F\}$$

$$Q = \{q_0, q_1, q_2, q_3, q_4\}$$

$$\Sigma = \{a, b\}$$

$q_0 = \text{start state}$

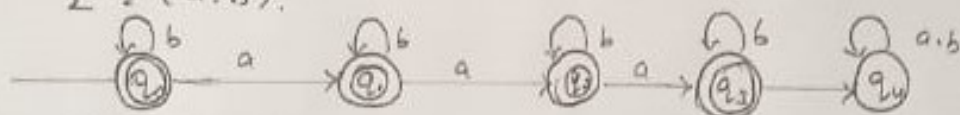
$$F = \{q_0, q_4\}$$



δ	a	b
q_0	q_1	q_3
q_1	q_2	q_4
q_2	q_1	q_3
q_3	q_4	q_3
q_4	q_1	q_3

iv) $L = \{w : \text{No } (w) \leq 3, w \in \{a, b\}^+\}$

$$\Sigma = \{a, b\}$$



$$Q = \{q_0, q_1, q_2, q_3, q_4\}$$

$$F = \{q_0, q_4\}$$

$q_0 = \text{starting state}$

$$\delta$$

$$q_0$$

$$q_1$$

$$q_2$$

$$q_3$$

$$q_4$$

For e.g. it means sense to implement parity checking FSM.



- * An FSM can be simulated by general purpose interpreter.
- * An FSM can be used as a specification for can be implemented in software just as any specification might be and the correctness of the implementation can be shown by verifying that the implementation satisfies the specification.

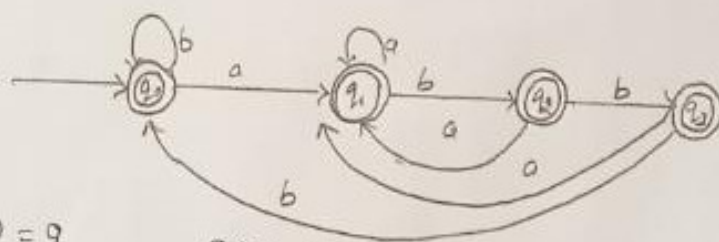
7. Design a DFA for the following.

i) DFA to accept string of a's and b's not ending with string abb

$$M = (Q, \Sigma, \delta, q_0, F)$$

$$Q = \{q_0, q_1, q_2, q_3\} \quad F = \{q_0, q_1, q_2\}$$

$$\Sigma = \{a, b\}$$



$$\delta(q_0, a) = q_1$$

$$\delta(q_0, b) = q_0$$

$$\delta(q_1, a) = q_1$$

$$\delta(q_1, b) = q_2$$

$$\delta(q_2, a) = q_1$$

$$\delta(q_2, b) = q_3$$

$$\delta(q_3, a) = q_1$$

$$\delta(q_3, b) = q_0$$

$$\delta$$

$$q_0$$

$$q_1$$

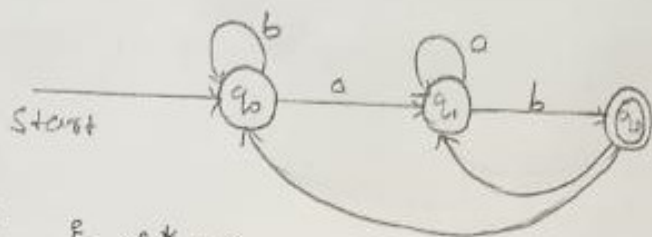
$$q_2$$

$$q_3$$

ii) $L = \{w \mid w \text{ contains an even number of } a\text{'s and } b\text{'s}\}$

iii) DFA to accept strings of a's and b's ending with ab or ba.

Then $\delta^+(q, w) = \delta^+(q, x_k) = \{r_1, r_2, r_3, \dots, r_k\}$



prefix ϵ $\delta^+(q_0, \epsilon) = \{q_0\}$

prefix a $\delta^+(q_0, a) = \delta(\delta^+(q_0, \epsilon), a)$
 $= \delta(q_0, a)$
 $= q_1$

prefix ab $\delta^+(q_0, ab) = \delta(\delta^+(q_0, a), b)$
 $= \delta(q_1, b)$
 $= q_2$

prefix aba $\delta^+(q_0, aba) = \delta(\delta^+(q_0, ab), a)$
 $= \delta(q_2, a)$
 $= q_1$

prefix $abaa$ $\delta^+(q_0, abaa) = \delta(\delta^+(q_0, aba), a)$
 $= \delta(q_1, a)$
 $= q_1$

prefix $abab$ $\delta^+(q_0, abab) = \delta(\delta^+(q_0, abaa), b)$
 $= \delta(q_1, b)$
 $= q_2$

\therefore The final transition.

$q_0 \xrightarrow{a} q_1 \xrightarrow{b} q_2 \xrightarrow{a} q_1 \xrightarrow{a} q_1 \xrightarrow{b} q_2$

6) Categorize How FSM's are used in operational systems?

\Rightarrow An FSM is an abstraction.

* FSMs for real problem can be formed into operational systems in any of number ways.

* An FSM can be translated into a circuit design and implemented directly in hardware.

→ E.NFA: A transition which on empty string is called an ϵ -transition i.e., if there is a transition from one state to another state without any input is called ϵ -transition.

E.NFA is 5-tuple

$$M = (Q, \Sigma, \delta, q_0, F)$$

$\delta: Q \times (\Sigma \cup \epsilon) \rightarrow 2^Q$ i.e., δ is the transition function which is a mapping from $Q \times (\Sigma \cup \epsilon)$ to 2^Q . Based on the current state there can be a transition to another states with or without any input symbols.

5) Define extended transition function for DFA and what are the transition made for string "abacab".

⇒ The extended transition function δ describe what happens to a state of machine when the input is a string.

Let $M = (Q, \Sigma, \delta, q_0, F)$ be an DFA. The extended transition

$\delta^* = Q \times \Sigma^+ \rightarrow 2^Q$ defined recursively as shown below.

Base: $\delta^*(q, \epsilon) = \{q\}$ This indicates that if the machine is in state q and read no input then the machine is state q .

Induction: Let $w = \overset{x}{\cancel{a}}u$ when a is last symbol of w and x is the remaining string of w . Let q is the current state and x is the string to be processed & after consuming the string.

x_1 - Let the state of machine is $\{P_1, P_2, P_3, \dots, P_n\}$.

$$\text{i.e., } \delta^*(c, x) = \{P_1, P_2, P_3, \dots, P_n\}$$

Let the transition from $\{P_1, P_2, P_3, \dots, P_n\}$ on input symbol a is

$$\delta(\{P_1, P_2, P_3, \dots, P_n\}, a) = \{r_1, r_2, r_3, \dots, r_k\}$$

$$\text{i.e., } \bigcup_{i=1}^n \delta(P_i, a) = \{r_1, r_2, \dots, r_k\}$$

$$i=1$$

→ Deterministic finite automata.

finite state machine is computational device where input is a string and where output is one of two values that we can call accept or reject.

DFA: DFA:

The DFA is a Deterministic finite Automata is 5 tuple or Quintuple indicating five components.

$$M = (Q, \Sigma, \delta, q_0, F) \text{ where}$$

M is the name of the machine it can be also be (5-tuple) called by any name.

Q is non-empty finite set of state.

Σ is non-empty finite set of input alphabets.

$\delta: Q \times \Sigma \rightarrow Q$ i.e., δ is transition function which is a mapping from $Q \times \Sigma$ to Q . Based on the component state and input symbol, the machine enters into another state.

$q_0 \in Q$ - is the start state.

$F \subseteq Q$ - is set of accepting or final state.

A configuration of DFSA of M is $k \times \Sigma^*$

NFA :-

it is defined as 5-tuple a Quintuple indicating five components

$$M = (Q, \Sigma, \delta, q_0, F)$$

where M is the name of machine.

Q is non-empty, finite set of state

Σ is non-empty, finite set of input alphabets.

$\delta: Q \times \Sigma \rightarrow 2^Q$ i.e., δ is transition function.

which is mapping from $Q \times \Sigma$ to 2^Q

$q_0 \in Q$ is the start state.

F is set of accepting or final state.

$$3a \quad \Sigma^+ = \Sigma^0 \cup \Sigma^1 \cup \Sigma^2 \cup \Sigma^3 \cup \dots$$

$$\Sigma^+ = \{ \epsilon, 0, 1, 00, 01, 10, 11, 000, 001, \dots \}$$

$\{0\}^+ = \{ \epsilon, 0, 1, 00, 10, 11, 000, 001, \dots \}$ which is set of strings of 0's of any length.

3b Define Automata with an example.

→ Theory of Automata is a theoretical branch of computer science and mathematical. It is the study of abstract machine and the computation problem that can be solved using these machines.

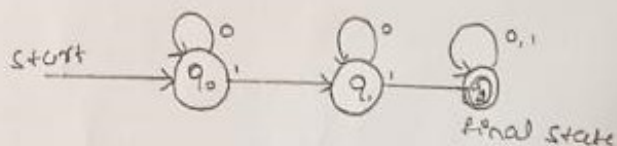
Computability, understanding the internal processing of the machine. Abstract machine is a conceptual model or theoretical model of a computer. Hardware and hardware are not actual machine & hence, they are called hypothetical computer.

Eg:- $\Sigma = \{a, b\}$

$$\Sigma = \{A, B, C, D\}$$

$$\Sigma = \{0, 1, 2\}$$

$$\Sigma = \{0, 1, \dots, 5\}$$



These machines are studied with following methods.

1). finite Automata or finite state machines.

2). Linear bounded Automata.

3). push down Automata.

4). Turing machine.

4b. Define Deterministic finite Automata Non Deterministic finite Automata and ε-NFA.

language: A language can be defined as set of strings obtained from Σ^n where Σ is set of alphabets of a particular language. formally, a language 'L' over Σ is subset of Σ which is denoted by $L \subseteq \Sigma^+$

E.g. $L = \{ \epsilon, 01, 0011, 000111, \dots \}$

2) Define kleene plus and kleene closure with an examples.
 → kleene plus: Σ^+

the kleene plus is a variation of kleene star operator. the kleene plus denoted by Σ^+ is defined as follows.

$$\Sigma^+ = \Sigma^1 \cup \Sigma^2 \cup \Sigma^3 \cup \dots$$

which is the set of words of any length except the null string i.e., $\epsilon \in (\Sigma^n)$ is not part of Σ^+ and hence $\epsilon \notin \Sigma^+$ for e.g.: let $\Sigma = \{0, 1\}$. Then it is shown below.

$$\Sigma^+ = \{0, 1, 00, 0001, 10, 11, 000, 001, \dots\}$$

The above set is defined as $\{$ strings of 0's and 1's of any length except the null string.

Note $\Sigma^+ = \Sigma^+ \cup \epsilon$. this can be written as $\Sigma^+ \cdot \Sigma^+ = \Sigma^+ \cdot \epsilon$.

kleene closure (or kleene star / star operator): Σ^*

The kleene closure is defined as follows:

$$\Sigma^* = \Sigma^0 \cup \Sigma^1 \cup \Sigma^2 \cup \dots$$

which is the set of words of any length each string is made up of symbols only Σ .

E.g.: Let $\Sigma = \{0, 1\}$ then Σ^* is balanced.

$$\Sigma^0 = \{ \epsilon \}$$

set of words of length 0.

$$\Sigma^1 = \{0, 1\}$$

set of words of length 1.

$$\Sigma^2 = \{0, 0, 0, 1, 11\}$$

set of words of length 2.

$$\Sigma^3 = \{000, 001, 010, 100, 011, 101, 110, 111\}$$

set of words of length 3.

Sub: Automata theory and compatibility

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Sec: B

Assignment - I

1) Define Alphabet, String, power set, language with an example for each

→ Alphabet:- A language consists of various symbols from which the word and statement can be obtained. These symbols are called alphabets.

$$\text{Ex} = \Sigma = \{0, 1\}$$

$$\Sigma = \{a, b, \dots, z, A, B, \dots, Z, 0, 1, \dots, 9, \dots\}$$

String: A string is defined as a finite sequence of symbols from an alphabet Σ .

* The shortest string is empty string & it is denoted by symbol ϵ .

* The set of all possible strings over an alphabet Σ is written as Σ^* for e.g. $\Sigma = \{0, 1\}$ is set of binary or alphabet.

power set: Let A be the set, the set of all subsets of set A is called power set of A and is denoted by $P(A)$.

E.g. Let $A = \{1, 2, 3\}$.

The subsets of set A are shown below.

$$\{\emptyset, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}, \{1, 2, 3\}\}$$

The set of above subset is called and is denoted by 2^A .

$$2^A = \{\emptyset, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}, \{1, 2, 3\}\}.$$