

①

ATC - Assignment - 3.

1. write a neat diagram & explain the working of turning machine?

Turning machine is a generalized machine which can recognise all types of languages viz, regular languages, context free languages, context sensitive languages.

Turning machine also accepts the languages generalized from unrestricted grammar, turning machine can accept any generalized languages.

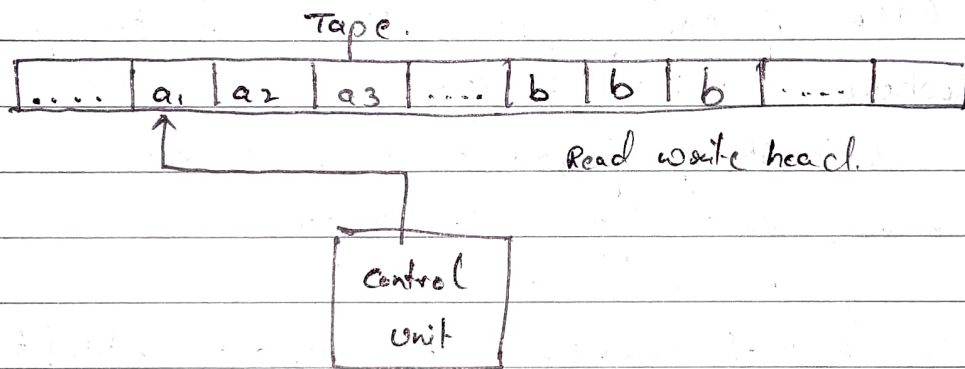
Turning machine model.

* It is a finite automata connected to read-write head with the following components.

(i) Tape

(ii) Read-write head.

(iii) control unit



Tape:-

- * It is a temporary storage and it is divided into cells.
- * Each cell can store the information of only one symbol.

Read-write head:-

- * Reading/writing from/to the tape is determined by control unit
- * Different moves performed by the machine depends on current scanned symbol & current state
- * Various moves performed by the machine.

② Define CNF & GNF with an example for each?

CNF (Chomsky Normal form) If a CFG is in CNF if all production rules satisfy one of the following condition.

→ start symbol generating ϵ .

Eg:- $A \rightarrow \epsilon$

→ A non terminal generating two non terminals

Eg $S \rightarrow AB$

Eg:-

$G_1 = \{S \rightarrow AB, S \rightarrow \epsilon, A \rightarrow a, B \rightarrow b\}$

$G_2 = \{S \rightarrow aA, A \rightarrow a, B \rightarrow \epsilon\}$

GNF =

Greibach Normal form.

A context free grammar, $G = (V, T, R, S)$ is said to be GNF if every production is of the form $A \rightarrow a\alpha$ where $a \in T$ & $\alpha \in V^*$.

α is string of zero or more variable.

→ A start symbol should generate ϵ

Eg:- $S \rightarrow \epsilon$

Eg. $G_1 = \{S \rightarrow aAB \mid AB, A \rightarrow aA \mid a, B \rightarrow bB \mid b\}$

The production rule of grammar G_2 does not satisfy the rules specified from GNF as $A \rightarrow \epsilon, B \rightarrow \epsilon$ contains ϵ .

So the grammar G_2 is not in GNF

~~$G_2 = \{S \rightarrow aAB\}$~~

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$G_2 = \{S \rightarrow aAB \mid AB, A \rightarrow aA \mid \epsilon, B \rightarrow bB \mid \epsilon\}$

④

obtain PDA to accept

$L = \{a^n b^n \mid n \geq 0\}$

→

if $n=2$
 $aabb$

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Step (i)

$$\delta(q_0, \epsilon, \epsilon) = (q_0, z_0)$$

↓
I/P
↓
empty
stack.

↳ z_0 is pushed stack is empty

z_0

$$(ii) \delta(q_0, a, z_0) = (q_1, a, z_0) \text{ push operation.}$$

↓
I/P
stack
↓
Top of
stack.

↓
Stack contents.

a
z_0

$$(iii) \delta(q_1, a, z_0) = (q_1, aa, z_0) \text{ push operation.}$$

↓
I/P
stack

↓
stack operation.

$$(iv) \delta(q_1, b, a) = (q_2, \epsilon) \rightarrow \text{pop state.}$$

↳ popping.

$$(v) \delta(q_2, \epsilon, z_0) = (q_3, \epsilon) \rightarrow \text{string accepted.}$$

a
a
z_0

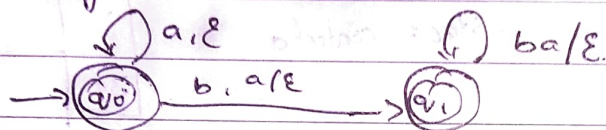
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∴ string is accepted.

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sr no	state	unread i/p	stack	transition
1	q_0	ϵ	z_0	1
2	q_1	a	az_0	2
3	q_1	b	abz_0	3
4	q_2	b	abz_0	4
5	q_2	ϵ	z_0	5
6	q_3	ϵ	ϵ	6

Diagram Representation



finally PDA is given by

$$M = (Q, \Sigma, \Gamma, \delta, q_0, \sqsubset)$$

$$Q = \{q_0, q_1\}$$

$$\Sigma = \{a, b\}$$

$\Gamma = \{z_0\}$ shown above.

Q. Write the application of pumping lemma for context free language?

→ i) Pumping lemma is often used to prove that a given language L is not context free.

Eg:- $B = \{w \mid w \in \{0,1\}^+ \}$ is not context free.

proof:- Assume B is context free. Let p be the context from the pumping lemma for B .

Let $w = 0^p 1^p 0^p$, which is in B .

$$w = uvxy^iz$$

$$1. |vxy| \leq p$$

$$2. |vy| \geq 1$$

$$3. \text{For every } i \geq 0, uv^i xy^i z \in B$$

If v contains a symbol from the first 0^p then y contains cannot contain one from the second 0^p so pumping does not work.

i.e. hence in general CFL is not closed under Intersection.

(7) Define language acceptability of TM?

Let $M = (Q, \Sigma, \Gamma, \delta, q_0, B, F)$ be a TM

The language $L(M)$ accepted by M is defined as

$$L(M) = \{ w \mid \exists q_0, w \vdash \dots \vdash P \}$$

where

$$w \in \Sigma^*, P \in F$$

$$E, \alpha_1, \alpha_2 \in \Gamma^* \}$$

i.e. set of all those words w in Σ^* which causes M to move from start state q_0 to final state P .

The language acceptable by TM is called recursively enumerable language.

→ The string w which is the string to be scanned should end with infinite number of blanks.