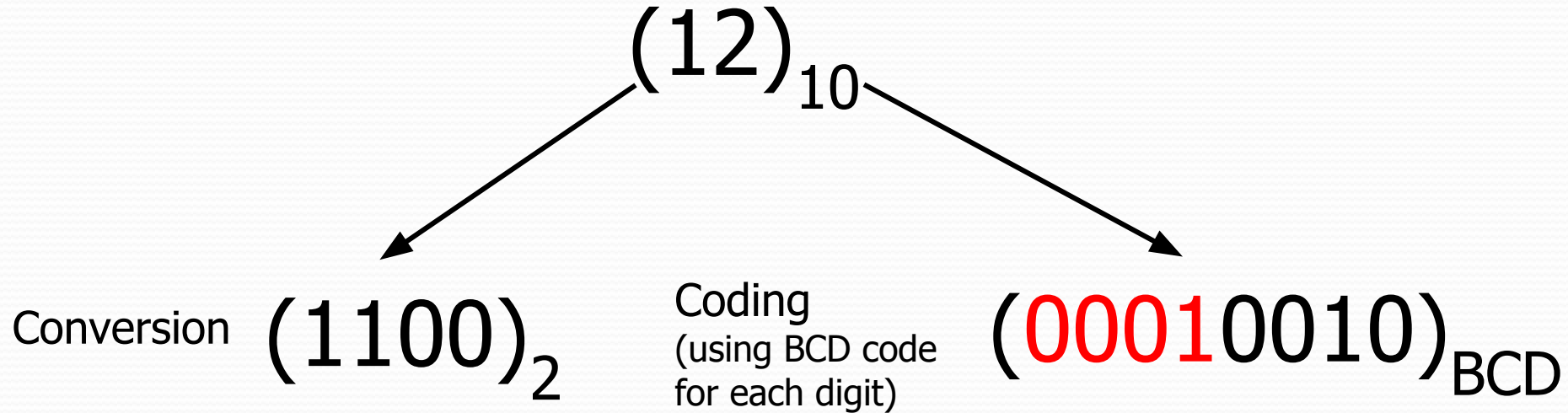


Conversion and Coding



BCD Adder

Design a circuit that calculates the Arithmetic addition of two decimal digits.

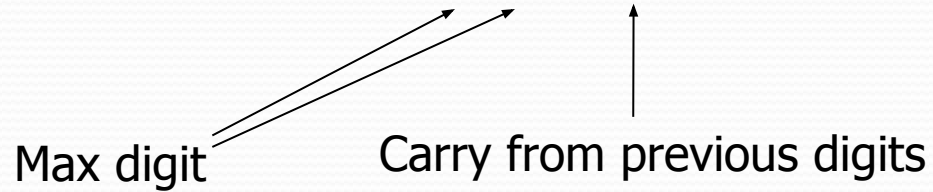
$$\begin{array}{r} 9 \\ + 3 \\ \hline 2 \end{array}$$

1
carry

BCD Adder

- Maximum sum is $9+9 + 1 = 19$

Max digit Carry from previous digits



BCD adder (sum up to 9)

Number	C	S3	S2	S1	S0
0	0	0	0	0	0
1	0	0	0	0	1
2	0	0	0	1	0
3	0	0	0	1	1
4	0	0	1	0	0
5	0	0	1	0	1
6	0	0	1	1	0
7	0	0	1	1	1
8	0	1	0	0	0
9	0	1	0	0	1

The sum is the same with BCD adder

BCD adder (sum is 10 to 19)

Number	C	S3	S2	S1	S0
10	1	0	0	0	0
11	1	0	0	0	1
12	1	0	0	1	0
13	1	0	0	1	1
14	1	0	1	0	0
15	1	0	1	0	1
16	1	0	1	1	0
17	1	0	1	1	1
18	1	1	0	0	0
19	1	1	0	0	1

BCD adder (sum is 10 to 19)

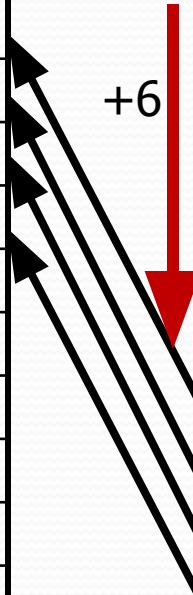
BCD adder sum

Number	C	S3	S2	S1	S0
10	1	0	0	0	0
11	1	0	0	0	1
12	1	0	0	1	0
13	1	0	0	1	1
14	1	0	1	0	0
15	1	0	1	0	1
16	1	0	1	1	0
17	1	0	1	1	1
18	1	1	0	0	0
19	1	1	0	0	1

Binary sum

K	Z3	Z2	Z1	Z0
0	1	0	1	0
0	1	0	1	1
0	1	1	0	0
0	1	1	0	1
0	1	1	1	0
0	1	1	1	1
1	0	0	0	0
1	0	0	0	1
1	0	0	1	0
1	0	0	1	1

+6



Algorithm for BCD Adder

- If sum is up to 9
 - Use the regular Adder.
- If the sum > 9
 - Use the regular adder and **add 6** to the result

When is the result > 9

Binary sum

Number	Correction	C _{out}	Z3	Z2	Z1	Z0
10	1	0	1	0	1	0
11	1	0	1	0	1	1
12	1	0	1	1	0	0
13	1	0	1	1	0	1
14	1	0	1	1	1	0
15	1	0	1	1	1	1
16	1	1	0	0	0	0
17	1	1	0	0	0	1
18	1	1	0	0	1	0
19	1	1	0	0	1	1

C _{out} Z ₃ Z ₂ \ Z ₁ Z ₀				
	00	01	11	10
000				
001				
011	1	1	1	1
010			1	1
110	X	X	X	X
111	X	X	X	X
101	X	X	X	X
100	1	1	1	1

$Z_1 Z_0$					
$C_{out} Z_3 Z_2$		00	01	11	10
		000	001	011	010
	000				
	001				
	011	1	1	1	1
	010			1	1
	110	X	X	X	X
	111	X	X	X	X
	101	X	X	X	X
	100	1	1	1	1

C_{out}

$Z_1 Z_0$					
$C_{out} Z_3 Z_2$		00	01	11	10
		000	001	011	010
	000				
	001				
	011	1	1	1	1
	010			1	1
	110	X	X	X	X
	111	X	X	X	X
	101	X	X	X	X
	100	1	1	1	1

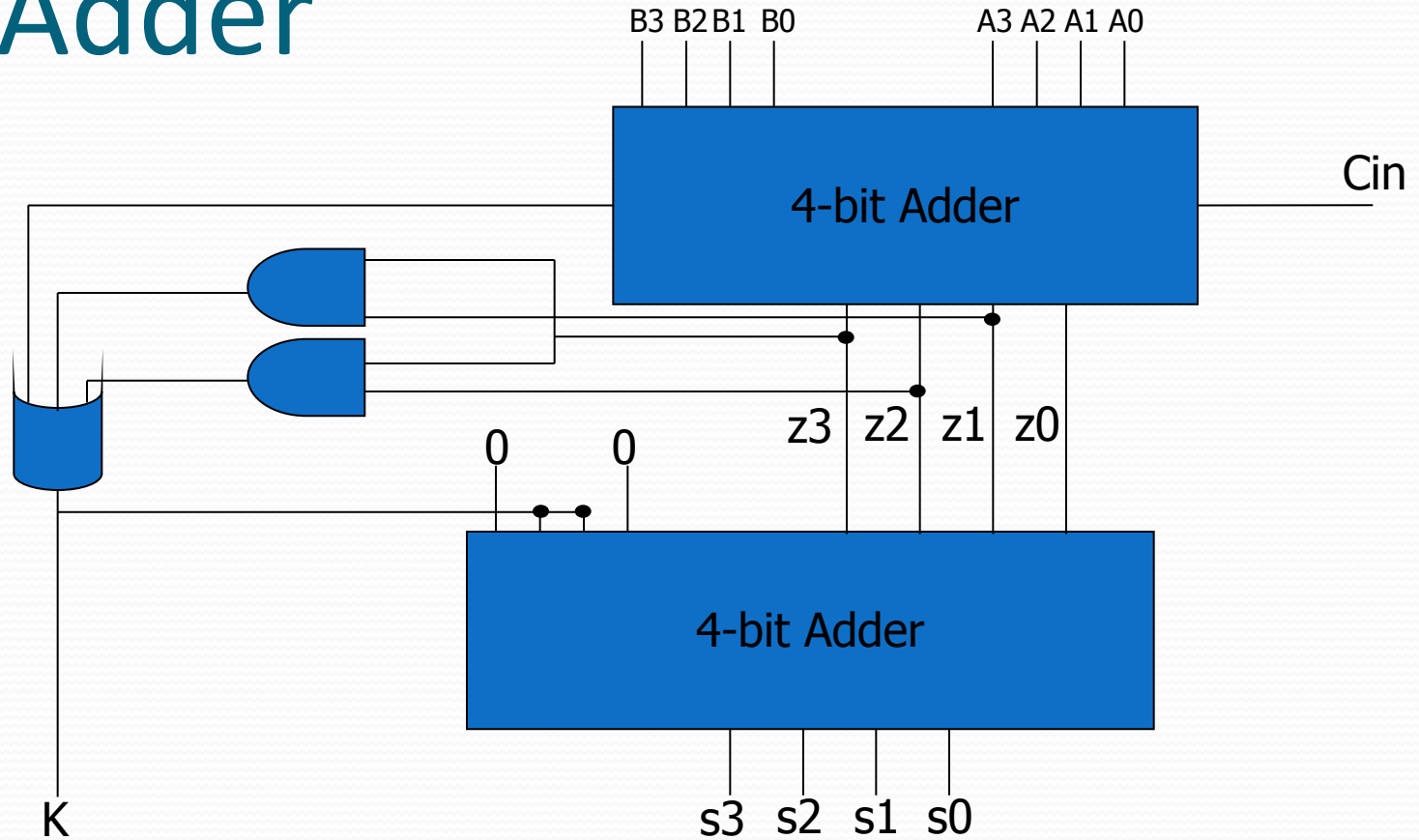
$Z_3 Z_1$

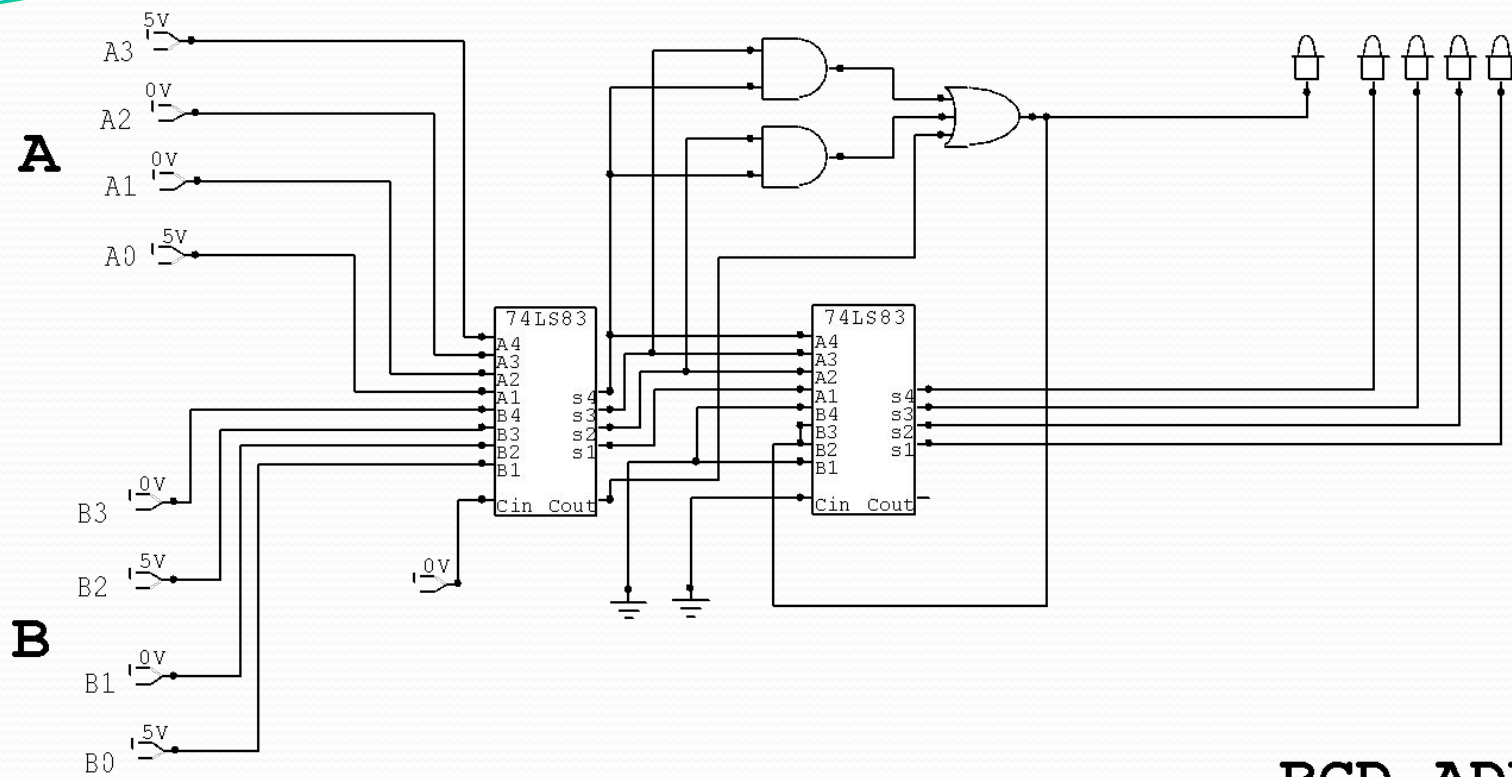
$Z_1 Z_0$					
$C_{out} Z_3 Z_2$		00	01	11	10
		000	001	011	010
	000				
	001				
	011	1	1	1	1
	010			1	1
	110	X	X	X	X
	111	X	X	X	X
	101	X	X	X	X
	100	1	1	1	1

$Z_3 Z_2$

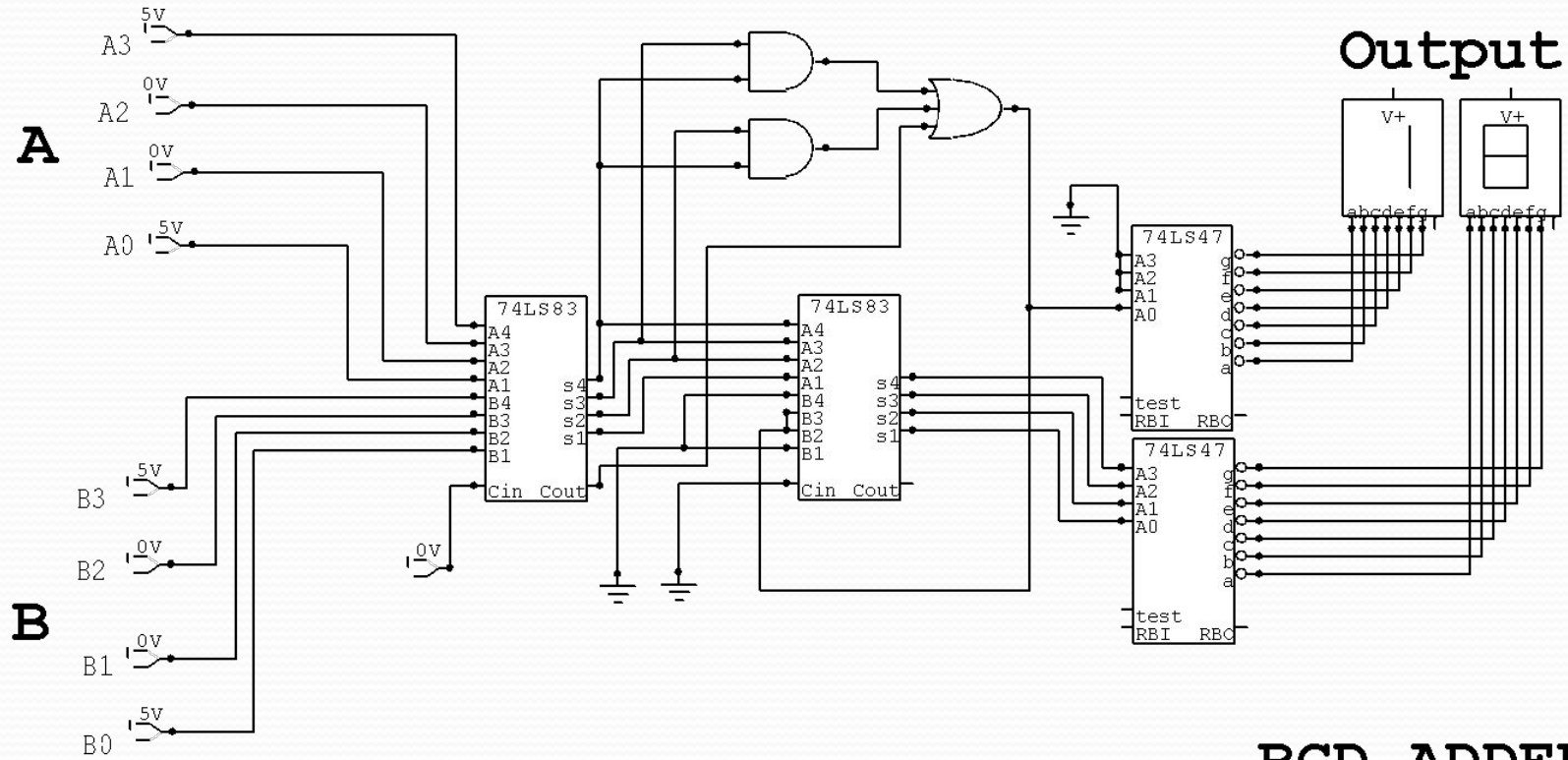
$$\text{Correction} = C_{out} + Z_3 Z_1 + Z_3 Z_2$$

BCD Adder





BCD ADDER



BCD ADDER