

# Landmarks

## Definitions, Discovery Methods and Uses

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ICAPS 2010 Tutorial

# Outline

- 1 What Landmarks Are
- 2 How Landmarks Are Discovered
- 3 Landmark Uses
  - Subgoals
  - Heuristic Estimates
  - Admissible Heuristic Estimates
  - Enriching the Problem
  - Beyond Classical Planning
- 4 Summary

- SAS<sup>+</sup> is a language for describing planning tasks compactly
- A SAS<sup>+</sup> task is given by a 4-tuple  $\Pi = \langle \mathcal{V}, \mathcal{A}, s_0, G \rangle$ 
  - $\mathcal{V} = \{v_1, \dots, v_n\}$  is a set of **state variables**, each associated with a **finite domain**  $dom(v_i)$ . By  $v \mapsto d$  we denote that variable  $v$  is assigned value  $d \in dom(v)$
  - Each complete assignment  $s$  to  $\mathcal{V}$  is called a *state*
  - $s_0$  is an *initial state*
  - *goal*  $G$  is a partial assignment to  $\mathcal{V}$
  - $\mathcal{A}$  is a finite set of *actions*
  - Each action  $a$  is a pair  $\langle pre(a), eff(a) \rangle$  of partial assignments to  $\mathcal{V}$  called *preconditions* and *effects*
- In cost-sensitive planning, each action  $a$  is also associated with a **cost  $C(a)$**

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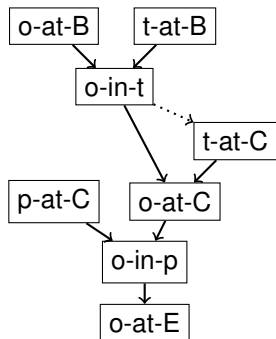
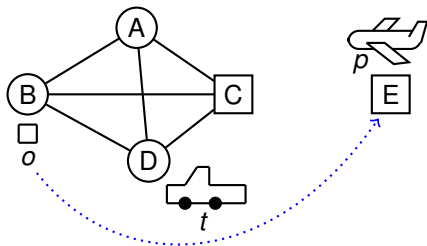
# Landmarks

- A **landmark** is a formula that **must be true** at some point in **every** plan (Hoffmann, Porteous & Sebastia 2004)
- Landmarks can be (partially) **ordered** according to the order in which they must be achieved
- Some landmarks and orderings can be discovered automatically
- Current approaches consider only landmarks that are **facts** or **disjunctions** of facts  
(work on conjunctive landmarks to appear)

## Action Landmarks

- An **action landmark** is an action **which occurs in every plan**
- Landmarks may imply actions landmarks (e.g., sole achievers)
- Action landmarks imply landmarks (e.g., preconditions and effects)
- Action landmarks might capture even more information
- Some action landmarks can be discovered automatically

## Example Planning Problem - Logistics



Partial landmarks  
graph

## Types of Landmark Orderings

- **Sound** landmark orderings are guaranteed to hold - they do not prune the solution space
- **Unsound** landmark orderings are **additional** constraints on plans - they may prune the solution space
- It is even possible that no plan exists that respects the unsound orderings
- However, unsound orderings are likely to hold and may save effort in planning



## Sound Landmark Orderings

- *Natural* ordering  $A \rightarrow B$ , iff  $A$  true some time before  $B$
- *Necessary* ordering  $A \rightarrow_n B$ , iff  $A$  always true before  $B$  becomes true
- *Greedy-necessary* ordering  $A \rightarrow_{gn} B$ , iff  $A$  true one step before  $B$  becomes true for the first time

Note that  $A \rightarrow_n B \implies A \rightarrow_{gn} B \implies A \rightarrow B$

## Reasonable Orderings

- Not sound - not guaranteed to hold in all plans
- *Reasonable* ordering  $A \rightarrow_r B$ , iff given  $B$  was achieved **before**  $A$ , any plan must **delete**  $B$  on the way to  $A$ , and re-achieve achieve  $B$  **after** or at the same time as  $A$

$$B \rightsquigarrow \neg B \rightsquigarrow A \rightsquigarrow B \implies A \rightarrow_r B$$

- Initial state landmarks can be reasonably ordered after other landmarks (e. g., if they must be made false and true again)
- This can never happen with sound orderings

## Obedient-Reasonable Orderings

- Assume that a plan obeys reasonable orderings  $\Rightarrow$  find more orderings
- *Obedient-reasonable* ordering  $A \rightarrow_{or} B$ , iff given  $B$  was achieved before  $A$ , any plan **that obeys reasonable orderings** must delete  $B$  on the way to  $A$  and re-achieve  $B$  after or at the same time as  $A$
- Not sound

# Landmark Complexity

- Everything is PSPACE-complete
- Deciding if a given fact is a landmark is PSPACE-complete
- Proof Sketch: it's the same as deciding if the problem without actions that achieve this fact is unsolvable
- Deciding if there is a natural / necessary / greedy-necessary / reasonable ordering between two landmarks is PSPACE-complete

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# Landmark Discovery in Theory

## Theory

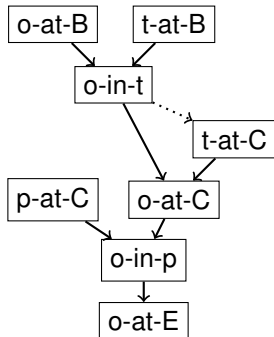
- $A$  is a landmark  $\iff \pi'_A$  is unsolvable  
where  $\pi'_A$  is  $\pi$  without the actions that achieve  $A$
- The delete relaxation of  $\pi'_A$  is unsolvable  $\implies \pi'_A$  is unsolvable  
(delete-relaxation landmarks) – but better methods exist
- Other heuristics can be used to prove  $\pi'_A$  unsolvable:  $h^m$ , structural patterns, ...

# Landmark Discovery I

Find landmarks and orderings by **backchaining** (Hoffmann et al. 2004, Porteous & Cresswell 2002)

- Every goal is a landmark
- If  $B$  is landmark and **all actions that achieve  $B$  share  $A$  as precondition**, then
  - $A$  is a landmark
  - $A \rightarrow_n B$

Useful restriction: consider only the case where  $B$  is achieved **for the first time**  $\rightsquigarrow$  find more landmarks (and  $A \rightarrow_{\text{gn}} B$ )

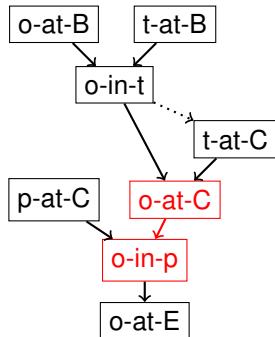


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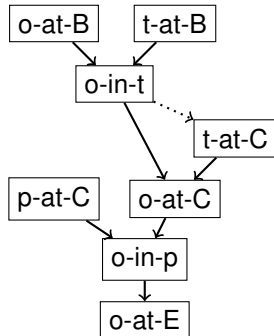


## Landmark Discovery I (ctd.)

PSPACE-complete to find first achievers

$\rightsquigarrow$  **over-approximation** by building relaxed planning graph for  $\pi'_B$

- This graph contains no actions that add  $B$
- Any action applicable in this graph can possibly be executed before  $B$  first becomes true  $\rightsquigarrow$  **possible first achievers**

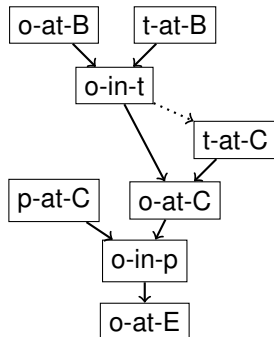


Additionally, if  $C$  not in the graph and  $C$  later proven to be a landmark, introduce  $B \rightarrow C$

## Landmark Discovery I (ctd.)

Disjunctive landmarks also possible,  
e.g.,  $(o\text{-in-}p_1 \vee o\text{-in-}p_2)$ :

- If  $B$  is landmark and all actions that (first) achieve  $B$  have  $A$  or  $C$  as precondition, then  $A \vee C$  is a landmark
- Generalises to any number of disjuncts
- Large number of possible disjunctive landmarks  $\rightsquigarrow$  must be restricted



## Domain Transition Graphs (DTGs)

Find landmarks through DTGs (Richter et al. 2008)

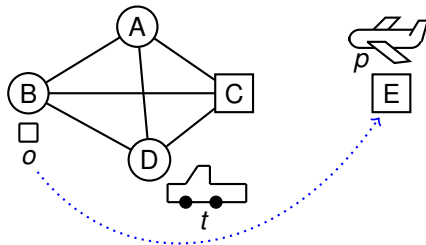
The **domain transition graph of  $v \in \mathcal{V}$**  ( $\text{DTG}_v$ ) represents how the value of  $v$  can change.

Given: a SAS<sup>+</sup> task  $\langle \mathcal{V}, \mathcal{A}, s_0, G \rangle$

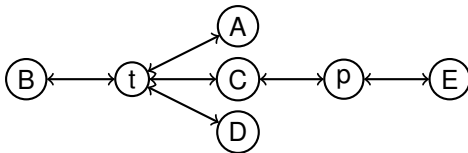
$\text{DTG}_v$  is a directed graph with **nodes**  $\mathcal{D}_v$  that has **arc**  $\langle d, d' \rangle$  iff

- $d \neq d'$ , and
- $\exists$  action with  $v \mapsto d'$  as effect, and either
  - $v \mapsto d$  as precondition, or
  - no precondition on  $v$

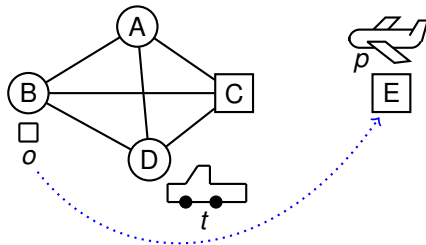
## DTG Example



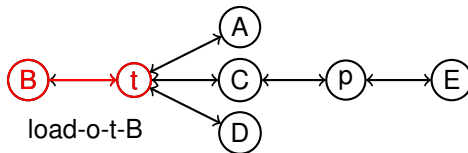
DTG for  $v_o$ :



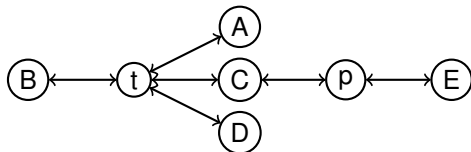
## DTG Example



DTG for  $v_o$ :

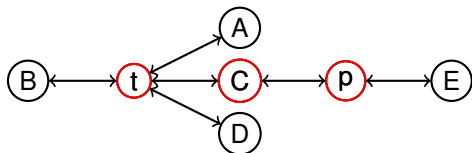


## Landmark Discovery II



- Find landmarks through DTGs: if
  - $s_0(v) = d_0$ ,
  - $v \mapsto d$  landmark, and
  - every path from  $d_0$  to  $d$  passes through  $d'$ ,then  $v \mapsto d'$  landmark, and  $(v \mapsto d') \rightarrow (v \mapsto d)$

## Landmark Discovery II



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## Landmark Discovery III

Find landmarks through forward propagation in relaxed planning graph  
(Zhu & Givan 2003)

- Finds **causal** landmarks only (preconditions for actions)
- Finds **all** causal delete-relaxation landmarks in polynomial time
- Propagate information on **necessary predecessors**
  - Label each fact node with itself
  - Propagate labels along arcs



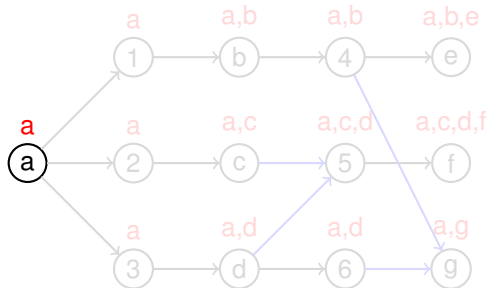
## Landmark Discovery III (ctd.)

Actions (numbers): propagate **union** over labels on preconditions

— all preconditions are necessary

Facts (letters): propagate **intersection** over labels on achievers

— only what's necessary for all achievers is necessary for a fact



No-ops and repeated  
nodes not shown

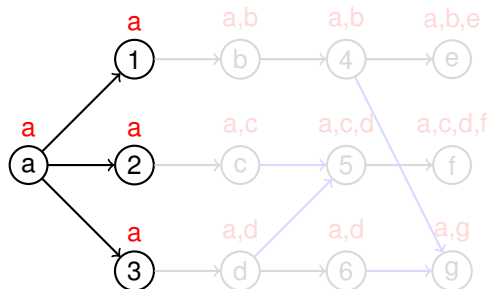
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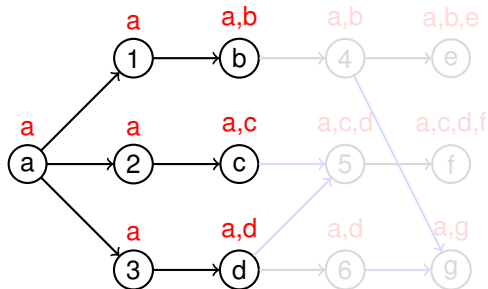
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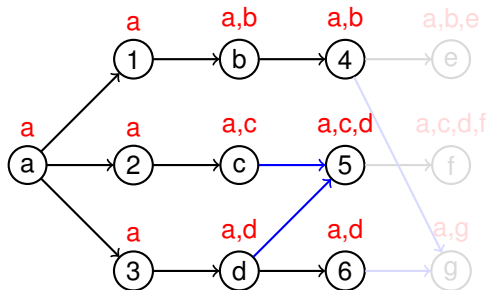
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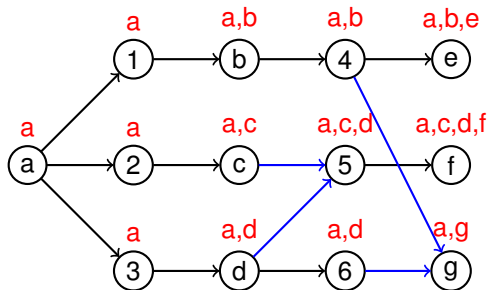
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## Landmark Discovery III (ctd.)

- Goal nodes in final layer: labels are landmarks
- $A \rightarrow B$  if  $A$  forms part of the label for  $B$  in the final layer
- $A \rightarrow_{\text{gn}} B$  if  $A$  is precondition for all possible first achievers of  $B$
- Possible first achievers of  $B$  are achievers that do not have  $B$  in their label (Keyder, Richter & Helmert 2010)

Advanced version of this method **counts re-occurrences** of landmarks

# Approximating reasonable orderings

We want to introduce  $A \rightarrow_T B$  if

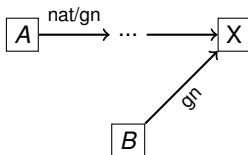
- 1  $B$  must be true **after** or at the same time as  $A$ 's first occurrence,  
and
- 2 Achieving  $B$  **first** means losing it on the way to  $A$

## Approximating reasonable orderings (ctd.)

- 1  $B$  must be true **after** or at the same time as  $A$ 's first occurrence

Holds if

- $B$  is a goal
- or
- there is a chain of natural/greedy-nec. orderings  
 $A \rightarrow \dots \rightarrow X$ , and  $B \rightarrow_{\text{gn}} X$



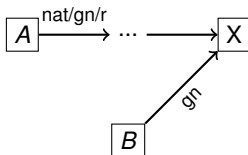


## Approximating obedient reasonable orderings

- 1  $B$  must be true **after** or at the same time as  $A$ 's first occurrence

Holds if

- $B$  is a goal
- or
- there is a chain of natural/greedy-nec./**reasonable** orderings  
 $A \rightarrow \dots \rightarrow X$ , and  $B \rightarrow_{\text{gn}} X$



## Approximating reasonable orderings (ctd.)

- ② Achieving  $B$  **first** means losing it on the way to  $A$

Holds if

- $A$  and  $B$  are inconsistent (mutually exclusive), or
- All actions achieving  $A$  have an effect inconsistent with  $B$ , or
- There is a landmark  $X$  inconsistent with  $B$  and  $X \rightarrow_{\text{gn}} A$

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# Using Landmarks

- Some landmarks and orderings can be discovered efficiently
- So what can we do once we have these landmarks?
- We assume that landmarks and orderings are discovered in a pre-processing phase, and the same landmark graph is used throughout the planning phase

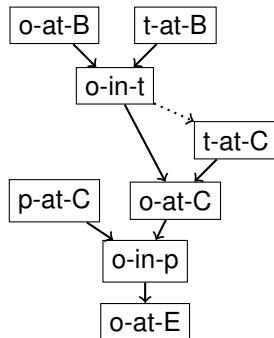
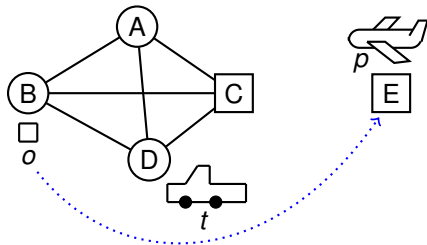
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# Using Landmarks as Subgoals

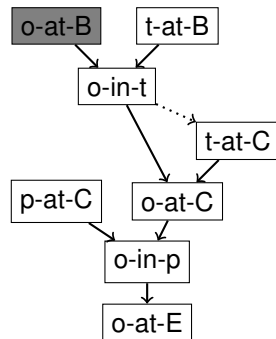
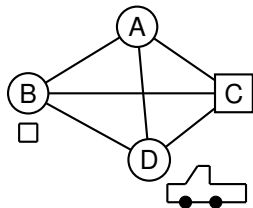
- Landmarks can be used as subgoals for a base planner
- The landmarks which could be achieved in the next iteration are passed as a disjunctive goal to a base planner
- After a landmark is achieved, repeat

## Using Landmarks as Subgoals - Logistics Example



- Partial plan:
- Goal:

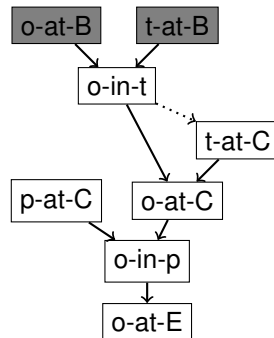
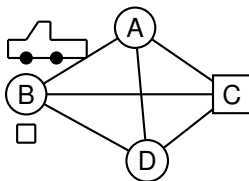
## Using Landmarks as Subgoals - Logistics Example



- Partial plan:  $\emptyset$
- Goal:  $t\text{-at-B} \vee p\text{-at-C}$

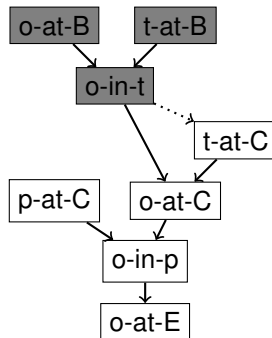
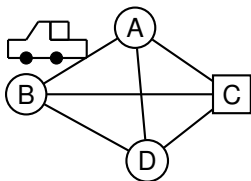


## Using Landmarks as Subgoals - Logistics Example



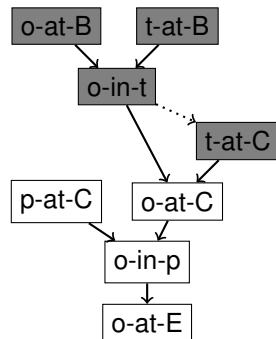
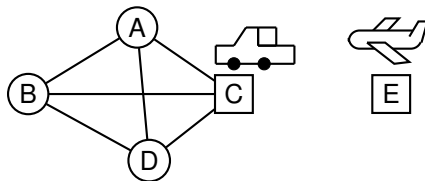
- Partial plan: Drive-t-B
- Goal:  $o\text{-in-}t \vee p\text{-at-}C$

## Using Landmarks as Subgoals - Logistics Example



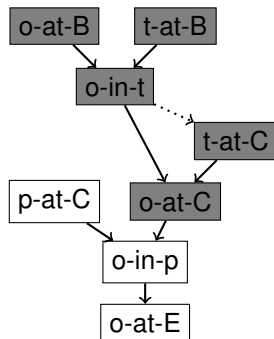
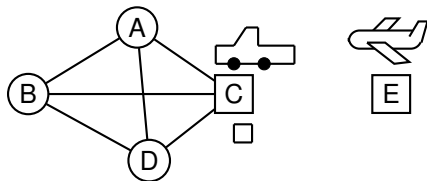
- Partial plan: Drive-t-B, Load-o-B
- Goal:  $t\text{-at-C} \vee p\text{-at-C}$

## Using Landmarks as Subgoals - Logistics Example



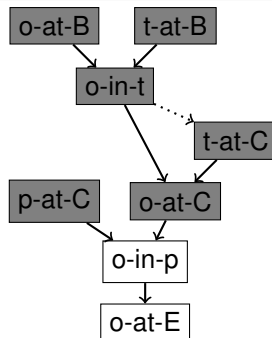
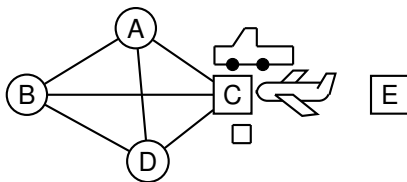
- Partial plan: Drive-t-B, Load-o-B, Drive-t-C
- Goal:  $o\text{-at-C} \vee p\text{-at-C}$

## Using Landmarks as Subgoals - Logistics Example



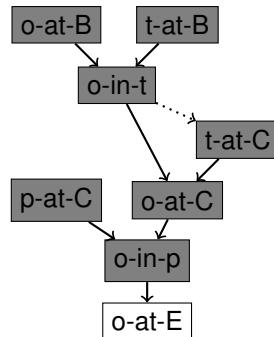
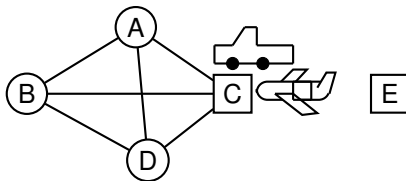
- Partial plan: Drive-t-B, Load-o-B, Drive-t-C, Unload-o-C
- Goal: p-at-C

## Using Landmarks as Subgoals - Logistics Example



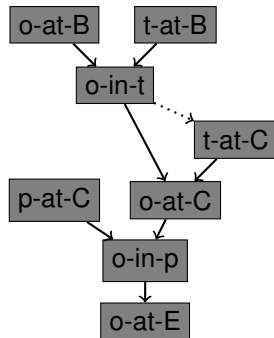
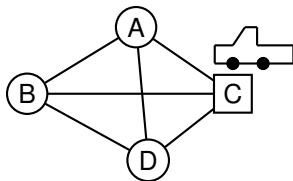
- Partial plan: Drive-t-B, Load-o-B, Drive-t-C, Unload-o-C, Fly-p-C
- Goal: o-in-p

## Using Landmarks as Subgoals - Logistics Example



- Partial plan: Drive-t-B, Load-o-B, Drive-t-C, Unload-o-C, Fly-p-C, Load-o-p
- Goal: o-at-E

## Using Landmarks as Subgoals - Logistics Example



- Partial plan: Drive-t-B, Load-o-B, Drive-t-C, Unload-o-C, Fly-p-C, Load-o-p, Fly-p-E, Unload-o-E
- Goal:  $\emptyset$

# Using Landmarks as Subgoals

- That was a good example
- Now let's see a bad one

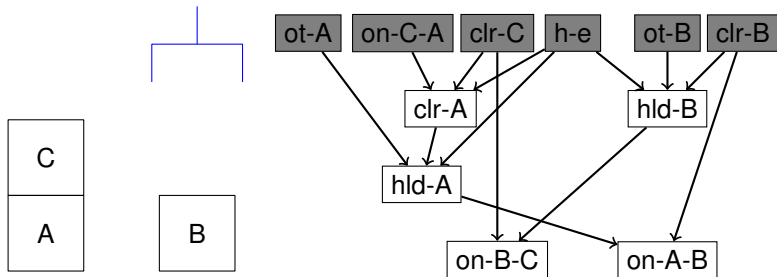


## Using Landmarks as Subgoals - Sussman Example

- Consider the following blocks problem (“The Sussman Anomaly”)

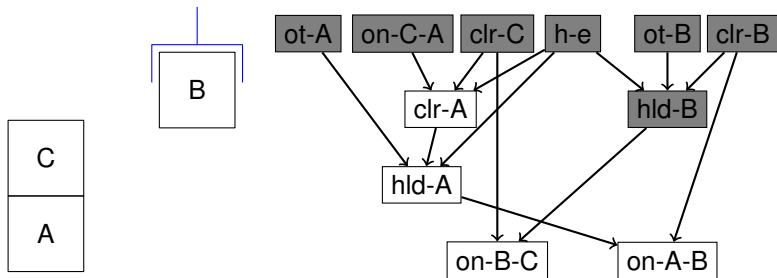
- Initial State 
- Goal: *on-A-B*, *on-B-C*

## Using Landmarks as Subgoals - Sussman Example



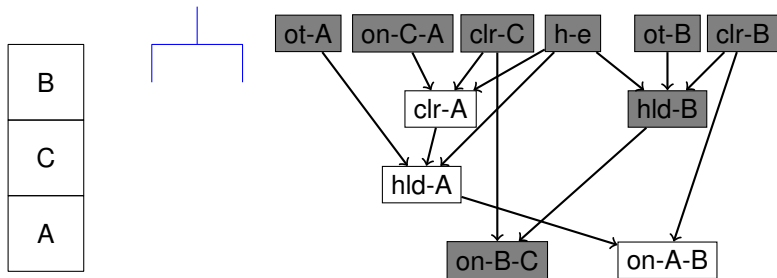
- Partial plan:  $\emptyset$
- Goal:  $\text{clear-A} \vee \text{holding-B}$

## Using Landmarks as Subgoals - Sussman Example



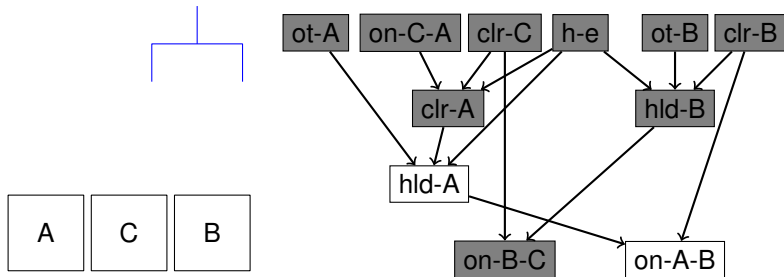
- Partial plan: Pickup-B
- Goal:  $\text{clear-A} \vee \text{on-B-C}$

## Using Landmarks as Subgoals - Sussman Example



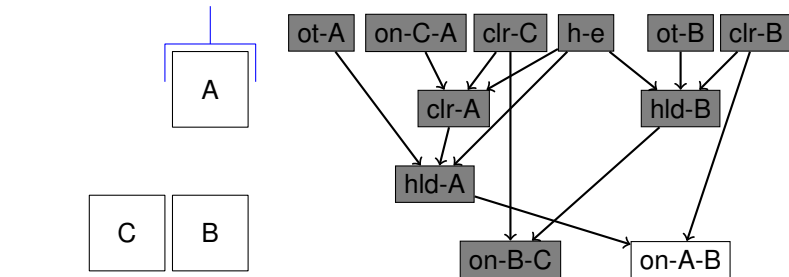
- Partial plan: Pickup-B, Stack-B-C
- Goal: clear-A

## Using Landmarks as Subgoals - Sussman Example



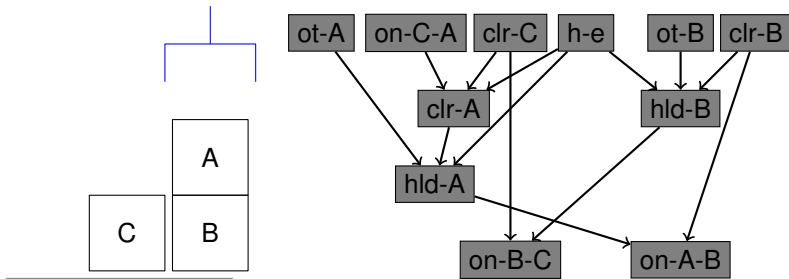
- Partial plan: Pickup-B, Stack-B-C, Unstack-B-C, Putdown-B, Unstack-C-A, Putdown-C
- Goal: holding-A

## Using Landmarks as Subgoals - Sussman Example



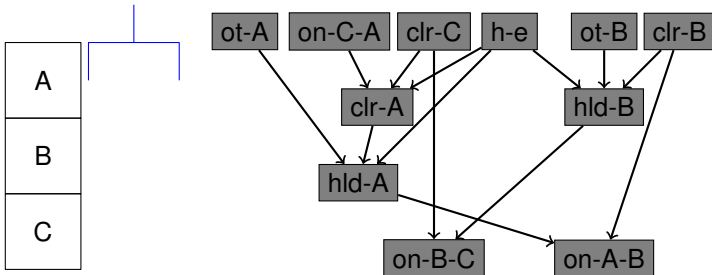
- Partial plan: Pickup-B, Stack-B-C, Unstack-B-C, Putdown-B, Unstack-C-A, Putdown-C, Pickup-A
- Goal: on-A-B

## Using Landmarks as Subgoals - Sussman Example



- Partial plan: Pickup-B, Stack-B-C, Unstack-B-C, Putdown-B, Unstack-C-A, Putdown-C, Pickup-A, Stack-A-B
- Goal: Still need to achieve on-B-C

## Using Landmarks as Subgoals - Sussman Example



- Partial plan: Pickup-B, Stack-B-C, Unstack-B-C, Putdown-B, Unstack-C-A, Putdown-C, Pickup-A, Stack-A-B, Unstack-A-B, Putdown-A, Pickup-B, Stack-B-C, Pickup-A, Stack-A-B
- Goal:  $\emptyset$



# Using Landmarks as Subgoals - Pros and Cons

- Pros:
  - Planning is very fast - the base planner needs to plan to a lesser depth
- Cons:
  - Can lead to much longer plans
  - Not complete in the presence of dead-ends

# Outline

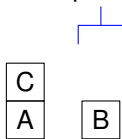
- 1 What Landmarks Are
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# Using Landmarks for Heuristic Estimates

- The number of landmarks that still need to be achieved is a heuristic estimate (Richter, Helmert and Westphal 2008)
- Used by *LAMA* - winner of the IPC-2008 sequential satisficing track

# Path-dependent Heuristics

- Suppose we are in state  $s$ . Did we achieve landmark  $A$  yet?
- Example: did we achieve holding( $B$ )?



- There is no way to tell just by looking at  $s$
- Achieved landmarks are a function of path, not state
- The number of landmarks that still need to be achieved is a **path-dependent** heuristic

# The Landmark Heuristic

- The landmarks that still need to be achieved after reaching state  $s$  via path  $\pi$  are

$$L(s, \pi) = (L \setminus \text{Accepted}(s, \pi)) \cup \text{ReqAgain}(s, \pi)$$

- $L$  is the set of all (discovered) landmarks
- $\text{Accepted}(s, \pi) \subset L$  is the set of *accepted* landmarks
- $\text{ReqAgain}(s, \pi) \subseteq \text{Accepted}(s, \pi)$  is the set of *required again* landmarks - landmarks that must be achieved again

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## Accepted Landmarks

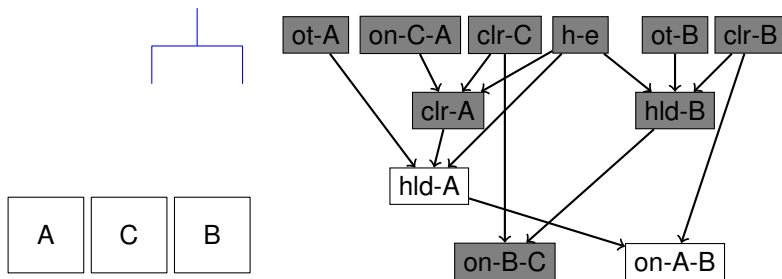
- In LAMA, a landmark  $A$  is first accepted by path  $\pi$  in state  $s$  if
  - all predecessors of  $A$  in the landmark graph have been accepted, and
  - $A$  becomes true in  $s$
- Once a landmark has been accepted, it remains accepted

## Required Again Landmarks

- A landmark  $A$  is required again by path  $\pi$  in state  $s$  if:
  - false-goal  $A$  is false in  $s$  and is a goal, or
  - open-prerequisite  $A$  is false in  $s$  and is a greedy-necessary predecessor of some landmark  $B$  that is not accepted
- It's also possible to use (Buffet and Hoffmann, 2010):
  - doomed-goal  $A$  is true in  $s$  and is a goal, but one of its greedy-necessary successors was not accepted, and is inconsistent with  $A$
- Unsound rule:
  - required-ancestor is the transitive closure of *open-prerequisite*

## Accepted and Required Again Landmarks - Example

- In the Sussman anomaly, after performing: Pickup-B, Stack-B-C, Unstack-B-C, Putdown-B, Unstack-C-A, Putdown-C



- on-B-C is a *false-goal*, and so it is required again

## Problems With Reasonable Orderings

- Heuristic value of a goal state may be non-zero (if the plan found does not obey all reasonable orderings, and consequently not all landmarks are accepted).  
Solution: explicitly test states for goal condition
- The definition of reasonable orderings allows an ordering  $A \rightarrow_r B$  if  $A$  and  $B$  become true simultaneously.  
Two solutions:
  - Accept a landmark if it has been made true at the same time as its predecessor (Buffet and Hoffmann, 2010)
  - Modify the definition of reasonable orderings to disallow such orderings

# Outline

- 1 What Landmarks Are
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# Admissible Heuristic Estimates

- LAMA's heuristic: the number of landmarks that still need to be achieved (Richter, Helmert and Westphal 2008)
- LAMA's heuristic is inadmissible - a single action can achieve multiple landmarks
  - Example: *hand-empty* and *on-A-B* can both be achieved by *stack-A-B*
- Admissible heuristic: assign a cost to each landmark, sum over the **costs** of landmarks (Karpas and Domshlak, 2009)

## Conditions for Admissibility

- Each action shares its cost between all the landmarks it achieves

$$\forall a \in \mathcal{A} : \sum_{B \in L(a|s, \mathcal{P})} cost(a, B) \leq C(a)$$

$cost(a, B)$ : cost “assigned” by action  $a$  to  $B$

$L(a|s, \mathcal{P})$ : the set of landmarks achieved by  $a$

- Each landmark is assigned at most the cheapest cost any action assigned it

$$\forall B \in L(s, \mathcal{P}) : cost(B) \leq \min_{a \in \text{ach}(B|s, \mathcal{P})} cost(a, B)$$

$cost(B)$ : cost assigned to landmark  $B$

$\text{ach}(B|s, \mathcal{P})$ : the set of actions that can achieve  $B$

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# Admissible Cost Sharing

- Idea: the cost of a set of landmarks is no greater than the cost of any single action that achieves them
- Given that, the sum of costs of landmarks that still need to be achieved is an admissible heuristic,  $h_L$

$$h_L(s, \pi) := \text{cost}(L(s, \pi)) = \sum_{B \in L(s, \pi)} \text{cost}(B)$$

- Proof: left up to the reader 😊

## Cost Partitioning - how?

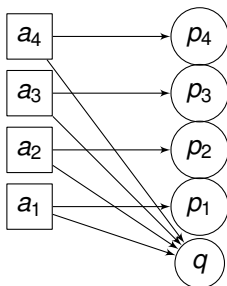
- How can we find such a partitioning?
- Easy answer - **uniform cost sharing** - each action shares its cost equally between the landmarks it achieves

$$\text{cost}(a, B) = \frac{C(a)}{|L(a|s, \pi)|}$$

$$\text{cost}(B) = \min_{a \in \text{ach}(B|s, \pi)} \text{cost}(a, B)$$

# Uniform Cost Sharing

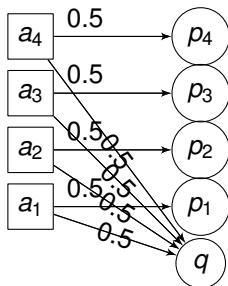
- Advantage: Easy and fast to compute
- Disadvantage: can be much worse than the optimal cost partitioning



# Uniform Cost Sharing

- Advantage: Easy and fast to compute
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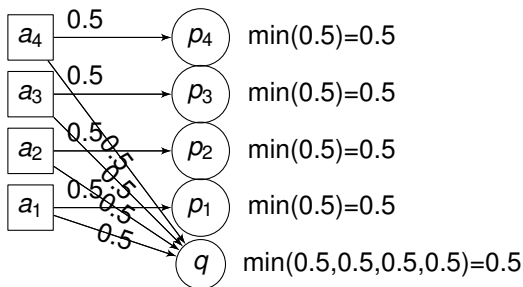
Uniform cost sharing



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Uniform cost sharing

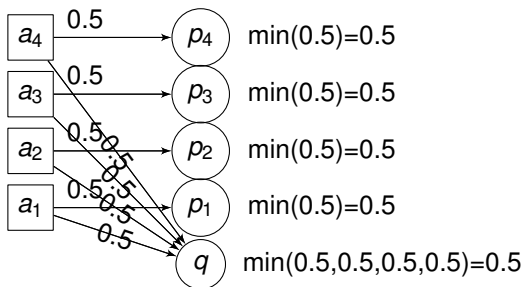


# Uniform Cost Sharing

- Advantage: Easy and fast to compute
- Disadvantage: can be much worse than the optimal cost partitioning

Uniform cost sharing

$$h_L = 2.5$$

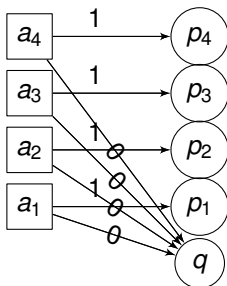


# Uniform Cost Sharing

- Advantage: Easy and fast to compute
- Disadvantage: can be much worse than the optimal cost partitioning

Optimal cost sharing

uniform  $h_L = 2.5$

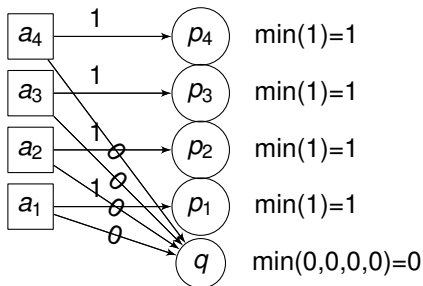


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- Advantage: Easy and fast to compute
- Disadvantage: can be much worse than the optimal cost partitioning

Optimal cost sharing

uniform  $h_L = 2.5$





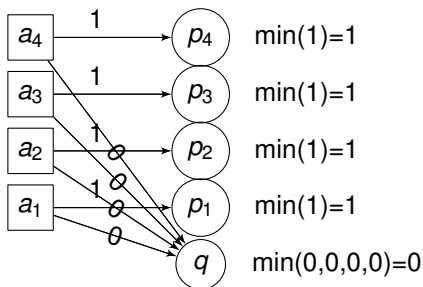
# Uniform Cost Sharing

- Advantage: Easy and fast to compute
- Disadvantage: can be much worse than the optimal cost partitioning

Optimal cost sharing

$$h_L = 4$$

$$\text{uniform } h_L = 2.5$$



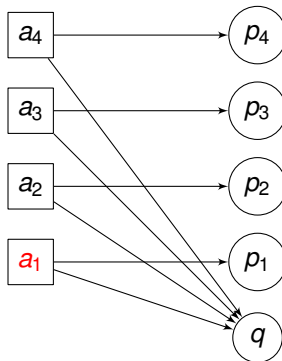
# Optimal Cost Sharing

- The good news: the optimal cost partitioning is poly-time to compute
  - The constraints for admissibility are linear, and can be used in a **Linear Program** (LP)
  - Objective: maximize the sum of landmark costs
  - The solution to the LP gives us the optimal cost partitioning
- The bad news: poly-time can still take a long time

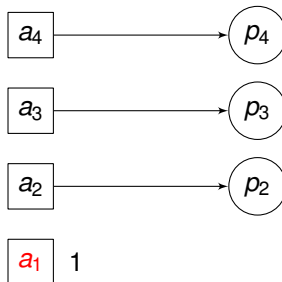
## How can we do better?

- So far:
  - Uniform cost sharing is easy to compute, but suboptimal
  - Optimal cost sharing takes a long time to compute
- Q: How can we get better heuristic estimates that don't take a long time to compute?
- A: Exploit additional information - action landmarks

# Using Action Landmarks - by Example



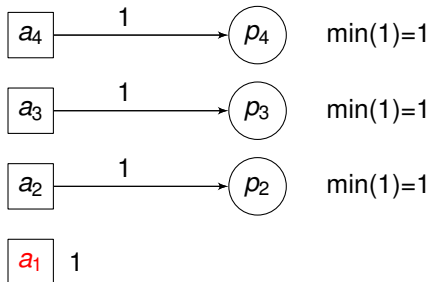
# Using Action Landmarks - by Example



## Using Action Landmarks - by Example

Uniform Cost Sharing

$$h_{LA} = 4$$



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# Using Landmarks to Enrich the Problem

- Landmarks are, in essence, implicit goals
- We can make these **explicit** by reformulating the planning problem
- Two different methods for doing this have been proposed (Wang, Baier and McIlraith, 2009 and Domshlak, Katz and Lefler, 2010)



## Viewing Landmarks as Temporally Extended Goals

- Landmarks and their orderings can be viewed as temporally extended goals (Wang, Baier and McIlraith, 2009)
- These temporally extended goals can be expressed in Linear Temporal Logic (LTL)
- Each LTL formula can be compiled into a finite-state automaton
- Each FSA can be encoded as a single variable in an **enriched** planning problem

## A Simpler Approach

- A simpler approach of encoding landmarks into a planning problem is to encode the landmarks directly (Domshlak, Katz and Lefler, 2010)
  - Each landmark is represented by a single binary state variable
  - The two values represent landmark accepted / not accepted
  - Each action that achieves the landmark has an additional effect added to it, changing the landmark variable value to accepted
  - The accepting value of each landmark variable is added to the goal state

## Why Enrich Problems?

- Landmarks and orderings are **implicit**, encoding them into the problem makes them **explicit**
- Allows other heuristics to use landmark information
- Example: structural pattern heuristic on the enriched problem accounts not only for explicit goals (Domshlak, Katz and Lefler, 2010)
- In fact, the landmark count heuristic can be seen as the goal count heuristic on the landmark enriched problem
- Caveat - since current landmark discovery procedures are based on delete-relaxation, this adds no information to delete-relaxation based heuristics

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# Landmarks in Probabilistic Planning

- Landmarks can also be adapted to probabilistic planning (Buffet and Hoffmann, 2010)
- In a probabilistic planning task, a landmark is a fact which must be true in every successful trajectory (possible execution)
- Using the landmark count heuristic in FPG yields good results

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# Summary

- Landmarks provide a way to utilize the implicit structure of a planning problem
- They can (and have been) used successfully for both satisficing and optimal planning

# Challenges

- Discover more landmarks and orderings using different techniques (why use only relaxed planning?)
- Discover and exploit more complex types of landmarks (conjunctive, CNF, first order logic . . . )
- Discover and exploit landmarks in a problem-independent manner (for example, in Logistics - a package that is not at its destination must always be loaded on a truck or an airplane)



## More Challenges

- A landmark / ordering must be true in every plan
- An optimal landmark / ordering must be true in every optimal plan
  - All landmarks are also optimal landmarks, but can we find facts which are optimal landmarks and NOT landmarks?
- An existential landmark / ordering must be true in a plan
  - We must be careful not to mix between existential landmarks from different plans
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# Thank You

Enjoy ICAPS!

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