DS2500 Day 18 Mar 20

Admin:

- submitting data & analysis plan
- April 4th and 7th
- Project meetings with Prof Higger
 - sign up link available on course schedule
 - 1 student per team sign up (share the link within team please) no classes will be held (to allow time to meet)

Part 1: Bayes Rule

- basic probability (review)
- binary problems (review)
- bayes rule & independence

(Part 2 of today's notes has its own content table of contents too)

PROBABILITY (NOTOTION + DEFINITIONS)

LET X BE A RANDOM VARIABLE REPRESENTING OUTCOME OF FAIR 6 SIDED DIE ROLL " X = X, A> DIE ROLL WAS 1" CAPITAL - RANDOM LOWERCASE W SOBSCA.PT 5 PARTICULAR OUTCOME VARIABLE

PROBABILITY (NOTOTION + DEFINITIONS)

SHORTHAND

WE DROP MENTION OF RANDOM VARIABLE

TO SAVE SPACE

$$P(\chi_{\circ}) = P(\chi = \chi_{\circ})$$

SOM OF PROBABILITY OF ALL OUTCOMES IS 1

Conditional Probability (motivation)

Let C=1 indicate the event that a person has covid (C=0 otherwise) Let A=1 indicate the event that an antigen test is positive (A=0 otherwise)

Let us discuss (and express) the following probabilities:

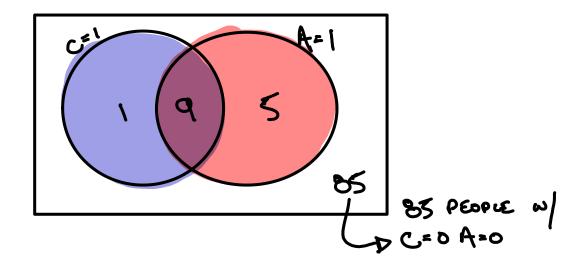
- probability person has a positive antigen test
- probability person has covid and a positive antigen test
- probability person has covid given a positive antigen test

A conditional probability gives the probability of one event given that another has occured.

A conditional probability P(a|b) ignores all states which don't meet a condition

Given the following, esitmate

- the prob of covid
- the prob of covid given a positive antigen test



$$P(a|b) = \frac{P(a|b)}{P(b)} + \frac{P(a|b)P(b)}{P(a|b)} = P(a|b)$$

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Multiplying
- a conditional probability

Takeaway above:

- the probability of condition

Will yield

-prob both outcomes happen together

$$P(a|b)P(b) = P(ab) = P(b|a)P(a)$$

$$\Rightarrow P(a|b) = P(b|a)P(a)$$

$$P(b)$$

Notice: this formula "swaps" the order of the conditioning: P(A|B) on left P(B|A) on right Its typical in a Bayes question to be given variables in one order while question asks for other.

Remember: To compute P(B) we can sum P(B, A) for all outcomes in sample space of A $P(b=b) = \angle P(b=b | A=a)$

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A HELPFUL MANIPULATION

$$P(b) = \sum_{\alpha} P(\alpha b)$$

$$= \sum_{\alpha} P(ab)$$

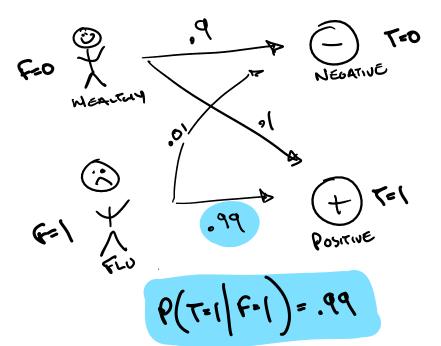
$$= \sum_{\alpha} P(b|a) P(a)$$

$$= \sum_{\alpha} P(b|a) P(a)$$

WHY WAS THAT HELPFUL? P(a|b) = P(b|a)P(a) $P(a|b) = \frac{P(b|a)P(a)}{P(b)}$ BAYES RULE 2 P(a/b) = P(b/a) P(a)

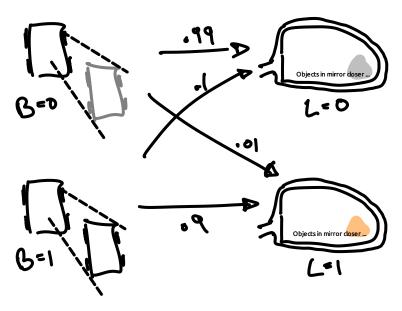
Z P(b/ai)P(ai) BAYES PLOVE EX

Given flu occurs in .04 of population, what is the probability one has flu given they test positive?



In Class Assignment 1

A blind spot monitor produces a warning light (L=1) when it estimates that a car is in one's blind spot (B=1). Given that the light is off, whats the probability that a car is one's blind spot? (Assume that a car is in your blindspot .02 percent of the time while driving.)



ALGEBRA + NTUITION LOVE STORY AMEAD ...

INDEPENDENCE + CONDITIONAL PROB

INDEDENDENCE

INTUITION:

Random variables x, y are independent if observing any outcome of one doesn't impact our beliefs about the other.

ALOGBRA:
FOR EACH OUTCOME PAIR XIY
$$P(X=xY=y)=P(X=x)P(Y=y)$$

Bayes Rule shows the equivilence of the algebraic and intuitive definitions above!

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INTUITION:

Random variables x, y are independent if observing any outcome of one doesn't impact our beliefs about the other.

ALDEBRA:
FOR EACH OUTCOME PAIR XIY
$$P(X=x)=P(X=x)P(Y=y)$$

$$b(x|\lambda) = \frac{b(\lambda)}{b(\lambda)} = \frac{b(\lambda)}{b(\lambda)} = b(x)$$

Notice that P(X|Y) = P(X). Observing Y has no impact on the prob of X!