

The Condorcet Jury Theorem

The Condorcet Jury Theorem is a political science and probability theory concept named after the French mathematician and philosopher Marquis de Condorcet. The theorem explores the relationship between the accuracy of individual decision-makers (voters or jurors) and the accuracy of the collective decision made by the group.

The theorem assumes that:

- Each individual in the group has a probability p of making the correct decision (independently of the others), where $0.5 < p < 1$. In other words, each individual is more likely than not to make the correct decision.
- The individuals make their decisions independently of each other.

Under these conditions, the Condorcet Jury Theorem states that:

As the group size (number of individuals) increases, the probability that the group makes the correct decision approaches 1 (certainty). If each individual's probability of making the correct decision is above 0.5, then adding more individuals to the group will improve the group's decision-making accuracy. Conversely, if each individual's probability of making the correct decision is below 0.5, then adding more individuals to the group will reduce the group's decision-making accuracy. In simpler terms, the theorem suggests that, under the specified conditions, the "wisdom of the crowd" prevails. A larger group of individuals, each with a better-than-random chance of making the correct decision, will collectively make better decisions than any single individual or a smaller group. However, if the individual's probability of making the correct decision is below 0.5, the group's collective decision-making would worsen with additional members.

The Condorcet Jury Theorem has applications in various fields, such as political science, economics, and decision-making theory. It provides a basis for understanding how collective decision-making can lead to more accurate outcomes, given that certain conditions are met.

```
In [151]: 1 # Review of for loops
          2 print("Count to 10")
          3 for i in range(10):
          4     print(i)
          5
          6 print("Iterate over values in a list")
          7 for item in [5, 'hello', 3.13, True, [1,2,3]]:
          8     print(item)
```

Count to 10

0
1
2
3
4
5
6
7
8
9

Iterate over values in a list

5
hello
3.13
True
[1, 2, 3]

```
In [150]: 1 # Review of list comprehension
          2
          3 [x**2 for x in range(10)]
          4
          5 [len(word) for word in "to be or not to be that is the question"]
```

Out[150]: [2, 2, 2, 3, 2, 2, 4, 2, 3, 8]

```
In [114]: 1 # Review of random number generation
          2 import random as rnd
          3
          4 rnd.seed(3.14159)
          5 [rnd.randrange(1,5) for _ in range(5)]
          6 [rnd.choice(['a', 'b', 'c']) for _ in range(5)]
          7 [rnd.uniform(.2, .3) for _ in range(5)]
          8 [rnd.gauss(0, 1) for _ in range(5)]
```

Out[114]: [-0.6239279552210337,
0.255883175412692,
0.19679498371365348,
0.012348240098453199,
0.301546769068397]

```
In [124]: 1 # Review of counter library
2 dna = "agctagctagcatgcatcgatagtcgatctattctaataattcggcggcgattatcg
3 counts = Counter(dna)
4 print(cnt)
5
6 print("Most common: ", counts.most_common(1)[0][0])
```

Counter({'t': 18, 'a': 16, 'g': 15, 'c': 13})
Most common: t

```
In [135]: 1 # Create 11 "jurors" with verdict accuracy in range (0.5, x)
2 n = 11
3 max_accuracy = 0.667
4 jury = [rnd.uniform(.5, max_accuracy) for _ in range(n)]
5 jury
```

Out[135]: [0.5386514461914312,
0.6490018875549747,
0.6509485369268001,
0.6264403149307383,
0.6006604526422817,
0.6456462101085015,
0.5836102701615514,
0.5656482996136852,
0.6288250691054713,
0.5792069752540076,
0.5114937016621027]

```
In [136]: 1 # Create a series of outcomes (0=innocent or 1=guilty) to be decided
2 n_outcomes = 100000
3 outcomes = [rnd.choice([0,1]) for _ in range(n_outcomes)]
4
```

```
In [137]: 1 # for each outcome, and each juror makes a verdict decision
2 # In this model, we don't require unanimity. Instead, the jurors
3 # The majority vote is the decision of the jury.
4 verdicts = []
5 for out in outcomes:
6     verdict = []
7     for juror in jury:
8         if rnd.random() < juror:
9             verdict.append(out)
10        else:
11            verdict.append(1-out)
12    verdicts.append(Counter(verdict).most_common(1)[0][0])
13
```

```
In [138]: 1 # Compute the jury verdict accuracy for each
          2
          3 correct = 0
          4 for i in range(len(outcomes)):
          5     if outcomes[i] == verdicts[i]:
          6         correct += 1
          7 print(correct / len(outcomes))
          8
```

0.7494

```
In [ ]: 1
```