

HW5

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PROBLEM 1:

x-axis: list the different categories of household income, based on NES. NES divided the annual income of household voters (across all states) into five quantiles: 0-16, 17-33, 34-67, 68-95, and 96-100. In this study, each quantile is number as -2, -1, 0, 1, 2 respectively and correspondingly for the ease of interpreting regression (as they center around 0)

y-axis: is the probability of voting for Republican. If the value is >0.5 , meaning that the in general, the households in that specific income category supports Republican.

Circles (or the points): each point corresponds to the probability an individual support Rep in relation to their income level. 'The open circles show the relative proportion (as compared to national averages) of households in each income category in each of the three states, and the solid circles show the average income level and estimated average support for Bush for each state.'

The line: each line represents the trend of households' voting in a state, based on voters' income category. The slope of the line tells us how strong the relation between voting preference vs. income. The steeper the slope, the stronger the relation. As a result, 'income is a very strong predictor of vote preference in Mississippi, a weaker predictor in Ohio, and only weakly predicts vote choice at all in Connecticut.'

Different slopes between right and left panels:

In Figure 3, the model only consider the relation between income vs. voting preference so that the lines representing each State only vary by income. In Figure 4, however, the calculated probability takes into the consideration of respondents' geography and income (2 vars). When taking into consideration of 2 vars, we don't require the plotted points to construct a specific linear relationship between voting preference vs. income or in other words, allows the model for varying slope. By allowing varying slope, the model reduces the deviance (as seen in 2000 vs. 2004 graph) and improved its estimation's accuracy.

Test: Below is only the method - or pseudocode - I think of.

Let x be the respondents' income, y is the probability voting for Republican, and z is the respondents' geography. n is the number of respondents where i is the n (th) respondent.

Without z , our calculation for y knowing x :

$y \leftarrow a \cdot x + b$ (linear relationship)

a, b : constants (is not provided)

See the regression without z :

`summary(lm(y~x))`

With z , our calculation for y :

$y \leftarrow \text{for } (i \text{ in } n) \{ \log(i)^{-1} (\alpha[z] + \beta[z]x) \}$

Formula from p.9

α, β : constants (is not provided)

See the regression with z:
summary(lm(y~x+z))

The second regression should return a higher R-squared value.

PROBLEM 2:

```
load('~/Desktop/Policy Research/HW5/fraud.RData')
```

a. To analyze the 2011 Russian election results, first compute United Russia's vote share as a proportion of the voters who turned out. Identify the 10 most frequently occurring fractions for the vote share. Create a histogram that sets the number of bins to the number of unique fractions, with one bar created for each uniquely observed fraction, to differentiate between similar fractions like $1/2$ and $51/100$. This can be done by using the breaks argument in the hist function. What does this histogram look like at fractions with low numerators and denominators such as $1/2$ and $2/3$? Ans:

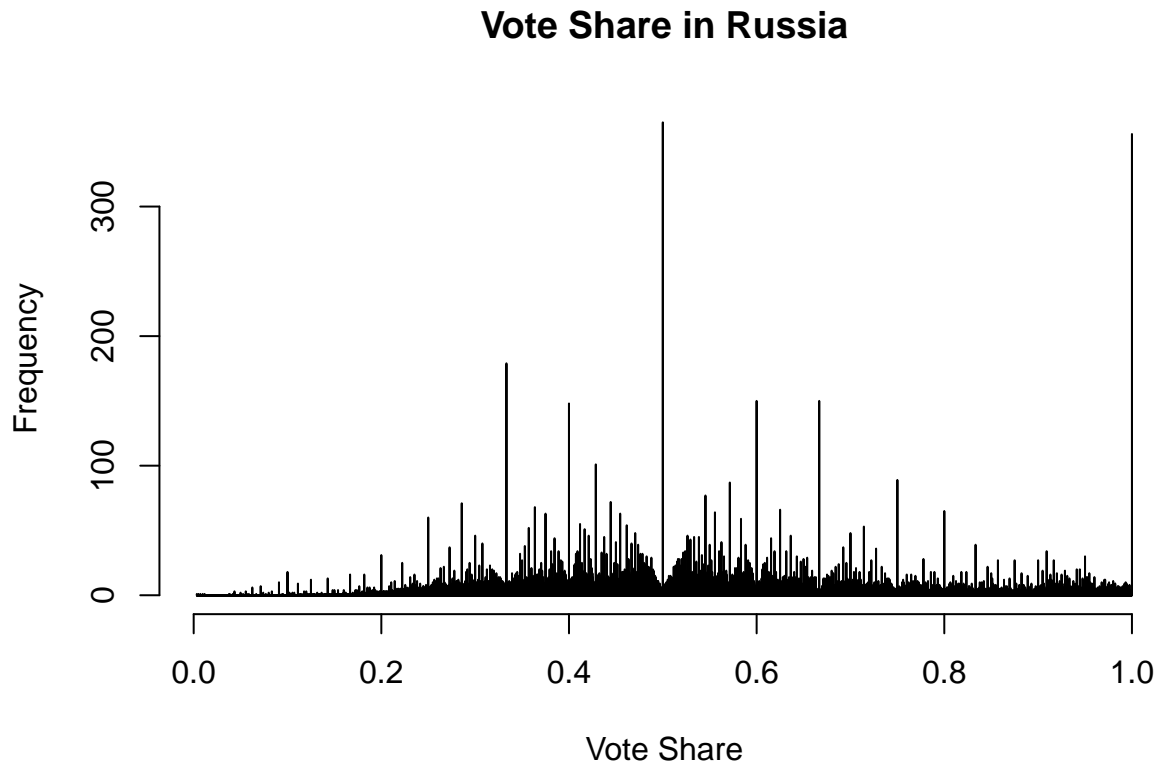
Fractions with low numerators and denominators (i.e. $1/2$, $2/3$, $3/4$) appear with the significant higher frequency than others.

```
#Calculate vote share
russia2011$vote_share <- russia2011$votes/russia2011$turnout
```

```
#Find frequency
vote_share_freq <- table(russia2011$vote_share)
#Find 10 most frequently occurring values
head(sort(vote_share_freq, decreasing=TRUE), n=10)
```

```
##
##          0.5          1 0.333333333333333          0.6
##          365          356          179          150
## 0.666666666666667          0.4 0.428571428571429          0.75
##          150          148          101          89
## 0.571428571428571 0.545454545454545
##          87          77
```

```
#Create histogram
hist(russia2011$vote_share, breaks=length(vote_share_freq), xlab="Vote Share", main="Vote Share in Russia")
```



b. The mere existence of high frequencies at low fractions may not imply election fraud. Indeed, more numbers are divisible by smaller integers like 2, 3, and 4 than by larger integers like 22, 23, and 24. To investigate the possibility that the low fractions arose by chance, assume the following probability model:

- Turnout for a precinct is binomially distributed, with size equal to the number of voters in the precinct and success probability equal to its observed turnout rate.
- Conduct a Monte Carlo simulation under these assumptions. 1000 simulated elections should be sufficient. (Note that this may be computationally intensive code. Write your code for a small number of simulations to test before running all 1000 simulations.) Ans:
See below.

```
#Turnout rate
russia2011$turnout_rate <- russia2011$turnout/russia2011$N

#Initiate number of sims
sims <- 1000

#Function: Simulate an election
simulated_election <- function(dataset) {
  #Simulate a random sample of turn out
  turnout_sample <- rbinom(nrow(dataset), size=dataset$N, prob=dataset$turnout_rate)
  #Simulate a random sample of votes
```

```

votes_sample <- rbinom(nrow(dataset), size=turnout_sample, prob=dataset$vote_share)
#Calculate the vote shares
return (vote_share_sample <- votes_sample/turnout_sample)
}

#NOTE: (This is where I got the issue)

#Initially, I used a for-loop for simulation
#When using loop (like the following below code), the vote_share_sim will only
#return the last, or the 1000th simulated election
  #for (i in 1:sims) {vote_share_sim = simulated_election(russia2011)}
#This affects our analysis in (d) and (e)

#I thought of two possible solutions for using a for-loop in large simulation:
#(1) Turn the vote_share_sim (which is the vote share of a simulated election)
#into a vector, then create a list and store all such vectors. This method, however,
#is really slow because the computer takes time to both convert and append values
#(2) Create a class for simulation with a function to generate vote share of a simulated
#election. Then each simulated election will be an instance of the class.
#We then can add the instances into the list. Working with instances in a list
#will be less error-prone than working with vectors in a list in (1)

#The book p297 shows one way to store values from large simulations. However, in the example,
#the range of values in Obama.ev is equal the number of sims since each of its
#value is the sum of votes in one election. We cannot apply, because in our case,
#we are calculating vote share, not the total number of votes which is aggregated data.

#Use a loop, regardless, will make our code for question (c) and above too complicated
#Use replicate: which instead returns a matrix (or 2-dimensional list),
#where each simulation is store in a column, and rows is vector of vote share of a simulation
vote_share_sim <- replicate(sims, simulated_election(russia2011))

#Visualization (for checking outcomes)
#Find frequency
#vote_share_freq_sim <- table(vote_share_sim)
#Create histogram
#hist(vote_share_sim, breaks=length(vote_share_freq_sim), xlab="Vote Share", main="Vote Share in Russia")

```

c. To judge the Monte Carlo simulation results against the actual results of the 2011 Russian election, we compare the observed fraction of observations within a bin of certain size with its simulated counterpart. To do this, create histograms showing the distribution of part (b)'s four most frequently occurring fractions, i.e., $1/2$, $1/3$, $3/5$, and $2/3$, and compare them with the corresponding fractions' proportion in the actual election. Briefly interpret the results.

Ans:

The distribution of most of our observed fraction is close to the approximate value generated from Monte Carlo simulations, with the exception seen in the $3/5$ fraction. Though this seems to be unusual and hints for voting manipulation, the difference observed in one fraction alone could hardly tell us anything about our analysis for whether or not fraud occur (there would be so many possible fractions that we can consider instead, not to mention the fact that the fraction of $1/2$ - the one that looks to be most suspicious - turned out to have a 'natural' distribution so far).

```

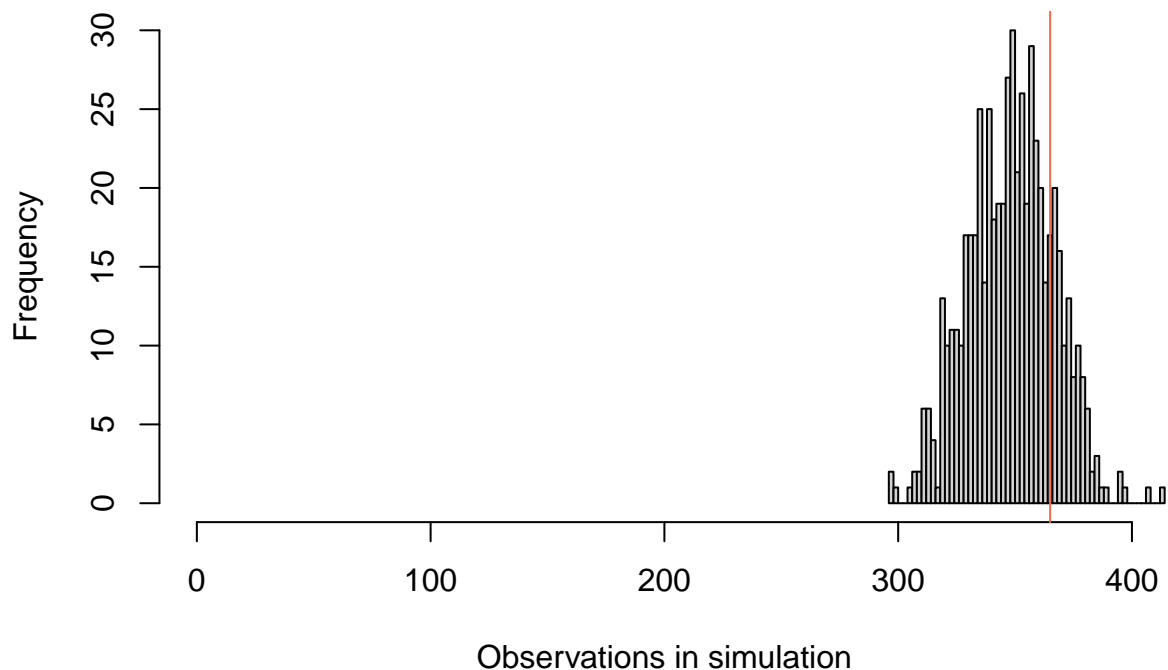
#Number of observations in each fraction
obs_1_2 = sum(russia2011$vote_share==1/2)
obs_1_3 = sum(russia2011$vote_share==1/3)
obs_3_5 = sum(russia2011$vote_share==3/5)
obs_2_3 = sum(russia2011$vote_share==2/3)

#Number of observations in each fraction from simulations
obs_1_2_sim = apply(vote_share_sim==1/2,2,sum)
obs_1_3_sim = apply(vote_share_sim==1/3,2,sum)
obs_3_5_sim = apply(vote_share_sim==3/5,2,sum)
obs_2_3_sim = apply(vote_share_sim==2/3,2,sum)

#Create histogram for distribution of obs of fraction in simulation and compare
#with that in the actual dataset
hist(obs_1_2_sim, xlim=c(0,400), breaks= 50, xlab='Observations in simulation', main='Observations in Actual vs. Simulated Election')
abline(v=obs_1_2, col = 'coral2')

```

Observations in Actual vs. Simulated Election

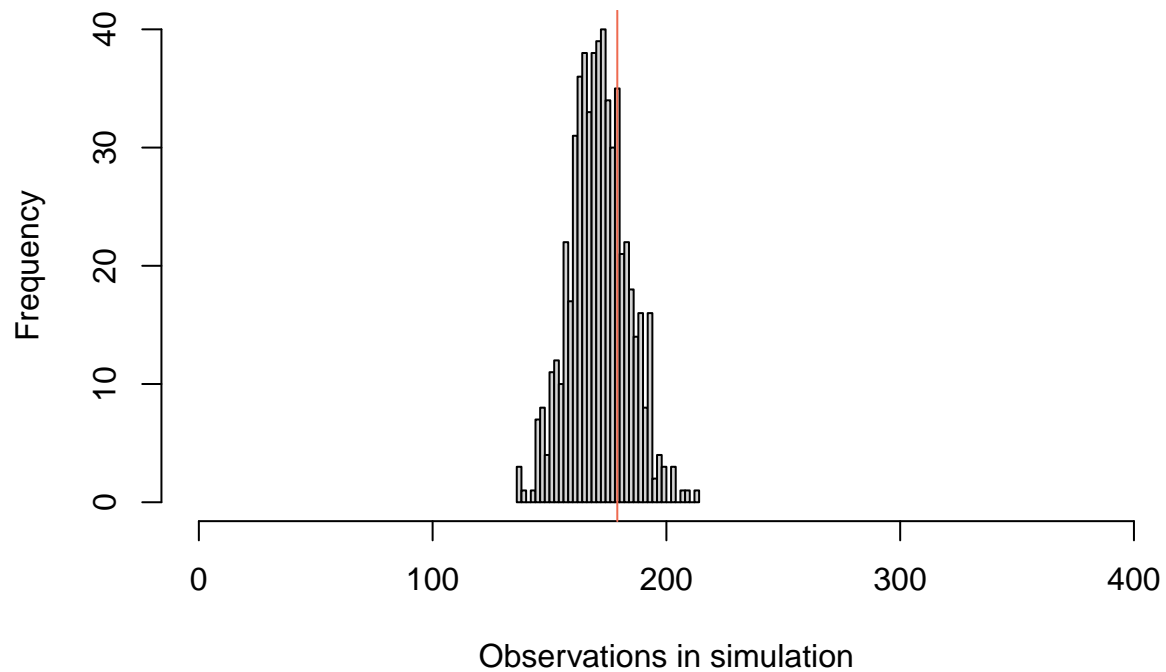


```

hist(obs_1_3_sim, xlim=c(0,400), breaks= 50, xlab='Observations in simulation', main='Observations in Actual vs. Simulated Election')
abline(v=obs_1_3, col = 'coral2')

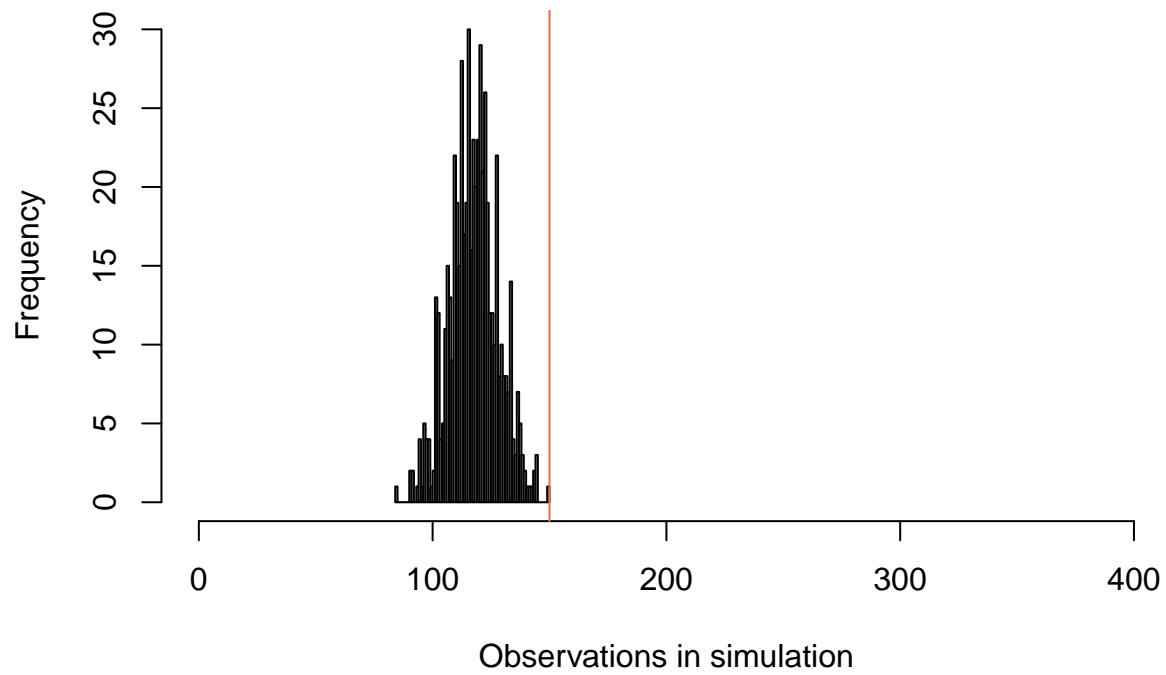
```

Observations in Actual vs. Simulated Election



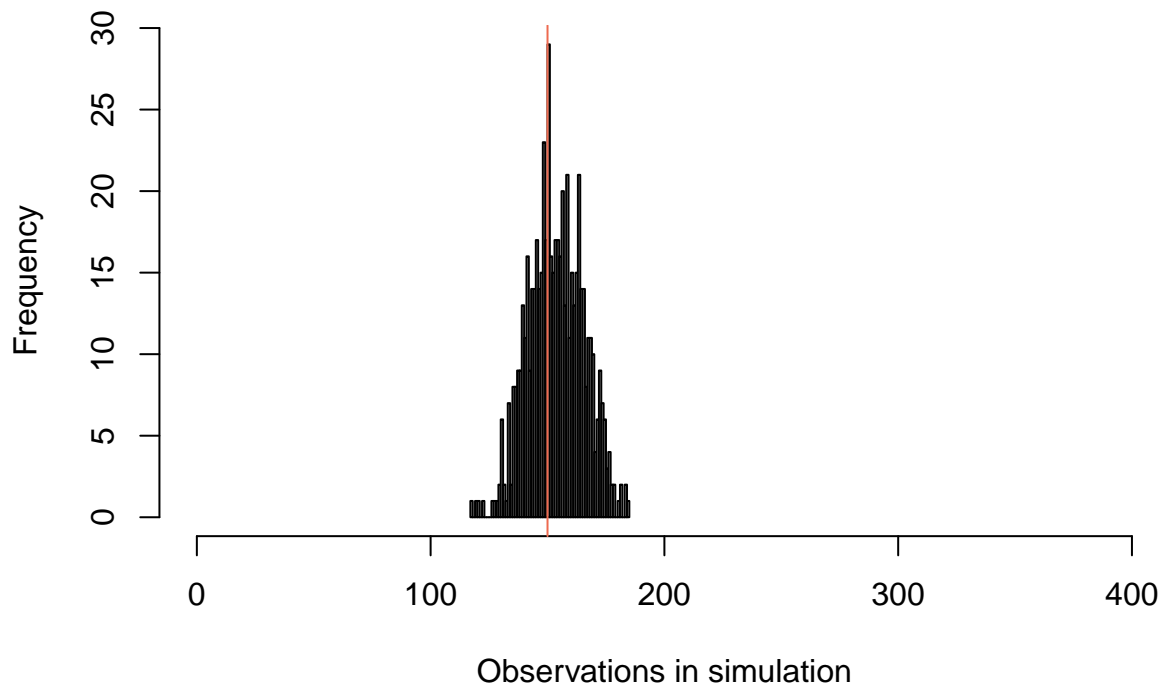
```
hist(obs_3_5_sim, xlim=c(0,400), breaks= 50, xlab='Observations in simulation', main='Observations in Actual vs. Simulated Election')  
abline(v=obs_3_5, col = 'coral2')
```

Observations in Actual vs. Simulated Election



```
hist(obs_2_3_sim, xlim=c(0,400), breaks= 50, xlab='Observations in simulation', main='Observations in Actual vs. Simulated Election')
abline(v=obs_2_3, col = 'coral2')
```

Observations in Actual vs. Simulated Election



d. We now compare the relative frequency of observed fractions with the simulated ones beyond the four fractions examined in the previous question. To do this, we choose a bin size of 0.01 and compute the proportion of observations that fall into each bin. We then examine whether or not the observed proportion falls within the 2.5 and 97.5 percentiles of the corresponding simulated proportions. Plot the result with vote share bin on the horizontal axis and estimated vote share on the vertical axis. This plot attempts to reproduce the one held by protesters in the figure. Now count the number of times an observed precinct vote share falls outside its simulated interval. Interpret the results. Ans:

There are 31 observed precinct vote share falls outside its simulated interval, meaning that almost 1/3 of the actual proportion of vote share falls out the range of 'natural' proportion of vote shares. This might be a implication of manipulation in the voting behavior. However, noted that since we only compared the actual observed vs. that of simulated elections in the range between 2.5 to 97.5 percentiles, there would possibly be chances that the 31 fall-out is within the range that we fall short to cover.

```
#Function: Get vote share and return proportion
bin_share = function(voteshare){
  seq1=seq(0,1,length.out=101)[-101]
  seqh=seq(0,1,length.out=101)[-1]
  count=c()
  for (ii in 1:100){
    count[ii]=length(which(voteshare>seq1[ii]&voteshare<=seqh[ii]))
  }
  prop=count/sum(count)
  return (prop)
}
```



```

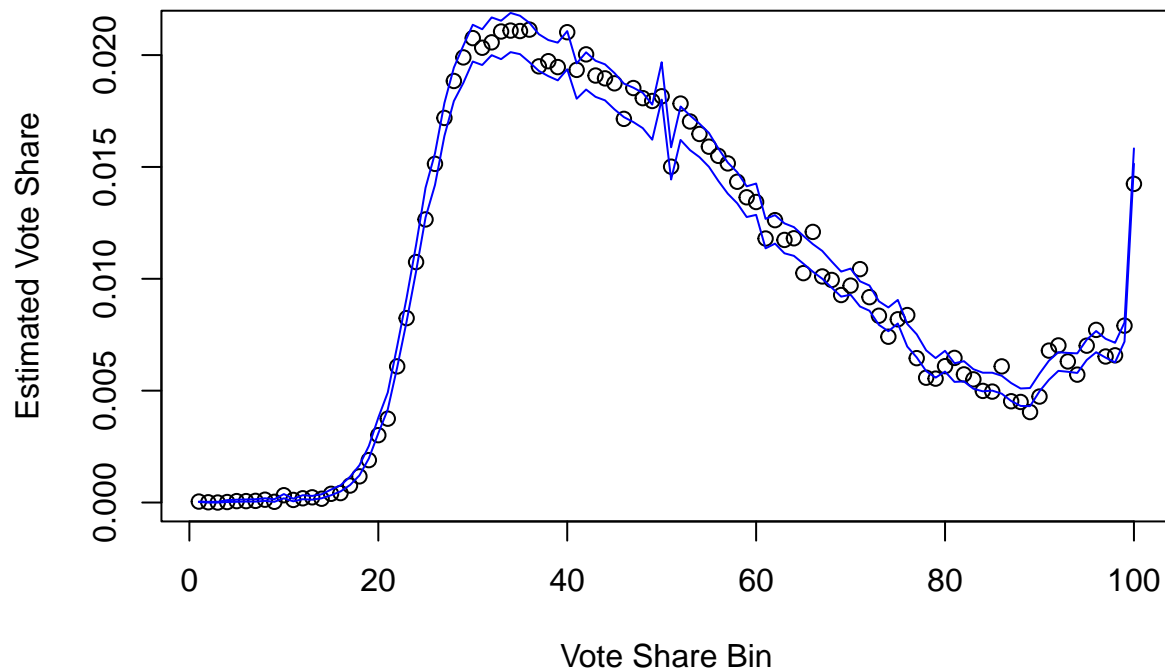
#Find observed proportion that fall into each bin
obs_bin = bin_share(russia2011$vote_share)

#Find the vote share prop at the 2.5 and 97.5 percentiles in the simulated elections
sim_obs_bin <- apply(vote_share_sim, 2, bin_share)
sim_2_5 <- apply(sim_obs_bin, 1, quantile, probs=0.025, na.rm=TRUE)
sim_97_5 <- apply(sim_obs_bin, 1, quantile, probs=0.975, na.rm=TRUE)

#Plot
plot(obs_bin, xlab="Vote Share Bin", ylab="Estimated Vote Share", main="Observed Vote Share vs. Simulated")
lines(sim_2_5, col="blue")
lines(sim_97_5, col="blue")

```

Observed Vote Share vs. Simulated Distribution



```

#Number of time an observed falls outside its simulated interval
sum(obs_bin < sim_2_5 | obs_bin > sim_97_5)

```

```
## [1] 32
```

e. To put the results of the previous question in perspective, apply the procedure developed in the previous question to the 2011 Canadian elections and the 2003 Russian election, where no major voting irregularities were reported. In addition, apply this procedure to the 2012 Russian presidential election, where election fraud allegations were reported. No plot needs to be produced. Briefly comment on the results you obtain. Ans:

The results are similar for all three: 21 fall-out observations for canada 2011, 23 for russia 2003, and 23 for russia 2012.

When a fraud reported election (russia 2012) generated such similar results to a non-fraud reported ones (russia 2003), it indicates that the result we found earlier for russia 2011 might not be sufficient for the conclusion whether fraud occurs or not.

Simultaneously, as noted earlier in (d), there are chances that the fall-outs are actually just a result of our lack of inclusion when using the 2.5 to 97.5 percentiles to compare. This fact further complicates our interpretation for whether or not fraud exists just by basing on the fall-out.

```
fraud_detection <- function(dataset){
  dataset$vote_share <- dataset$votes/dataset$turnout
  dataset$turnout_rate <- dataset$turnout/dataset$N
  VoteShareSim <- replicate(sims, simulated_election(dataset))
  ObsBin <- bin_share(dataset$vote_share)
  SimObsBin <- apply(VoteShareSim, 2, bin_share)
  Sim25 <- apply(SimObsBin, 1, quantile, probs=0.025, na.rm=TRUE)
  Sim975 <- apply(SimObsBin, 1, quantile, probs=0.975, na.rm=TRUE)
  return (sum(ObsBin < Sim25 | ObsBin > Sim975))
}
```

```
#No fraud: Canada and Russia 2003
fraud_detection(canada2011)
```

```
## [1] 20
```

```
fraud_detection(russia2003)
```

```
## [1] 21
```

```
#Fraud: Russia 2012
fraud_detection(russia2012)
```

```
## [1] 22
```

PROBLEM 3:

```
#Simulate and generate random var
sims<-1000
x <- runif(sims, min=1, max=1111)
y <- runif(sims, min=0, max=99999)
z <- runif(sims, min=0, max=100)

#Add var to a table
data <- list(x,y,z)
as.data.frame(data)
```

```
##          c.720.565746721346..867.464332207106..464.99430664489..273.09848694969..
## 1                                     720.565747
## 2                                     867.464332
## 3                                     464.994307
```

## 4	273.098487
## 5	5.360726
## 6	1028.156712
## 7	610.012055
## 8	191.028635
## 9	604.410376
## 10	354.499203
## 11	658.693855
## 12	821.927187
## 13	377.363789
## 14	625.700355
## 15	609.790391
## 16	966.912482
## 17	1036.375354
## 18	486.047684
## 19	1025.565420
## 20	212.157855
## 21	172.958641
## 22	564.583075
## 23	1064.947192
## 24	330.501349
## 25	262.924867
## 26	1060.300289
## 27	754.563068
## 28	358.319477
## 29	797.395044
## 30	142.332714
## 31	197.121643
## 32	307.010079
## 33	616.509359
## 34	925.738015
## 35	332.677237
## 36	1074.743973
## 37	394.536376
## 38	817.243571
## 39	629.690642
## 40	248.323355
## 41	172.760544
## 42	627.829748
## 43	367.701945
## 44	770.062556
## 45	4.327793
## 46	642.928834
## 47	31.596925
## 48	664.061351
## 49	418.541696
## 50	465.872401
## 51	90.145264
## 52	676.450286
## 53	341.228156
## 54	583.375507
## 55	158.870271
## 56	644.917514
## 57	358.789177

## 58	606.932637
## 59	557.414081
## 60	247.565925
## 61	636.302414
## 62	726.199767
## 63	342.605119
## 64	602.878004
## 65	1082.494984
## 66	525.946956
## 67	660.458337
## 68	751.548943
## 69	702.020775
## 70	425.368374
## 71	732.962115
## 72	920.287084
## 73	121.929354
## 74	748.439689
## 75	1067.467468
## 76	108.810502
## 77	603.351186
## 78	347.894259
## 79	405.736124
## 80	817.227052
## 81	1093.752879
## 82	485.348271
## 83	939.468758
## 84	962.304843
## 85	933.641959
## 86	1104.583250
## 87	391.323031
## 88	1058.869267
## 89	313.923472
## 90	543.615378
## 91	440.854447
## 92	38.109394
## 93	994.476337
## 94	446.138528
## 95	427.478950
## 96	139.111068
## 97	196.325402
## 98	445.886760
## 99	69.898981
## 100	763.587880
## 101	461.598134
## 102	1084.054775
## 103	411.900849
## 104	378.730190
## 105	320.797990
## 106	936.968945
## 107	1062.232129
## 108	765.574726
## 109	506.376665
## 110	525.324388
## 111	696.524648

## 112	1049.322200
## 113	401.040352
## 114	87.300408
## 115	249.851402
## 116	752.128687
## 117	906.838336
## 118	56.482528
## 119	1072.949267
## 120	1029.746560
## 121	162.604255
## 122	247.346141
## 123	430.983111
## 124	46.051793
## 125	550.503205
## 126	299.101771
## 127	270.700936
## 128	401.177647
## 129	285.658281
## 130	994.740000
## 131	1012.163103
## 132	329.321141
## 133	340.404111
## 134	783.110557
## 135	775.145787
## 136	780.725608
## 137	138.240262
## 138	353.445210
## 139	946.853162
## 140	2.558061
## 141	253.808219
## 142	378.488772
## 143	318.725562
## 144	1019.808462
## 145	602.488739
## 146	138.010694
## 147	667.328476
## 148	528.571130
## 149	13.752183
## 150	398.014489
## 151	410.414059
## 152	992.323231
## 153	714.045827
## 154	782.289866
## 155	931.564171
## 156	890.244997
## 157	843.054292
## 158	1032.279027
## 159	1092.501492
## 160	614.734243
## 161	431.148527
## 162	675.734176
## 163	115.225126
## 164	605.209850
## 165	845.201616

## 166	921.695254
## 167	27.808512
## 168	546.625783
## 169	332.997518
## 170	301.092514
## 171	73.155245
## 172	299.344218
## 173	789.501014
## 174	97.457171
## 175	651.673786
## 176	491.894569
## 177	1055.603838
## 178	713.904669
## 179	626.991455
## 180	346.863438
## 181	650.359091
## 182	920.684686
## 183	1021.215222
## 184	438.911841
## 185	141.016531
## 186	269.550999
## 187	1074.361532
## 188	846.628359
## 189	485.204122
## 190	987.298641
## 191	384.880659
## 192	542.556819
## 193	384.580442
## 194	621.515884
## 195	338.662995
## 196	17.472073
## 197	535.649787
## 198	607.831887
## 199	782.332317
## 200	1079.165197
## 201	512.078460
## 202	409.601126
## 203	556.018006
## 204	634.132878
## 205	666.382275
## 206	690.483951
## 207	460.666018
## 208	480.689461
## 209	302.229142
## 210	855.430614
## 211	37.311523
## 212	201.712157
## 213	652.057664
## 214	1020.626478
## 215	819.262020
## 216	940.249362
## 217	761.772591
## 218	715.661432
## 219	766.713898

## 220	1001.902943
## 221	379.793481
## 222	586.640051
## 223	336.151291
## 224	565.213725
## 225	412.430270
## 226	680.348836
## 227	539.182707
## 228	511.445391
## 229	853.062496
## 230	650.103544
## 231	131.921609
## 232	115.327062
## 233	61.881055
## 234	146.340833
## 235	699.115799
## 236	654.856160
## 237	256.483893
## 238	532.958302
## 239	628.676232
## 240	351.155010
## 241	759.445851
## 242	305.396382
## 243	80.283750
## 244	689.017692
## 245	979.939238
## 246	278.240113
## 247	1056.177522
## 248	192.454185
## 249	289.691896
## 250	665.317641
## 251	955.548297
## 252	498.161712
## 253	332.821328
## 254	79.341691
## 255	259.976882
## 256	142.869508
## 257	590.473028
## 258	460.595590
## 259	144.730611
## 260	594.977008
## 261	182.980387
## 262	331.195062
## 263	699.275728
## 264	685.777956
## 265	267.781742
## 266	446.877500
## 267	55.033645
## 268	606.578537
## 269	1000.308394
## 270	224.486687
## 271	79.534810
## 272	546.982634
## 273	853.887484

## 274	809.413759
## 275	639.678938
## 276	1058.089721
## 277	670.876255
## 278	77.685114
## 279	443.729322
## 280	491.096396
## 281	1026.301996
## 282	289.212422
## 283	480.508681
## 284	858.658708
## 285	746.797399
## 286	719.195059
## 287	77.283539
## 288	597.774079
## 289	48.969177
## 290	126.480819
## 291	119.954834
## 292	830.379482
## 293	804.747144
## 294	37.735992
## 295	35.989186
## 296	337.511900
## 297	1023.370993
## 298	151.293756
## 299	523.436499
## 300	41.950462
## 301	548.940917
## 302	764.072783
## 303	395.312788
## 304	1077.393280
## 305	1100.289832
## 306	720.183439
## 307	980.750452
## 308	872.145622
## 309	594.867012
## 310	804.474290
## 311	37.377134
## 312	310.016446
## 313	40.227775
## 314	967.050326
## 315	433.161459
## 316	595.347874
## 317	684.913720
## 318	629.586389
## 319	528.828548
## 320	194.093284
## 321	961.959898
## 322	967.377808
## 323	175.800916
## 324	41.608060
## 325	293.707011
## 326	6.336859
## 327	150.517882

## 328	163.756406
## 329	1009.979389
## 330	1009.231754
## 331	28.364716
## 332	1061.258194
## 333	298.998471
## 334	284.661391
## 335	409.381850
## 336	509.360000
## 337	544.795358
## 338	945.628634
## 339	506.307756
## 340	527.746865
## 341	318.525361
## 342	310.325897
## 343	165.302089
## 344	535.126459
## 345	284.539230
## 346	223.858067
## 347	889.358356
## 348	173.955233
## 349	217.488073
## 350	742.249518
## 351	391.382590
## 352	298.444010
## 353	887.200612
## 354	119.317656
## 355	393.965424
## 356	477.792012
## 357	613.554437
## 358	447.183523
## 359	290.465599
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## 689	99.08556815
## 690	15.29580590
## 691	26.28805644
## 692	25.69525253
## 693	48.32300732
## 694	17.04009555
## 695	89.76991938
## 696	46.37537033
## 697	80.10966470
## 698	48.22827745
## 699	44.98977726
## 700	39.01365949
## 701	71.53370674

## 702	13.24025765
## 703	81.80450909
## 704	31.56660213
## 705	54.41374078
## 706	61.11794584
## 707	51.11972976
## 708	4.96905039
## 709	60.24830020
## 710	75.51273741
## 711	45.45582815
## 712	85.05697029
## 713	14.86388620
## 714	22.60926152
## 715	93.81532813
## 716	45.71837662
## 717	60.59007393
## 718	73.53935416
## 719	72.99183735
## 720	50.41961700
## 721	63.45484622
## 722	53.84752993
## 723	26.66188399
## 724	96.30878982
## 725	17.53248323
## 726	28.55943271
## 727	92.96287331
## 728	29.37965670
## 729	34.69263611
## 730	69.98749520
## 731	61.58198596
## 732	43.66356225
## 733	68.82513792
## 734	8.07439685
## 735	62.55796966
## 736	55.91668582
## 737	65.81408130
## 738	80.05835868
## 739	87.97451588
## 740	97.78407447
## 741	21.28252813
## 742	91.17807352
## 743	51.49690369
## 744	86.27380328
## 745	55.23182943
## 746	93.72643698
## 747	19.84793828
## 748	63.22093923
## 749	3.81256212
## 750	86.00544613
## 751	56.66922953
## 752	52.42840440
## 753	67.87570200
## 754	37.05283052
## 755	90.61152232

## 756	32.80246400
## 757	68.10257540
## 758	78.39589012
## 759	10.11417492
## 760	41.32698439
## 761	16.43005237
## 762	66.90659844
## 763	16.99012886
## 764	47.67568784
## 765	91.08802746
## 766	40.71236015
## 767	25.44237678
## 768	81.37022385
## 769	81.01426708
## 770	11.10880519
## 771	14.12924952
## 772	41.32019293
## 773	39.72006519
## 774	84.22261428
## 775	36.72400902
## 776	79.92491359
## 777	23.43459458
## 778	73.68199199
## 779	69.48343555
## 780	40.57813857
## 781	73.62850977
## 782	88.81335147
## 783	19.85335797
## 784	41.50958373
## 785	72.48283343
## 786	98.56543762
## 787	25.02803698
## 788	9.70246438
## 789	21.20901307
## 790	86.71684426
## 791	31.07866491
## 792	30.29173408
## 793	48.16194363
## 794	94.67430587
## 795	57.93531288
## 796	23.37930878
## 797	75.60627991
## 798	86.83949071
## 799	14.04069015
## 800	99.09957745
## 801	53.20313259
## 802	14.65138467
## 803	35.13064531
## 804	82.61391923
## 805	37.87572344
## 806	66.10701680
## 807	43.90837667
## 808	94.20507862
## 809	82.39889594

## 810	57.65496013
## 811	95.43111792
## 812	86.83323592
## 813	88.37894397
## 814	20.37441593
## 815	95.22614444
## 816	25.53631719
## 817	54.40891075
## 818	12.56978395
## 819	9.82031010
## 820	60.48946436
## 821	71.34951209
## 822	77.84917306
## 823	5.99903569
## 824	39.98640352
## 825	30.27915640
## 826	50.73539733
## 827	34.99737110
## 828	83.58068487
## 829	59.29547520
## 830	37.27567717
## 831	23.41254221
## 832	24.30543408
## 833	1.42273773
## 834	79.67912471
## 835	28.94749991
## 836	88.26382130
## 837	69.10426405
## 838	60.77590203
## 839	36.76313921
## 840	7.71585426
## 841	40.89278055
## 842	80.92506295
## 843	28.01815753
## 844	77.65723842
## 845	79.60131560
## 846	74.44307741
## 847	68.27497934
## 848	17.52927231
## 849	42.69393587
## 850	60.97932917
## 851	74.74391453
## 852	73.05275023
## 853	41.88166270
## 854	26.88560423
## 855	13.52717560
## 856	84.48656404
## 857	13.43926534
## 858	84.58617139
## 859	59.30071103
## 860	97.15851531
## 861	93.79307781
## 862	51.79235472
## 863	53.70801010

## 864	89.34464999
## 865	45.91624413
## 866	89.95125659
## 867	49.31397289
## 868	46.98063435
## 869	34.68827133
## 870	89.84524466
## 871	71.67440346
## 872	37.58794346
## 873	97.37931110
## 874	60.41151057
## 875	10.53788289
## 876	66.09289427
## 877	78.47510797
## 878	42.18119811
## 879	68.25320788
## 880	20.95887621
## 881	86.28839992
## 882	92.47778067
## 883	38.19576586
## 884	16.79507261
## 885	0.98168945
## 886	34.40264391
## 887	6.30311042
## 888	16.10024052
## 889	96.84345517
## 890	79.99750874
## 891	65.51876129
## 892	89.06828589
## 893	4.12535283
## 894	38.46251380
## 895	46.51529475
## 896	12.07466195
## 897	2.58746569
## 898	42.80414756
## 899	47.99406205
## 900	9.80527825
## 901	0.80805237
## 902	22.16399487
## 903	98.03874984
## 904	20.14927894
## 905	17.31488144
## 906	56.02264453
## 907	31.48877285
## 908	11.31107113
## 909	87.03157345
## 910	51.02112878
## 911	64.46557511
## 912	97.19157685
## 913	13.53731004
## 914	73.71007006
## 915	60.86336293
## 916	6.79235610
## 917	80.97120738

## 918	51.95108980
## 919	65.65871073
## 920	79.51100059
## 921	59.27334675
## 922	28.50131486
## 923	40.67670139
## 924	28.07860989
## 925	13.42942421
## 926	61.54518591
## 927	3.97357855
## 928	1.22609911
## 929	37.98938473
## 930	68.54550827
## 931	56.41012301
## 932	84.17225906
## 933	39.44885153
## 934	90.10607989
## 935	56.95758034
## 936	1.13956505
## 937	94.77483339
## 938	41.86145382
## 939	6.68439032
## 940	91.92479867
## 941	16.87983971
## 942	0.08832628
## 943	53.25049537
## 944	47.22957008
## 945	80.65966682
## 946	16.67234369
## 947	33.55116039
## 948	60.97535247
## 949	50.90929032
## 950	43.93564560
## 951	76.90490331
## 952	22.10864327
## 953	24.54460885
## 954	30.92975526
## 955	91.46904026
## 956	64.57764765
## 957	55.30938257
## 958	59.90366172
## 959	98.07481887
## 960	38.06929972
## 961	53.70757261
## 962	95.99008774
## 963	70.36226906
## 964	8.57676708
## 965	67.67733663
## 966	3.68829344
## 967	0.16953128
## 968	87.50024545
## 969	21.61473497
## 970	83.16137532
## 971	82.40688720

```
## 972 6.21638463
## 973 31.67994933
## 974 65.85642418
## 975 19.32962257
## 976 11.76851594
## 977 76.31080158
## 978 0.26430166
## 979 45.28354905
## 980 21.27914003
## 981 11.80727158
## 982 80.36879345
## 983 96.02432605
## 984 38.59421879
## 985 27.20064069
## 986 53.59365414
## 987 88.30015883
## 988 51.32460648
## 989 18.19359534
## 990 30.89875565
## 991 9.84706129
## 992 7.31788056
## 993 20.21615829
## 994 37.36310415
## 995 60.91907928
## 996 95.53492877
## 997 28.13942449
## 998 94.76623395
## 999 37.14683352
## 1000 86.58091426
```

```
#View regression relation
#between y and x
summary(lm(formula = y~x, data=data))
```

```
##
## Call:
## lm(formula = y ~ x, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -50635 -24754   -496   26076  49904
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 50784.9414  1841.2508   27.582  <2e-16 ***
## x           -0.7168     2.9525   -0.243    0.808
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 29490 on 998 degrees of freedom
## Multiple R-squared:  5.906e-05, Adjusted R-squared:  -0.0009429
## F-statistic: 0.05894 on 1 and 998 DF, p-value: 0.8082
```

```
#between y and x (adjusted for coufounding z)
summary(lm(formula = y~x+z, data=data))
```

```
##
## Call:
## lm(formula = y ~ x + z, data = data)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -50557 -24741   -538   26073   49856
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) 51008.9550  2385.4360  21.383  <2e-16 ***
## x           -0.6858    2.9614   -0.232   0.817
## z           -4.7823    32.3536   -0.148   0.883
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 29510 on 997 degrees of freedom
## Multiple R-squared:  8.097e-05, Adjusted R-squared:  -0.001925
## F-statistic: 0.04037 on 2 and 997 DF, p-value: 0.9604
```