# **GKROM**

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```
class GKROM (M, path = None, folder_name = None, simuSize = None, match4 = False, fixedOmega = True, initStyle = 'uniform', maxT_col2 = 30, maxT_incr = 4, edf = 2, xtol = None, maxiter = None, max_RO = 20)
```

This class generate a simulated sample that matches a given sample 'M' in its mean, variance and Kollo skewness (match4 = False), as well as Kollo kurtosis if required (match4 = True).

# **Dependencies:** import numpy as np

import math as math import random as random import time as time

import os

from scipy.optimize import root from scipy.linalg import cholesky

#### Parameters: M : ndarray

A target sample to match.

#### path: Nonetype or str, optional

The path under which the simulated sample is saved. The default value is None. If None, no path is provided, and the simulated sample will not be exported. If path is assigned by a string identifying the path to save the results, the simulated sample will be saved into a folder under the provided path.

## folder\_name : Nonetype or str, optional

The name of the folder under the given path where the simulated sample is saved. The default value is None, indicating no folder name is provided.

When None and yet the simulated sample is still required exporting (path is given a string), a folder called "simulated\_path" will be created under the given path for the simulated sample recorded in csv.

#### simuSize: Nonetype or int, optional

The number of observations per dimension in the simulated sample. The default value is None.

If None, the simulated sample will be set with the same number of observations as the target sample.

## match4: Nonetype or bool, optional

The default value is False.

If False, and only the first three moments are matched.

If True, all first four moments are matched.

## fixedOmega: bool, optional

The default value is True.

If True, and a fixed rotation matrix (see paper page 9) is applied.

If False, a random normal rotation matrix is applied.

\*\* The parameters below are only <u>relevant</u> to matching all first four moments (match4 = True) \*\*

#### initStyle: str, optional

The method of generating initial guesses for solving the equation system. The default value is 'uniform'.

If 'uniform', the initial guesses are drawn from a uniform (-1,1) distribution.

If 'equal', the initial guesses are set equal across all dimensions.

## maxT\_col2: int or float, optional

Time limit (in seconds) for solving the second column. The default value is 30.

When this time limit is breached, the code is bounced back to regenerate column 1 and search for a feasible column 2.

## maxT\_incr: int or float, optional

Incremental multiplier on the time limit for solving the next column. The default value is 4.

For example, when maxT\_incr = 4 and maxT\_col2 = 30, the time limit for solving the third column is  $30 \times 4 = 120$  seconds, and the time limit for solving the fourth column is  $120 \times 4 = 480$  seconds.

When the time limit is breached, the code is bounced back to regenerate column  $1, 2, 3 \dots \text{etc.}$ 

#### edf: int, optional

Extra number of orthogonal vectors need for each column. The default value is 2.

### xtol: Nonetype or float, optional

Tolerance for termination when searching for a real solution of the equation system. The default value is None.

If None, the tolerance is set as default given by the scipy solver.

## maxiter: Nonetype or int, optional

Maximum iterations for finding a real solution of the equation system. The default value is None.

If None the maximum iterations is set as default given by the scipy solver.

## max\_RO: int or float, optional

Time limit (in seconds) for finding a set of proper orthogonal vectors. The default value is 20.

## Generating a simulated sample (Example):

```
# Import GKROM class from GKROM_core file %run "xxx/GKROM.ipynb" import GKROM # xxx is str of the path where the class file is say
```

# xxx is str of the path where the class file is saved; it does not have to be the same as the path where the simulated sample is exported to (as .csv)

```
# Launch function with pre—defined parameters result = GKROM(M, path, folder name, simuSize, match4, fixedOmega)
```

```
# Compute simulated sample result.run()
```

## Output: result.output: ndarray

The matrix of a simulated sample that matches the target sample.

When exported, it is saved in a file named "Simulated\_sample\_xxx.csv" where xxx is an integer generated from the time stamp at which the file is exported.

## result.stdized\_output: ndarray

The matrix of a standardized simulated sample that matches the target sample.

#### result.m:int

The number of observations in the simulated sample.

## result.mu: ndarray

The mean vector of the target sample.

# result.A: ndarray

The matrix of the Cholesky decomposition of the target covariance.

#### result.b: ndarray

The matrix of the target Kollo skewness.

### result.L\_o: ndarray

The matrix of the standardized target sample.

## result.path: Nonetype or str

The path under which the simulated sample is saved.

#### result.math4:bool

False: only the first three moments are matched.

True: all first four moments are matched.

#### result.fixedOmega: bool

True, and a fixed rotation matrix (see paper page 9) is applied.

False, a random normal rotation matrix is applied.

\*\* The output below are only meaningful to matching all first four moments \*\*

## result.K: ndarray

The matrix of the target Kollo kurtosis.

## result.initStyle: str

The way of generating initial guesses for solving the equation system.

'uniform': the initial guesses are drawn from a uniform (-1,1) distribution.

'equal': the initial guesses are set equal across all dimensions.

## result.maxT\_col2: int or float

Time limit (in seconds) for solving the second column.

## result.maxT\_incr: int or float

Incremental multiplier on the time limit for solving the next column.

#### result.edf: int

Extra number of orthogonal vectors need for each column.

## result.xtol: Nonetype or float

Tolerance for termination when searching for a real solution of the equation system. None when the tolerance is set as default given by the scipy solver.

## result.maxiter: Nonetype or int

Maximum iterations for finding a real solution of the equation system.

None when the tolerance is set as default given by the scipy solver.

## $result.max\_RO: int\ or\ float$

Time limit (in seconds) for finding a set of proper orthogonal vectors.