```
In [1]: import numpy as np
  import pandas as pd

import matplotlib.pyplot as plt
  import seaborn as sns
  from sklearn.preprocessing import StandardScaler
  from sklearn.cluster import KMeans
  import time
  import random
```

Out[2]:

| | fixed acidity | volatile acidity | citric acid | residual sugar | chlorides | free sulfur dioxide | total sulfur dioxide | density | рН | sulphates | alcohol |
|------|------------------|---------------------|----------------|-------------------|-----------|---------------------------|----------------------------|---------|------|-----------|---------|
| 0 | 7.4 | 0.700 | 0.00 | 1.9 | 0.076 | 11.0 | 34.0 | 0.99780 | 3.51 | 0.56 | 9.4 |
| 1 | 7.8 | 0.880 | 0.00 | 2.6 | 0.098 | 25.0 | 67.0 | 0.99680 | 3.20 | 0.68 | 9.8 |
| 2 | 7.8 | 0.760 | 0.04 | 2.3 | 0.092 | 15.0 | 54.0 | 0.99700 | 3.26 | 0.65 | 9.8 |
| 3 | 11.2 | 0.280 | 0.56 | 1.9 | 0.075 | 17.0 | 60.0 | 0.99800 | 3.16 | 0.58 | 9.8 |
| 4 | 7.4 | 0.700 | 0.00 | 1.9 | 0.076 | 11.0 | 34.0 | 0.99780 | 3.51 | 0.56 | 9.4 |
| | | | | | | | | | | | |
| 1594 | 6.2 | 0.600 | 0.08 | 2.0 | 0.090 | 32.0 | 44.0 | 0.99490 | 3.45 | 0.58 | 10.5 |
| 1595 | 5.9 | 0.550 | 0.10 | 2.2 | 0.062 | 39.0 | 51.0 | 0.99512 | 3.52 | 0.76 | 11.2 |
| 1596 | 6.3 | 0.510 | 0.13 | 2.3 | 0.076 | 29.0 | 40.0 | 0.99574 | 3.42 | 0.75 | 11.0 |
| 1597 | 5.9 | 0.645 | 0.12 | 2.0 | 0.075 | 32.0 | 44.0 | 0.99547 | 3.57 | 0.71 | 10.2 |
| 1598 | 6.0 | 0.310 | 0.47 | 3.6 | 0.067 | 18.0 | 42.0 | 0.99549 | 3.39 | 0.66 | 11.0 |

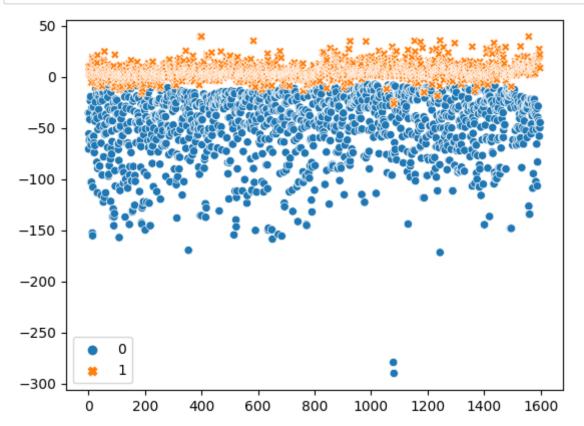
1599 rows × 12 columns

```
In [3]: ds.shape
Out[3]: (1599, 12)
In [4]: t_ds= ds.to_numpy().T

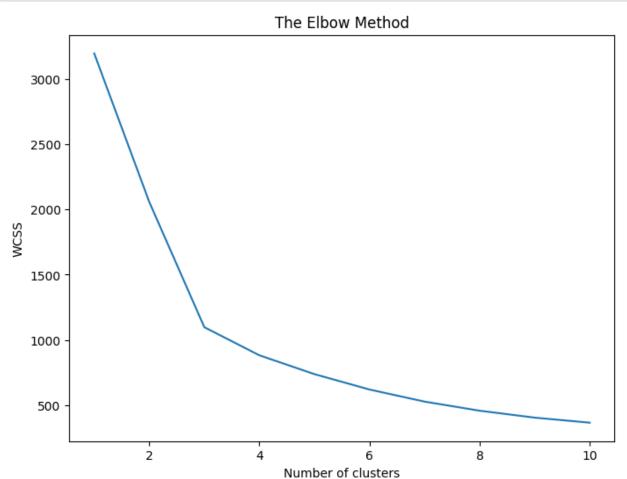
In [5]: t_ds.shape
Out[5]: (12, 1599)
In [6]: covariance_matrix = np.cov(t_ds)
eigen_value, eigen_vector = np.linalg.eig(covariance_matrix)
```

```
eigen_pairs = [(np.abs(eigen_value[i]), eigen_vector[:,i]) for i in range(1
          eigen pairs.sort(key=lambda x: x[0], reverse=True)
 In [8]: eigen_value_list = [j.reshape(len(ds.columns), 1) for _,j in eigen_pairs[:2
         matrix_w = np.hstack(eigen_value_list)
         print('Matrix W:\n', matrix_w)
         Matrix W:
           [[ 6.13296554e-03 -2.38646792e-02]
           [-3.84670318e-04 -2.02021707e-03]
           [-1.70762384e-04 -3.02675912e-03]
           [-8.64864277e-03 1.11453593e-02]
           [-6.37476516e-05 -2.37525597e-04]
           [-2.18852809e-01 9.75212313e-01]
           [-9.75669835e-01 -2.18850408e-01]
           [-3.72590009e-06 -2.50439091e-05]
           [ 2.67974074e-04
                             3.26939011e-03]
           [-2.23244233e-04 6.25945868e-04]
           [ 6.35985376e-03 1.46377527e-02]
           [ 4.31953676e-03 1.15350784e-02]]
 In [9]: transformed = matrix_w.T.dot(t_ds)
         transformed.shape
 Out[9]: (2, 1599)
In [10]: new ds = pd.DataFrame(transformed.T)
         new ds
Out[10]:
                      0
                               1
             0 -35.469286
                          3.336638
             1 -70.731567
                          9.770351
             2 -55.856674
                          2.860240
             3 -62.119682
                          3.422528
               -35.469286
                          3.336638
                      ...
          1594 -49.823118 21.673219
          1595 -58.179579 26.999311
          1596 -45.258381 19.642837
          1597 -49.826886 21.676253
          1598 -44.815392
                          8.498672
          1599 rows × 2 columns
```

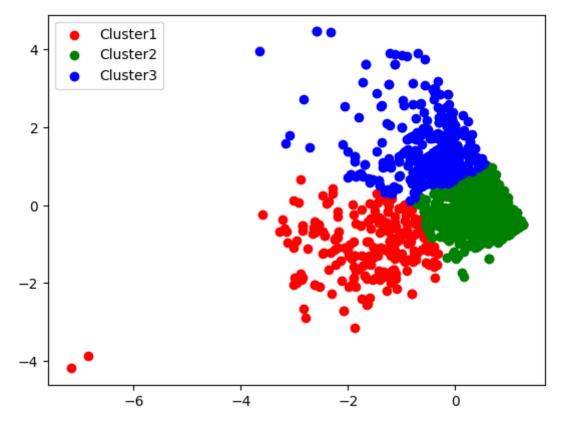
```
In [11]: sns.scatterplot(new_ds)
plt.show()
```



```
In [14]: f3, ax = plt.subplots(figsize=(8, 6))
    plt.plot(range(1,11),wcss)
    plt.title('The Elbow Method')
    plt.xlabel('Number of clusters')
    plt.ylabel('WCSS')
    plt.show()
```



```
In [15]: #From above graph, we got to know number of clusters=3. Hence, applying kme
kmeans = KMeans(n_clusters = 3)
clusters = kmeans.fit_predict(X_scaled)
```



```
In [ ]:
```